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6.1 8 puzzle - IDA\* . . . . . . . . . . . . . . . .

# **Enviroment Settings**

1	1.1	·viiiiC
1	" se	et encoding
	set	encoding=utf-8
2	set	fileencodings=utf-8,big5
	set	showmode
2	2 syntax on	
2	set	hlsearch
		background=dark
3		laststatus=2
		wildmenu
2		scrolloff=5 " keep at least 5 lines above/
3		below
-		ruler
5		cursorline
	set	<pre>ic " ignore case when searching bs=2 " enable backspace</pre>
7		number
7		tabstop=4
		shiftwidth=4
′		autoindent
۵		smarttab
9		smartindent
9		o <f9> <esc>:w<enter><f9></f9></enter></esc></f9>
9	map∢	<pre><f9> :!g++ "%:t" -o "%:r.out" -Wall -Wshadow -</f9></pre>
9	•	02 -Im && "./%:r.out"
10	map	<pre><f10> :!g++ "%:t" -o "%:r.out" -Wall -Wshadow</f10></pre>
		-02 -Im
10		
10		
10		
10		
1 1		

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## 2 Data Structure

## 2.1 Fenwick Tree [1, size]

```
inline int lowbit(int x) { return x&-x; }
template < class T>
class fenwick {
public:
  fenwick(int __size=SIZE) {
    size = \__size+10;
    a = new T[size], b=new T[size];
    memset(a, 0, sizeof(T)*size);
    memset(b, 0, sizeof(T)*size);
  ~fenwick() { delete[] a, delete[] b;}
  inline void add(int 1, int r, long long n) {
  __add(a, r, r*n), __add(a, l-1, (l-1)*-n);
     _add(b, r, n), __add(b, l-1, -n);
  inline long long sum(int 1, int r) { return
      _{sum(r)-_{sum(1-1);}}
private:
  int size;
  T *a, *b;
  inline void __add(T *arr, int x, T n) { for(; x
      &&n&&x<size; x+=lowbit(x)) arr[x]+=n; }
  inline T __sum(T x) { return __sum(a, x)+(__sum
      (b, size)-__sum(b, x))*x; }
  inline T __sum(T *arr, int x) {
    T res=0;
    for(; x; x-=lowbit(x)) res+=arr[x];
    return res;
};
2.2 Fenwick Tree 2D - [1, size][1, size]
int tree[size+1][size+1]={{0}};
inline int lowbit(const int &x) {return x&(-x);}
inline void add(int x, int y, int z) {
  for(int i; x<=n; x+=lowbit(x))</pre>
    for(i=y; i<=n; i+=lowbit(i)) tree[x][i]+=z;</pre>
inline int query(short x, short y) {
  int res=0;
  for(int i; x; x-=lowbit(x))
```

for(i=y; i; i-=lowbit(i))

res+=tree[x][i];

return res;

### **2.3** Heap

```
// max heap tree
#define ParentIndex(i) i==0 ? 0 : ((i-1) >> 1)
#define LeftChildIndex(i) ((i)<<1)+1</pre>
#define RightChildIndex(i) ((i)<<1)+2</pre>
void BuildMaxHeap(int*, const int&);
void MaxHeapBalance(int*, const int&, const int&)
void MaxHeapDelete(int*, int&);
inline bool comp(int &a, int &b) {return a>b;}
void BuildMaxHeap(int all[], const int &size) {
  for(int i=(size-1) >> 1; i>=0; i--)
    MaxHeapBalance(all, size, i);
void MaxHeapBalance(int all[], const int &size,
   const int &root) {
  int aim = root, aim2;
  while(1) {
    aim2 = aim;
    int L = LeftChildIndex(aim2);
    int R = RightChildIndex(aim2);
    if( L < size && comp( all[aim], all[L] ) )</pre>
        aim = L;
    if( R < size && comp( all[aim], all[R] ) )</pre>
        aim = R;
    if( aim != aim2 ) swap(all[aim], all[aim2]);
    else return;
}
void MaxHeapAdd(int all[], int &size, const int &
   AddNum) {
  all[size] = AddNum;
  ++size;
  int P, index = size-1;
  while( index != 0 ) {
    P = ParentIndex(index);
    if( comp(all[P], all[index]) ) {
      swap(all[P], all[index]);
      index = P;
    }
    else return;
  }
}
void MaxHeapDelete(int all[], int &size) {
  all[0] = all[size-1], --size;
  MaxHeapBalance(all, size, 0);
}
```

