#### Population Growth, Ideas and the Speed of History

#### Kevin Kuruc

Population Wellbeing Initiative, University of Texas at Austin Global Priorities Institute, University of Oxford

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- 2. A larger economy/population produces more non-rival ideas (Romer, 1990; Jones, 1995)
  - ► I.e., the production of ideas depends on people
- 3. So, a small and shrinking population generates less economic growth (Jones, 2022)
  - In the limit, growth goes to zero in these models without population growth (Jones, 1995)

("semi-endogenous" growth)

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## Should we be concerned about the loss of innovation in a small or shrinking world?

It seems straightforward that—if these theories are correct—this could be an important loss coming from depopulation

► TFP improvements that expand our social choice set are good! And, in fact, there *is* concern:





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- 1. **Endogenous** (e.g., human- or technology-caused): Extinction is brought forward along with lives and new technologies; population size compresses, but does not change, history
- 2. **Exogenous** (e.g., nature-caused): The faster history moves, the more advanced we would be by the time an (e.g.,) asteroid is bearing down; population size *does* matter

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**General Lesson:** Formalizing which factors evolve per human life vs. per unit time is crucial for understanding how per capita variables are affected by population size

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- **Result 2:** The effects of ideas-based growth will depend on the existence of factors that evolve exogenously
  - ▶ Demonstrate this with alternative extinction risks
- **Result 3:** Generally, we need to clarify how time *per se* matters for different economic processes
  - To make lives better, we need to change the arrival rate of people *relative* to something
  - Agglomeration/natural resource constraints can be framed as time-based considerations

# Simple Model: Scale-based growth does not

improve individual living standards

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For concreteness, let's say it takes 1 trillion people-years of effort to get to state H

Does increasing the population size increase individual welfare?

Let's focus on a marginal increase in population from (constant) N = 10 (billion) to N = 11 (billion)

 $\triangleright$  So it takes either 100 years or 91 years to get to H, respectively

What are the effects of getting there faster?

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We've stipulated that it takes 1 trillion people-years to get to H

So the first  $i \le 1$  trillion do not benefit from technological progress being accelerated in this way

(They have more contemporaries, but I'll set that aside)

Do people i > 1 trillion benefit?

What changes for the people who come afterwards?

Consider things from the vantage of person i = 1 trillion + 1

- ► She lives in the *H*-state, *no matter what*
- ▶ What changes for her is *when* she comes into existence

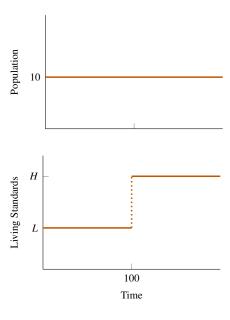
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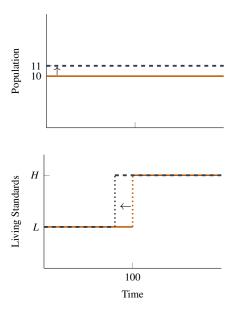
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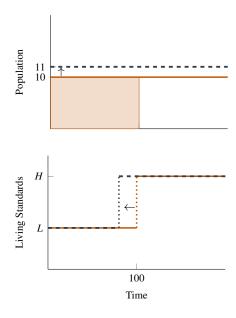
No individual is made better off by increasing population sizes

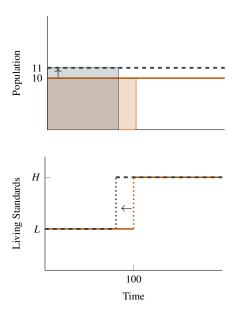
#### Larger populations speed up technological progress...

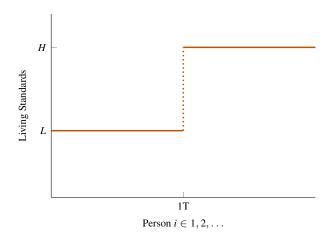


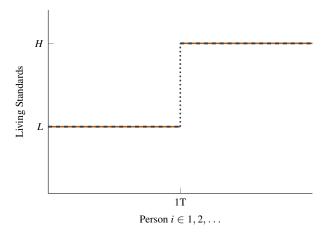
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**Result**: Being in a larger population world, with faster technological progress, has not made anyone's life better

## This invariance can be formalized in standard models

#### Aggregate TFP growth increases in scale

Standard semi-endogenous growth setting (Jones, 1995):

$$\frac{\dot{A}(t)}{A(t)} = \theta(t)N(t)^{\lambda}A(t)^{-\beta}$$

 $\dot{A}(t)$  is the (instantaneous) growth in TFP N(t) is the population size  $\theta(t)$  captures human or physical capital per person (Assume constant, to isolate scale effects)

 $\lambda, \beta$  govern the degree of diminishing returns (For simplicity, and exactness, I'll start with  $\lambda=1$ )

