**Enviroment Settings** 

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## 2 Computational Geometry

#### 2.1 Geometry on Plane

```
struct node {
  double x,y;
  node() {}
  node(double _x, double _y) : x(_x),y(_y) {}
  node operator+(const node& rhs)const
    { return node(x+rhs.x,y+rhs.y); }
  node operator-(const node& rhs)const
    { return node(x-rhs.x,y-rhs.y); }
  node operator*(const double& rhs)const
    { return node(x*rhs,y*rhs); }
  node operator/(const double& rhs)const
    { return node(x/rhs,y/rhs); }
  double operator*(const node& rhs)const
    { return x*rhs.x+y*rhs.y; }
  double len2()const{ return x*x+y*y; }
  double len()const{ return sqrt(x*x+y*y); }
  node unit()const{ return *this/len(); }
  double operator^(const node& rhs)const{ return
      x*rhs.y-y*rhs.x; }
  node T()const{ return node(-y,x); }
  node rot(double rad)const{ //逆時針旋轉 弧度
    return node(cos(rad)*x-sin(rad)*y, sin(rad)*x
       +cos(rad)*y);
  }
};
node mirror(node normal, double constant, node
   point){ //2D3D
  double scale=(normal*point+constant)/(normal*
      normal);
  return point-normal*(2*scale);
}
node mirror(node p1, node p2, node p3){ //2D3D
  return __mirror((p2-p1).T(),(p2-p1).T()*p1*(-1)
      ,p3);
double ori(const node& p1,const node& p2, const
   node& p3){ //平行四邊形面積(帶正負)
  return (p2-p1)^(p3-p1);
bool intersect(const node& p1, const node& p2,
   const node& p3, const node& p4){
  return (ori(p1,p2,p3)*ori(p1,p2,p4)<0 && ori(p3</pre>
      ,p4,p1)*ori(p3,p4,p2)<0);
}
pair<node, node> two_circle_intersect(node p1,
   double r1, node p2, double r2){
  double degree=acos(((p2-p1).len2()+r1*r1-r2*r2)
      /(2*r1*(p2-p1).len()));
  return make_pair(p1+(p2-p1).unit().rot(degree)*
     r1, p1+(p2-p1).unit().rot(-degree)*r1);
node intersectionPoint(node p1, node p2, node p3,
    node p4){
  double a123 = (p2-p1)^{(p3-p1)};
  double a124 = (p2-p1)^{(p4-p1)};
  return (p4*a123-p3*a124)/(a123-a124);
2.2 KDTree
struct NODE{
  int x , y;
  int x1 , x2 , y1 , y2;
  NODE *L , *R;
bool cmpx( const NODE& a , const NODE& b ){
  return a.x < b.x;</pre>
```

```
bool cmpy( const NODE& a , const NODE& b ){
  return a.y < b.y;</pre>
NODE* KDTree( int L , int R , int depth ){
  if ( L > R ) return 0;
  int M = (L + R) >> 1;
  node[M].f = depth % 2;
  nth_element( node+L , node+M , node+R+1 , node[
     M].f ? cmpy : cmpx );
  node[M].L = KDTree( L , M-1 , depth+1 );
  node[M].R = KDTree( M+1 , R , depth+1 );
  node[M].x1 = node[M].x2 = node[M].x;
  node[M].y1 = node[M].y2 = node[M].y;
  if ( node[M].L ){
    node[M].x1 = min(node[M].x1, node[M].L->x1
    node[M].y1 = min(node[M].y1, node[M].L->y1
       );
  if ( node[M].R ){
    node[M].x2 = max(node[M].x2, node[M].L->x2
    node[M].y2 = max(node[M].y2, node[M].L->y2
       );
  return node+M;
inline int mayTouchRectangle( NODE* r , int x ,
   int y , long long d2 ){
  long long d = (long long)(sqrt(d2) + 1);
  return x >= r->x1 - d && x <= r->x2 +d && y >=
     r->y1 - d \&\& y <= r->y2 + d;
// find the nearest point near p
// r is tree node
void nearest( NODE* r , NODE* p , long long &dmin
  if ( !r || !mayTouchRectangle( r , p->x , p->y
     , dmin ) ) return;
  if ( p->i != r->i ) dmin = min( dmin , dis( *r
     , *p ) ); // dis returns the dis^2
  int whichFirst = r->f ? p->y < r->y: p->x < r->
     х;
  if ( whichFirst ){
    nearest( r->L , p , dmin );
    nearest( r->R , p , dmin );
  else{
    nearest( r->R , p , dmin );
    nearest( r->L , p , dmin );
```

#include <ext/pb\_ds/assoc\_container.hpp>

### 3 Data Structure

using namespace std;

```
3.1 PB DS
```

```
using namespace __gnu_pbds;
#include <ext/pb ds/priority queue.hpp>
typedef __gnu_pbds::priority_queue<T, greater<T>,
    pairing_heap_tag> Heap;
  method: push, pop, modify(iter, val), erase,
    join
  tags: pairing_heap_tag, binary_heap_tag,
    binomial_heap_tag, rc_binomial_heap_tag,
    thin_heap_tag
#include <ext/pb_ds/tree_policy.hpp>
typedef tree<int, null_type, less<int>,
   rb_tree_tag,
   tree_order_statistics_node_update> RBTree;
typedef tree<int, null_type, less<int>,
    splay_tree_tag,
   tree_order_statistics_node_update> Splay;
 * point_iterator find_by_order(size_type order)
  size_type order_of_key(const_key_reference
    r_key) - number of elements < r_key
  void split(const_key_reference r_key, tree &
    other) - move elements > r_key
#include <ext/pb_ds/hash_policy.hpp>
typedef cc_hash_table<string, int> Hash;
typedef gp_hash_table<string, int> Hash;
3.2 BigInteger
#include <cstdio>
#include <cstring>
#include <iostream>
#include <iomanip>
using namespace std;
template<class T>
T abs(const T& n) {return n>=T(0)?n:-n;}
class BigInteger {
public:
  BigInteger(const int& num=0) : len(0), sign(1)
      {
    int num2=num;
    memset(arr, 0, sizeof(arr));
    if( num2<0 ) sign=-1, num2*=-1;</pre>
    while( num2 ) arr[len++]=num2%step, num2/=
  BigInteger(const char* num0) : len(0), sign(1)
    *this = num0;
  BigInteger(const BigInteger& b) : len(b.len),
      sign(b.sign) {
    memset(arr, 0, sizeof(arr));
    for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>
  ~BigInteger() {}
  BigInteger & operator = (const BigInteger& b) {
    len=b.len;
    sign=b.sign;
    memset(arr, 0, sizeof(arr));
```

```
for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>
  return *this;
BigInteger & operator = (const int& num) {
  int num2=num;
  memset(arr, 0, sizeof(arr));
  len=0, sign=1;
  if( num2<0 ) sign=-1, num2*=-1;</pre>
  while( num2 ) arr[len++]=num2%step, num2/=
      step;
  return *this;
BigInteger & operator = (const char* num0) {
  char num[strlen(num0)];
  int offset = 0;
  len = 0;
  sign = 1;
  if( num0[0] == '-' ) sign = -1, ++offset;
else if( num0[0] == '+' ) ++offset;
  while( num0[offset] == '0' ) ++ offset;
  strcpy(num, num0+offset);
  int tmp = strlen(num);
  for(int i=tmp-digit; i>=0; i-=digit) {
    arr[len] = 0;
    for(int j=0; j<digit; ++j) arr[len] = arr[</pre>
        len]*10 + num[i+j]-'0';
    ++len;
  arr[len] = 0;
  for(int j=0; j<tmp%digit; ++j) arr[len] = arr</pre>
      [len]*10 + num[j]-'0';
  if( tmp%digit ) ++len;
  return *this;
BigInteger operator + (const BigInteger& b)
    const {
  if( *this>0 && b<0 ) return *this-(-b);</pre>
  if( *this<0 && b>0 ) return -(-*this-b);
  BigInteger res=*this;
  int len2=max(res.len, b.len);
  for(int i=0; i<len2; ++i) {</pre>
    res.arr[i]+=b.arr[i];
    if( res.arr[i]>=step ) res.arr[i]-=step,
        res.arr[i+1]++;
  res.len=len2;
  if(res.arr[len2]) ++res.len;
  return res;
BigInteger operator - (const BigInteger& b)
    const {
  if( *this<b ) return -(b-*this);</pre>
  if( *this<0 && b<0 ) return -(-*this+b);</pre>
  if( *this>0 && b<0 ) return *this+(-b);</pre>
  BigInteger res=*this;
  int len2=max(res.len, b.len);
  for(int i=0; i<len2; ++i) {</pre>
    res.arr[i]-=b.arr[i];
    if( res.arr[i]<0 ) res.arr[i]+=step, res.</pre>
        arr[i+1]--;
  while( len2>0 && res.arr[len2-1]==0 ) --len2;
  res.len=len2;
  return res;
BigInteger operator * (const BigInteger& b)
    const {
  if( *this==0 || b==0 ) return BigInteger(0);
  BigInteger res;
  for(int i=0; i<len; ++i) {</pre>
```

```
if( sign!=b.sign ) return false;
    for(int j=0; j<b.len; ++j) {</pre>
      res.arr[i+j]+=arr[i]*b.arr[j];
                                                        if( len!=b.len ) return false;
      res.arr[i+j+1]+=res.arr[i+j]/step;
                                                        for(int i=len-1; i>=0; --i)
      res.arr[i+j]%=step;
                                                          if( arr[i]!=b.arr[i] ) return false;
    }
                                                        return true;
  }
  res.len=len+b.len-1;
                                                      bool operator <= (const BigInteger& b) const {</pre>
  while( res.arr[res.len] ) ++res.len;
                                                          return *this<b || *this==b; }</pre>
                                                      bool operator > (const BigInteger& b) const {
  res.sign=sign*b.sign;
                                                         return b<*this; }</pre>
  return res;
                                                      bool operator >= (const BigInteger& b) const {
BigInteger operator / (const int& b) const {
                                                         return b<=*this; }</pre>
  if( b==0 ) return 0;
                                                      bool operator != (const BigInteger& b) const {
                                                         return !(*this==b); }
  BigInteger res;
  long long reduce=0;
                                                      BigInteger operator-() const {
  int signb=b>0?1:-1, b2=b*signb;
                                                        BigInteger res = *this;
  for(int i=len-1; i>=0; --i) {
                                                        if( res.len>0 ) res.sign*=-1;
    res.arr[i] = (arr[i]+reduce*step)/b2;
                                                        return res;
    reduce = (arr[i]+reduce*step)%b2;
                                                      template < class T> BigInteger operator + (const
  }
                                                           T& b) const {return *this+BigInteger(b);}
  res.len = len;
  while( res.len>0 && res.arr[res.len-1]==0 )
                                                      template < class T> BigInteger operator - (const
      --res.len;
                                                           T& b) const {return *this-BigInteger(b);}
  if( res.len==0 ) res.sign=1;
                                                      template<class T> bool
