

Table of Contents

- [Virtul Env](#)
- [Useful Command](#)
- [Expressions](#)
- [Functions](#)
 - [Environment Diagrams](#)
 - [Functions](#)
- [Testing](#)
- [Control](#)
- [Lambda](#)
- [Higher order Functions](#)
- [Recursive Functions](#)
- [Data Abstraction](#)
- [Built-in Types](#)
- [Trees](#)
- [Mutable Sequence](#)
- [Program Decomposition & Debugging](#)
- [Multable Functions & None Local](#)
- [Iterators](#)
- [Measuring Growth](#)
- [Object Oriented Programming](#)
- [Linked List, Tree and Property Methods](#)
- [Magic Methods](#)
- [Error Handling](#)
- [miscellaneous](#)
- [Scheme](#)
- [Streams](#)
- [Interpreter](#)
- [SQL\(Declarative Language\)](#)

Virtual Environment

```

1 #global
2 pip install virtualenv
3 pip list
4 which python
5 mkdir []
6 cd
7 virtualenv project1_env
8 virtualenv -p usr/bin/python2.6 py26_env #define python versino
9 source project1_env/bin/activate #activate
10 pip install ...
11 pip freeze --local > requirements.txt #save local environment packages list
12 pip install -r requirements.txt #install according to the txt file
13 deactivate #back to global
14 rm -rf #get rid of it

```

useful commands

```

1 python3 -i lab00.py //open interactive shell with this module
2 python3 -m doctest lab00.py //run doctests inside the file
3
4 //doctest example
5 """
6 >>> twenty_nineteen()
7 2019
8 """
9

```

Expressions

```

1 shakes = open('shakespeare.txt') #open file
2 text = shakes.read().split()
3 text.count('the') #count the number of apperence 'the'
4 words = set(text)
5 'the' in words #the value is a boolean 'True'
6
7 'draw'[::-1] #reverse the word, the last :-1 means step -1 (when it's neg
8 #It means starting from the end
9 w = "the"
10 words = set(open('/usr/share/dict/words').read().split()) #open the default dictionary in mac
11 {w for w in words if w[::-1] == w and len(w) == 4} #evaluated to a list of palindrome
12
13 7//4 #divide 7 by 4 and floor the result

```

Functions

```
1 ctrl+l //clear the screen
2
3 from math import pi
4 from math import sin
5 sin(pi/2)
6
7 f = max
8 f(1,2,3)    //return 3
9
10 from operator import add, mul
```

Python

Ways to bind a name

- import
- assignment
- def statement

"def" statement e.g. `python def square(x): return mul(x, x)`

Types of Expressions

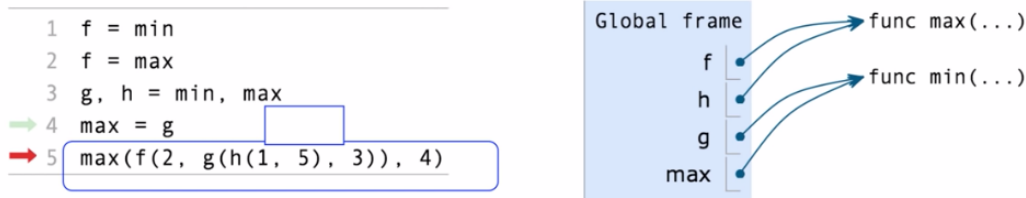
- Primitive expressions(2 add 'hello')
 - Number or Numeral (e.g. 2)
 - Name (e.g. add)
 - String (e.g. 'hello')
- Call expressions(max(2, 3))
 - operator (e.g. max)
 - operand(e.g. 2 | 3)

Environment Diagrams



Execution rule for assignment statements:

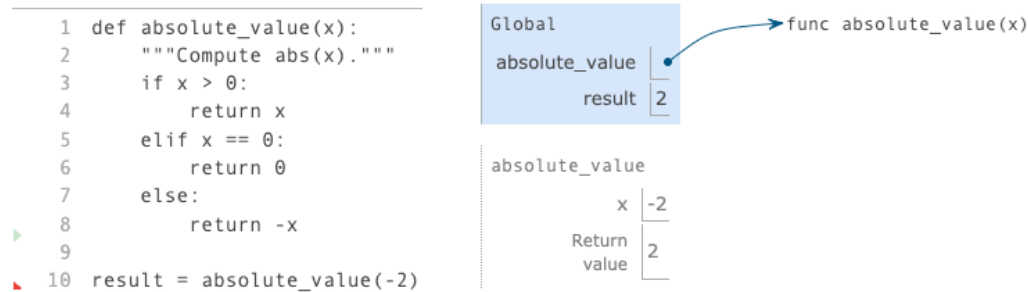
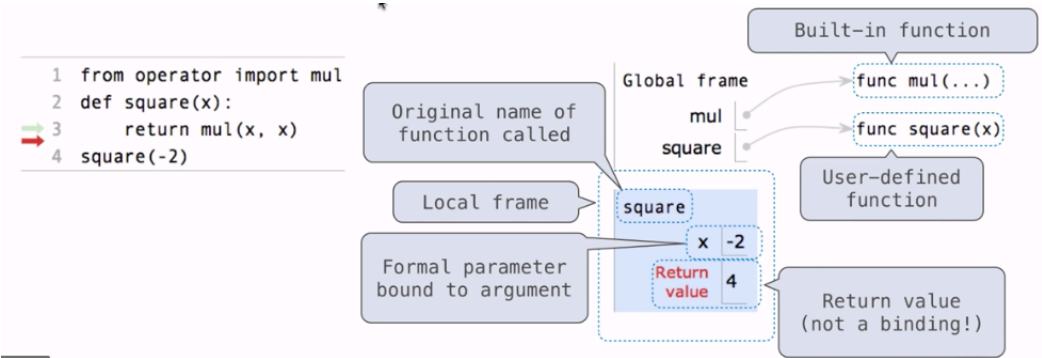
1. Evaluate all expressions to the right of = from left to right.
2. Bind all names to the left of = to the resulting values in the current frame.



Functions

Means of Abstraction

- Assignment
- Function definition



[return to the top](#)

Testing

Assertions

```
1 | assert fib(8) == 13, 'The 8th Fib number should be 13'
```

Python

If the expression is - True, nothing will happen - False, it will cause an error, halt the execution and print the message

Doctests

Python

```

1  """
2  >>> sum_nat(10)
3  55
4  >>> sum_nat(100)
5  5050
6  """

```

Run Tests

1. Run all the tests

Python

```

1  >>> from doctest import testmod
2  >>> testmod() //run all the tests

```

1. run specific function test

Python

```

1  >>> from doctest import run_docstring_examples
2  >>> run_docstring_examples(sum_nat, globals(), True)    //sum_nat: function name, globals(): get

```

1. Run all the tests in a file

```

1  python3 -m doctest <python_source_file>

```

[return to the top](#)

Control

Print

Python

```

1  print(1,2,3)
2  1 2 3
3
4  print(None, None)
5  None None
6
7  print(print(1), print(2))
8  1
9  2
10 None None

```

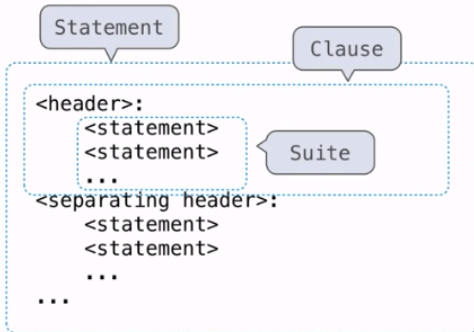
Miscellaneous Python Feature

```

1 | 2013 // 10 //truediv div and ignore the reminder (floordiv)
2 | 2013 % 10 //mod(2013, 10)

```

Compound Statements



The first header determines a statement's type

The header of a clause "controls" the suite that follows

```

def absolute_value(x):
    """Return the absolute value of x."""
    if x < 0:
        return -x
    elif x == 0:
        return 0
    else:
        return x

```

1 statement,
3 clauses,
3 headers,
3 suites

[return to the top](#)

Lambda

Lambda Expressions

```

1 | (lamdda x: x*x)(3) //call lambda function with arguement 3
2 |
3 | square = lambda x: x*x
4 | square(4) //return 16

```

Difference between def ~ and lambda - function has a name when using def

```

1 | //using lambda
2 | >>> square
3 | <function <lambda> at 0x1003c1bf8>
4 |
5 | //using def
6 | >>> square
7 | <function square at 0x10293e730>

```



[return to the top](#)

week1 miscellaneous

```
1 >>> 19 and 21
2 21
```

Python

- inner call goes first because operands must be evaluated before calling a function

```
1 def yes(guess):
2     if guess == 'yes':
3         return 'yes'
4     return 'no'
5
6 def go(x):
7     return x + yes(x)
8
9 go(go('yes'))
10
11 """
12 f global
13 f1 go(inside)
14 f2 yes
15 f3 go(outside)
16 f4 yes
17 """
```

Python

- There is no quotes for the output of print function but there is quotes if a string is returned

```
1 >>> print('fuck')
2 fuck
3
4 >>> 'fuck'
5 'fuck'
```

Python

- There is no difference between single and double quotes in python

""(empty string), 0, False, None means False**

- always prefer to show the latest one

- show nothing if None
- show only what evaluated
- comparison operator(like >) has higher priorities than the keywords: and, or

```
1 >>> -3 and True
2 True
3 >>> True and -3
4 -3
5
6 >>> False or None
7
8 >>> None or False
9 False
10
11 >>> True or 3
12 True
13
14 >>> 3 or True
15 3
16
17 >>> False and ''
18 False
19
20 >>> '' and False
21 ''
22
23 >>> 1 or 0==0
24 1
```

