Population, Ideas, and the Speed of History

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Economic	growth	may	fall	alongside	popul	ation	growth
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I'll refer to this as **scale-based growth**, separating it from growth that is caused by allocative improvements

Does this imply that a shrinking population leaves us all worse off?

This could be an important loss coming from depopulation

► TFP improvements that expand our social choice set are good!

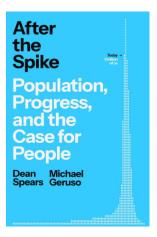
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This concern is now relatively widespread:





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Population size governs the speed of human history

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Regardless of per-period population size, we should expect that each:

- $ightharpoonup i < \frac{1}{p^{mc}}$ must live without her ideas
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A larger population brings forward the arrival of a Marie Curie, but it also brings forward all other lives

This paper makes two related contributions:

- 1) Formalizes this logic in a standard Romer/Jones semi-endogenous growth setting
 - ➤ To a first-order, population size per-period has no effect on innovation rates **per human life**(even if it *does* affect innovation per period)
 - More generally, I identify parameters which can rescue (or reverse) the original intuition

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 - More generally, I identify parameters which can rescue (or reverse) the original intuition
- 2) Assesses potential *extensive margin* effects of population size on per capita outcomes
 - ► Histories with larger populations may get through more total lives
 - Open question: whether and how to value these contingent existences?

When non-rival ideas drive growth, population size does not necessarily improve individual outcomes

Standard endogenous growth setting (Jones, 1995):

$$\frac{\dot{A}(t)}{A(t)} = \theta(t)N(t)^{\lambda}A(t)^{-\beta}$$

 $\dot{A}(t)$ is the (instantaneous) growth in TFP

N(t) is the population size

 $\theta(t)$ captures human or physical capital per person (Assume constant, to isolate scale effects)

 λ, β govern the degree of diminishing returns (I'll start with $\lambda=1$ to generate analytical insight; relaxed later)

A(t) determined by cumulative people-years

Integrate with respect to time:

$$A(t) = \left(\beta\theta \underbrace{\int_0^t N(\tau)d\tau}_{\text{People-years by }t} + A_0^{\beta}\right)^{\frac{1}{\beta}}$$

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Notice: time, per se, does not increase TFP

► It is cumulative human effort that increases TFP

 $i \in [0, I] \equiv$ "people-years" lived in this economy; $i(t) = \int_0^t N(\tau) d\tau$

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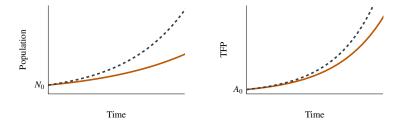
$$A(t) = \left(\beta \theta \int_0^t N(\tau) d\tau + A_0^{\beta}\right)^{\frac{1}{\beta}}$$

Because $i = \int_0^t N(\tau)d\tau$, we can rewrite as:

$$A(i) = \left(\beta\theta i + A_0^{\beta}\right)^{\frac{1}{\beta}} = y(i)$$

Result: The income of the *i*th person-year is determined by *i*'s order in history (conditional on θ , β)

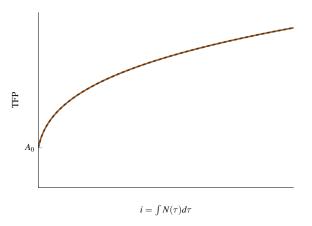
Larger populations speed up technological progress...



Blue dotted line is the history with faster population growth

For each *t* it has reached higher levels of TFP and population

...without any improvements to individual lives.



A(i) is independent of population growth or size

Overlapping lives complicate the interpretation, but do not break the result

If populations became larger next year, that would improve your life

► More would be discovered in your lifetime

The trade-off: More people need to live soon

"Soon" is the worst time to be alive, conditional on not having been born yet Larger populations can reduce inequality, but do not improve average outcomes

Recall
$$i(t) = \int_0^t N(\tau) d\tau$$

▶ Two people living for 10 years is i = 20 person-years

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- ► If we lived one at a time—a tiny population—the first person gets a terrible deal!

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A planner with an individual and time-separable objective function will not care about this...

...because I already showed you the quality of each person-year is independent of per period population size

Model relaxations highlight parameters that generate a non-zero effect of population size

Three model relaxations

- 1. Endogenous research effort
 - ► No straightforward effect on main result
- 2. Non-linearity in returns to research effort
 - Likely *reverses* the usual intuition (negative rather than independent relationship)
- 3. Depreciation of knowledge over time
 - ► Rescues the usual positive intuition, but of uncertain magnitude

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Previously under-appreciated parameters determine which side of the knife's edge we live on

Exact neutrality won't hold, but there are no strong reasons to assume the relationship is positive or negative

Intra-period non-linearity in research effort does not appear to rescue original intuition

I assumed the exponent on *N* within a period was one:

$$\frac{\dot{A}}{A} = \theta N(t)^{\lambda} A(t)^{-\beta}$$

If $\lambda > 1$, collaboration effects imply large populations disproportionately speed up idea creation

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But: researchers in this field seem to think $\lambda < 1$ is more likely