#### (range modify and query) class deap { public: class zkw\_seg\_tree { public: deap() {size=1;} struct node { ~deap() {} node() {add=sum=0, len=1;} inline void insert(int n) { int len, add, sum; arr[++size]=n; int now=size; zkw\_seg\_tree(int size) { // [1,size] if( (now&1) && arr[now-1]>arr[now] ) dep=lg2(size-1)+1;swap(arr[now-1], arr[now]), now--; delta=(1<<dep)-1; while( now>3 ) { arr=new node[1<<(dep+1)];</pre> **if**( arr[now>>2<<1]>arr[now] ) for(int i=delta; i>0; --i) arr[i].len=arr[i+i swap(arr[now>>2<<1], arr[now]),</pre> now=now>>2<<1;**else if**( arr[(now>>2<<1)+1]<arr[now] ) ~zkw\_seg\_tree() {delete[] arr;} swap(arr[(now>>2<<1)+1], arr[now]), inline void update(int 1, int r, int num=1) { now=(now>>2<<1)+1;l+=delta-1, r+=delta+1; else break; int 10=1, r0=r; } while( r-l>1 ) { } if( (1&1)^1 ) ++1, arr[1].add+=num, arr[1]. inline int min() { sum+=arr[1].len\*num; int res=arr[2]; if( (r&1)^0 ) --r, arr[r].add+=num, arr[r]. swap(arr[2], arr[size--]), down(2); sum+=arr[r].len\*num; return res; 1>>=1, r>>=1;} inline int max() { int res=arr[3]; } swap(arr[3], arr[size--]), down(3); inline int query(int 1, int r) { return res; \_down(l+delta), \_\_\_down(r+delta); } l+=delta-1, r+=delta+1; private: int res=0; int arr[1000005], size; while( r-l>1 ) { inline void down(int now) { if( (1&1)^1 ) res+=arr[l+1].sum; while( (now<<1)<=size ) {</pre> if( (r&1)^0 ) res+=arr[r-1].sum; int tmp; 1>>=1, r>>=1;**if**( (now&1)==0 ) { if( arr[now]>arr[now+1] ) return res; {swap(arr[now], arr[now+1]); } now++;continue;} private: tmp=now; node \*arr; if( arr[tmp]>arr[now<<1] )</pre> int dep, delta; tmp=now<<1;</pre> inline int lg2(int x) {int r; for(r=-1; x; x if( (now<<1)+2<=size && arr[tmp]>arr[(now >>=1, ++r); return r;} <<1)+2] ) tmp=(now<<1)+2; inline void \_\_update(int x) { while( x>1 ) x>>=1, arr[x].sum=arr[x+x].sum+ if( tmp==now ) break; else swap(arr[now], arr[tmp]), arr[x+x+1].sum+arr[x].len+arr[x].add; now=tmp; inline void down(int x) { **else if**( (now&1)==1 ) { for(int i=dep, tmp; i>0; --i) { if( arr[now] < arr[now-1] )</pre> tmp=x>>i; {swap(arr[now], arr[now-1]); arr[tmp<<1].add+=arr[tmp].add;</pre> now--;continue;} arr[(tmp<<1)+1].add+=arr[tmp].add;</pre> tmp=now; arr[tmp<<1].sum+=arr[tmp].add\*arr[tmp<<1]. if( arr[tmp]<arr[(now<<1)-1] )</pre> tmp=(now << 1)-1;arr[(tmp<<1)+1].sum+=arr[tmp].add\*arr[tmp if( (now<<1)+1<=size && arr[tmp]<arr[(now</pre> <<1].len; <<1)+1] ) tmp=(now<<1)+1; arr[tmp].add=0; if( tmp==now ) break; } else swap(arr[now], arr[tmp]), now=tmp; } } segtree(N); if( (now&1)==0 && now+1<=size && arr[now]>arr [now+1] ) swap(arr[now], arr[now+1]); if( (now&1) == 1 && arr[now] < arr[now-1] )</pre> swap(arr[now], arr[now-1]); } };

2.5 zkw Segment Tree

2.4 Deap

## 2.6 劃分樹

```
#include <iostream>
#include <cstdio>
#include <algorithm>
using namespace std;
#define N 100005
int a[N], as[N];//原數組, 排序後數組
int n, m;
int sum[20][N];//紀錄第i層的1~j
   劃分到左子樹的元素個數(包括j)
int tree[20][N];//紀錄第i層元素序列
void build(int c, int l, int r) {
 int i, mid=(l+r)>>1, lm=mid-l+1, lp=l, rp=mid
     +1;
 for (i=1; i<=mid; i++)</pre>
   if (as[i] < as[mid]) lm--;</pre>
     // 先假設左邊的 (mid-l+1) 個數都等于 as [mid],
         然后把實際上小于as[mid]的減去
 for (i = 1; i <= r; i++){
   if (i == 1) sum[c][i] = 0;
     //sum[i]表示[l, i]內有多少個數分到左邊,用
         DP來維護
   else sum[c][i] = sum[c][i-1];
   if (tree[c][i] == as[mid]){
     if (lm){
       lm--;
       sum[c][i]++;
       tree[c+1][lp++] = tree[c][i];
     }else
       tree[c+1][rp++] = tree[c][i];
   } else if (tree[c][i] < as[mid]){</pre>
     sum[c][i]++;
     tree[c+1][lp++] = tree[c][i];
   } else
     tree[c+1][rp++] = tree[c][i];
 if (l == r)return;
 build(c+1, 1, mid);
 build(c+1, mid+1, r);
int query(int c, int l, int r, int ql, int qr,
 int s;//[l, ql)內將被劃分到左子樹的元素數目
 int ss;//[ql, qr]內將被劃分到左子數的元素數目
 int mid=(l+r)>>1;
 if (1 == r)
   return tree[c][1];
 if (1 == q1){//這裡要特殊處理!
   s = 0;
   ss = sum[c][qr];
 }else{
   s = sum[c][ql 1];
   ss = sum[c][qr]-;
 } //假設要在區間[l,r]中查找第k大元素, t
     為當前節點,lch,rch為左右孩子,left,mid
     為節點 t 左邊界界和中間點。
 if (k <= ss)//sum[r]-sum[l-1]>=k, 查找lch[t],
     區間對應為[ left+sum[l-1], left+sum[r]-1 ]
   return query(c+1, 1, mid, 1+s, 1+s+ss-1, k);
 else
   //sum[r]-sum[l-1]<k,查找rch[t], 區間對應為
   [mid+1+l-left-sum[l-1], mid+1+r-left-sum[r]]
   return query(c+1, mid+1, r, mid-l+1+ql-s, mid
       -l+1+qr-s-ss, k-ss);
int main(){
 int i, j, k;
 while(~scanf("%d%d", &n, &m)){
   for(i=1; i<=n; i++) {</pre>
     scanf("%d", &a[i]);
```

```
tree[0][i] = as[i] = a[i];
    sort(as+1, as+1+n);
    build(0, 1, n);
    while(m--){
      scanf("%d%d%d", &i, &j, &k);
        // i,j分別為區間起始點, k 為該區間第 k
           大的數。
     printf("%d\n", query(0, 1, n, i, j, k));
   }
 }
  return 0;
}
```

```
2.7 BigInteger
                                                          BigInteger res=*this;
                                                          int len2=max(res.len, b.len);
#include <cstdio>
                                                          for(int i=0; i<len2; ++i) {</pre>
#include <cstring>
                                                            res.arr[i]+=b.arr[i];
#include <iostream>
                                                            if( res.arr[i]>=step ) res.arr[i]-=step,
#include <iomanip>
                                                                res.arr[i+1]++;
using namespace std;
template < class T>
                                                          res.len=len2;
T abs(const T& n) {return n>=T(0)?n:-n;}
                                                          if(res.arr[len2]) ++res.len;
class BigInteger {
                                                          return res;
public:
  BigInteger(const int& num=0) : len(0), sign(1)
                                                        BigInteger operator - (const BigInteger& b)
                                                           const {
    int num2=num;
                                                          if( *this<b ) return -(b-*this);</pre>
    memset(arr, 0, sizeof(arr));
                                                          if( *this<0 && b<0 ) return -(-*this+b);</pre>
    if( num2<0 ) sign=-1, num2*=-1;</pre>
                                                          if( *this>0 && b<0 ) return *this+(-b);</pre>
    while( num2 ) arr[len++]=num2%step, num2/=
                                                          BigInteger res=*this;
                                                          int len2=max(res.len, b.len);
                                                          for(int i=0; i<len2; ++i) {</pre>
  BigInteger(const char* num0) : len(0), sign(1)
                                                            res.arr[i]-=b.arr[i];
                                                            if( res.arr[i]<0 ) res.arr[i]+=step, res.</pre>
    *this = num0;
                                                                arr[i+1]--;
  BigInteger(const BigInteger& b) : len(b.len),
                                                          while( len2>0 && res.arr[len2-1]==0 ) --len2;
      sign(b.sign) {
                                                          res.len=len2;
    memset(arr, 0, sizeof(arr));
                                                          return res;
    for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>
  }
                                                        BigInteger operator * (const BigInteger& b)
  ~BigInteger() {}
                                                           const {
  BigInteger & operator = (const BigInteger& b) {
                                                          if( *this==0 || b==0 ) return BigInteger(0);
    len=b.len;
                                                          BigInteger res;
    sign=b.sign;
                                                          for(int i=0; i<len; ++i) {</pre>
    memset(arr, 0, sizeof(arr));
                                                            for(int j=0; j<b.len; ++j) {</pre>
    for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>
                                                              res.arr[i+j]+=arr[i]*b.arr[j];
    return *this;
                                                              res.arr[i+j+1]+=res.arr[i+j]/step;
  }
                                                              res.arr[i+j]%=step;
  BigInteger & operator = (const int& num) {
                                                            }
    int num2=num;
                                                          }
    memset(arr, 0, sizeof(arr));
                                                          res.len=len+b.len-1;
    len=0, sign=1;
                                                          while( res.arr[res.len] ) ++res.len;
    if( num2<0 ) sign=-1, num2*=-1;</pre>
                                                          res.sign=sign*b.sign;
    while( num2 ) arr[len++]=num2%step, num2/=
                                                          return res;
        step;
    return *this;
                                                        BigInteger operator / (const int& b) const {
                                                          if( b==0 ) return 0;
  BigInteger & operator = (const char* num0) {
                                                          BigInteger res;
    char num[strlen(num0)];
                                                          long long reduce=0;
    int offset = 0;
                                                          int signb=b>0?1:-1, b2=b*signb;
    len = 0;
                                                          for(int i=len-1; i>=0; --i) {
    sign = 1;
                                                            res.arr[i] = (arr[i]+reduce*step)/b2;
    if( num0[0] == '-' ) sign = -1, ++offset;
                                                            reduce = (arr[i]+reduce*step)%b2;
    else if( num0[0] == '+' ) ++offset;
    while( num0[offset] == '0' ) ++ offset;
                                                          res.len = len;
    strcpy(num, num0+offset);
                                                          while( res.len>0 && res.arr[res.len-1]==0 )
    int tmp = strlen(num);
                                                              --res.len;
    for(int i=tmp-digit; i>=0; i-=digit) {
                                                          if( res.len==0 ) res.sign=1;
      arr[len] = 0;
                                                          else res.sign=sign*signb;
      for(int j=0; j<digit; ++j) arr[len] = arr[</pre>
                                                          return res;
          len]*10 + num[i+j]-'0';
      ++len;
                                                        BigInteger operator / (const BigInteger& b)
    }
                                                           const {
    arr[len] = 0;
                                                          BigInteger abs_this=abs(*this);
    for(int j=0; j<tmp%digit; ++j) arr[len] = arr</pre>
                                                          if( b==0 ) return 0;
        [len]*10 + num[j]-'0';
                                                          BigInteger st=0, ed, md;
    if( tmp%digit ) ++len;
                                                          if( b.arr[0]>0 ) ed=abs this/b.arr[0];
    return *this;
                                                          else if( b.arr[1]*b.step+b.arr[0]>0 ) ed=
                                                              abs_this/b.arr[1]*b.step+b.arr[0];
  BigInteger operator + (const BigInteger& b)
                                                          else ed=abs_this;
      const {
                                                          while( st<ed ) {</pre>
    if( *this>0 && b<0 ) return *this-(-b);</pre>
                                                            md = (st+ed)/2+1;
    if( *this<0 && b>0 ) return -(-*this-b);
```

```
if( md*b<=abs_this ) st=md;</pre>
                                                        return res<(111<<31) && res>=-(111<<31);</pre>
    else ed=md-1;
                                                      friend ostream& operator << ( ostream& out,</pre>
  if( st.len==0 ) st.sign=1;
                                                          const BigInteger &rhs ) {
                                                        if( rhs.len==0 ) out << '0';</pre>
  else st.sign=sign*b.sign;
                                                        else {
                                                          out << rhs.arr[rhs.len-1]*rhs.sign;</pre>
  return st;
                                                          for(int i=rhs.len-2; i>=0; --i) out <<</pre>
                                                               setfill('0') << setw(BigInteger::digit)</pre>
BigInteger operator % (const int& b) const {
  if( b<=0 ) return 0;</pre>
                                                               << rhs.arr[i];
  BigInteger res;
                                                        }
  long long reduce=0;
                                                        return out;
  for(int i=len-1; i>=0; --i)
    reduce = (arr[i]+reduce*step)%b;
                                                      long long toInt() const {return sign*(111*arr
  return reduce*sign;
                                                          [1]*step+arr[0]);}
                                                    private:
BigInteger operator % (const BigInteger& b)
                                                      static const int length = 100;
                                                      static const int digit = 4, step = 10000;
    const {
  if( b.isInt() ) return *this%int(b.toInt());
                                                      int arr[length];
  if( b<=0 ) return 0;</pre>
                                                      int len, sign;
  return *this-*this/b*b;
                                                    istream& operator >> ( istream& in, BigInteger &
bool operator < (const BigInteger& b) const {</pre>
                                                        rhs ) {
  if( sign!=b.sign ) return sign<b.sign;</pre>
                                                      char s[1000];
  if( len!=b.len ) return len*sign<b.len*b.sign</pre>
                                                      in >> s;
                                                      rhs = s;
  for(int i=len-1; i>=0; --i)
                                                      return in;
    if( arr[i]!=b.arr[i] ) return arr[i]*sign<b }</pre>
        .arr[i]*b.sign;
  return false;
}
bool operator == (const BigInteger& b) const {
  if( sign!=b.sign ) return false;
  if( len!=b.len ) return false;
  for(int i=len-1; i>=0; --i)
    if( arr[i]!=b.arr[i] ) return false;
  return true;
bool operator <= (const BigInteger& b) const {</pre>
    return *this<b || *this==b; }</pre>
bool operator > (const BigInteger& b) const {
    return b<*this; }</pre>
bool operator >= (const BigInteger& b) const {
    return b<=*this; }</pre>
bool operator != (const BigInteger& b) const {
    return !(*this==b); }
BigInteger operator-() const {
  BigInteger res = *this;
  if( res.len>0 ) res.sign*=-1;
  return res;
template < class T > BigInteger operator + (const
     T& b) const {return *this+BigInteger(b);}
template < class T > BigInteger operator - (const
     T& b) const {return *this-BigInteger(b);}
template < class T > bool operator == (const T&
    b) const {return *this==BigInteger(b);}
void print(const char *str="") const {
  if( len==0 ) printf("0");
  else {
    printf("%d", arr[len-1]*sign);
    for(int i=len-2; i>=0; --i) printf("%04d",
        arr[i]);
  }
  printf("%s", str);
bool isInt() const {
  if( len>2 ) return false;
  if( len<2 ) return true;</pre>
  long long res=toInt();
```