                                                                                operator == (const T&
  else res.sign=sign*signb;
                                                          b) const {return *this==BigInteger(b);}
                                                      void print(const char *str="") const {
  return res;
                                                        if( len==0 ) printf("0");
BigInteger operator / (const BigInteger& b)
                                                          printf("%d", arr[len-1]*sign);
  BigInteger abs_this=abs(*this);
                                                          for(int i=len-2; i>=0; --i) printf("%04d",
  if( b==0 ) return 0;
                                                              arr[i]);
  BigInteger st=0, ed, md;
                                                        }
  if( b.arr[0]>0 ) ed=abs_this/b.arr[0];
                                                        printf("%s", str);
  else if( b.arr[1]*b.step+b.arr[0]>0 ) ed=
      abs_this/b.arr[1]*b.step+b.arr[0];
                                                      bool isInt() const {
  else ed=abs_this;
                                                        if( len>2 ) return false;
                                                        if( len<2 ) return true;</pre>
  while( st<ed ) {</pre>
    md = (st+ed)/2+1;
                                                        long long res=toInt();
    if( md*b<=abs_this ) st=md;</pre>
                                                        return res<(111<<31) && res>=-(111<<31);</pre>
    else ed=md-1;
                                                      friend ostream& operator << ( ostream& out,</pre>
  if( st.len==0 ) st.sign=1;
                                                         const BigInteger &rhs ) {
  else st.sign=sign*b.sign;
                                                        if( rhs.len==0 ) out << '0';</pre>
                                                        else {
                                                          out << rhs.arr[rhs.len-1]*rhs.sign;</pre>
  return st;
}
                                                          for(int i=rhs.len-2; i>=0; --i) out <<</pre>
BigInteger operator % (const int& b) const {
                                                              setfill('0') << setw(BigInteger::digit)</pre>
  if( b<=0 ) return 0;</pre>
                                                               << rhs.arr[i];
  BigInteger res;
                                                        }
  long long reduce=0;
                                                        return out;
  for(int i=len-1; i>=0; --i)
    reduce = (arr[i]+reduce*step)%b;
                                                      long long toInt() const {return sign*(111*arr
  return reduce*sign;
                                                          [1]*step+arr[0]);}
}
                                                   private:
BigInteger operator % (const BigInteger& b)
                                                      static const int length = 100;
    const {
                                                      static const int digit = 4, step = 10000;
  if( b.isInt() ) return *this%int(b.toInt());
                                                      int arr[length];
  if( b<=0 ) return 0;</pre>
                                                      int len, sign;
  return *this-*this/b*b;
                                                   };
                                                    istream& operator >> ( istream& in, BigInteger &
bool operator < (const BigInteger& b) const {</pre>
                                                       rhs ) {
  if( sign!=b.sign ) return sign<b.sign;</pre>
                                                      char s[1000];
  if( len!=b.len ) return len*sign<b.len*b.sign</pre>
                                                      in >> s;
                                                      rhs = s;
  for(int i=len-1; i>=0; --i)
                                                      return in;
    if( arr[i]!=b.arr[i] ) return arr[i]*sign<b }</pre>
        .arr[i]*b.sign;
                                                   3.3 Fenwick Tree Range Modify [1, size]
  return false;
                                                   inline int lowbit(int x) { return x&-x; }
bool operator == (const BigInteger& b) const {
                                                   template < class T>
```

```
class fenwick {
                                                     struct TNode {
public:
                                                       TNode<T> *c[2], *fa;
  fenwick(int __size=SIZE) {
                                                        T val, inc, sum;
    size = \__size+10;
                                                        int sz;
                                                       void down() {
    a = new T[size], b=new T[size];
    memset(a, 0, sizeof(T)*size);
                                                          val += inc;
                                                          if( lc->fa ) lc->inc += inc;
    memset(b, 0, sizeof(T)*size);
                                                          if( rc->fa ) rc->inc += inc;
  ~fenwick() { delete[] a, delete[] b;}
                                                          inc = 0;
  inline void add(int 1, int r, long long n) {
                                                        }
    \_add(a, r, r*n), \_add(a, l-1, (l-1)*-n);
                                                       void up() {
    __add(b, r, n), __add(b, l-1, -n);
                                                          sz = lc \rightarrow sz + rc \rightarrow sz + 1;
                                                          sum = val;
  inline long long sum(int 1, int r) { return
                                                          if( lc->fa ) sum += lc->sum + lc->inc*lc->sz;
       _sum(r)-__sum(l-1); }
                                                          if( rc->fa ) sum += rc->sum + rc->inc*rc->sz;
private:
  int size;
                                                     };
  T *a, *b;
                                                     template < class T>
  inline void __add(T *arr, int x, T n) { for(; x
                                                     class SplayTree {
      &&n&&x<size; x+=lowbit(x)) arr[x]+=n; }
                                                     public:
  inline T __sum(T x) { return __sum(a, x)+(__sum
                                                       void init(const int& n) {
      (b, size)-_sum(b, x)*x; }
                                                          null = &node[0];
  inline T __sum(T *arr, int x) {
                                                          null->fa = NULL;
                                                          null->val = null->inc = null->sum = null->sz
    T res=0:
    for(; x; x-=lowbit(x)) res+=arr[x];
    return res;
                                                          ncnt = 0;
                                                          root = newnode(-1, null);
  }
                                                          root->rc = newnode(-1, root);
};
                                                          root->rc->lc = build(1, n, root->rc);
     Fenwick Tree 2D - [1, size][1, size]
                                                          root->rc->up(), root->up();
int tree[size+1][size+1]={{0}};
                                                        void update(int 1, int r, T val) {
inline int lowbit(const int &x) {return x&(-x);}
                                                          RotateTo(1-1, null);
inline void add(int x, int y, int z) {
                                                          RotateTo(r+1, root);
  for(int i; x<=n; x+=lowbit(x))</pre>
                                                          root->rc->lc->inc += val;
    for(i=y; i<=n; i+=lowbit(i)) tree[x][i]+=z;</pre>
                                                          root->rc->lc->up();
inline int query(short x, short y) {
                                                        11 query(int 1, int r) {
  int res=0;
                                                          if( 1>r ) swap(1, r);
  for(int i; x; x-=lowbit(x))
                                                          RotateTo(1-1, null);
    for(i=y; i; i-=lowbit(i))
                                                          RotateTo(r+1, root);
      res+=tree[x][i];
                                                          TNode<T> *now = root->rc->lc;
  return res;
                                                          now->up();
                                                          return now->sum + now->inc*now->sz;
                                                       }
3.5 Skew Heap
                                                     private:
                                                       TNode<T> *root, *null;
 * merge : root = merge(x, y)
                                                        TNode<T> node[MAXN];
         : root = merge(root.lc, root.rc)
                                                        int ncnt;
  рор
                                                        TNode<T>* newnode(T val, TNode<T> *fa) {
const int MAXSIZE = 10000;
                                                          TNode<T> *x = &node[++ncnt];
                                                          x->1c = x->rc = null;