Python

- variables passed in as parameters can be changed directly

```
1 def say(s0):
2     for i in range(10):
3         s0 += 1
4     return s0
```

Python

- print

```
1 >>> print(10, 20)
2 10 20
```

Python

[return to the top](#)

Higher-order function:

- A function that takes a function as an argument or returns a function

- A function's domain is the set of all inputs it might possibly take as arguments.
- A function's range is the set of output values it might possibly return.
- A function's behavior is the relationship it creates between input and output.

```

1 def apply_twice(f, x):
2     return f(f(x))
3
4 def square(x):
5     return x * x
6
7 result = apply_twice(square, 2)

```

[Edit code](#)

<< First < Back Program terminated Forward > Last >>

→ line that has just executed
→ next line to execute

Frames	Objects
Global frame	func apply_twice(f, x) [parent=Glob]
apply_twice	func square(x) [parent=Global]
square	
result	16
f1: apply_twice [parent=Global]	
f	func square(x) [parent=Global]
x	2
Return value	16
f2: square [parent=Global]	
x	2
Return value	4
f3: square [parent=Global]	
x	4
Return value	16

```

1 #return a function
2 """
3 >>> adder = make_adder(3)
4 >>> adder(4)
5 7
6 """
7
8 def make_adder(n):
9     def adder(k):
10         return k + n
11     return adder
12
13
14
15 >>> make_adder(1)(3)
16 >>> 4

```

Python

Nested def

```

1 def make_adder(n):
2     def adder(k):
3         return k + n
4     return adder
5
6 add_three = make_adder(3)
7 add_three(4)

```

Frames	Objects
Global frame	func make_adder(n) [parent=Global]
make_adder	func adder(k) [parent=f1]
add_three	
f1: make_adder [parent=G]	
n	3
adder	func adder(k) [parent=f1]
Return value	
f2: adder [parent=f1]	
k	4
Return value	7

[return to the top](#)

Recursive Functions

- A function is called recursive if the body of that function calls itself, either directly or indirectly.

```
1 def fact_iter(n):
2     total, k = 1, 1
3     while k <= n:
4         total, k = total*k, k+1
5     return total
```

Python

$$n! = \prod_{k=1}^n k$$

```
1 def fact(n):
2     if n == 0:
3         return 1
4     else:
5         return n * fact(n - 1)
6
7 fact(3)
```

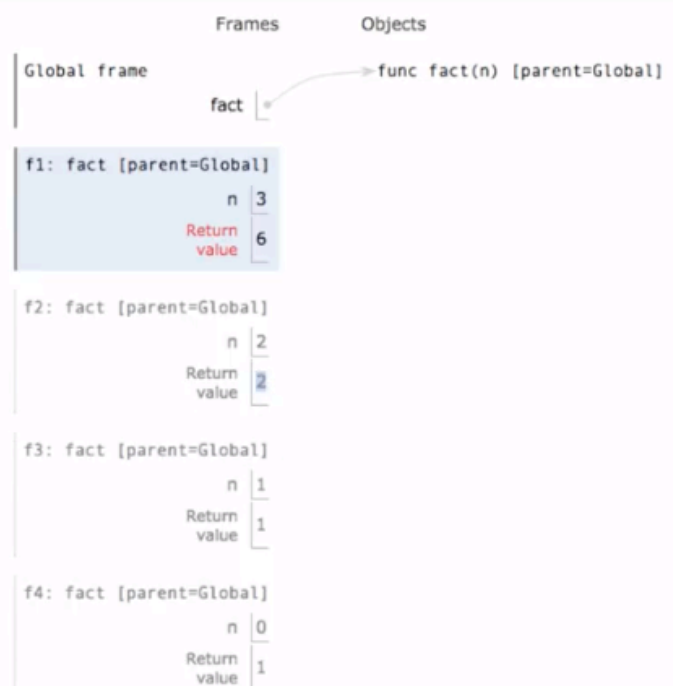
Python

```
1 def fact(n):
2     if n == 0:
3         return 1
4     else:
5         return n * fact(n-1)
6
7 fact(3)
```

[Edit code](#)

Step 18 of 18

line that has just executed
next line to execute



Tree Recursion

```

1 #like a true
2 def fib(n):
3     if n == 1:
4         return 1
5     elif n == 0:
6         return 0
7     else:
8         return fib(n) + fib(n-1)

```

trace decorator

```

1 from ucb import trace
2 @trace #???
3 def fib(n):
4     if n == 1:
5         return 1
6     elif n == 0:
7         return 0
8     else:
9         return fib(n) + fib(n-1)
10
11 """trace enable tracing for every step like:
12 >>> fib(0)
13     fib(0):
14     fib(0) -> 0
15     1
16 """

```

Mutual Recursion

The Luhn Algorithm

- Used in the numbers of credit cards
- If any digit is changed, the sum won't be a multiple of 10

original	1	3	8	7	4	3	sum
result	2	3	1+6=7	7	8	3	30

- Start from the right most digit
- Double the value of every second digit
- If product is greater than 9 then sum the 2 digits
- Take the sum of all the digits, it is a multiple of 10

```

1  def split(n):
2      return n // 10, n % 10
3
4  def sum_digits(n):
5      if n < 10:
6          return n
7      else:
8          all_but_last, last = split(n)
9          return sum_digits(all_but_last) + last
10
11 def luhn_sum(n):
12     if n < 10:
13         return n
14     else:
15         all_but_last, last = split(n)
16         return last + luhn_sum_double(all_but_last)
17
18 def luhn_sum_double(n):
19     all_but_last, last = split(n)
20     luhn_digit = sum_digits(2 * last)
21     if n < 10:
22         return luhn_digit
23     else:
24         return luhn_sum(all_but_last) + luhn_digit

```

- Be able to convert between iteration and recursion

Cascade

```

1  def cascade(n):
2      if n < 10:
3          print(n)
4      else:
5          print(n)
6          cascade(n//10)
7          print(n)
8
9  """
10 >>> cascade(5)
11 12345
12 1234
13 123
14 12
15 1
16 12
17 123
18 1234
19 12345
    """

```

```

1  def invese_cascade(n):
2      grow(n)
3      print(n)
4      shrink(n)
5
6  def f_then_g(f, g, n):
7      if n:
8          f(n)
9          g(n)
10
11  grow = lambda n: f_then_g(grow, print, n // 10)
12  shrink = lambda n: f_then_g(print, shrink, n // 10)
13  """
14  >>> inverse_cascade(4)
15  1
16  12
17  123
18  1234
19  123
20  12
21  1
22  """

```

Count Partitions

$2 + 4 = 6$
 $1 + 1 + 4 = 6$
 $3 + 3 = 6$
 $1 + 2 + 3 = 6$
 $1 + 1 + 1 + 3 = 6$
 $2 + 2 + 2 = 6$
 $1 + 1 + 2 + 2 = 6$
 $1 + 1 + 1 + 1 + 2 = 6$
 $1 + 1 + 1 + 1 + 1 + 1 = 6$

Divide and Conquer

- include 4
- not include 4

```

1  """
2  >>> count_partitions(6, 4)
3  9
4  """
5
6  def count_partitions(n, m):
7      if n == 0:
8          return 1
9      elif n < 0:
10         return 0
11         elif m == 0:      #If m reaches 0 first, it will rely on the first term to add all 1s into the
12             return 0
13
14         return count_partitions(n - m, m) + count_partitions(n, m - 1)

```

[return to the top](#)

Data Abstraction

- Compound objects combine objects together
 - A data: a year, a month, and a day
- An abstract data type lets us manipulate compound objects as units
- Isolate two parts of any program that uses data:
 - How data are represented (as parts)
 - How data are manipulated (as units)
- Data abstraction: a methodology by which functions enforce an abstraction barrier between representation and use
- Terminology
 - ADT : Abstract Data Type ``python import fractions import gcd #constructor def rational(n, d):
g = gcd(n, d) return [n//g, d//g]

alternative way, instead of list

```
def rational(n, d): g = gcd(n, d) def select(name): if name == 'n': return n//g: elif name == 'd': return d//g return select
```

selector

```
def numer(x): return x[0]
```

selector:

```
def denom(x): return x[1]
```

```
def mul_rational(x, y): return rational(number(x) * number(y), denom(x) * denom(y))
```

```
def equal_rational(x, y): return number(x) * denom(y) == number(y) * denom(x)
```

```
1  
2 ##### Pairs  
3 ```python  
4 >>> pair = [1, 2]  
5  
6 >>> x, y = pair #unpacking a list  
7  
8 >>> from operator import getitem  
9 >>> getitem(pair 0)  
10 1  
11 >>> getitem(pair 1)  
12 2
```

Abstraction Barriers

Parts of the program that...	Treat rationals as...	Using...
Use rational numbers to perform computation	whole data values	<code>add_rational, mul_rational</code> <code>rational_are_equal, print_rational</code>
Create rationals or implement rational operations	numerators and denominators	<code>rational, numer, denom</code>
Implement selectors and constructor for rationals	two-element lists	list literals and element selection
<i>Implementation of lists</i>		

[return to the top](#)

Built-in Types

Lists

```
1 digits = [1, 2]  
2 from operator import mul, add  
3 >>> add[2, 7] + mul(digits, 2)  
4 [2, 7, 1, 2, 1, 2]  
5 >>> [2, 7] + digits * 2  
6 [2, 7, 1, 2, 1, 2]
```

