# hw4

### February 6, 2024

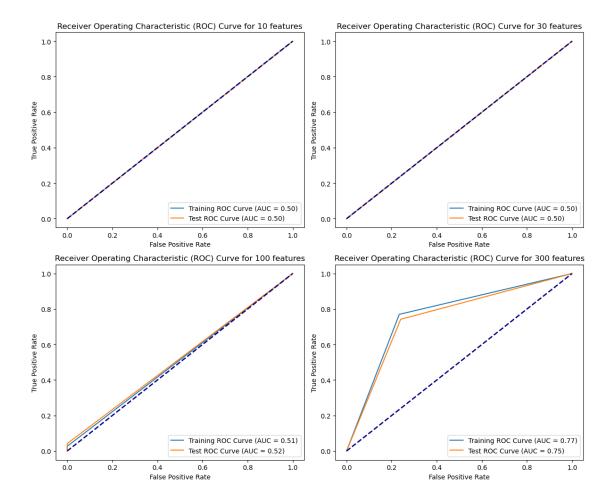
```
[]: import numpy as np
     import pandas as pd
     from sklearn import datasets
     from sklearn.preprocessing import StandardScaler
     from sklearn.linear_model import LogisticRegression
     from sklearn.metrics import accuracy_score, roc_curve, auc
     import matplotlib.pyplot as plt
[]: data_direc = "/Users/kevin_smith/Documents/GitHub/Applied-Machine-Learning/hw4/
     train = pd.read_csv(data_direc + "Gisette/gisette_train.csv")
     train_labels = pd.read_csv(data_direc + "Gisette/gisette_train_labels.csv")
     test = pd.read_csv(data_direc + "Gisette/gisette_valid.csv")
     test_labels = pd.read_csv(data_direc + "Gisette/gisette_valid_labels.csv")
     train = np.delete(train, 5000, axis=1)
     test = np.delete(test, 5000, axis=1)
[]: # Assuming train, test, train_labels, and test_labels are defined
     scaler = StandardScaler()
     train = scaler.fit_transform(train)
     test = scaler.transform(test)
     max_iter = 100
     learning_rate = 1 / train.shape[1]
     # Lists to store results
     train errors = []
     test_errors = []
     num selected features = []
     lambda_values = []
     # Define a list of lambda values to test
     lambda_values_to_test = [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.05, 0.1, 0.5, 1.
      ⇔0]
     fig, axs = plt.subplots(2, 2, figsize=(12, 10))
```

```
for i, num_features in enumerate([10, 30, 100, 300]):
   test_errors_for_lda = []
   train_errors_for_lda = []
   weights = np.zeros((num_features, 1))
   train_temp = pd.DataFrame(train).loc[:, range(num_features)].to_numpy()
   for lda in lambda_values_to_test:
       temp = weights.copy()
        for iter in range(max iter):
            temp = weights + learning_rate * np.dot(train_temp.T, (train_labels_
 → 1 / (1 + np.exp(-np.dot(train_temp, weights)))))
            temp[np.abs(temp) <= lda] = 0</pre>
            weights = temp
        train_labels_pred = (1 / (1 + np.exp(-pd.DataFrame(train).loc[:,__
 arange(num_features)].to_numpy() @ weights))) > 0.5
        test_labels_pred = (1 / (1 + np.exp(-pd.DataFrame(test).loc[:,__
 →range(num_features)].to_numpy() @ weights))) > 0.5
        # Calculate misclassification error
       test_error = 1 - accuracy_score(test_labels, test_labels_pred)
        train_error = 1 - accuracy_score(train_labels, train_labels_pred)
       test errors for lda.append(test error)
       train_errors_for_lda.append(train_error)
    # Find the best lambda (minimize test error)
   best lda index = np.argmin(test errors for lda)
   best_lda = lambda_values_to_test[best_lda_index]
   best_test_error = test_errors_for_lda[best_lda_index]
   train_errors.append(train_errors_for_lda[best_lda_index])
   test_errors.append(best_test_error)
   num_selected_features.append(num_features)
   lambda_values.append(best_lda)
   # Plot ROC curve
   false_pos_rate_train, true_pos_rate_train, _ = roc_curve(train_labels,_

→train labels pred)
   roc_auc_train = auc(false_pos_rate_train, true_pos_rate_train)
   false_pos_rate_test, true_pos_rate_test, _ = roc_curve(test_labels,_u

→test_labels_pred)
   roc_auc_test = auc(false_pos_rate_test, true_pos_rate_test)
   ax = axs[i // 2, i % 2]
   ax.plot(false_pos_rate_train, true_pos_rate_train,
             label="Training ROC Curve (AUC = {:.2f})".format(roc_auc_train))
```

```
ax.plot(false_pos_rate_test, true_pos_rate_test,
            label="Test ROC Curve (AUC = {:.2f})".format(roc_auc_test))
   ax.plot([0, 1], [0, 1], color="navy", lw=2, linestyle="--")
   ax.set_xlabel("False Positive Rate")
   ax.set_ylabel("True Positive Rate")
   ax.set_title(f"Receiver Operating Characteristic (ROC) Curve for ____
 ax.legend(loc="lower right")
plt.tight_layout()
plt.show()
# Create a table of results
results_df = pd.DataFrame({
   "Number of Selected Features": num_selected_features,
   "Lambda": lambda_values,
   "Train Misclassification Error": train_errors,
   "Test Misclassification Error": test_errors
})
print("Results:")
print(results_df)
```



