

# How to Make Your Programs Very Safe

## A Review of Practical Applications of Dependent Types

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## 1 Introduction

Programs crash. Static type systems serve to make the life of a programmer easier by providing static compile-time guarantees of certain program behaviour, guaranteeing that a function will map from a domain to a co-domain. A dependently typed programming language gives a programmer even additional expressive power, allowing types to be expressed relative to values given at runtime. For example, consider a function *replicate*, that takes in any Peano natural number  $n$  and returns a length-indexed vector of  $n$  Peano natural numbers of the value  $n$ . We can express this in Idris, a dependently typed functional programming language, as follows in Figure 1.

**Figure 1.** Implementation of Replicate in Idris

```
-- replic 3 will give us (3 :: 3 :: 3 :: Nil)
replic : (n : Nat) -> Vect n Nat
replic n = replHelp n n where
  replHelp : (n : Nat) -> Nat -> Vect n Nat
  replHelp Z _ = Nil
  replHelp (S n) val = (val :: replHelp n val)
```

Thus, the co-domain of our function is dependent upon some value that is provided at runtime. Calling `replic 5` will limit the co-domain of the function to all length-indexed vectors of length 5, etc. Having written this type, a programmer now has compile-time guarantees that the logic for a function was expressed correctly and behaviour will correspond closer to what is expected.

While research in dependent types has traditionally been in the domains of theoretical mathematics, where researchers

use dependently typed theorem provers to write mathematical formalisms, dependent types have applications outside of such a theoretical domain. In my work, I seek to find patterns in the existing body of literature around practical applications of dependent types. My goal is to enumerate signs that a programmer should look for that the solution to a problem could benefit from the use of dependent types.

## 2 Work Covered

This review is a tour of potential applications of dependent types. In this abstract, I have chosen a brief example, units of measurement, in order to demonstrate their potency. However, in addition to units of measurement, dependent types have far ranging applications. A poster of my research would contain a couple of the applications which I am exploring:

1. Complicated pattern matching in the Cryptol DSL for cryptographic applications. [7]
2. Generating file format parsers from a data description language. [7]
3. A relational database and algebra. [3, 7]
4. An alternative to monadic transformations with an algebraic effects DSL [2]
5. Programming distributed systems with  $F^*$  and dependent types. [8]
6. A low-level domain-specific language demonstrating the applicability of dependent types to systems programming. [1]

## 3 Units of Measurement

My first example is to

A practical application for dependent types from is to eliminate bugs that can arise from improper unit conversions [4]. Units of measurement are already implemented in Microsoft's F# Programming Language [6]. If numbers carry a type denoting their unit of measurement with them, we can ensure at compile time that improper unit conversions are not going to occur at runtime. These bugs can be catastrophic, as made evident by NASA's loss of the \$125-million Mars Climate Orbiter when "spacecraft engineers failed to convert from English to Metric units of measurement" [5].

An implementation of units of measurement should have types that support decidable equality by definition. Two typed variables can only be equal because they have the same unit of measurement or derived unit of measurement

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**Figure 2.** Displays a unit error that would be caught at compile-time with units of measurement.

```

distanceTraveled : Quantity Inches
distanceTraveled = inches 20

distanceLeft : Quantity Metres
distanceLeft = (metres 1000) -
    distanceTraveled

```

and the same value. This means that if coding style guidelines enforce that all numeric values must be well-typed with units of measurement, there will be compile-time guarantees that errors of conversion between units of measurement will not occur. See Figure 2 for an example of a program that should error.

While units of measurement are implemented as a feature in the F# language, which is not dependently typed, a dependently typed programming language would allow for a units of measurement system to be implemented [4]. Gundry invites us to consider a system for describing units in terms of a constructor that allows us to both enumerate elementary units and also express derived units in terms of one another [4].

**Figure 3.** Basic SI unit declarations in adapted from Dependent Haskell to Idris [4]

```

data Unit : Int -> Int -> Int -> Type

Dimensionless : Type
Dimensionless = Unit 0 0 0

Metres : Type
Metres = Unit 1 0 0

Seconds : Type
Seconds = Unit 0 1 0

Kilograms : Type
Kilograms = Unit 0 0 1

data Quantity u = Q Double

metres : Double -> Quantity Metres
metres v = (Q v)

seconds : Double -> Quantity Seconds
seconds v = (Q v)

kilograms : Double -> Quantity Kilograms
kilograms v = (Q v)

plus : Quantity u -> Quantity u -> Quantity u
plus (Q x) (Q y) = Q (x + y)

```

For now, our data declaration for `Unit` only supports three elementary units (metres, seconds, kilograms), but one can imagine a full library implementing the entire SI Units system. Each elementary unit is implemented as a single 1 in the call to the `Unit` constructor with all entries as zero. Thus, we can express derived units in a call to the `Unit` constructor where negative integers would represent elementary units present in the denominator.

We can define quantities as a type containing a `Unit` and an integer. This then allows us to write simple constructors for the quantity type. We can then define well-typed multiplication and addition operations giving us similar guarantees to that which is given by units of measurement in F#.

As defined above, this enforces well-typed addition, requiring that two additions be of the same type. we can also define operations that allow us to express fractional units. For example, a Newton of force is defined as a  $kg \times ms^{-2}$ . Therefore, if we are able to compose types through multiplication and division, we can express a Newton with our units system. See Figure 4.

**Figure 4.** Definition of division and multiplication of dependently typed units of measurement. Ported to Idris from [4]

```

Newtons : Type
Newtons = Unit 1 -2 1

newtons : Double -> Quantity Newtons
newtons val = over
    (times (kilograms val) (metres 1))
    (times (seconds 1) (seconds 1))

```

What we've shown here is that while units of measurement can be first-class features in a programming language like F#, a dependently typed language allows us to build certain functionality easily into the language without changing the language specification whatsoever.

## 4 Conclusions

Through a review of the practical applications of dependent types in existing and implemented functional programming languages, I demonstrate that while dependent types are often thought of as far-off and theoretical, they are currently available in advanced functional programming languages and serve practical purposes.

I set out to look for patterns that signal to a programmer that dependent types would be particularly useful for their work. So far, I've found that the problems that I'm exploring seem to be focused around two main themes: the serializing and deserializing of data, and building domain-specific languages. As I continue my research, I will expand on these ideas and make the scenarios more concrete and identifiable to a programmer, which I hope to present at POPL.

## References

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