Python

Containers

```
1 >>> 1 in digits
2 True
3
4 >>> 1 not in digits
5 False
6
7 >>> [1, 7] in digits
8 False
9
10 >>> [1, 2] in [3, [1, 2], 4]
11 True
12 >>> [1, 2] in [3, [[1, 2]], 4]
13 False
```

Python

For Statements

```
1 for <name> in <expression>:
2     <suite>
3
4 #unpacking in for
5 for x, y in pairs:
6     if x == y:
7         print(1)
```

Python

Range

- a sequence of consecutive integers ``python >>> List(range(-2, 2)) [-2, -1, 0, 1]

```
for _ in range(3): #Don't care about the number print('Go Bears!')
```

List Comprehensions

```
1 >>> letters = ['a', 'b', 'c', 'd', 'e', 'f', 'g', 'h', 'm', 'n', 'o', 'p']
2 >>> [letters[i] for i in [3, 4, 6, 8]]
3 ['d', 'e', 'm', 'o']
4
5 >>> odds = [1, 3, 5, 7, 9]
6 >>> [x+1 for x in odds if 25 % x == 0]
7 [2, 6]
```

Python

Strings


```

1  >>> exec('curry = lambda f: lambda x: lambda y: f(x, y)')
2  >>> curry
3  'curry = lambda f: lambda x: lambda y: f(x, y)'
4
5  >>> """The highness"""
6  'The highness'
7
8  >>> city = 'Berkeley'
9  >>> city[3]
10 'k' #no character, only string
11
12 >>> 'here'in "where's Waldo?"
13 True

```

Dictionaries

- No order at all ``python >>> n = {'a':1, 'b':2} >>> n.keys() >>> n.values() >>> n.items()

```
itemslist = [('a', 1), ('b', 2), ('c', 3)] a = dict(itemslist) a['a'] 1
```

```
a.get['a', 0] #default 0
```

```
{x:x*x for x in range(10)} {0: 0, 1: 1, 2: 4, 3: 9, 4: 16, 5: 25, 6: 36, 7: 49, 8: 64, 9: 81}
```

```
{1: 2} #error `` return to the top
```

Trees

Slicing

```

1  >>> odds = [3, 5, 7, 9, 11]
2  >>> odds[:3] = [3, 5, 7]

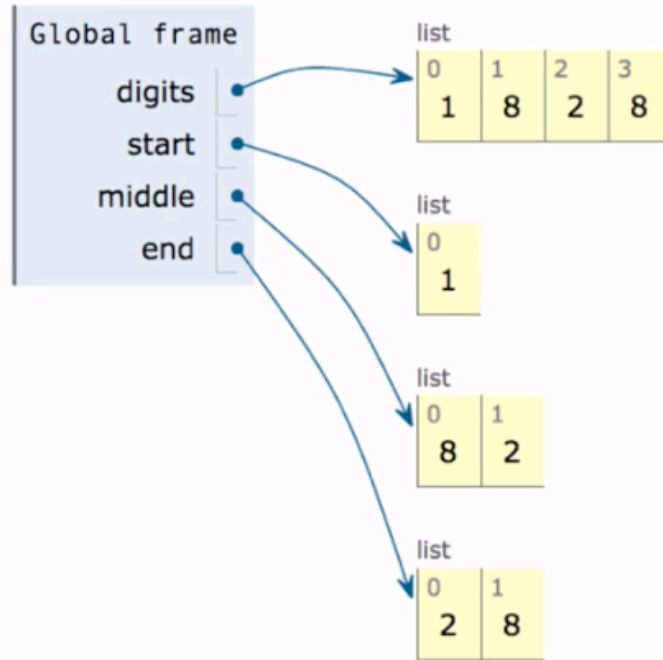
```

slicing creates new values

```

1 digits = [1, 8, 2, 8]
2 start = digits[:1]
3 middle = digits[1:3]
→ 4 end = digits[2:]

```



Processing Container Values

```

1 >>> sum([2,3,4], 1)      #Doesn't work with string, 1 is starting value not index
2 7
3 >>> sum([2,3], [4]), []
4 [2, 3, 4]
5
6 >>> max(0, 1, 2, 3, 4)
7 4
8 >>> max(range(5))
9 4
10 >>> max(range(10), key=lambda x: 7-(x-4)*(x-2))
11 3
12 >>> bool(5)
13 True
14
15 >>> all(range(0, 5})     #return True is every element bool(e) is True
16 >>r all(range(1, 5})
17 True

```

Python

Tree

```

1 def tree(label, branches=[]):
2     for branch in branches:
3         assert is_tree(branch), 'branches must be trees'
4     return [label] + list(branches)
5
6 def is_tree(tree):

```

Python

```

7     if len(tree) < 1 or type(branch) != list:
8         return False
9     for branch in branches(tree):
10         if not is_tree(branch):
11             return False
12
13     return True
14
15 def label(tree):
16     return tree[0]
17
18 def branches(tree):
19     return tree[1:]
20
21 def is_leaf(tree):
22     return not branches(tree)
23
24 def fib_tree(n):
25     if n <= 1:
26         return tree(n)
27     else:
28         left, right = fib_tree(n-2), fib_tree(n-1)
29         return tree(label(left)+label(right), [left, right])
30
31 def count_leaves(t):
32     if is_leaf(t):
33         return 1
34     else:
35         return count([count_leaves for b in branches(t)])
36
37 def leaves(tree):
38     if is_leaf(tree):
39         return [label(tree)]
40     else:
41         sum([leaves(l) for l in branches(tree)], [])
42
43 #only increment leaves
44 def increment_leaves(t):
45     if is_leaf(t):
46         return tree(label(t)+1)
47     else:
48         bs = [increment_leaves(b) for b in branches(t)]
49         return tree(label(t), bs)
50
51 def increment_leaves(t):
52     return tree(label(t)+1, [increment(b) for b in branches(t)])
53
54 def print_tree(t, indent=0):
55     print(' ' * indent + str(label(t)))
56     for b in branches(t):
57         print_tree(b, indent+1)
58

```

```
59 >>> print(' ' * 5 + str(5))
60     5
```

[return to the top](#)

Mutable Sequence

Objects

```
1 >>> from datetime import date
2 >>> today = date(2015, 2, 20)
3 >>> final = date(2015, 5, 12)
4 >>> str(freedom - today)
5 '81 days, 0:00:00'
6 >>> today.year
7 2015
8 >>> today.month
9 2
10 >> today.strftime('%A %B %d')
11 'Friday February 20'
```

Python

- A type of object is a class; classes are first-class values in Python, can be passed as parameters
- Everything in python is an object

Mutation Operations

```
1 >>> suits = ['coin', 'string', 'myriad']
2 >>> suits.pop()
3 'myriad'
4 >>> suits.pop(0)
5 'coin'
6 >>> suits.remove('string') #return None, no return
7 >>> suits.extend(['sword', 'club'])
```

Python

Tuples

```
1 >>> (3, 4) + (5, 6)
2 (3, 4, 5, 6)
3
4 >>> {(3, 4):5} #a tuple can be a key
5 >>> {(3, [4, 6]):5} #wrong a tuple can't be a key if there's any list inside
6
7 >>> a = ([1,2], 4)
8 >>> a[0].append(3)
9 >>> a
10 ([1,2,3], 4)
```

Python

Mutation

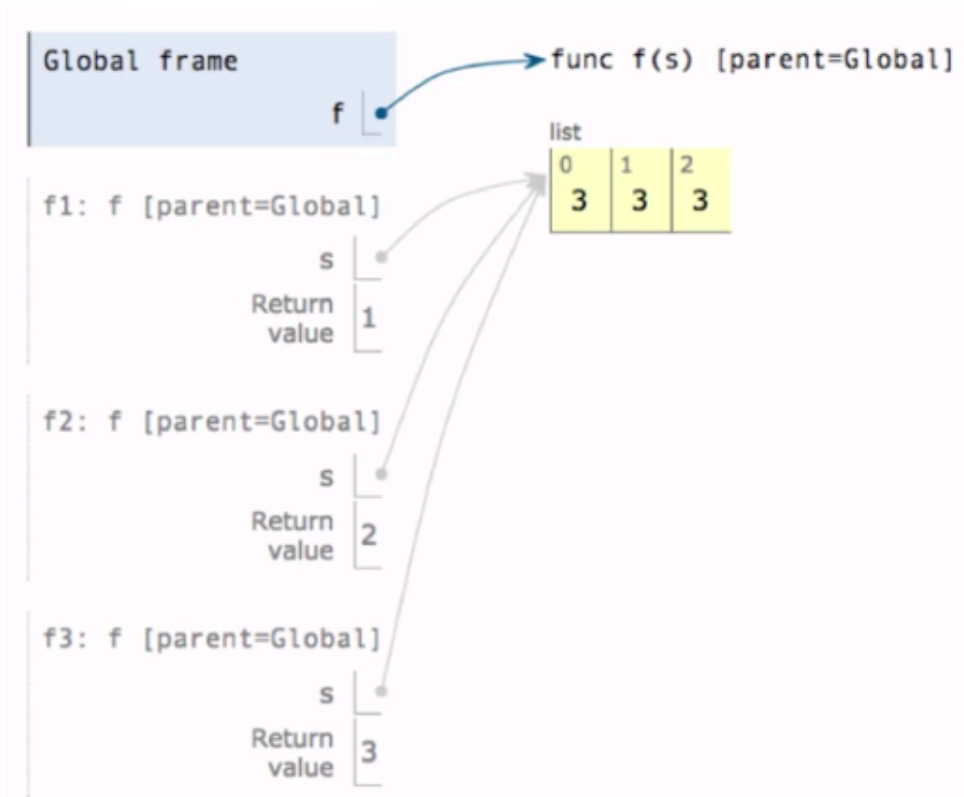
```
1 >>> a = [10]
2 >>> b = a
3 >>> a == b
4 True
5 >>> a.append(20)
6 >>> a == b
7 True
8
9 >>> a = [10]
10 >>> b = [10]
11 >>> a == b
12 True
13 #identity operator
14 >>> a is b
15 False
```

