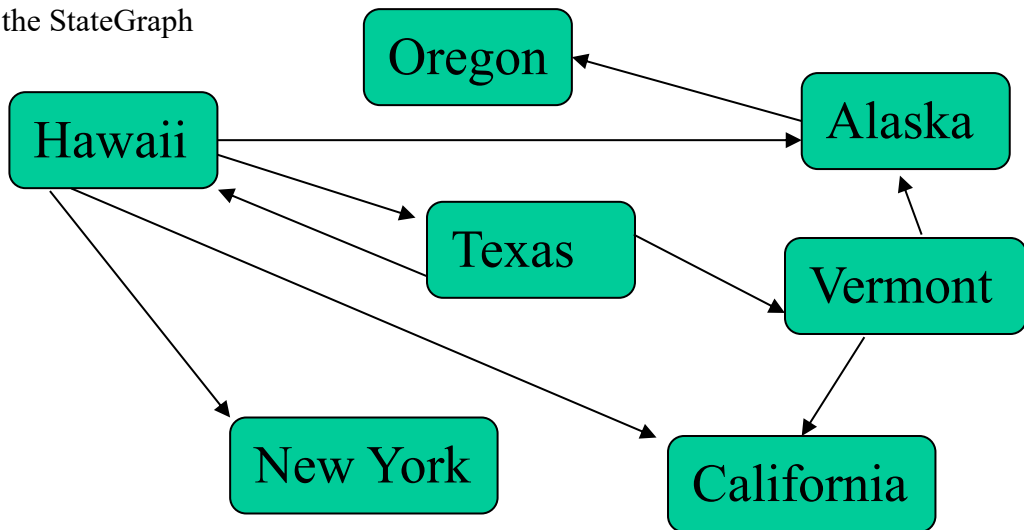


$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$
 $E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

1. Draw the StateGraph



1. Describe the graph pictured above, using the formal graph notation.

$V(\text{StateGraph}) =$ Not needed

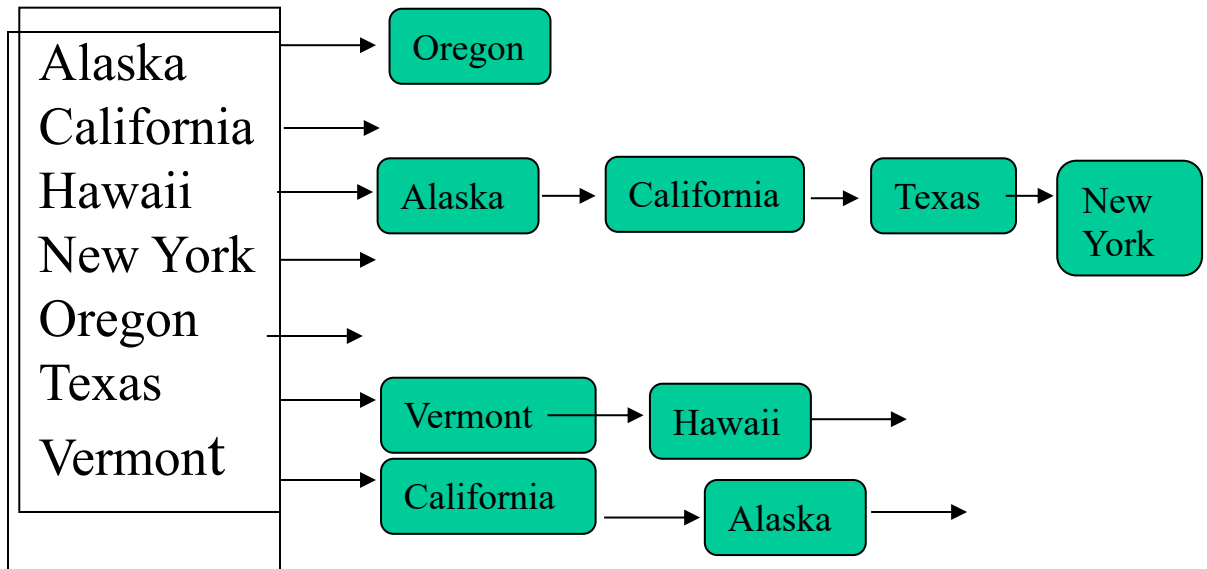
$E(\text{StateGraph}) =$

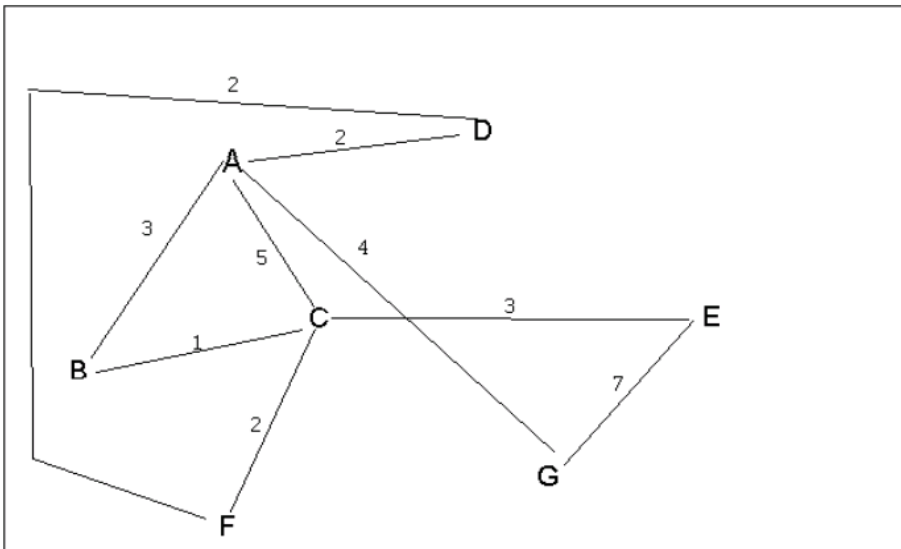
2. a. Is there a path from Oregon to any other state in the graph? No
- b. Is there a path from Hawaii to every other state in the graph? Yes
- c. From which state(s) in the graph is there a path to Hawaii? Texas

3. a. Show the adjacency matrix that would describe the edges in the graph.
Store the vertices in alphabetical order

States							
Alaska	0	0	0	0	1	0	0
California	0	0	0	0	0	0	0
Hawaii	1	1	0	1	0	1	0
New York	0	0	0	0	0	0	0
Oregon	0	0	0	0	0	0	0
Texas	0	0	1	0	0	0	1
Vermont	1	1	0	0	0	0	0