                                                          x->fa = fa;
class Node {
                                                          x\rightarrow val = x\rightarrow sum = val, x\rightarrow inc = 0, x\rightarrow sz = 1;
public:
                                                          return x;
  int num, lc, rc;
  Node(int _{v=0}) : num(_{v}), lc(-1), rc(-1) {}
                                                       TNode<T>* build(int 1, int r, TNode<T> *fa) {
} tree[MAXSIZE];
                                                          if( l>r ) return null;
int merge(int x, int y){
                                                          int md = (1+r) >> 1;
    if( x==-1 ) return y;
                                                          TNode<T> *now = newnode(all[md], fa);
    if( y==-1 ) return x;
                                                          now->lc = build(l, md-1, now);
    if( tree[x].num<tree[y].num ) // key</pre>
                                                          now->rc = build(md+1, r, now);
        swap(x, y);
                                                          now->up();
    tree[x].rc = merge(tree[x].rc, y);
                                                          return now;
    swap(tree[x].lc, tree[x].rc);
                                                       void RotateTo(int x, TNode<T> *aim) {
    return x;
                                                          // find k-th element
}
                                                          TNode<T> *now = root;
     Splay Tree
                                                          while (now->lc->sz != x) {
                                                            if( now->lc->sz > x ) now = now->lc;
template < class T>
```

```
else x -= now->lc->sz+1, now = now->rc;
                                                       ranx += (ranx << 2) + 1;
    }
                                                       return ranx;
    splay(now, aim);
                                                     void New_node(Node *&o, int val) {
  void splay(TNode<T> *now, TNode<T> *aim) {
                                                       if(list == NULL) {
                                                         Node *tt = new Node[100];
    // make now become aim's child
    TNode<T> *fa, *fafa;
                                                         for(int i = 0; i < 100; i ++) {
    while( now->fa != aim ) {
                                                           tt[i].w = ran();
      if( now->fa->fa == aim ) Rotate(now, now->
                                                           tt[i].r = list;
          fa->lc==now);
                                                           list = tt + i;
                                                         }
      else {
                                                       }
        fa = now->fa, fafa = fa->fa;
        int pos = ( fafa->c[1] == fa );
                                                       o = list;
        if( fa->c[pos] == now ) Rotate(fa, !pos);
                                                       list = o \rightarrow r;
        else Rotate(now, pos);
                                                       o \rightarrow 1 = o \rightarrow r = NULL;
        Rotate(now, !pos);
                                                       o->v = o->minx = val;
      }
                                                       o \rightarrow size = 1;
    }
                                                       o->delta = o->rev = 0;
    now->up();
                                                     }
                                                     void Reuse(Node *o) { if(o) { o->r = list; list =
    if( aim == null ) root = now;
                                                          o; } }
  void Rotate(TNode<T> *now, int fl) {
                                                     void cut(Node *o, Node *&p, Node *&q, int num) {
    // fl : 0 - L-Rotate
                                                       if(num == 0) {
                                                         p = NULL; q = o;
            1 - R-Rotate
    //
    TNode<T> *fa = now->fa;
                                                       } else if(num == sz(o)) {
    now->down();
                                                         p = o; q = NULL;
    fa->c[!fl] = now->c[fl];
                                                       } else {
    if( now->c[f1] != null ) now->c[f1]->fa = fa;
                                                         o->down();
    now->fa = fa->fa;
                                                         if(num <= sz(o->1)) {
    if( fa->fa != null ) fa->fa->c[ fa->fa->c
                                                           q = o;
        [1] == fa ] = now;
                                                           cut(o->1,p,q->1,num);
    now->c[fl] = fa, fa->fa = now;
                                                           q->up();
    now->inc = fa->inc, fa->inc = 0;
                                                         } else {
    fa->up();
                                                           p = o;
 }
                                                           cut(o->r,p->r,q,num-sz(o->1)-1);
};
                                                           p->up();
SplayTree<11> tree;
                                                         }
                                                       }
3.7 Treap
                                                     void merge(Node *&o, Node *p, Node *q) {
struct Node {
                                                       if(!p || !q) {
  Node *1,*r;
                                                         o = p ? p : q;
  int v,delta,rev,size,minx,w;
                                                       } else {
  void up() {
                                                         if(p->w > q->w) {
    minx = v;
                                                           p->down();
    size = 1;
                                                           o = p;
    if(1) size += 1->size, minx = min(minx, 1->
                                                           merge(o->r,p->r,q);
        minx);
                                                         } else {
    if(r) size += r->size, minx = min(minx, r->
                                                           q->down();
        minx);
                                                           o = q;
                                                           merge(o->1,p,q->1);
  void down() {
    if(delta) {
                                                         o->up();
      if(1) 1->delta += delta, 1->v += delta, 1->
          minx += delta;
      if(r) r->delta += delta, r->v += delta, r->
                                                     void insert(Node *&o, int pos, int val) {
          minx += delta;
                                                       if(o == NULL) {
      delta = 0;
                                                         New_node(o,val);
                                                       } else {
    if(rev) {
                                                         Node *1 , *r , *n;
      swap(1,r);
                                                         New_node( n , val );
      if(1) 1->rev ^= 1;
                                                         cut ( o , l , r , pos );
      if(r) r->rev ^= 1;
                                                         merge( 1 , 1 , n );
      rev = 0:
                                                         merge( root , 1 , r );
    }
                                                       }
}*root = NULL, *list = NULL;
                                                     void add(int 1, int r, int val) {
inline int sz(Node *o) { return o ? o->size : 0;
                                                       Node *a, *b, *c;
                                                       cut(root,a,b,l-1);
int ran() {
                                                       cut(b,b,c,r-l+1);
  static int ranx = 123456789;
```

```
b->v += val;
                                                      } else if (tree[c][i] < as[mid]){</pre>
 b->minx += val;
                                                        sum[c][i]++;
                                                        tree[c+1][lp++] = tree[c][i];
 b->delta += val;
                                                      } else
 merge(a,a,b);
 merge(root,a,c);
                                                        tree[c+1][rp++] = tree[c][i];
                                                    if (1 == r)return;
void remove(int pos) {
 Node *a, *b, *c;
                                                    build(c+1, 1, mid);
  cut(root,a,b,pos-1);
                                                    build(c+1, mid+1, r);
  cut(b,b,c,1);
                                                  int query(int c, int l, int r, int ql, int qr,
 merge(root,a,c);
                                                     int k){
 Reuse(b);
                                                    int s;//[l, ql)內將被劃分到左子樹的元素數目
int query(int 1, int r) {
                                                    int ss;//[ql, qr]內將被劃分到左子數的元素數目
 Node *a, *b, *c;
                                                    int mid=(l+r)>>1;
 cut(root,a,b,l-1);
                                                    if (1 == r)
 cut(b,b,c,r-l+1);
                                                      return tree[c][1];
 int ret = b->minx;
                                                    if (1 == q1){//這裡要特殊處理!