Python

Mutable Default Arguments are Dangerous

```
1 >>> def f(s=[]):
2 ...     s.append(5)
3 ...     return len(s)
4 >>> f()
5 1
6 >>> f()
7 2
8 >>> f()
9 3
```

Python



[return to the top](#)

Program Decompositio and Debugging

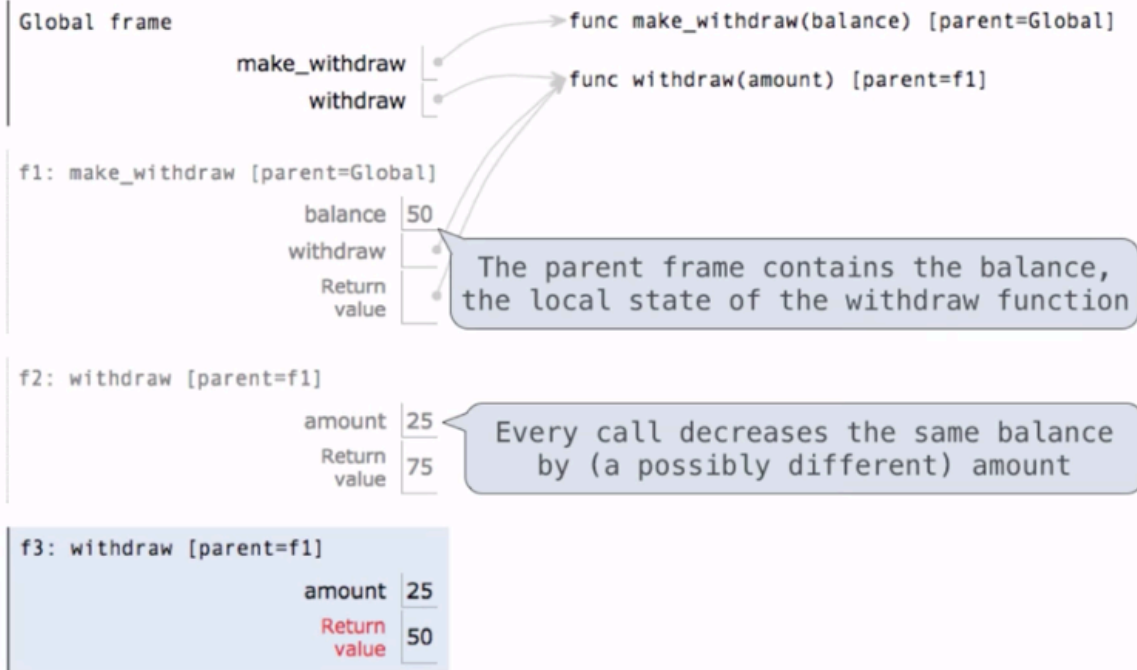
- Function Rules in Practice
 - solve one problem
 - smallest number of parameters
 - repeated sequence should be put in its own function

[return to the top](#)

Mutable Functions and None Local

```
1 >>> withdraw = make_withdraw(100)
2 >>> withdraw(25)
3 75
4 >>> withdraw(25)
5 50
```

Python



```

1
2 def make_withdraw(balance):
3     def withdraw(amount):
4         nonlocal balance
5         if amount > balance:
6             return 'Insufficient funds'
7         balance = balance - amount
8         return balance
9     return withdraw

```

Python

- balance is rebind in the first non-local frame (enclosing scope in python doc)
- The name must not collide with pre-existing bindings in the local scope
- If there's not 'balance' exist in the upper layers of frames, it will cause an error
- If there's a local binding for 'balance', it will also cause an error
- a variable defined in the global frame can not be declared non-local, must be used in higher order functions

python particularly pre-computes wich frame contains each name before executing the body of a function.

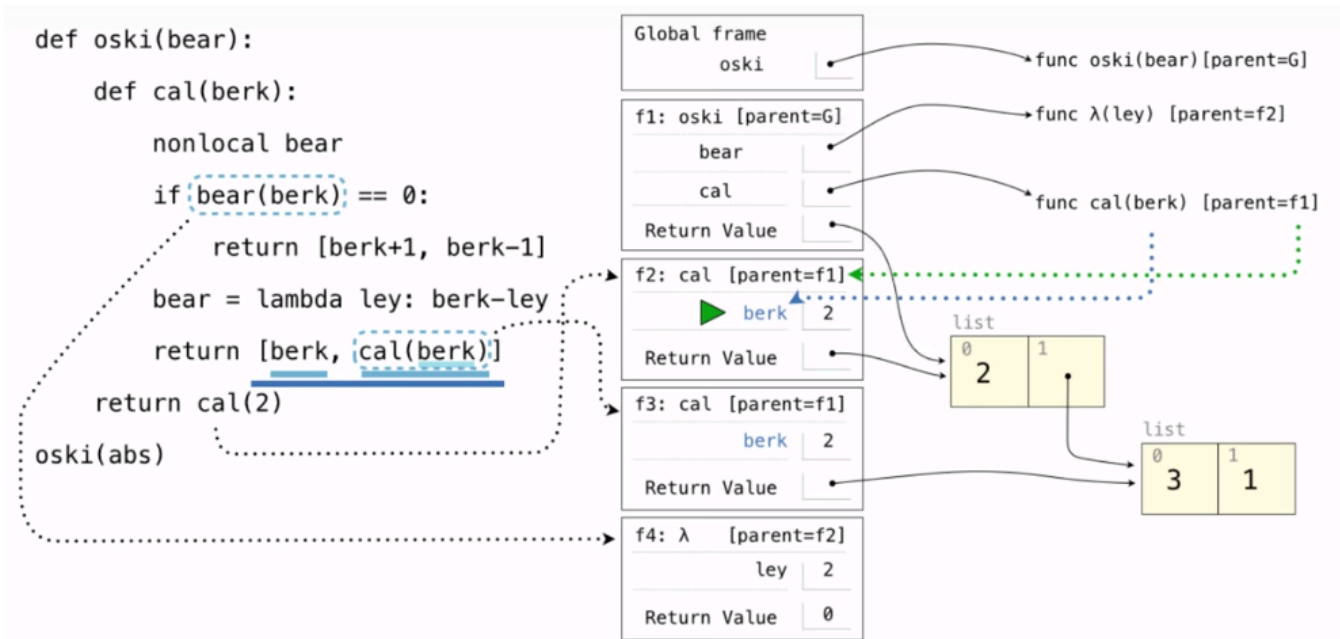
Within the body of a function, all instances of a name must refer to the same frame

```

1 #alternative
2 def make_withdraw_list(balance):
3     b = [balance]
4     def ...

```

Python



[return to the top](#)

Iterators

```
1 """
2 iter(iterable)
3 next(iterator)
4 """
5 >>> s = [3, 4, 5]
6 >>> t = iter(s)
7 >>> next(t)
8 3
9 >>> next(t)
10 4
11 >>> next(t)
12 5
13 >>> next(t)
14 StopIteration Error #end if go outside the list
```

Iterate through dictionary

- keys, values, items of a dictionary are all iterables, the order of items is the order they were added(python 3.6+)
- if the shape or structure of the dictionary is changed while being iterated, there will be an error.(It's ok to change the values)
- The modification of the list will affect the result of showing through an iterator

```
1 >>> i = iter(d.items())
2 >>> next(i)
3 ('one', 1)
```


Iterator and For

- Iterator will be moved by for

```
1 >>> r = range(3, 6)
2 >>> it = iter(r)
3 >>> next(it)
4 3
5 >>> for i in it:
6 ...     print(i)
7 ...
8 4
9 5
10 >>> for i in it:
11 ...     print(i)
12 ...
13 #Nothing because it already reached the end of the iterable
```

Python

- Built-in functions for Iteration

```
1 #func here will apply lazily (when we ask for the ith value
2 #they all return iterators
3
4 map(func, iterable)    #Iterate over func(x) for x in iterable, return map object
5 filter(func, iterable) #Iterate over x in iterable if func(x)
6 zip(first_iter, second_iter) #Iterate over co-indexed (x, y) pairs
7 reversed(sequence)    #Iterate over x in a sequence in reverse order
8
9 list(iterable)
10 tuple(iterable)
11 sorted(iterable)      #Create a sorted list containing x in iterable
12
13 >>> bcd = ['b', 'c', 'd']
14 >>> [x.upper() for x in bcd]
15
16 >>> list(iterator)    #create a list using iterator
```

Python

Generators

```
1 #yield all the paths that reach the value x
2 #yield will only 1 layer a time, it won't cause duplicated sub-paths
3 def generate_paths(t, x):
4     if t.label == x:
5         yield [t.label]
6     for b in t.branches:
7         for path in generate_paths(b, x):
8             if path:
9                 yield [t.label] + path
```