3. b. Show the adjacency lists that would describe the edges in the graph



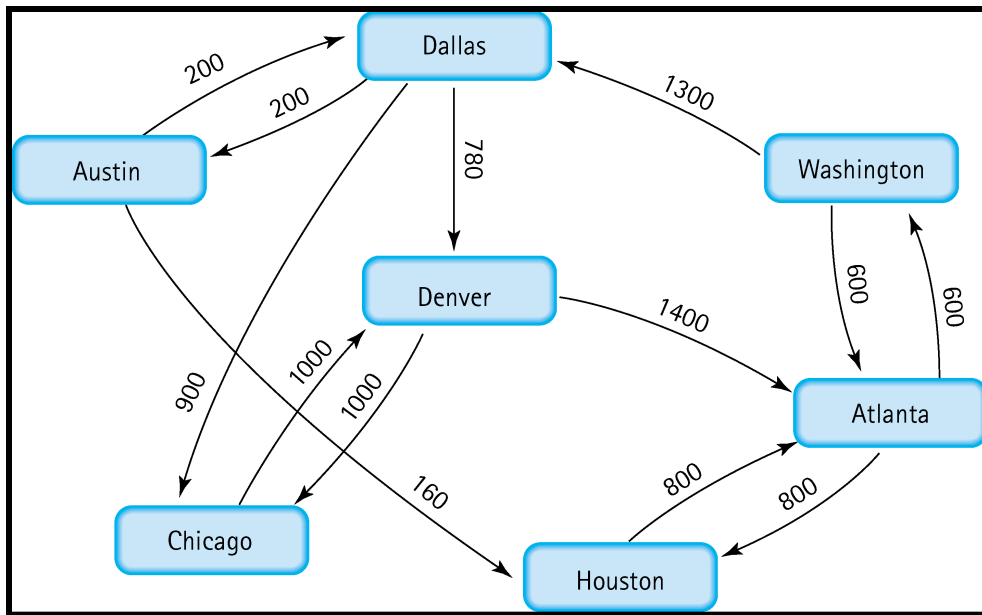


4 a. Which of the following lists the graph nodes in depth first order beginning with E?

- A) E, G, F, C, D, B, A
- B) G, A, E, C, B, F, D
- C) E, G, A, D, F, C, B**
- D) E, C, F, B, A, D, G

4 b. Which of the following lists the graph nodes in breadth first order beginning at F?

- A) F, C, D, A, B, E, G**
- B) F, D, C, A, B, C, G
- C) F, C, D, B, G, A, E
- D) a, b, and c are all breadth first traversals



5. Find the shortest distance from Atlanta to every other city

Atlanta → Austin: $600 + 1300 + 200 = 2100$

Atlanta → Chicago: $600 + 1300 + 900 = 2800$

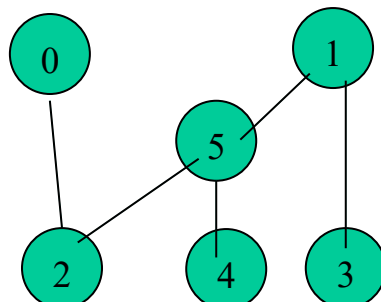
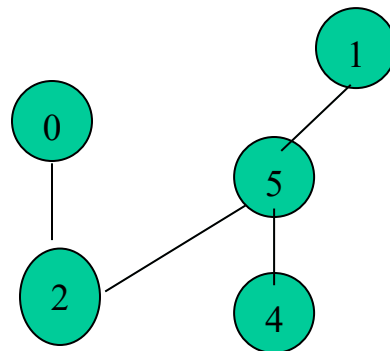
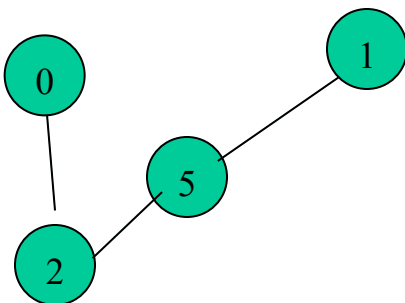
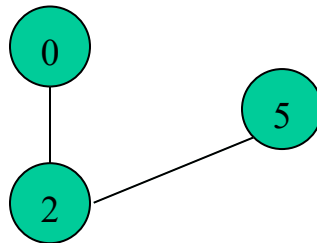
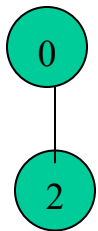
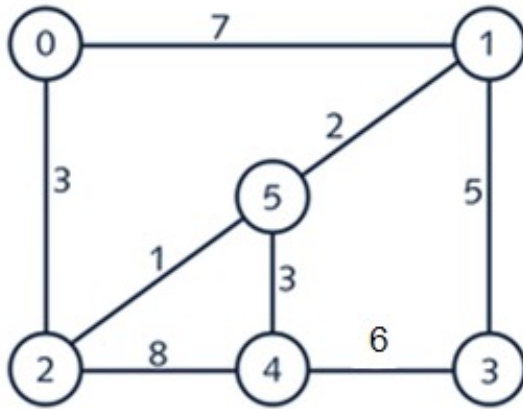
Atlanta → Dallas: $600 + 1300 = 1900$

Atlanta → Denver: $600 + 1300 + 780 = 2680$

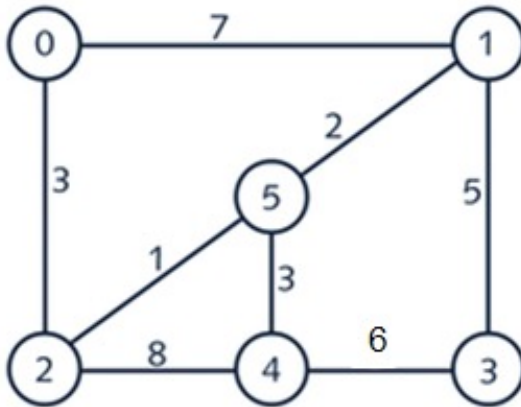
Atlanta → Houston: 800

Atlanta → Washington: 600

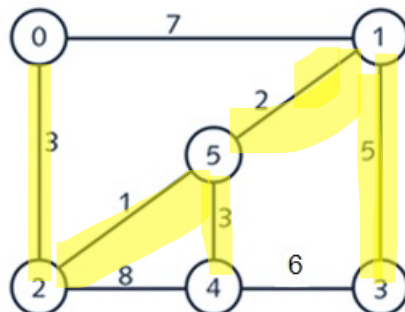
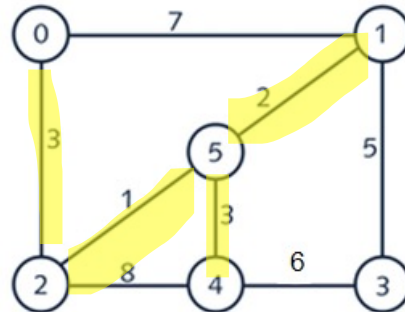
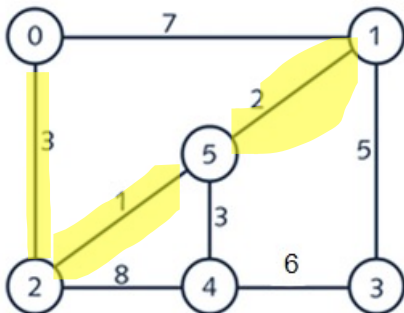
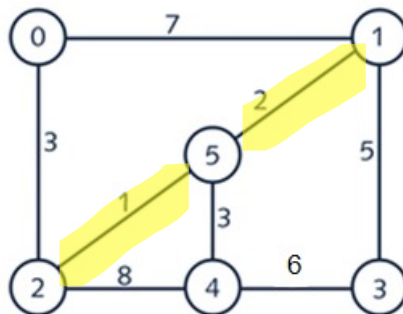
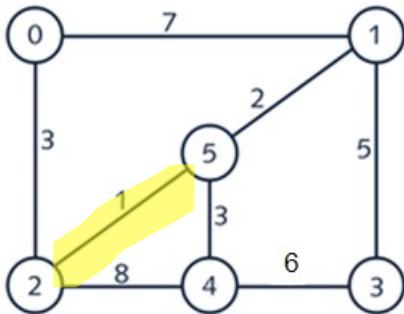
6. Find the minimal spanning tree using Prim's algorithm. Use 0 as the source vertex . Show the steps.