# A(t) determined by cumulative people-years

Integrate with respect to time:

$$A(t) = \left(\beta\theta \underbrace{\int_{0}^{t} N(\tau)d\tau}_{\text{People-years by } t} + A_{0}^{\beta}\right)^{\frac{1}{\beta}}$$

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Notice: time, per se, does not increase TFP

► It is cumulative human effort that increases TFP

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Because  $i = \int_0^t N(\tau) d\tau$ , we can rewrite as:

$$A(i) = \left(\beta\theta i + A_0^{\beta}\right)^{\frac{1}{\beta}} = y(i)$$

**Result**: The wellbeing of the *i*th person-year is predetermined by *i*'s order in history

# From this perspective, what matters is only how many lives are ever lived

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We need to make assumptions about extinction

Case I: Endogenous extinction (e.g., Bostrom, 2019; Jones 2016,2024; Ord, 2020)

Consider Jones' "Russian Roulette" model of growth:

- ► Each new idea carries some risk of ending civilization
  - Weapons of mass destruction; etc.

Or: conditional on A, each person has a chance of ending civilization

► Intentional terrorism; unintentionally causing a global pandemic

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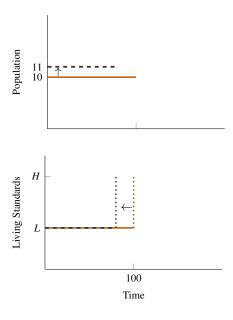
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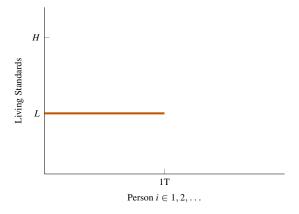
If extinction is endogenous in this way, we **bring forward extinction** along with lives and innovations

Under linearity assumptions, exactly proportionately

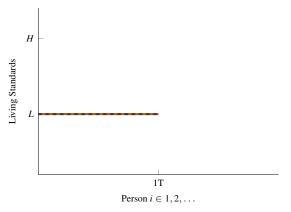
In this case, extinction is brought forward



Large and small populations traverse exactly the same quantity and quality of lives



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A human-caused extinction event is a non-rival bad, offsetting the non-rival good of knowledge

► (i.e., if scale brought forward mRNA vaccine development, why shouldn't we also think it brought forward the covid pandemic?)

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Suppose a natural event (e.g., asteroid) will end humanity in some future year

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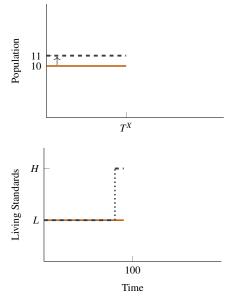
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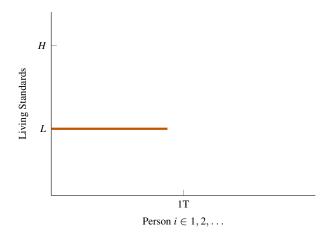
Trivially, the larger population will, ex-post, get through more lives (and discoveries)

➤ Similarly, if the planner intrinsincally prefers that things happen earlier in time (i.e., a positive rate of pure time preference) then there will be value in speeding up history

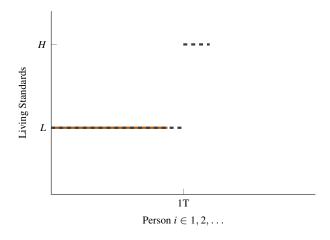
Each population lives for the same number of periods, but the larger population has more happen in those periods



Larger populations make it through more of our potential history



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We need more research on this: the demographic-implications of idea-based growth models rely on a stance about how the model ends

# General Lesson: Clarifying how time, per se,

matters for different processes will be crucial to understanding the effects of population size

Imagine a tree that drops C fruit each period (or e.g., any natural resource producing ecosystem services)

Individual fruit consumption:  $\frac{C(t)}{N(t)}$ 

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Speeding up the arrival of humans, without speeding up fruit production, is equivalent to *slowing down* the speed of fruit production

► There is less fruit *per human life* 

(Similar phenomenon for the existing stock of capital—it produces economic services per unit of time)

Consider **specialization**: To fill a niche in the economy, we need someone who **currently** knows a particular skill

Learning a task is a fixed cost that needs to be re-paid once every 40-50 years

► E.g., Someone learns something once, can apply it for 40-50 years

This will be more affordable per person if more people live per unit of time

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Or: Imagine that knowledge depreciates per unit of time

► It will cost less to preserve for the next *M* people the earlier they live

Other time-based effects that will interplay with how fast ideas/people arrive?

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I've found thinking about the **arrival rate of humans** (and everything we do) speeding up or slowing down as a useful way to clarify which things will be impacted by population size, and which will not