 merge(a,a,b);
                                                      s = 0;
 merge(root,a,c);
                                                      ss = sum[c][qr];
 return ret;
                                                    }else{
}
                                                      s = sum[c][ql 1];
void reverse(int 1, int r) {
                                                      ss = sum[c][qr]-;
                                                    } //假設要在區間[l,r]中查找第k大元素, t為當前節
 Node *a, *b, *c;
 cut(root,a,b,l-1);
                                                        點,lch,rch為左右孩子,left,mid為節點t左
                                                        邊界界和中間點。
 cut(b,b,c,r-l+1);
 b->rev ^= 1;
                                                    if (k <= ss)//sum[r]-sum[l-1]>=k, 查找lch[t],區
                                                      間對應為[ left+sum[l-1], left+sum[r]-1 ] return query(c+1, l, mid, l+s, l+s+ss-1, k);
 merge(a,a,b);
 merge(root,a,c);
                                                    else
void revolve(int 1, int m, int r) {
                                                      //sum[r]-sum[l-1]<k,查找rch[t], 區間對應為
 Node *a, *b, *c, *d;
                                                      [mid+1+l-left-sum[l-1], mid+1+r-left-sum[r]]
 cut(root,a,b,l-1);
                                                      return query(c+1, mid+1, r, mid-l+1+ql-s, mid
 cut(b,b,c,m-l+1);
                                                         -l+1+qr-s-ss, k-ss);
 cut(c,c,d,r-m);
 merge(a,a,c);
                                                  int main(){
 merge(a,a,b);
                                                    int i, j, k;
                                                    while(~scanf("%d%d", &n, &m)){
 merge(root,a,d);
}
                                                      for(i=1; i<=n; i++) {</pre>
                                                        scanf("%d", &a[i]);
    劃分樹
3.8
                                                        tree[0][i] = as[i] = a[i];
#include <iostream>
                                                      sort(as+1, as+1+n);
#include <cstdio>
                                                      build(0, 1, n);
#include <algorithm>
                                                      while(m--){
using namespace std;
                                                        scanf("%d%d%d", &i, &j, &k);
#define N 100005
                                                          // i,j分別為區間起始點, k為該區間第k大的
int a[N], as[N];//原數組, 排序後數組
int n, m;
                                                        printf("%d\n", query(0, 1, n, i, j, k));
int sum[20][N]; // 紀錄第 i 層的 1~j 劃分到左子樹的元素
                                                      }
    個數(包括i)
                                                    }
int tree[20][N];//紀錄第i層元素序列
                                                    return 0;
void build(int c, int l, int r) {
  int i, mid=(l+r)>>1, lm=mid-l+1, lp=l, rp=mid
     +1;
  for (i=1; i<=mid; i++)</pre>
    if (as[i] < as[mid]) lm--;</pre>
     //先假設左邊的(mid-L+1)個數都等于as[mid],然
         后把實際上小于as[mid]的減去
  for (i = 1; i <= r; i++){
    if (i == 1) sum[c][i] = 0;
      //sum[i]表示[l, i]內有多少個數分到左邊, 用
         DP 來 維 護
    else sum[c][i] = sum[c][i-1];
    if (tree[c][i] == as[mid]){
     if (lm){
       lm--;
        sum[c][i]++;
        tree[c+1][lp++] = tree[c][i];
       tree[c+1][rp++] = tree[c][i];
```

## 4 Graph

#### 4.1 Bron-Kerbosch

```
typedef long long 11;
int n;
vector<ll> v, ne;
// ne[u] is the neighbours of u
// v is the result, P = (1 << n) - 1
void BronKerbosch(11 R, 11 P, 11 X){
  if ((P == 0LL) && (X == 0LL)) {v.push_back(R);
      return ;}
  int u = 0;
  for (; u < n; u ++) if ( (P|X) & (1LL << u) )
      break;
  for (int i = 0; i < n; i ++)
    if ( (P\&\neg ne[u]) \& (1LL << i) ){
      BronKerbosch(R | (1LL \langle\langle i), P & ne[i], X &
           ne[i]);
      P -= (1LL << i); X |= (1LL << i);
}
4.2 Dinic
class Flow {
public:
  Flow(int _ncnt) :ncnt(_ncnt), ecnt(1), path(new
       int[_ncnt + 2]), d(new int[_ncnt + 2]),
      visited(new bool[_ncnt + 2]){
    memset(path, 0, sizeof(int)*(_ncnt + 1));
  }
  ~Flow(){
    delete[](path);
    delete[](d);
    delete[](visited);
  void Reset(){
    memset(path, 0, sizeof(int)*(ncnt + 1));
    ecnt = 1;
  }
  void AddEdge(int s, int t, int cap){
    edge[++ecnt].tar = t, edge[ecnt].cap = cap,
        edge[ecnt].next = path[s], path[s] = ecnt
    edge[++ecnt].tar = s, edge[ecnt].cap = 0,
        edge[ecnt].next = path[t], path[t] = ecnt
  int MaxFlow(int s, int t){ // Dinic
    int f = 0, df;
    while (BFS(s, t) < ncnt){</pre>
      while (true){
        memset(visited, 0, sizeof(bool)*(ncnt +
        df = DFS(s, INF, t);
        if (!df) break;
        f += df;
      }
    }
    return f;
  }
private:
  static const int eMaxSize = 40002, INF = (int)
      1e9;
  int ecnt, ncnt;
  int *path, *d; // d for Dicic distance
  bool *visited;
  struct Edge{
```

```
int tar, cap, next;
  }edge[eMaxSize];
  int DFS(int a, int df, int t){
    if (a == t) return df;
    if (visited[a]) return 0;
    visited[a] = true;
    for (int i = path[a]; i; i = edge[i].next){
      int b = edge[i].tar;
      if (edge[i].cap > 0 && d[b] == d[a] + 1){
        int f = DFS(b, std::min(df, edge[i].cap),
             t);
        if (f){
          edge[i].cap -= f, edge[i ^ 1].cap += f;
          return f;
        }
      }
    }
    return 0;
  }
  int BFS(int s, int t){
    memset(d, 0x7f, sizeof(int)*(ncnt + 1));
    memset(visited, 0, sizeof(bool)*(ncnt + 1));
    d[s] = 0; visited[s] = true;
    std::queue<int> Q;
    Q.push(s);
    while (!Q.empty()){
      int a = Q.front(); Q.pop();
      for (int i = path[a]; i; i = edge[i].next){
        int b = edge[i].tar;
        if (visited[b] || edge[i].cap == 0)
            continue;
        visited[b] = true;
        d[b] = d[a] + 1;
        if (b == t) return d[b];
        Q.push(b);
      }
    return d[t];
  }
};
Flow flow( 1001 );
4.3 Hungarian
#include <stdio.h>
#include <string.h>
#include <algorithm>
using namespace std;
#define N 550
                          //max number of
    vertices in one part
#define INF 100000000
                          //just infinity
int cost[N][N];
                          //cost matrix
int n, max_match;
                          //n workers and n jobs
                          //labels of X and Y
int 1x[N], 1y[N];
   parts
int xy[N];
                          //xy[x] - vertex that is
    matched with x,
int yx[N];
                          //yx[y] - vertex that is
    matched with y
                         //sets S and T in
bool S[N], T[N];
   algorithm
int slack[N];
                          //as in the algorithm
   description
                          //slackx[y] such a
int slackx[N];
   vertex, that l(slackx[y]) + l(y) - w(slackx[y])
    ],y) = slack[y]
int pre[N];
                          //array for memorizing
   alternating paths
```

```
matched with y, to the queue
                                                               add_to_tree(yx[y], x);
void init_labels() {
                                                                                                 //add
  memset(lx, 0, sizeof(lx));
                                                                   edges (x,y) and (y,yx[y]) to the
  memset(ly, 0, sizeof(ly));
  for (int x = 0; x < n; x++)
                                                           if (y < n) break;
    for (int y = 0; y < n; y++)
      lx[x] = max(lx[x], cost[x][y]);
                                                               //augmenting path found!
void update_labels() {
                                      //init delta
                                                         if (y < n) break;
  int x, y, delta = INF;
      as infinity
  for (y = 0; y < n; y++)
                                      //calculate
                                                            //augmenting path found!
     delta using slack
                                                         update_labels();
    if (!T[y])
      delta = min(delta, slack[y]);
                                                             //augmenting path not found, so improve
  for (x = 0; x < n; x++)
                                      //update X
                                                            Labelina
      labels
                                                         wr = rd = 0;
    if (S[x]) 1x[x] -= delta;
                                                         for (y = 0; y < n; y++)
                                      //update Y
  for (y = 0; y < n; y++)
                                                           if (!T[y] \&\& slack[y] == 0){
      labels
                                                             if (yx[y] == -1){
    if (T[y]) ly[y] += delta;
                                                                 //exposed vertex in Y found -
  for (y = 0; y < n; y++)
                                      //update
     slack array
                                                                 augmenting path exists!
    if (!T[y])
                                                               x = slackx[y];
      slack[y] -= delta;
                                                               break;
}
                                                             }
                                                             else{
void add_to_tree(int x, int prex) {
                                                               T[y] = true;
  S[x] = true;
  pre[x] = prex;
                                                                   //else just add y to T,
                                                               if (!S[yx[y]]){
  for (int y = 0; y < n; y++)
     \textbf{if} \ (1x[x] + 1y[y] - cost[x][y] < slack[y]) \{ \\
                                                                 q[wr++] = yx[y];
      slack[y] = lx[x] + ly[y] - cost[x][y];
                                                                                                     //
      slackx[y] = x;
                                                                     add vertex yx[y], which is
    }
                                                                     matched with y, to the queue
}
                                                                 add_to_tree(yx[y], slackx[y]);
                                                                                       //and add edges
void augment() {
                                                                     (x,y) and (y, yx[y]) to the tree
  if (max_match == n) return;
                                                               }
  int x, y, root;
                                                             }
                                                           }
  int q[N], wr = 0, rd = 0;
                                                         if (y < n) break;
  memset(S, false, sizeof(S));
  memset(T, false, sizeof(T));
                                                            //augmenting path found!
  memset(pre, -1, sizeof(pre));
                                                      if (y < n){
  for (x = 0; x < n; x++)
    if (xy[x] == -1){
      q[wr++] = root = x;
                                                          //we found augmenting path!
      pre[x] = -2;
                                                         max_match++;
      S[x] = true;
      break;
                                                             //increment matching
    }
                                                         //in this cycle we inverse edges along
                                                            augmenting path
  for (y = 0; y < n; y++){
                                                         for (int cx = x, cy = y, ty; cx != -2; cx =
    slack[y] = lx[root] + ly[y] - cost[root][y];
                                                            pre[cx], cy = ty){
    slackx[y] = root;
                                                           ty = xy[cx];
                                                           yx[cy] = cx;
                                                           xy[cx] = cy;
  while (true){
                                                         }
    while (rd < wr){</pre>
                                                         augment();
      x = q[rd++];
      for (y = 0; y < n; y++)
                                                             //recall function, go to step 1 of the
        if (cost[x][y] == 1x[x] + 1y[y] && !T[y]
                                                            algorithm
                                                      }
            ]){
          if (yx[y] == -1) break;
          T[y] = true;
                                                     int hungarian(){
          q[wr++] = yx[y];
                                                       int ret = 0;
                                                                                          //weight of
                                                           the optimal matching
              //add vertex yx[y], which is
```

```
max_match = 0;
                                    //number of
                                                      InBlossom[Base[link[i]]]=true;
     vertices in current matching
 memset(xy, -1, sizeof(xy));
                                                    for (i=y;Base[i]!=lca;i=pre){
  memset(yx, -1, sizeof(yx));
                                                      if (Base[pre]!=lca) Father[pre]=link[i]; //同
  init_labels();
                                    //step 0
                                    //steps 1-3
                                                      InBlossom[Base[i]]=true;
  augment();
  for (int x = 0; x < n; x++)
                                    //forming
                                                      InBlossom[Base[link[i]]]=true;
     answer there
    ret += cost[x][xy[x]];
                                                    #undef pre
                                                                                     //注意不能從
  return ret;
                                                    if (Base[x]!=lca) Father[x]=y;
                                                        Lca這個奇環的關鍵點跳回來
}
int main(){
                                                    if (Base[y]!=lca) Father[y]=x;
 while ( scanf("%d",&n) == 1 ){
                                                    for (i=1;i<=n;i++)</pre>
    for ( int i = 0 ; i < n ;i++ )
                                                      if (InBlossom[Base[i]]){
      for ( int j = 0 ; j < n ; j++ )
                                                        Base[i]=lca;
       scanf("%d",&cost[i][j]);
                                                        if (!in_Queue[i]){
    int ret = hungarian();
                                                          Q[++tail]=i;
                                                          in_Queue[i]=true; //要注意如果本來連向
    for ( int i = 0 ; i < n ;i++ )
      printf("%d%c",lx[i],i==n-1?'\n':' ');
                                                              BFS樹中父結點的邊是非匹配邊的點,可能
    for ( int i = 0 ; i < n ; i++ )
                                                              是沒有入隊的
      printf("%d%c",ly[i],i==n-1?'\n':' ');
                                                        }
    printf("%d\n",ret);
                                                      }
  }
  return 0;
                                                  void Change(){
                                                    int x,y,z;
}
                                                    z=Finish;
    maximum matching in general graph
                                                    while (z){
                                                      y=Father[z];
//Problem:http://acm.timus.ru/problem.aspx?space
                                                      x=link[y];
   =18num=1099
                                                      link[y]=z;
#include <cstdio>
                                                      link[z]=y;
#include <cstdlib>
                                                      z=x;
#include <cstring>