#### Results:

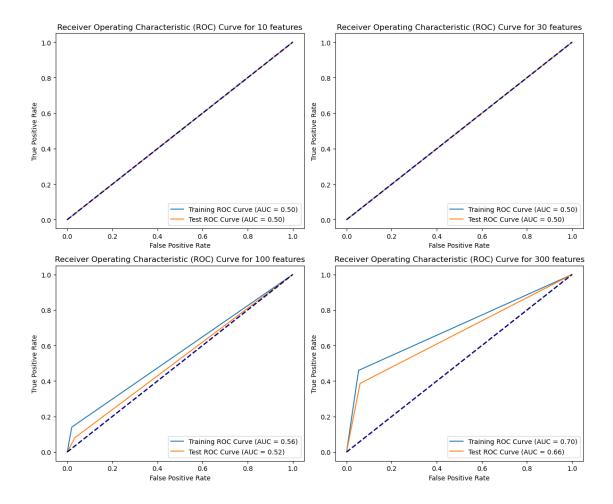
	Number of	Selected Features	Lambda	Train Misclassification Error	\
0		10	0.05	0.420000	
1		30	0.10	0.308333	
2		100	0.10	0.197667	
3		300	0.10	0.069500	

```
test_labels = pd.read_csv(data_direc + "dexter_valid_labels.csv", header

None)
```

```
[]: # Assuming train, test, train labels, and test labels are defined
     scaler = StandardScaler()
     train = scaler.fit transform(train)
     test = scaler.transform(test)
     max iter = 100
     learning_rate = 1 / train.shape[1]
     # Lists to store results
     train_errors = []
     test_errors = []
     num_selected_features = []
     lambda_values = []
     # Define a list of lambda values to test
     lambda_values_to_test = [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.05, 0.1, 0.5, 1.
      ∽07
     fig, axs = plt.subplots(2, 2, figsize=(12, 10))
     for i, num_features in enumerate([10, 30, 100, 300]):
         test_errors_for_lda = []
         train_errors_for_lda = []
         weights = np.zeros((num_features, 1))
         train_temp = pd.DataFrame(train).loc[:, range(num_features)].to_numpy()
         for lda in lambda_values_to_test:
             temp = weights.copy()
             for iter in range(max_iter):
                 temp = weights + learning_rate * np.dot(train_temp.T, (train_labels_
      → 1 / (1 + np.exp(-np.dot(train_temp, weights)))))
                 temp[np.abs(temp) <= lda] = 0</pre>
                 weights = temp
             train_labels_pred = (1 / (1 + np.exp(-pd.DataFrame(train).loc[:,u
      →range(num_features)].to_numpy() @ weights))) > 0.5
             test labels pred = (1 / (1 + np.exp(-pd.DataFrame(test).loc[:,]
      range(num_features)].to_numpy() @ weights))) > 0.5
             # Calculate misclassification error
             test_error = 1 - accuracy_score(test_labels, test_labels_pred)
             train_error = 1 - accuracy_score(train_labels, train_labels_pred)
             test_errors_for_lda.append(test_error)
             train_errors_for_lda.append(train_error)
```

```
# Find the best lambda (minimize test error)
   best_lda_index = np.argmin(test_errors_for_lda)
   best_lda = lambda_values_to_test[best_lda_index]
   best_test_error = test_errors_for_lda[best_lda_index]
   train_errors.append(train_errors_for_lda[best_lda_index])
   test_errors.append(best_test_error)
   num selected features.append(num features)
   lambda_values.append(best_lda)
    # Plot ROC curve
   false_pos_rate_train, true_pos_rate_train, _ = roc_curve(train_labels,_
 →train_labels_pred)
   roc_auc_train = auc(false_pos_rate_train, true_pos_rate_train)
   false_pos_rate_test, true_pos_rate_test, _ = roc_curve(test_labels,_
 →test_labels_pred)
   roc_auc_test = auc(false_pos_rate_test, true_pos_rate_test)
   ax = axs[i // 2, i % 2]
   ax.plot(false_pos_rate_train, true_pos_rate_train,
             label="Training ROC Curve (AUC = {:.2f})".format(roc_auc_train))
   ax.plot(false_pos_rate_test, true_pos_rate_test,
             label="Test ROC Curve (AUC = {:.2f})".format(roc_auc_test))
   ax.plot([0, 1], [0, 1], color="navy", lw=2, linestyle="--")
   ax.set xlabel("False Positive Rate")
   ax.set_ylabel("True Positive Rate")
   ax.set_title(f"Receiver Operating Characteristic (ROC) Curve for_
 ax.legend(loc="lower right")
plt.tight_layout()
plt.show()
# Create a table of results
results_df = pd.DataFrame({
    "Number of Selected Features": num_selected_features,
   "Lambda": lambda values,
    "Train Misclassification Error": train_errors,
    "Test Misclassification Error": test_errors
})
print("Results:")
print(results_df)
```