Python

```
10
11
12
13 >>> def plus_minus(x):
14 ...     yield x
15 ...     yield -x
16
17 >>> t = plus_minus(3)
18 >>> next(t)
19 3
20 >>> next(t)
21 -3
22 >>> t
23 <generator object ....>
24
25 def evens(start, end):
26     even = start + (start % 2)
27     while even < end:
28         yield even
29         even += 2
30
31 >>> list(evens(1, 10))
32 [2, 4, 6, 8]
33 >>> t = evens(2, 10)
34 >>> next(t)
35 2
36
37
38 >>> list(a_then_b[3, 4], [5, 6]))
39 [3, 4, 5, 6]
40
41 def a_then_b(a, b):
42     yield from a
43     yield from b
44
45
46
47 >>> list(countdown(5))
48 [5, 4, 3, 2, 1]
49
50 def countdown(k):
51     if k > 0:
52         yield k
53         yield from countdown(k-1)
54
55
56 def countdown(k):
57     if k > 0:
58         yield k
59         yield countdown(k-1)
60 >>> t = countdown(3)
61 >>> next(t)
```

```

62 3
63 >>> next(t)
64 <generator object countdown ....>
65
66
67 def prefixes(s):
68     if s:
69         yield from prefixes(s[:-1])
70         yield s
71 >>> list(prefixes('both'))
72 ['b', 'bo', 'bot', 'both']
73
74 def substrings(s):
75     if s:
76         yield from prefixes(s)
77         yield from substrings(s[1:])
78 >>> list(substrings('tops'))
79 t, 'to', 'top', 'tops', 'o', 'op', 'ops', 'p', 'ps', 's']

```

[return to the top](#)

Growth

```

1 total = 0
2 def count(f):
3     def counted_f(*args):
4         global total
5         total += 1
6         return f(*args)
7     return counted_f
8
9 def fact(n):
10     if n<=1:
11         return 1
12     return n * fact(n-1)
13
14 >>> fact = count(fact)
15 >>> fact(10)
16 xxxxx
17 >>> total
18 10

```

Python

[return to the top](#)

Object Oriented

- Method calls are messages passed between objects
- A class statement creates a new class and binds that class to in the first frame of the current environment

```
1 #find in instance, then class
2 >>> getattr(tom_account, 'balance')
3 10
4
5 >>> hasattr(tom_account, 'deposit')
6 True
7
8 >>> type(Account.deposit)
9 <class 'function'>
10 >>> type(tom_account.deposit)
11 <class 'method'>
12
13 >>> Account.deposit(tom_account, 1001)
14 1001
```

Attributes

- All objects have attributes, which are name-value pairs
- Methods are also attributes of the class

```

1 class Account:
2     interest = 0.02
3     def __init__(self, holder):
4         self.holder = holder
5         self.balance = 0
6
7 #If the attribute of the instance doesn't exist, it will create one
8 >>> tom_account.interest = 0.08
9 >>> tom_account.interest
10 0.08
11
12 #use parent class method
13 Account.withdraw(self, ~)
14
15 >>> self.withdraw_fee #This will evaluated to the class attribute if there's no one for the inst
16 >>> self.withdraw_fee += 10 #This will also evaluated to the class attribute if there's no one f
17
18
19 class Dog:
20     def bark(self):
21         print('woof!')
22
23 >>> lacey = Dog()
24 >>> lacey.bark = Dog.bark
25
26 >>> lacey.bark()
27 Error #need an arguement self
28
29 #kind is a class name
30 def get_object(kind):
31     return kind()

```

Composition

- One object hold another one as an attribute

```

1 class B:
2     n = 4
3     def __init__(self, y):
4         self.z = self.f(y)
5
6 class C(B):
7     def f(self, x):
8         return x
9
10 #Even if it calls the parent's method, the self is still represent itself
11 >>> C(2).z
12 2

```

[return to the top](#)

Linked Lists

```
1 | isinstance(rest, Link) #to see whether rest is a Link
```

Python

Property Methods

- They are called implicitly

```
1 | class Link:
2 |     @property
3 |     def second(self):
4 |         return self.rest.first
5 |
6 |     @second.setter
7 |     def second(self, value):
8 |         self.rest.first = value
9 |
10 | #[3, 4, 5]
11 | >>> s.second
12 | 4
13 | >>> s.second = 5
14 | >>> s.second
15 | 5
```

Python

[return to the top](#)

Magic Methods

```

1 class A:
2
3     def __str__(self):
4         return 'A object'
5
6
7 >>> print(A())
8 A object
9
10
11 class A:
12     def __repr__(self):
13         return 'A object'
14
15 >>> a = A()
16 #str default use repr
17 >>> print(a)
18 A object
19 >>> a
20 A object

```

```

1 #Full linked list
2 class Link:
3     empty = ()
4     def __init__(self, first, rest=empty):
5         assert type(rest) is Link or \
6             rest is Link.empty, \
7             'rest must be a linked list or empty'
8         self.first = first
9         self.reset = rest
10
11     def __repr__(self):
12         if self.reset is Link.empty:
13             return 'Link(' + repr(self.first) + ')'
14         return 'Link(' + repr(self.first) + ', ' + repr(self.reset) + ')'
15
16     def __str__(self):
17         s = '<'
18         while self.reset is not Link.empty:
19             s += str(self.first) + ', '
20             self = self.reset
21         return s + str(self.first) + '>'
22
23     def __contains__(self, elem):
24         if self.first == elem:
25             return True
26         elif self.reset is Link.empty:
27             return False
28         return elem in self.reset
29

```

```

30     def __add__(self, other):
31         if self.rest is Link.empty:
32             if other.rest is Link.empty:
33                 return link(self.first, Link(other.first))
34             else:
35                 return Link(self.first, Link(other.first) + other.rest)
36         else:
37             return Link(self.first, self.rest + other)
38
39     #l*2
40     def __mul__(self, other):
41         temp = self
42         for _ in range(other - 1):
43             temp = temp + self
44         return temp
45
46     #2*l
47     def __rmul__(self, other):
48         return self * other
49
50     #len(l)
51     def __len__(self):
52         return 1 + len(self.rest)
53
54     #l[0], max(l), min(l)
55     def __getitem__(self, index):
56         if type(index) is int:
57             if index == 0:
58                 return self.first
59             return self.rest[index - 1]
60         #for slicing [1:3]
61         elif type(index) is slice:
62             start = slice.start or 0 #None then 0
63             stop = slice.stop or len(self) #None then len(self)
64             steop = index.step or 1
65
66             if stop <= start:
67                 return Link.empty
68             if start == 0:
69                 return Link(self.first, self[start + step:stop:step])
70             return self.rest[start - 1:stop - 1:step]
71
72     #start 1 stop 2 steps 3
73     >>> slice(1, 2, 3)
74
75     >>> max(l)
76     3
77     >>> min(l)
78     1
79
80     >>> l = Link(1, Link(2, Link(3)))
81     >>> l

```



```

82 Link(1, Link(2, Link(3)))
83
84 >>> print(l)
85 <1, 2, 3>
86
87 >>> 3 in l
88 True
89 >>> 5 in l
90 False
91
92 >>> l2 = Link(1, Link(3))
93
94 >>> l + l2
95 Link(1, Link(2, Link(3, Link(1, Link(3)))))

```

[return to the top](#)

Error Handling

```

1 try:
2     1 + 'hello'
3 except NameError as e:
4     print('Error message:', e)

```

Python

[return to the top](#)

Miscellaneous

week2 miscellaneous

- we aren't normally allowed to modify variables defined in parent frames

```
python def parent(previous_val): def child(): previous_val += 1 #not allowed, will cause error
```

week3 miscellaneous

```

1  >>> party = [1, 2]
2  >>> rival = party
3  >>> party = party + [4]
4  >>> rival
5  1, 2
6
7  >>> random.choice([1,2,3]) #randomly choose an element
8
9  >>> a = [1, 2]
10 >>> b = [3, 4]
11 >>> c = zip(a, b)    #c is an object
12 >>> list(c)
13 [(1, 3), (2, 4)]
14
15 >>> a = [1, 2]
16 >>> b = [3]
17 >>> list(zip(a, b))
18 [(1, 3)]

```

Which of the following operations breaks the abstraction barrier?

- a. branches(t)[0]
- b. label(t)
- c. label(branches(t)[0])
- d. t[0]
- e. branches(t)[0][1]

d e

Which of the following are necessary qualities of a function that does not need to be broken into smaller functions?

- a. The function is called in multiple other parts of the program.
- b. The function solves one problem.
- c. The function does not contain repeated sequences of code. The function is recursive.
- e. A subset of the body of the function contains logic that could be re-used in another program.

b c

Midterm Miscellaneous

```
1 >>> 1==True
2 True
3 >>> 0==False
4 True
5 >>> 2==True
6 False
7 >>> 2==False
8 False
9 >>> list(a) is a
10 False
11
12 >>> def f():
13 ...     return 'test'
14 >>> f()
15 'test'
16
17 >>> sum([1, 2, 3], 5)
18 11
19 >>> sum([1, 2, 3], [3])
20 Error
21 >>> sum([[1, 2, 3]], [4])
22 [1, 2, 3, 4]
23
24 #==, != only return True False, but and, or returns last possible value evaluated
25 >>> True==1
26 True
27 >>> True and 1
28 1
```

List

```

1  append(obj)->None
2  count(val)->int
3  extend(iterable)->None
4
5  index(val, start=0, stop=9~)->:
6  - first index of val
7  - Value Error if not exist
8
9  insert(index, object)->None
10
11 pop(index=-1)->:
12 - item removed
13 - Index Error if not found
14
15 remove(val)->: (remove first occurrence)
16 - None
17 - Error if not found
18
19 reverse()->None
20
21 sort(key=None, reverse=False)->None (default asc)

```

Dictionary

```

1  get(key, default=None)->
2  items()->iterable->iterable->tuples
3  keys()->iterable inside
4  pop(key, [d])->
5  - val
6  - d if not found
7  - error if no d and not found
8  update(dict)->None
9  values()->iterable