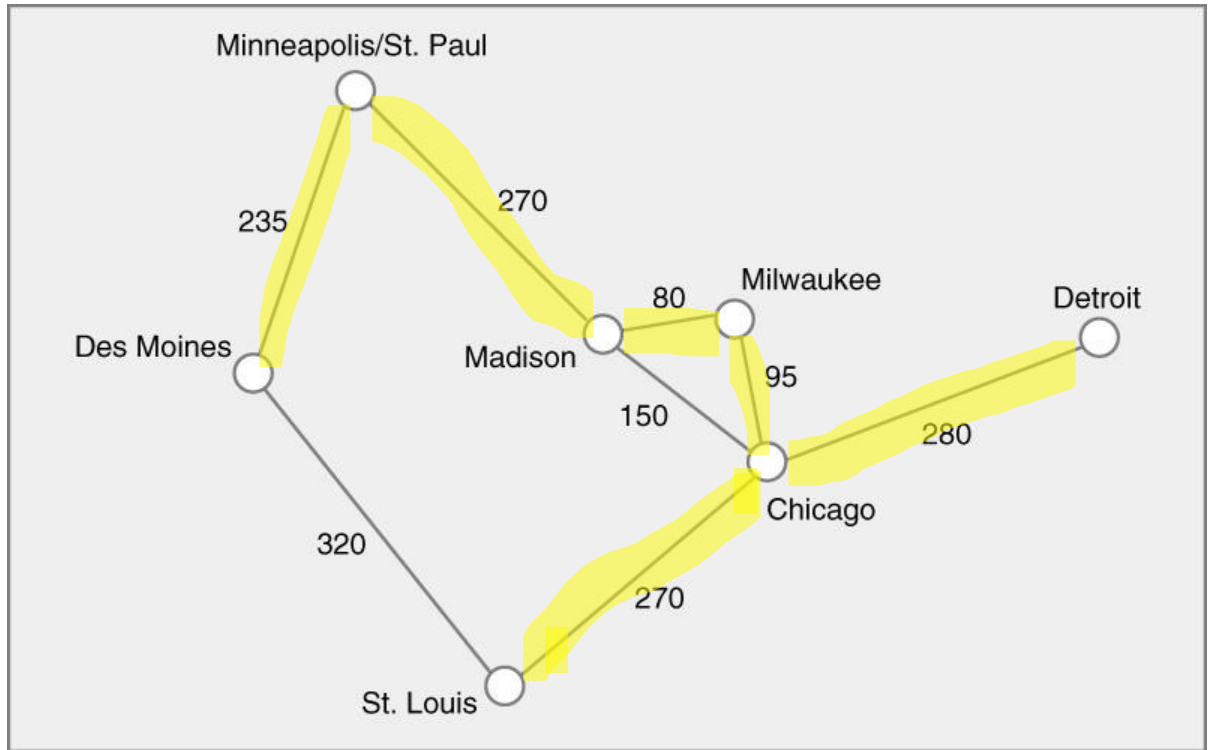
7. Find the minimal spanning tree using Kruskal's algorithm. Show the weights in order and the steps.



$2 \rightarrow 5 : 1$
 $1 \rightarrow 5 : 2$
 $0 \rightarrow 2 : 3$
 $4 \rightarrow 5 : 3$
 $1 \rightarrow 3 : 5$



8. Find the minimal spanning tree using the algorithm you prefer. Use Minneapolis/St. Paul as the source vertex



Kruskal's Algorithm:

Madison → Milwaukee: 80

Milwaukee → Chicago: 95

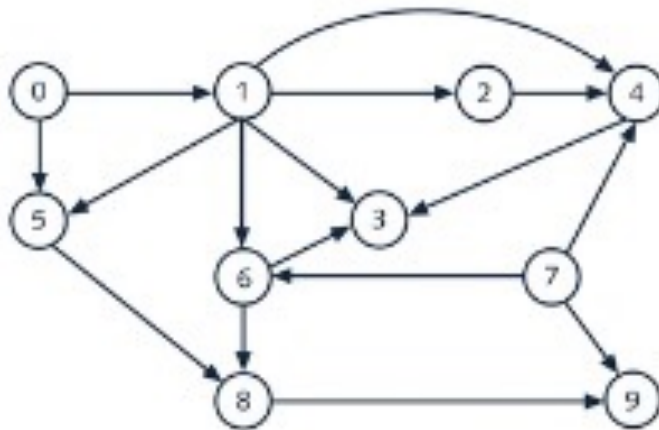
Minneapolis → Des Moines: 235

Minneapolis → Madison: 270

Chicago → St. Louis: 270

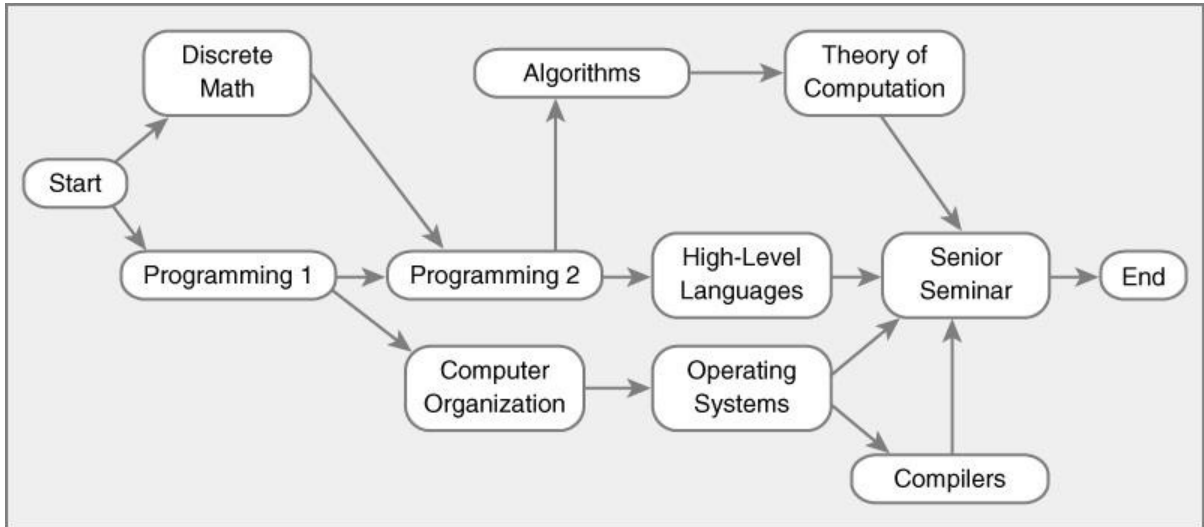
Chicago → Detroit: 280

9. List the nodes of the graph in a breadth first topological ordering. Show the steps using arrays predCount, topologicalOrder and a queue



predCount	topologicalOrder	queue
0, 1, 1, 3, 3, 2, 2, 0, 2, 2		0, 7
0, 0, 1, 3, 3, 1, 2, 0, 2, 2	0	7, 1
0, 0, 1, 3, 2, 1, 1, 0, 2, 1	0, 7	1
0, 0, 0, 2, 1, 0, 0, 0, 2, 1	0, 7, 1	2, 5, 6
0, 0, 0, 2, 0, 0, 0, 0, 2, 1	0, 7, 1, 2	5, 6, 4
0, 0, 0, 2, 0, 0, 0, 0, 1, 1	0, 7, 1, 2, 5	6, 4
0, 0, 0, 1, 0, 0, 0, 0, 0, 1	0, 7, 1, 2, 5, 6	4, 8
0, 0, 0, 0, 0, 0, 0, 0, 0, 1	0, 7, 1, 2, 5, 6, 4	8, 3
0, 0, 0, 0, 0, 0, 0, 0, 0, 0	0, 7, 1, 2, 5, 6, 4, 8	3, 9
0, 0, 0, 0, 0, 0, 0, 0, 0, 0	0, 7, 1, 2, 5, 6, 4, 8, 3	9
0, 0, 0, 0, 0, 0, 0, 0, 0, 0	0, 7, 1, 2, 5, 6, 4, 8, 3, 9	

10. List the nodes of the graph in a breadth first topological ordering.



1. Start
2. Discrete Math
3. Programming 1
4. Computer Organization
5. Programming 2
6. Operating Systems
7. Algorithms
8. High-Level Languages
9. Compilers
10. Theory of Computation
11. Senior Seminar
12. End