

# Singular Lorentz Transformations and Pure Radiation Fields

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Layout

- Introduction
- Line Element in Minkowskian Space-Time
- Test
- Singular Lorentz transformation

- 1 Introduction
- 2 Line Element in Minkowskian Space-Time
- 3 Test
- 4 Singular Lorentz transformation

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# Introduction: Lorentz Transformations

- A Lorentz transformation is defined by the preservation of the quadratic form

$$x'^2 + y'^2 + z'^2 - t'^2 = x^2 + y^2 + z^2 - t^2$$

in the transformation  
 $(x, y, z, t) \rightarrow (x', y', z', t')$

- Take the Proper Orthochronous Lorentz transformations which form the restricted Lorentz group  $SO^+(1, 3)$
- In general lorentz transformations have two invariant null directions

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• Proper Orthochronous Lorentz transformations  
→ restricted Lorentz group  
 $SO^+(1, 3)$   
• All Lorentz transformations are generated by  
space rotations and boosts

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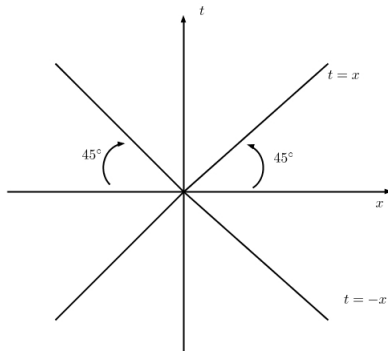
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–Proper is  $\det 1$  . preserves the orientation of spacial axes, preserves handedness–orthochronous means time is always positive and the direction of time is preserved–Think of the standard Lorentz transformation, always two null directions at  $x \pm t$