```

str

```

1  index(sub, [start], [end])->:
2  - int
3  - Error if not found
4
5  find(sub, [start], [end])->:
6  - int
7  - -1
8
9  replace(old, new, count=-1)->copy of str (-1 means all)
10
11 '{0} is a good {1}'.format('ly', 'boy')

```

Week5 Miscellaneous

```
1 | float('inf')    #infinity
```

Python

[return to the top](#)

Scheme

Expressions

Call Expressions

```
1  
2 > quotient  
3 #[quotient]  
4 > 'quotient  
5 quotient  
6 > /  
7 #[/]  
8  
9 ;operator in the parenthesis  
10 > (quotient 10 2)  
11 5  
12  
13 > (quotient (+ 8 7) 5)  
14 3  
15  
16 > (quotient 1 2)  
17 0  
18 > (/ 1 2)  
19 0.5  
20  
21 ;change line anywhere  
22 > (+ (* 3  
23       (+ (* 2 4)  
24           (+ 3 5)))  
25       (+ (- 10 7)  
26           6))  
27 57  
28  
29 //special cases  
30 scm> (+)  
31 0  
32 scm> (*)  
33 1  
34 scm> (* 2 2 2)  
35 8  
36 scm> +
```

Scheme

```
37 #[+]
38
39 ;number? is a name
40 scm> (number? 3)
41 #t
42 scm> (number? +)
43 #f
44 scm> (zero? 2)
45 #f
46 scm> (zero? 0)
47 #t
48 scm> (integer? 2)
49 #t
50
51 > (modulo 35 4)
52 3
53
54 > (even? 2)
55 #t
56 > (odd? 2)
57 #f
58
59 > (not (= 1 2))
60 #t
61
62 > (eq? 1 2)
63 #f
64 > (= `a `b)
65 Error
66 > (eq? `a `b)
67 #f
68 > (equal? `a `a)
69 #t
70
71 > (pair? (cons 2 nil))
72 #t
```

Special Forms

- A combination that is not a call expression

```
1 - If expression: (if <predicate> <consequent> <alternative>)
2 - And and or: (and <e1> ... <en>), (or <e1> ... <en>)
3 - Binding symbols: (define <symbol> <expression>)
4 - New procedres: (define (<symbol> <formal
5 - parameters>) <doby>)
6
7 > (define pi 3.14)
8 > (* pi 2)
9 6.28
10
11 > (define (abs x)
12     (if (< x 0)
13         (- x)
14         (x)))
15
16 >(abs -3)
17 >3
18
19 > (define (average x y)
20     (/ (+ x y) 2))
21 > (average 3 7)
22 5
23
24 > (let ((a 1)) a)
25 1
26 > (let ((a 1)(b a)) b)
27 Error
```

Recursion

```

1 scm> (define (sqrt x)
2       (define (update guess)
3         (if (= (square guess) x)
4             guess
5             (update (average guess (/ x guess))))))
6       (update 1))
7 sqrt
8 scm> (sqrt 256)
9 16
10
11
12 (define (mystery lst)
13   (cond
14     ((null? lst) #f)
15     ((eq? (car lst) 61) #t)
16     (else (mystery (cdr lst))))
17   )
18 )
19
20 > (let (v 1) (b 2) (v+b))
21 3

```

(cdr `(10 21))

lambda Expressions

```

1 lambda (<formal-parameters>) <body>
2 ;Same here
3 (define (plus4 x) (+ x 4))
4 (define plus4 (lambda (x) (+ x 4)))
5
6 ((lambda (x y z) (+ x y (squarez))) 1 2 3)

```

Pairs and Lists

Pairs

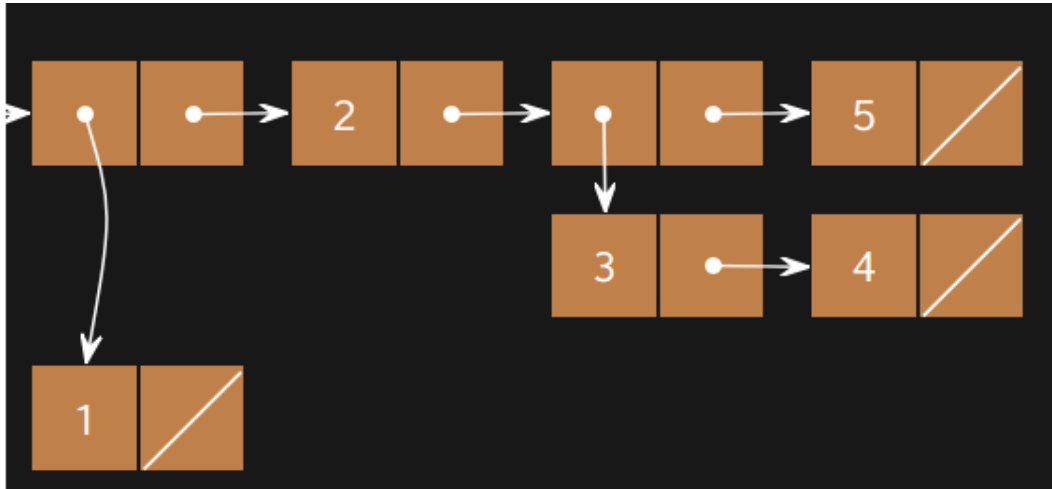
```

1 > (cons 1 2)
2 ;car return the first in the pair
3 ;cdr return the second
4 ;nil the empty list

```

List


```
1 ;The last element must be nil
2 > (cons 1 (cons 2 nil)) ;2 elements list
3 (1 2)
4
5 > (define a 1)
6 > (define b 2)
7 > (list a b)
8 (1 2)
9
10 > (list 'a 'b)
11 (a b)
12
13 > (car '(a b c))
14 a
15 > (cdr '(a b c))
16 (b c)
17
18 > (length `(1 2 3 4 5))
19 5
20
21 > (append `(1 2 3) `(4 5 6))
22 (1 2 3 4 5 6)
23
24 > (cdr (cons 1 (cons 2 nil)))
25 (2)
26 > (car (cons 1 (cons 2 nil)))
27 1
28
29 > (cons 1 `(list 2 3))
30 (1 list 2 3)
31
32 > (define l (cons 4 (cons 3 (cons 2 nil))))
33 > (append l '(1 0))
34 (4 3 2 1 0)
35
36 ;Tricky part
37 > (define a `(1))
38 > (define b (cons 2 a))
39 > b
40 (2 1)
41 > (define c (list 3 b))
42 (3 (2 1))
43 > (cdr c)
44 ((2 1))
```



- The first is val, the second is pointer - next node is at the same level - If the first is a pointer, there'll be a sub list

```

1 | > (cons (cons 1 nil) (cons 2 (cons (cons 3 (cons 4 nil)) (cons 5 nil))))
2 | ((1) 2 (3 4) 5)
3 |
4 | > (list (cons 1 nil) (cons 2 (cons (cons 3 (cons 4 nil)) (cons 5 nil))))
5 | ((1 ()) 2 (3 4) 5)

```

Scheme

Note: null? is a symbol to verify if the thing behind it is nil or not. There's no 'null'. 'nil' is just () empty list

Dynamic Scope and Lexical scope

```

1 | > (define f (lambda (x) (+ x y)))
2 |
3 | > (define g (lambda (x y) (f (+ x x))))
4 |
5 | > (g 3 7)

```

Scheme

- Lexical scope: The parent for f is the global (will cause error, no y)
- Dynamic scope: The parent for f is g

Functional Programming

- All functions are pure functions
- No re-assignment and no mutable data types
- Name-value bindings are permanent
- Advantages
 - The value of an expression is independent of the order in which sub-expressions are evaluated
 - Sub-expressions can safely be evaluated in parallel or on demand (lazily)
 - Referential transparency: The value of an expression does not change when we substitute one of its subexpression with the value of that subexpression.

But... no for/while statements, how to iteration efficient? Tail Recursion

Tail Recursion

A procedure call that has not yet returned is active. Some procedure calls are tail calls. A Scheme interpreter should support an unbounded number of active tail calls using only a constant amount of space.

A tail call is a call expression in a tail context:

- The last body sub-expression in a lambda expression
- Sub-expressions 2 & 3 in a tail context if expression
- All non-predicate sub-expressions in a tail context cond
- The last sub-expression in a tail context and or or
- The last sub-expression in a tail context begin

```
(define (factorial n k)
  (if (= n 0) k
      (factorial (- n 1)
                  (* k n))))
```

- A call expression is not a tail call if more computation is still required in the calling procedure.
- Linear recursive procedures can often be re-written to use tail calls.

```
(define (length s)
  (if (null? s) 0
      (+ 1 (length (cdr s)))))
```

Not a tail context

```
(define (length-tail s)
  (define (length-iter s n)
    (if (null? s) n
        (length-iter (cdr s) (+ 1 n))))
  (length-iter s 0))
```

More Examples

```
;; Compute the length of s.
(define (length s)
  (+ 1 (if (null? s)
            -1
            (length (cdr s))) ) )
```

Not a tail recursion call

Map and Reduce

Reduce

```
1 (define (reduce procedure s start)
2   (if (null? s) start
3       (reduce procedure
4               (cdr s)
5               (procedure start (car s)))))
6 ;it depends on the procedure, if it's a constant space produce it's constant space
7
8 > (reduce * `(3 4 5) 2)    ;2 * 3 * 4 *5
9 120
10 > (reduce (lambda (x y) (cons y x)) `(3 4 5) `(2))
11 (5 4 3 2)
```

