

## 1 Warm-up

Algorithm	Best-case	Worst-case	Stable
Selection Sort			
Insertion Sort			
Merge Sort			
Quicksort			
Heapsort			

- 1.1 Give a best and worst case input for insertion sort.
- 1.2 Do you expect selection or insertion sort to run more quickly on a reverse list?
- 1.3 Give a worst case input for quicksort. Assume that we're always picking the left-most item as our pivot.
- 1.4 Why does Java's built-in `Array.sort` method use quicksort for `int`, `long`, `char`, or other primitive arrays, but merge sort for all `Object` arrays?

## 2 Inversions & Decisions

We have a list of  $N$  elements that should be sorted, but to our surprise we recently discovered that there are at most  $k$  pairs out of order, or  $k$  **inversions**, in the list. As a small example, the list  $\{ 0, 1, 2, 6, 4, 5, 3 \}$  contains 5 inversions:  $(6,4), (6,5), (6,3), (4,3), (5,3)$ .

- 2.1 Given a list of objects that is totally sorted except for  $K < \log N$  randomly chosen elements that are out of place, choose the best sorting algorithm to solve the problem and give a tight asymptotic runtime bound.
  
- 2.2 What's the best sorting algorithm to apply on an array of  $N$  randomly distributed objects? Give a tight asymptotic runtime bound as well.

## 3 What's that sort?

- 3.1 Each of the following sequences represent an array being sorted at some intermediate step. Match each sample with one of the following sorting algorithms: **insertion sort**, **selection sort**, **heap sort**, **merge sort**, **quicksort**. The original array is below.

5103 9914 0608 3715 6035 2261 9797 7188 1163 4411

- |     |  |                |
|-----|--|----------------|
| (a) | 5103 9914 0608 3715 2261 6035 7188 9797 1163 4411<br>0608 2261 3715 5103 6035 7188 9797 9914 1163 4411 | Merge sort     |
| (b) | 0608 1163 5103 3715 6035 2261 9797 7188 9914 4411<br>0608 1163 2261 3715 6035 5103 9797 7188 9914 4411 | Selection sort |
| (c) | 9797 7188 5103 4411 6035 2261 0608 3715 1163 9914<br>4411 3715 2261 0608 1163 5103 6035 7188 9797 9914 | Heap sort      |
| (d) | 5103 0608 3715 2261 1163 4411 6035 9914 9797 7188<br>0608 2261 1163 3715 5103 4411 6035 9914 9797 7188 | Quicksort      |
| (e) | 0608 5103 9914 3715 6035 2261 9797 7188 1163 4411<br>0608 2261 3715 5103 6035 9914 9797 7188 1163 4411 | Insertion sort |