                                                    }
#include <iostream>
                                                  }
#include <algorithm>
                                                  void FindAugmentPath(){
using namespace std;
                                                    fill(Father, Father+n+1,0);
const int N=250;
                                                    fill(in_Queue,in_Queue+n+1,false);
int n;
                                                    for (int i=1;i<=n;i++) Base[i]=i;</pre>
int head;
                                                    head=0; tail=1;
int tail;
                                                    Q[1]=Start;
int Start;
                                                    in_Queue[Start]=1;
int Finish;
                                                    while (head!=tail){
int link[N];
                //表示哪個點匹配了哪個點
                                                      int x=Q[++head];
int Father[N];
                  //這個就是增廣路的Father……但
                                                      for (int y=1;y<=n;y++)
    是用起來太精髓了
                                                        if (map[x][y] && Base[x]!=Base[y] && link[x
               //該點屬於哪朵花
int Base[N];
                                                                   //無意義的邊
                                                            ]!=y)
int Q[N];
                                                          if ( Start==y || link[y] && Father[link[y
bool mark[N];
                                                              ]] ) //精髓地用Father表示該點是否
bool map[N][N];
                                                            BlossomContract(x,y);
bool InBlossom[N];
                                                          else if (!Father[y]){
bool in_Queue[N];
                                                            Father[y]=x;
                                                            if (link[y]){
void CreateGraph(){
                                                              Q[++tail]=link[y];
  int x,y;
                                                              in_Queue[link[y]]=true;
  scanf("%d",&n);
                                                            }
 while (scanf("%d%d",&x,&y)!=EOF)
                                                            else{
    map[x][y]=map[y][x]=1;
                                                              Finish=y;
                                                              Change();
void BlossomContract(int x,int y){
                                                              return;
 fill(mark, mark+n+1, false);
                                                            }
  fill(InBlossom, InBlossom+n+1, false);
                                                          }
 #define pre Father[link[i]]
                                                    }
  int lca,i;
                                                  }
  for (i=x;i;i=pre) {i=Base[i]; mark[i]=true; }
                                                  void Edmonds(){
  for (i=y;i;i=pre) {i=Base[i]; if (mark[i]) {lca
                                                    memset(link,0,sizeof(link));
     =i; break;} } //尋找 Lca之旅……一定要注意i
                                                    for (Start=1;Start<=n;Start++)</pre>
     =Base[i]
                                                      if (link[Start]==0)
  for (i=x;Base[i]!=lca;i=pre){
                                                        FindAugmentPath();
    if (Base[pre]!=lca) Father[pre]=link[i]; //對
       於BFS樹中的父邊是匹配邊的點, Father向後跳
                                                  void output(){
    InBlossom[Base[i]]=true;
```

```
fill(mark,mark+n+1,false);
  int cnt=0;
  for (int i=1;i<=n;i++)</pre>
    if (link[i]) cnt++;
  printf("%d\n",cnt);
  for (int i=1;i<=n;i++)</pre>
    if (!mark[i] && link[i]){
      mark[i]=true;
      mark[link[i]]=true;
      printf("%d %d\n",i,link[i]);
    }
}
int main(){
  CreateGraph();
  Edmonds();
  output();
  return 0;
```

#### 5 Math

```
5.1
    China remainder theorem
  ans \equiv a_i \pmod{m_i}
int china_remainder_theorem(int n, int ai[], int
    mi[]) {
  int gcdn, x, y, reduce, tmp;
  for(int i=1; i<n; ++i) {</pre>
     gcdn=ext_gcd(mi[i-1], mi[i], x, y);
     reduce=ai[i]-ai[i-1];
     if( reduce%gcdn!=0 )
       return -1;
     tmp=mi[i]/gcdn;
     x=(reduce/gcdn*x%tmp+tmp)%tmp;
    ai[i] = ai[i-1] + mi[i-1]*x;
    mi[i] = mi[i-1]*tmp;
  return ai[n-1]%mod;
}
5.2 Euler's phi function O(n)
1. gcd(x,y) = d \Rightarrow \phi(xy) = \frac{\phi(x)\phi(y)}{\phi(d)}
2. p \text{ is } prime \Rightarrow \phi(p^k) = p^{k-1}\phi(p)
3. p \text{ is } prime \Rightarrow \phi(p^k) = \phi(p^{k-1}) \times p
4. n = p_1^{k_1} p_2^{k_2} \cdots p_m^{k_m}
   \Rightarrow \phi(n) = p_1^{k_1 - 1} \phi(p_1) \ p_2^{k_2 - 1} \phi(p_2) \cdots p_m^{k_m - 1} \phi(p_m)
const int MAXN = 100000;
int phi[MAXN], prime[MAXN], pn=0;
memset(phi, 0, sizeof(phi));
for(int i=2; i<MAXN; ++i) {</pre>
  if( phi[i]==0 ) prime[pn++]=i, phi[i]=i-1;
  for(int j=0; j<pn; ++j) {</pre>
     if( i*prime[j]>MAXN ) break;
     if( i%prime[j]==0 ) {
       phi[i*prime[j]] = phi[i] * prime[j];
       break;
    phi[i*prime[j]] = phi[i] * phi[prime[j]];
  }
5.3 Extended Euclid's Algorithm
  ax + by = gcd(a, b)
int ext_gcd(int a, int b, int &x, int &y){
  int x2;
  if( b==0 ) {
    x=1, y=0;
     return a;
  int gcdn=ext_gcd(b, a%b, x, y), x2=x;
  x=y, y=x2-a/b*y;
  return gcdn;
int ext_gcd(int a, int b, int &x, int &y){
  int t, px=1, py=0, tx,ty;
  x=0, y=1;
  while(a%b!=0) {
    tx=x, ty=y;
    x=x*(-a/b)+px, y=y*(-a/b)+py;
     px=tx, py=ty;
    t=a, a=b, b=t%b;
  }
  return b;
}
```

```
5.4
    FFT
                                                         ll iter=1, p2=p*p;
                                                         for(int i=0; i<half_n; i++) {</pre>
#include<cstdio>
                                                           11 odd_part=iter*odd_b[i];
#include < cstdlib >
                                                           b[i]=(even_b[i]+odd_part)%p;
#include<vector>
                                                           b[half_n|i]=(even_b[i]+p2-odd_part)%p;
using namespace std;
                                                           iter*=r;
                                                            iter%=p;
typedef long long 11;
                                                         }
                                                       }
int ODD[1<<20], EVEN[1<<20], ODD_B[1<<20], EVEN_B</pre>
                                                       else b[0]=a[0];
   [1<<20];
int mul_order(int n) {
                                                     void print(int *a, int n) {
                                                       for(int i=0; i<n; i++)</pre>
  int high_bit = n&(-n);
                                                         printf("%d%c",a[i],i==n-1?'\n':' ');
  for(n-=high_bit; n; n-=high_bit)
    high_bit = n&(-n);
  return high_bit<<2;
                                                     // c=a*b where c is initially empty
}
                                                     void multiply(int *a, int *b, int *c,
                                                       int n, ll inv_n, ll r, ll inv_r, ll p) {
// return a^x mod p
                                                       int *f, *g, *h;
int mod_pow(int a, int x, int p) {
                                                       f=new int[n];
  if(x==0) return 1;
                                                       g=new int[n];
  11 ret = mod_pow(a,x>>1,p);
                                                       h=new int[n];
  ret*=ret;
                                                       cooley_tukey(a,f,n,r,p);
  ret%=p;
                                                       cooley_tukey(b,g,n,r,p);
  return (x&1)?(ret*a)%p:ret;
                                                       for(int i=0; i<n; i++) h[i]=(11)f[i]*g[i]%p;</pre>
}
                                                       cooley_tukey(h,c,n,inv_r,p);
                                                       for(int i=0; i<n; i++) c[i]=c[i]*inv_n%p;</pre>
// only works for prime p
                                                       delete[] f;
int mod_inverse(int x, int p) { return mod_pow(x,
                                                       delete[] g;
   p-2,p); }
                                                       delete[] h;
// n is a power of 2 and answer is at most
   upper bound
                                                     int main() {
// 2013265921=1+2^27*3*5 is a prime
                                                       int n, N;