- ► That would mean each *i* benefits from smaller populations, even when non-rival idea-production is the only externality (An exact reversal of what Romer (1990) has been thought to imply!)
- ► Granted, very little work on this; maybe $\lambda > 1$, or becomes greater than one for tiny populations

Knowledge depreciation *does* rescue the positive relationship

Suppose knowledge depreciates over time

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This addition does rescue original intuition, and for the 'right' reasons

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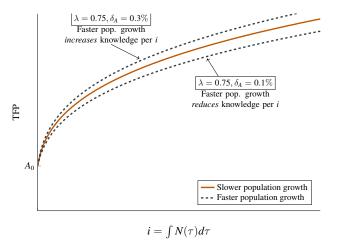
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Imagine $\delta_A = 1$

- ► Then, ideas are only accessible in the period they are discovered More contemporaries ⇒ more ideas for you that period
 - ► Is knowledge depreciation quantitatively meaningful?

Knowledge depreciation vs. $\lambda < 1$



Larger populations – moving through lives and discoveries faster – can improve or worsen individual outcomes depending on parameters

The extensive margin effect could remain important, if the social planner values it

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The relationship between per-period population size and total lives depends on extinction assumptions

Case I: Exogenous extinction (e.g., Stern, 2006)

Suppose a natural event (e.g., asteroid) will end humanity in some future year

► This is one rationale for discounting

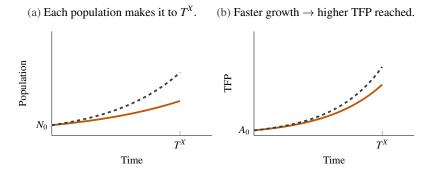
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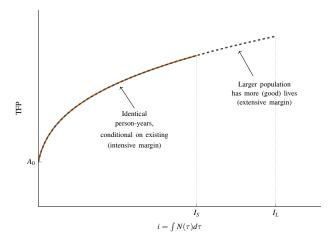
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The larger population will, ex-post, **get through more lives** (and discoveries)

Each population lives for the same number of periods, but the larger population has more happen in those periods



Larger populations make it through more history



Notice: identical to extending humanity's lifespan temporally

► How valuable would it be to push extinction off for *z* years?

Case II: Endogenous extinction (e.g., Jones 2016,2024)

Karger et al (2024) elicit forecasts on extinction risks and find 99% attributable to endogenous risks

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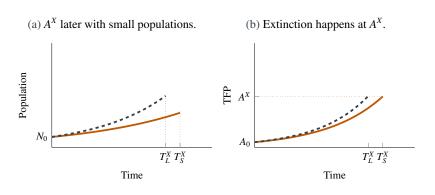
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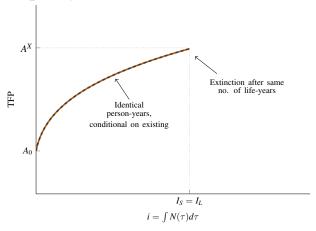
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If extinction is endogenous in this way, we **bring forward extinction** along with lives and innovations

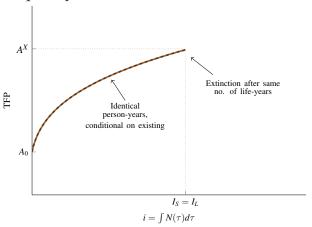
In this case, extinction is brought forward with people and ideas



Large and small populations traverse exactly the same quantity and quality of lives



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A human-caused extinction event is a non-rival bad, offsetting the non-rival good of knowledge

(i.e., if scale brought forward mRNA vaccine development, why shouldn't we also think it brought forward the covid pandemic?)

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Taking Stock

- 1. Scale-based growth has ambiguous effects on the quality of each person-year, *conditional on existing*
- 2. Per capita outcomes increase in the number of total existences
 - ► (More good lives are lived ⇒ per capita outcomes increase)
- 3. So, what matters is how current population size/growth influences the total number of existences
 - Which depends on assumptions about extinction

The effect of N on long-run welfare depends on extinction risks and returns to per-period populations

	$\lambda < 1$	$\lambda = 1$	$\lambda > 1$
	$(\& \delta_A = 0)$	$(\& \delta_A = 0)$	(or $\delta_A > 0$)
T^X causes extinction (e.g., asteroid)		$\bar{y}_L \ge \bar{y}_S$ $I_L > I_S$	
A^X causes extinction (e.g., advanced A.I.)	$I_L > I_S$	$ \bar{y}_L = \bar{y}_S I_L = I_S $	$I_L < I_S$
I^X causes extinction (e.g., rogue actor)	$\bar{y}_L < \bar{y}_S$	$ \bar{y}_L = \bar{y}_S I_L = I_S $	$\bar{y}_L > \bar{y}_S$
A decreases risk (e.g., carbon capture)		$\bar{y}_L > \bar{y}_S$ $I_L > I_S$	
\bar{N} causes extinction (e.g., ecological collapse)		$\bar{y}_L(?)\bar{y}_S$ $I_L(?)I_S$	