Scheme

Map

```

1 ;Not a tail recursion version
2 (define (map procedure s)
3   (if (null? s)
4       nil
5       (cons (procedure (car s))
6             (map procedure (cdr s)))))
7
8 exp:
9 (map (lambda (x) (- 5 x)) (list 1 2))
10
11 (define (map procedure s)
12   (define (map-reverse s m)
13     (if (null? s)
14         m
15         (map-reverse (cdr s)
16                       (cons (procedure (car s))
17                             m))))
18   (reverse (map-reverse s nil)))
19
20 (define (reverse s)
21   (define (reverse-iter s r)
22     (if (null? s)
23         r
24         (reverse-iter (cdr s)
25                       (cons (car s) r))))
26   (reverse-iter s nil))

```

Filter

```

1 (define (unique s)
2   (if (null? s)
3       nil
4       (cons (car s)
5             (unique (filter (lambda (x) (not (eq? x (car s))))
6                             (cdr s))
7             )
8       )
9   )
10 )
11 )

```

append

```

1 scm> (append '(1 2 3) '(4 5 6))
2 (1 2 3 4 5 6)
3 scm> (append)
4 ()
5 scm> (append '(1 2 3) '(a b c) '(foo bar baz))
6 (1 2 3 a b c foo bar baz)
7 scm> (append '(1 2 3) 4)
8 Error

```

Macro

```

1 Primitive: 2 3 true + quotient
2 Combinations: (quotient 10 2) (not true)
3
4 > (list 'quotient 10 2)
5 (quotient 10 2)
6
7 > (eval (list 'quotient 10 2))
8 5
9
10 > (list + 1 2)
11 (#[+] 1 2)
12
13 > (list '+ 1 2)
14 (+ 1 2)
15
16 > (list '+ (+ 2 3))
17 (+ 5)
18
19 > (define (fact-exp n)
20   (if (= n 0) 1 (list '* n (fact-exp (- n 1)))))
21 > (fact-exp 5)
22 (* 5 (* 4 (* 3 (* 2 (* 1 1)))))
23
24 > (eval (fact-exp 5))
25 120
26
27 > (define (fib-exp x)
28   (if (<= n 1) n (list '+ (fib-exp (- n 2)) (fib-exp (- n 1)))))
29
30 > (fib-exp 4)
31 (+ (+ 1 (+ 0 1)) (+ (+ 0 1) (+ 1 (+ 0 1))))

```

- A macro is an operation performed on the source code of a program before evaluation
- Evaluate the operator, if it evaluates to a macro call the macro on the source code (eval the source code and replace the user input as string into the source code unless there's a comma)
- Then evaluate the expression returned from the macro procedure

```
1 > (define-macro (twice expr)
2   (list 'begin expr expr))
3
4 > (print 2)
5 2
6
7 > (begin (print 2) (print 2))
8 2
9 2
10
11 > (define (twice expr) (list 'begin expr expr))
12 > (twice (print 2))
13 (begin None None)
14 > (twice '(print 2)) ;' stop it from evaluating
15 (begin (print 2) (print 2))
16 > (eval (twice '(print 2)))
17 2
18 2
19 > (defin-macro (twice expr) (list 'begin expr expr))
20 > (twice (print 2))
21 2
22 2
23
24 > (define (check val) (if val 'passed 'failed))
25 > (define-macro (check expr)(list 'if expr ''passed ''failed))
26 > (define x -2)
27 x
28 > (check (> x 0))
29 failed
30
31
32 > (define-macro (check expr)(list 'if expr ''passed
33   (list 'quote (list 'failed: expr))))
34 > (check (> x -2))
35 (failed: (> x -2))
36
37 None is true
38 ;for macro
39 > (define (map fn vals)
40   (if (null? vals)
41       ()
42       (cons (fn (car vals))
43             (map fn (cdr vals)))))
44
45 > (define-macro (for sym vals expr)
46   (list 'map (list 'lambda (list sym) expr) vals))
47 > (for x '(2 3 4 5) (* x x))
48 (4 9 16 25)
49
```

Quasi-Quotation

- parts of it can be evaluate

```
1 > (define b 2)
2 > '(a b c)
3 (a b c)
4 > `(a b c)
5 (a b c)
6
7 > `(a ,b c) ;if b can't be evaluate, there'll be an error
8 (a 2 c)
9
10 > '(a ,b c)
11 (a (unquote b) c)
12
13 > (define expr '(* x x))
14 > `(lambda (x) ,expr)
15 (lambda (x) (* x x))
16
17 scm> (define-macro (f x) (car x))
18 scm> (f (+ 2 3))
19 #[+]
20
21 scm> (f (quote (1 2)))
22 Error
23 ;anything will be evaluate to a val finally and quote can't be evaluate to a val alone
24 scm> quote
25 Error
26
27 scm> +
28 #[+]
29
30 scm> (define quote 7000)
31 scm> (f (quote (1 2)))
32 7000
33
34 scm> '(1 ,x 3)
35 (1 (unquote x) 3)
```

- simplify `scheme (define-macro (check expr) `(if ,expr 'passed '(failed: ,expr)))`

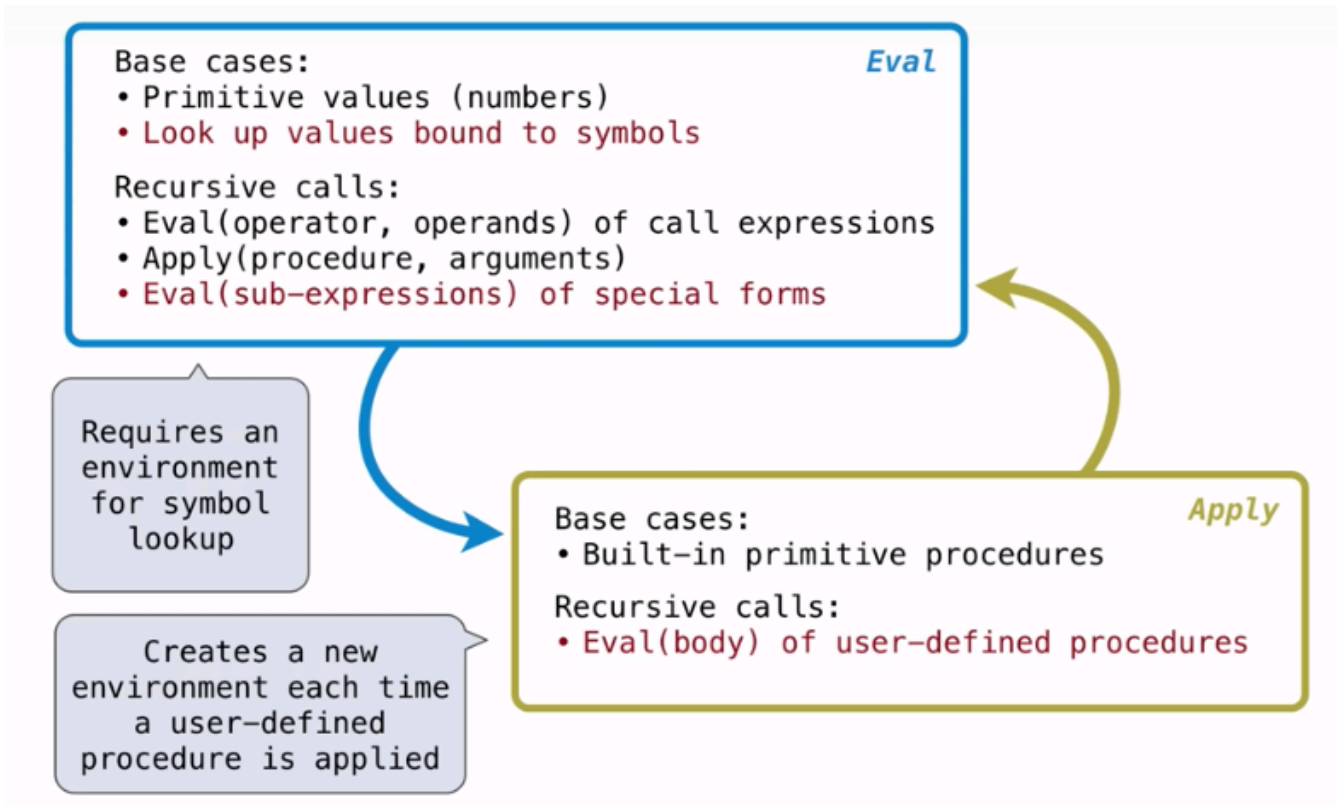

```

1 ;for loop
2 (define (cddr s) (cdr (cdr s)))
3 (define-macro
4   (list-of map-expr for var in lst (variadic y))
5   (list 'map
6         (list 'lambda (list var) map-expr)
7         (if (null? y)
8             lst
9             `(filter (lambda (,var) ,(cadr y)) ,lst)
10        )
11   )
12 )
13
14 ; ; List all ways to make change for TOTAL with DENOMS
15 (define (list-change total denoms)
16   (define (l-change total denoms path)
17     (cond
18       ((null? denoms)
19        nil
20       )
21       ((< total (car denoms))
22        (l-change total (cdr denoms) path)
23       )
24       ((> total (car denoms))
25        (append (l-change (- total (car denoms))
26                          denoms
27                          (append path (list (car denoms))))
28              )
29              (l-change total (cdr denoms) path)
30        )
31       )
32       ((= total (car denoms))
33        (append (list (append path (list (car denoms))))
34              (l-change total (cdr denoms) path)
35        )
36       )
37     )
38   )
39   (l-change total denoms nil)
40 )

```

[Back to Top](#)