inline int suitable_prime(int n, int upper_bound)
                                                       scanf("%d",&n);
     { return 2013265921; }
                                                       N=mul_order(n);
                                                       printf("N=%d\n",N);
// not general version
                                                       int *a, *b, *c;
int primitive_root(int p) {
                                                       a=new int[N];
  int ret;
                                                       b=new int[N];
  srand(714091); // THOR
                                                       c=new int[N];
   srand(time(NULL));
                                                       for(int i = 0; i < n; i++) scanf("%d",&a[i]);</pre>
  for(ret=rand()%p;;ret=rand()%p) {
                                                       for(int i = 0; i < n; i++) scanf("%d",&b[i]);</pre>
    if(mod_pow(ret,(p-1)/2,p)!=1 &&
                                                       for(int i = n; i< N; i++)</pre>
                                                                                   a[i]=b[i]=0;
      mod_pow(ret,(p-1)/3,p)!=1 \&\&
                                                       int p=suitable_prime(N,10007);
      mod_pow(ret,(p-1)/5,p)!=1)
                                                       11 r=principal_root(N,p);
      return ret;
                                                       11 inv_r=mod_inverse(r,p);
  }
                                                       11 inv_n=mod_inverse(N,p);
}
                                                       multiply(a,b,c,N,inv_n,r,inv_r,p);
                                                       int last=N-1;
// nth principle root of unity (mod p)
                                                       while(last>=0 && c[last]==0) last--;
int principal_root(int n, int p) {
                                                       for(int i = 0; i<=last; i++)</pre>
  int g=primitive_root(p);
                                                         printf("%d%c",c[i],last==i?'\n':' ');
  return mod_pow(g,(p-1)/n,p);
                                                       return 0;
}
void cooley_tukey(int *a, int *b, int n, ll r, ll 5.5 Gaussian Elimination
     p) {
  if(n>1) {
                                                     // default for module version, comments for
    int half n=n>>1;
                                                         double version
    int *odd=ODD+half n, *even=EVEN+half n;
                                                     //double mmap[row][column];
    int *odd_b=ODD_B+half_n, *even_b=EVEN_B+
                                                     const 11 modn = 1000000007;
                                                     11 mmap[row][column];
        half n:
    for(int i=0; i<n; i+=2) {</pre>
                                                     11 inv(11 b)
      even[i>>1]=a[i];
                                                     {
                                                       return (b==1)?1:inv(modn%b)*(modn-modn/b)%modn;
      odd[i>>1]=a[1|i];
    }
                                                     void gauss(ll mat[row][column],int n,int m)
    cooley_tukey(even,even_b,n>>1,r*r%p,p);
    cooley_tukey(odd,odd_b,n>>1,r*r%p,p);
                                                     {
```

memset(mobius, true, sizeof(mobius));

```
int k=0;
                                                        memset(fcnt, 0, sizeof(fcnt));
  for(int i=0; i<m; i++)</pre>
                                                        for(int i=2; i<=n; ++i) {</pre>
                                                          if( isp[i] ) {
    for(int j=k; j<n; j++)</pre>
      if(mat[j][i]!=0){
                                                            fcnt[i] = 1;
        for(int l=i; l<m; l++)</pre>
                                                            for(int j=i+i; j<=n; j+=i) {</pre>
          swap(mat[k][1],mat[j][1]);
                                                              isp[j] = false;
        for(j++; j<n; j++){</pre>
                                                               if( fcnt[j]!=-1 ) fcnt[j]++;
          if(mat[j][i]==0)
             continue;
                                                            if( i<=10000 )
                                                              for(int ii=i*i, j=ii; j<=n; j+=ii) {</pre>
           //double scale=mat[j][i]/mat[k][i];
          long long scale=mat[j][i]*inv(mat[k][i
                                                                fcnt[j] = -1;
              ])%modn; //mod version
          for(int p=i+1; p<m; p++)</pre>
                                                          }
            //mat[j][p]-=mat[k][p]*scale;
                                                        }
             mat[j][p]=(mat[j][p]-mat[k][p]*scale%
                                                        mobius[0] = 0;
                                                        mobius[1] = 1;
                 modn+modn)%modn;
                                                        for(int i=2; i<=n; ++i) {</pre>
          mat[j][i]=0;
                                                          if( fcnt[i]==-1 ) mobius[i] = 0;
        }
        k++;
                                                          else if( fcnt[i]&1 ) mobius[i] = -1;
        break;
                                                          else mobius[i] = 1;
      }
                                                        }
                                                      }
}
     Miller Rabin
ll mul(ll a, ll b, ll n) { // a*b%n
  11 r = 0;
  a %= n, b %= n;
  while(b){
    if( b\&1 ) r = a+r>=n ? a+r-n : a+r;
    a = a+a>=n ? a+a-n : a+a;
    b >>= 1;
  }
  return r;
ll powmod(ll a, ll d, ll n) { // a^d%n
  if(d==0) return 111;
  if(d==1) return a%n;
  return mul(powmod(mul(a, a, n), d>>1, n), d%2?a
      :1, n);
bool miller_rabin(ll n, ll a) {
  if(__gcd(a,n)==n) return true;
  if(__gcd(a,n)!=1) return false;
  11 d = n-1, r = 0, res;
  while(d%2==0) { ++r; d>>=1; }
  res = powmod(a, d, n);
  if(res==1||res==n-1) return true;
  while(r--) {
    res = mul(res, res, n);
    if(res==n-1) return true;
  }
  return false;
bool isPrime(ll n) {
  ll as[7]={2, 325, 9375, 28178, 450775, 9780504,
       1795265022}; // 2, 7, 61
  for(int i=0; i<7; i++)
    if( !miller_rabin(n, as[i]) )
      return false;
  return true;
    Möbius function
5.7
int* isp;
char fcnt[N+5];
int mobius[N+5];
void make_mobius(int n) {
  isp = mobius;
```

# 6 String

```
AhoCorasick
#include <queue>
using namespace std;
template<int NodeSZ>
class AhoCorasick {
public:
  AhoCorasick() { clear(); }
  void clear() {
    all[0] = Node();
    ncnt = 1;
  void insert(char *s) {
    Node *curr = &all[0], *next;
    for(int i=0; s[i]; ++i) {
      next = curr->next[idx(s[i])];
      if( next == NULL )
        next = &all[ncnt], all[ncnt++] = Node();
      curr = curr->next[idx(s[i])] = next;
    }
    curr->val++;
  }
  void build() {
    queue<Node*> qq;
    qq.push(&all[0]);
    while( !qq.empty() ) {
      Node *curr = qq.front(), *fail;
      qq.pop();
      for(int i=0; i<NodeSZ; ++i) {</pre>
        if( !curr->next[i] ) continue;
        qq.push(curr->next[i]);
        fail = curr->fail;
        while( fail && !fail->next[i] )
          fail = fail->fail;
        curr->next[i]->fail = fail ? fail->next[i
            ] : &all[0];
      }
    }
  }
  int count(char *s) {
    build();
    int cnt = 0;
    Node *curr = &all[0], *tmp;
    for(int i=0, ch; s[i]; ++i) {
      ch = idx(s[i]);
      while( curr && !curr->next[ch] )
        curr = curr->fail;
      curr = curr ? curr->next[ch] : all[0].next[
          ch];
      tmp = curr;
      while( tmp && tmp->val ) {
        cnt += tmp->val;
        tmp->val = 0;
        tmp = tmp->fail;
      }
    }
    return cnt;
  }
private:
  struct Node {
    Node() : val(0), fail(NULL) {
      for(int i=0; i<NodeSZ; ++i) next[i] = NULL;</pre>
    int val;
    Node *fail, *next[NodeSZ];
  Node all[250005];
```

```
int ncnt;
  inline int idx(char c) { return c-'a'; }
AhoCorasick<26> AC;
6.2 KMP
int KMP(char pat[5005], char str[5005]) {
  if( strlen(pat)>strlen(str) ) return -1;
  int failure[5005];
  int len=strlen(pat);
  for(int i=1, j=failure[0]=-1; i<len; ++i) {</pre>
    while( j>=0 && pat[j+1]^pat[i] ) j=failure[j
    if( pat[j+1]==pat[i] ) ++j;
    failure[i]=j;
  for(int i=0, j=-1; str[i]; ++i) {
    while( j>=0 && str[i]^pat[j+1] ) j=failure[j
        1;
    if( str[i]==pat[j+1] ) ++j;
    if( j==len-1 ) {
      return i-len+1; // rec this!!