#### Results:

	Number of Selected Feat	ures Lamb	da Train M	isclassification Error $\setminus$
0		10 0.50	000	0.500000
1		30 0.50	000	0.500000
2		100 0.00	001	0.506667
3		300 0.00	01	0.666667

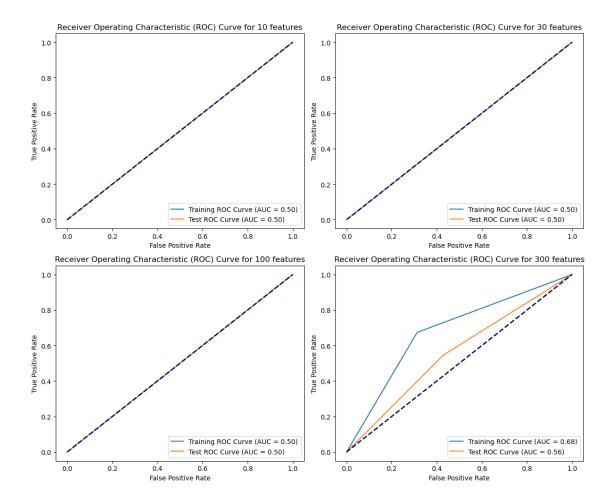
Test Misclassification Error 0.503333

0 0.503333 1 0.503333 2 0.543333 3 0.773333

```
test_labels = pd.read_fwf(data_direc + "madelon/madelon_valid.labels", header = _{\sqcup} _{\hookrightarrow}None)
```

```
[]: # Assuming train, test, train labels, and test labels are defined
     scaler = StandardScaler()
     train = scaler.fit transform(train)
     test = scaler.transform(test)
     max iter = 100
     learning_rate = 1 / train.shape[1]
     # Lists to store results
     train_errors = []
     test_errors = []
     num_selected_features = []
     lambda_values = []
     # Define a list of lambda values to test
     lambda_values_to_test = [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.05, 0.1, 0.5, 1.
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     fig, axs = plt.subplots(2, 2, figsize=(12, 10))
     for i, num_features in enumerate([10, 30, 100, 300]):
         test_errors_for_lda = []
         train_errors_for_lda = []
         weights = np.zeros((num_features, 1))
         train_temp = pd.DataFrame(train).loc[:, range(num_features)].to_numpy()
         for lda in lambda_values_to_test:
             temp = weights.copy()
             for iter in range(max_iter):
                 temp = weights + learning_rate * np.dot(train_temp.T, (train_labels⊔
      → 1 / (1 + np.exp(-np.dot(train_temp, weights)))))
                 temp[np.abs(temp) <= lda] = 0</pre>
                 weights = temp
             train_labels_pred = (1 / (1 + np.exp(-pd.DataFrame(train).loc[:,u
      →range(num_features)].to_numpy() @ weights))) > 0.5
             test labels pred = (1 / (1 + np.exp(-pd.DataFrame(test).loc[:,]
      range(num_features)].to_numpy() @ weights))) > 0.5
             # Calculate misclassification error
             test_error = 1 - accuracy_score(test_labels, test_labels_pred)
             train_error = 1 - accuracy_score(train_labels, train_labels_pred)
             test_errors_for_lda.append(test_error)
             train_errors_for_lda.append(train_error)
```

```
# Find the best lambda (minimize test error)
   best_lda_index = np.argmin(test_errors_for_lda)
   best_lda = lambda_values_to_test[best_lda_index]
   best_test_error = test_errors_for_lda[best_lda_index]
   train_errors.append(train_errors_for_lda[best_lda_index])
   test_errors.append(best_test_error)
   num selected features.append(num features)
   lambda_values.append(best_lda)
    # Plot ROC curve
   false_pos_rate_train, true_pos_rate_train, _ = roc_curve(train_labels,_
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   roc_auc_train = auc(false_pos_rate_train, true_pos_rate_train)
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   roc_auc_test = auc(false_pos_rate_test, true_pos_rate_test)
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   "Lambda": lambda values,
    "Train Misclassification Error": train_errors,
    "Test Misclassification Error": test_errors
})
print("Results:")
print(results_df)
```



## Results:

	Number of Selected Featur	es L	ambda	Train Misclassification Error	\
0		10 0	.1000	0.7405	
1		30 0	.1000	0.7295	
2	1	00 0	.0001	0.6940	
3	3	00 0	.0001	0.6640	

# Test Misclassification Error

0	0.753333
1	0.741667
2	0.703333
3	0.726667

# []: