The Lorentz Group and Singular Lorentz Transformations

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abstract

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I. THE LORENTZ TRANSFORMATION

The Lorentz Transform is defined by

$$(x,y,z,t) \to (x',y',z',t') \text{ such that }$$

$${x'}^2 + {y'}^2 + {z'}^2 - {t'}^2 = x^2 + y^2 + z^2 - t^2$$

If the transformation preserves the orientation of the spatial axes then is it called a proper Lorentz transformation. This is equivalent to saying the transformation does not change the handedness of the axes. Also If $t \geq 0 \Rightarrow t' \geq 0$ then it is called an orthochronous Lorentz transformation. This ensures that the time direction is preserved. In this project the "Lorentz transformation" will refer to the proper, orthochronous Lorentz transformation.

Consider a photon moving in the x direction at the speed of light, c=1, and starting at x=0. The space-time for such a photon can be illustrated as follows (FIGURE). It is clear that there are two null directions in this space-time, $x=\pm t$. Using the standard Lorentz transformation:

$$x' = \gamma(x-vt)$$
 , where $\gamma = (-v^2)^{-1/2}$ $t' = \gamma(t-vx)$

II. REPARAMETERISATION OF THE SCHWARZSCHILD SOLUTION

III. ACKNOWLEDGEMENTS