      j=failure[j];
    }
  }
  return -1;
}
    Longest Palindromic Substring
6.3
char t[1001];
                // 要處理的字串
cahr s[1001 * 2]; // 中間插入特殊字元的t。
int Z[1001 * 2], L, R; // Gusfield's Algorithm // 由a往左、由b往右,對稱地作字元比對。
int match(int a, int b) {
  int i = 0;
  while (a-i)=0 \&\& b+i < N \&\& s[a-i] == s[b+i]) i
      ++;
  return i;
}
void longest palindromic substring()
{
  int N = strlen(t);
  // 在t中插入特殊字元, 存放到s。
  memset(s, '.', N*2+1);
  for (int i=0; i<N; ++i) s[i*2+1] = t[i];</pre>
  N = N*2+1;
  // modified Gusfield's lgorithm
  Z[0] = 1;
  L = R = 0;
  for (int i=1; i<N; ++i) {</pre>
                            // i的映射位置
    int ii = L - (i - L);
    int n = R + 1 - i;
    if (i > R) {
      Z[i] = match(i, i);
      L = i;
      R = i + Z[i] - 1;
    }
    else if (Z[ii] == n) {
      Z[i] = n + match(i-n, i+n);
      L = i;
      R = i + Z[i] - 1;
    else Z[i] = min(Z[ii], n);
  // 尋找最長迴文子字串的長度。
  int n = 0, p = 0;
  for (int i=0; i<N; ++i)</pre>
    if (Z[i] > n) n = Z[p = i];
  // 記得去掉特殊字元。
```

int len = strlen(G);

```
cout << "最長迴文子字串的長度是" << (n-1) / 2;
                                                      z[0] = len;
  // 印出最長迴文子字串,記得別印特殊字元。
                                                       int L = 0, R = 1;
  for (int i=p-Z[p]+1; i<=p+Z[p]-1; ++i)</pre>
                                                       for ( int i = 1 ; i < len ; i++ ) {</pre>
    if (i & 1) cout << s[i];</pre>
                                                         if ( i >= R || z[i-L] >= R-i ) {
                                                           int x = (i >= R) ? i : R;
                                                           while ( x < len \&\& G[x] == G[x-i] )
6.4
    Suffix Array
                                                             x++;
                                                           z[i] = x - i;
int myrank[LEN], sa[LEN];
                                                           if (x > i) L = i, R = x;
int height[LEN];
int y[LEN], cnt[LEN], rr[2][LEN];
                                                         else z[i] = z[i-L];
inline bool same(int *_myrank, int a, int b, int
   1) { return _myrank[a]==_myrank[b]&&_myrank[a }
   +1]==_myrank[b+1]; }
void make_height(char str[]) {
  int len=strlen(str);
  MSET(height, 0);
  for(int i=0, j=0; i<len; ++i, j=height[myrank[i</pre>
      -1]]-1) {
    if( myrank[i]==1 ) continue;
    if( j<0 ) j=0;
    while( i+j<len && sa[myrank[i]-1]+j<len &&
      str[i+j]==str[sa[myrank[i]-1]+j]) ++j;
    height[myrank[i]]=j;
  }
}
void sa2(char str[], int n, int MAX = 256) {
  printf("%s!! %d %d\n", str, n, MAX);
  int *rank1=rr[0], *rank2=rr[1];
  int *myrank1=rr[0], *myrank2=rr[1]; // rolling
  int *y = myrank; // share memory
  MSET(rr[1], 0);
  MSET(cnt, 0);
  int i, p=0;
  for(i=0; i<n; ++i) myrank2[i]=str[i], cnt[</pre>
     myrank2[i]]++;
  for(i=1; i<MAX; ++i) cnt[i]+=cnt[i-1];</pre>
  for(i=n-1; i>=0; --i) sa[--cnt[myrank2[i]]]=i;
  for(int j=1; p<n; j<<=1, MAX=p) {</pre>
    // 表示用第二個key(myrank2)排序後 從 y[i] 開
        始的後綴排第i名
    for(p=0, i=n-j; i<n; ++i) y[p++]=i;</pre>
    for(i=0; i<n; ++i) if( sa[i]>=j ) y[p++]=sa[i
        ]-j;
    for(i=0; i<MAX; ++i) cnt[i]=0;</pre>
    for(i=0; i<n; ++i) cnt[ myrank2[y[i]] ] ++;</pre>
    for(i=1; i<MAX; ++i) cnt[i]+=cnt[i-1];</pre>
    for(i=n-1; i>=0; --i) sa[ --cnt[ myrank2[y[i
        ]] ]=y[i];
    for(p=i=1, myrank1[sa[0]]=0; i<n; ++i)</pre>
      myrank1[sa[i]]=same(myrank2, sa[i], sa[i
          -1], j)?p-1:p++;
    std::swap(myrank1, myrank2);
  }
  for(int i=0; i<n; ++i) myrank[i]=myrank2[i];</pre>
  make_height(str);
int main() {
  char str[LEN];
  scanf("%s", str);
  int len = strlen(str);
  sa2(str, len+1);
  for(int i=1; i<=len; ++i) printf("%d %d %s\n",</pre>
      i, height[i], str+sa[i]);
}
    Z Algorithm
void Z(char G[], int z[]){
```

const int  $dx[4] = \{-1, 1, 0, 0\}, dy[4] = \{0, 0, 0\}$ 

#### 7 Others

```
1, -1};
    8 puzzle - IDA*
                                                 char solution[30];
                                                  // 正確的推動方式,其數值是方向0~3。
// 一個盤面。其數值1~8代表方塊號碼,0代表空格。
                                                 const int reverse_dir[4] = {1, 0, 3, 2};
int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
                                                  // 用表格紀錄每一個方向的反方向。可用於避免來回
// 檢查 permutation inversion。檢查不通過,表示盤
                                                      推動的判斷。
    面不合理。
bool check_permutation_inversion(int board[3][3])
                                                 int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
                                                  // 起始狀態。其數值1~8代表方塊號碼,0代表空格。
  int inversion = 0;
  for (int a=0; a<9; ++a)</pre>
                                                 int sx = 1, sy = 2;
    for (int b=0; b<a; ++b) {</pre>
                                                  // 空格的位置。可馬上知道推動方塊的目的地。
      int i = a / 3, j = a % 3;
     int ii = b / 3, jj = b % 3;
                                                 bool onboard(int x, int y)
     if (board[i][j] && board[ii][jj]
                                                 {return x \ge 0 \&\& x < 3 \&\& y \ge 0 \&\& y < 3;}
       \&\&\ board[i][j]\ <\ board[ii][jj])
       inversion++;
                                                 int IDAstar(int x, int y, int gv, int prev_dir,
   }
                                                    int& bound, bool& ans) {
  int row number of 0 = 0;
                                                   int hv = h(board);
  for (int i=0; i<3 && !row number of 0; ++i)</pre>
                                                   if (gv + hv > bound) return gv + hv;
   for (int j=0; j<3 && !row_number_of_0; ++j)</pre>
                                                     // 超過,回傳下次的bound
     if (board[i][j] == 0)
                                                   if (hv == 0) {ans = true; return gv;}
       row_number_of_0 = i+1;
                                                     // 找到最佳解
  return (inversion + row_number_of_0) % 2 == 0;
}
                                                   int next_bound = 1e9;
for (int i=0; i<4; ++i) {
// heuristic function,採用不在正確位置上的方塊個
                                                     // 四種推動方向
                                                     int nx = x + dx[i], ny = y + dy[i];
int h(int board[3][3])
                                                      // 空格的新位置
                                                     if (reverse_dir[i] == prev_dir) continue;
  int cost = 0;
                                                      // 避免來回推動
  for (int i=0; i<3; ++i)
                                                     if (!onboard(nx, ny)) continue;
   for (int j=0; j<3; ++j)</pre>
                                                      // 避免出界
     if (board[i][j])
                                                     solution[gv] = oper[i];
       if (board[i][j] != i*3 + j + 1)
                                                      // 紀錄推動方向
         cost++;
                                                     swap(board[x][y], board[nx][ny]);
  return cost;
                                                      // 推動
}
                                                     int v = IDAstar(nx, ny, gv+1, i, bound, ans);
if (ans) return v;
int taxicab_distance(int x1, int y1, int x2, int
                                                     next_bound = min(next_bound, v);
   y2)
                                                     swap(board[nx][ny], board[x][y]);
{return abs(x1 - x2) + abs(y1 - y2);}
                                                      // 回復原狀態
// heuristic function, 採用taxicab distance。
                                                   return next_bound;
int h(int board[3][3]) {
  // 每塊方塊的正確位置。 {0,0}是為了方便編寫程式
     而多加的。
                                                 void eight_puzzle() {
  static const int right_pos[9][2] = {
                                                   if (!check_permutation_inversion(board)) {
    {0,0},
                                                     cout << "盤面不合理,無法解得答案。" << endl;
    \{0,0\}, \{0,1\}, \{0,2\},
                                                     return;
    \{1,0\}, \{1,1\}, \{1,2\},
                                                   }
    \{2,0\}, \{2,1\}
                                                   // IDA*
                                                   bool ans = false;
  // 計算每個方塊與其正確位置的 taxicab distance
                                                   int bound = 0;
     的總和。
                                                  while (!ans && bound <= 50)
  int cost = 0;
                                                     bound = IDAstar(sx, sy, 0, -1, bound, ans);
  for (int i=0; i<3; ++i)</pre>
                                                   if (!ans) {
    for (int j=0; j<3; ++j)</pre>
                                                     cout << "50步內無法解得答案。" << endl;
      if (board[i][j])
                                                     return;
       cost += taxicab_distance(
                                                  // 印出移動方法
             right pos[board[i][j]][0],
                                                  for (int i=0; i<bound; ++i)</pre>
             right_pos[board[i][j]][1]
                                                    cout << operation[solution[i]] << ' ';</pre>
                                                   cout << endl;</pre>
  return cost;
                                                 }
}
                                                 7.2 recursive to stack
// 上下左右
                                                   replace all variable in data into layer[lay].variable
const string operator[4] = {"up", "down", "right"
   , "left"};
                                                 struct data {
```

```
parameter;
  local variabla;
                 //new
  direction;
} layer[10000];
int lay=0; //new
type reval; //new
void go() {
// at the beginning
start:
// call recursive function
  direction = 1;
  lay++, parameter = value;
  goto start;
point1:
  variable = reval;
// return
 reval = value;
  lay--;
  goto trans;
// at the end
trans:
  switch (direction) {
    case 1:
      goto point1;
}
```

## The End