Interpreter



Special Forms

- Symbols are bound to values in the current environment
- else-evaluating expressions are returned.
- All other legal expressions are represented as Scheme lists, called combinations

```
1 ;high order function
2 (define (outer x y)
3   (define (inner z x)
4     (+ x (* y 2) (* z 3)))
5   inner)
6
7 > (outer 1 2)
8 inner
9
10 > ((outer 1 2) 1 10)
11 17
```

Scheme

Logical Special Forms

- May evaluate only part of it
- The interpreter convert ' to (quote ~)

```

1 | > (if #t 1 (/ 1 0)) ;No error at all
2 |
3 | > (and 0 1 nil #f 2)
4 | ;evaluated 0 1 nil #f, 0 and nil are all true
5 |
6 | > (quote (+ 1 2)) ;or '(+ 1 2)
7 | (+ 1 2)
8 |
9 | > `(1 2)
10 | (1 2)

```

Lambda Expressions

- Use a class

Frames and Environments

- Frames have parents(env)
- Frames are Python instances with methods lookup and define
- Lookup is a function recursively lookup from child to parent

Define Expressions

- binds a symbol to a value in the first frame of the current environment

- Procedure definition is shorthand of define with a lambda expression.

```

1 | (define (<name> <formal parameters>) <body>)
2 | (define <name> (lambda (<formal parameters>) <body>))

```

Applying User-Defined Procedures

- To apply a user-defined procedure, create a new frame in which formal parameters are bound to argument values, whose parent is the env of the procedure.
- Evaluate the body of the procedure in the environment that starts with this new frames.

```

1 | > (lambda (x)(+ x 6))
2 | (lambda (x)(+ x 6))

```

[return to the top](#)

Streams

```

1 def sum_primes(a, b):
2     return sum(filter(is_prime, range(a, b)))
3
4 def is_prime(x):
5     if x <= 1:
6         return False
7     return all(map(lambda y: x % y, range(2, x)))

```

- Space $\theta(1)$ (benefit by generator)

```

1 (define (range a b)
2   (if (>= a b) nil (cons a (range (+ a 1) b))))
3
4 (define (filter f s)
5   (if (null? s)
6       nil
7       (if (f (car s))
8           (cons (car s)
9                 (filter f (cdr s)))
10              (filter f (cdr s)))))
11
12 (define (reduce f s start)
13   (if (null? s)
14       start
15       (reduce f
16               (cdr s)
17               (f start (car s)))))
18
19 (define (sum s)
20   (reduce + s 0))
21
22 (define (prime? x)
23   (if (<= x 1)
24       false
25       (null? (filter (lambda (y) (= 0 (remainder x y))) (range 2 x)))))
26
27 (define (sum-primes a b)
28   (sum (filter prime? (range a b))))

```

- Space $\theta(n)$

Solution

```

1 ;only evaluate 2 when cdr-stream is called
2 (cdr-stream (cons-stream 1 2)) -> 2
3
4 (cons-stream 1 (cons-stream 2 nil))
5
6 (cons-stream 1 (/ 1 0)) -> (1 . #[delayed]) ; No error
7 (cdr-stream (cons-stream 1 (/ 1 0))) ;error

```

Build Stream

```

1 (define (range-stream a b)
2   (if (>= a b) nil (cons-stream a (range-stream (+ a 1) b))))kjl
3
4 ;Infinite stream
5 (define (int-stream start)
6   (cons-stream start (int-stream (+ 1 start))))
7
8 (define (square-stream s)
9   (cons-stream (* (car s)(car s))
10                (square-stream (cdr-stream s))))
11
12 (define ones (cons-stream 1 ones))
13
14 (define (add-streams s t)
15   (cons-stream (+ (car s) (car t))
16                (add-streams (cdr-stream s)
17                               (cdr-stream t))))
18
19 ;1 2 3 4 5....
20 (define ints (cons-stream 1 (add-streams ones ints)))
21
22 ;map filter reduce stream
23 (define (map-stream f s)
24   (if (null? s)
25       nil
26       (cons-stream (f (car s))
27                     (map-stream f
28                                   (cdr-stream s)))))
29
30 (define (reduce-stream f s start)
31   (if (null? s)
32       start
33       (reduce-stream f
34                       (cdr-stream s)
35                       (f start (car s)))))
36
37 (define (filter-stream f s)
38   (if (null? s)
39       nil

```

```

40      (if (f (car s))
41          (cons-stream (car s)
42                        (filter-stream f (cdr-stream s))))
43      (filter-stream f (cdr-stream s))))
44
45 ;stream of primes
46 ;filter all the multiple of 1 , 2, 3 until n
47 (define (sieve s)
48     (cons-stream (car s)
49                  (sieve (filter-stream
50                          (lambda (x) (not (= 0 (remainder x (car s)))))
51                          (cdr-stream s)))))
52
53 define primes (sieve (int-stream 2)))

```

Promise

- A promise is an expressions, along with an environment in which to evaluate it
- lexical scope
- Delaying an expression creates a promise to evaluate it later in the current environment

```

1 scm> (define promise (let ((x 2)) (delay (+ x 1))))
2 scm> (define x 5)
3 scm> (force promise)
4 3

```

Scheme

- Every time writing delay, it just like create a lambda with no arguments

```

1 (define-macro (delay expr) `(lambda () ,expr))
2 (define (force promise) (promise))
3
4 (define-macro (cons-stream a b) `(cons ,a (delay, b)))
5 (define (cdr-stream s) (force (cdr s))) //evaluate the lambda
6
7 scm> (define ones (cons-stream 1 ones))
8 (1 . #[promise (not forced)])
9 ; not forced means hasn't been evaluated, if it has been evaluated, it will store the value and

```

Scheme

Exp WWSD

Scheme

```

1 | scm> (define oski 61)
2 | oski
3 | scm> (define go-bears (cons-stream oski (cons-stream oski nil)))
4 | go-bears
5 | scm> (define oski 1866)
6 | oski
7 | scm> (car (cdr-stream go-bears))
8 | (1866)

```

[return to the top](#)

Declarative Language

- A "program" is a description of the desired result
- The interpreter figures out how to generate the result
- python is a imperative language
 - A "program" is a description of computational processes
 - The interpreter carries out execution/evaluation rules

SQL

Bash

```

1 | sqlite3 -init ex.sql
2 | sqlite>

```

SELECT

- select statement is used to create table

SQL

```

1 | //create new permanent table
2 | create table cities as
3 |     select 38 as latitude, 122 as longitude, "berkeley" as name union
4 |     select 42, 71, "Cambridge";
5 |
6 |
7 | select "west coast" as region, name from cities where longitude >= 115 union
8 | select "other", name from cities where longitude < 115;

```

- arithmetic

SQL

```

1 | select chair, single + 2 * couple as total from lift;
2 | select word, one+two+four+eight as value from ints where one + two/2 + four/4 + eight/8 = 1;

```

Joining Two Tables

```

1 //join table using child = name
2 select parent from parents, dogs where child = name and fur = "curly";

```

Aliases and Dot Expressions

```

1 select a.child as first, b.child as second
2     from parents as a, parents as b
3     where a.parent = b.parent and a.child < b.child

```

Numerical and String Expressions

```

1 //<> != are the same
2 sqlite> select "hello," || " world";
3 hello, world
4
5 //substr, instr(position) not very good low efficiency
6 sqlite> select substr(s, 4, 2) || substr(s, instr(s, " ")+1, 1) from phrase;
7 low
8
9 //not good
10 sqlite> create table lists as select "one" as car, "two, three, four" as cdr;
11 sqlite> select substr(cdr, 1, instr(cdr, ",")-1) as cadr from lists;
12 two

```

Aggregate Functions

```

create table animals as
  select "dog" as kind, 4 as legs, 20 as weight union
  select "cat"         , 4         , 10         union
  select "ferret"      , 4         , 10         union
  select "parrot"       , 2         , 6          union
  select "penguin"     , 2         , 10         union
  select "t-rex"       , 2         , 12000;

```



```

1  /*max min ... will only display the max/min row*/
2  select max(legs) from animals;
3
4  --support operator
5  select max(legs-weight) + 5 from animals;
6
7  select min(legs), max(weight) from animals where name <> "t-rex"
8  3/6
9
10 --count(*) count number of rows, the following have the same results
11 select count(legs) from animals;
12 select count(kind) from animals;
13 select count(*) from animals;
14
15 --1 for each type, 2types
16 select count(distinct legs) from animals;
17 2
18
19 select count(distinct weight) from animals;
20 4
21
22 select sum(distinct weight) from animals;
23 12036 --ignore the 2 redundant "10"

```

- An aggregate function also selects a row in the table, which may be meaningful

```

1  select max(weight), kind from animals; -- we get only 1 row
2  12000|t-rex
3
4  select avg(weight), kind from animals;
5  2009.33333333333|t-rex --t-rex is not meaningful
6
7  select max(legs), kind from animals;
8  4|cat --There're 3 maxs 'cat' is not meaningful
9
10 select kind from animals where weight > 10 and weight = min(weight)

```

- group by
 - partition the rows in the table by group

```
1 select legs, max(weight) from animals group by legs;
2
3 legs max(weight)
4 4      20
5 2     12000
6
7 -- group by the cartesian product of legs and weight
8 select legs, weight from animals group by legs, weight;
9 2|6
10 2|10
11 2|12000
12 2|10
13 2|20
14
15 select max(kind), weight/legs from animals group by weight/legs
16 ferret|2 --10/4 default is 2, use "weight/legs/1.0" to get float
17 parrot|3
18 penguin|5
19 t-rex|6000
20
21 select weight/legs, count(*) from animals group by weight/legs having count(*)>1;
22 5 2
23 2 2
24 -- having clause filter the groups to leave the ones we want
```