## 3 Graph

#### 3.1 Dinic

```
class Flow{
public:
  Flow(int _ncnt) :ncnt(_ncnt), ecnt(1), path(new
       int[_ncnt + 2]), d(new int[_ncnt + 2]),
      visited(new bool[_ncnt + 2]){
    memset(path, 0, sizeof(int)*(_ncnt + 1));
  ~Flow(){
    delete[](path);
    delete[](d);
    delete[](visited);
  void Reset(){
    memset(path, 0, sizeof(int)*(ncnt + 1));
    ecnt = 1;
  void AddEdge(int s, int t, int cap){
    edge[++ecnt].tar = t, edge[ecnt].cap = cap,
       edge[ecnt].next = path[s], path[s] = ecnt
    edge[++ecnt].tar = s, edge[ecnt].cap = 0,
       edge[ecnt].next = path[t], path[t] = ecnt
  }
  int MaxFlow(int s, int t){ // Dinic
    int f = 0, df;
    while (BFS(s, t) < ncnt){</pre>
      while (true){
        memset(visited, 0, sizeof(bool)*(ncnt +
        df = DFS(s, INF, t);
        if (!df) break;
        f += df;
      }
    }
    return f;
  }
private:
  static const int eMaxSize = 40002, INF = (int)
  int ecnt, ncnt;
  int *path, *d; // d for Dicic distance
  bool *visited;
  struct Edge{
    int tar, cap, next;
  }edge[eMaxSize];
  int DFS(int a, int df, int t){
    if (a == t) return df;
    if (visited[a]) return 0;
    visited[a] = true;
    for (int i = path[a]; i; i = edge[i].next){
      int b = edge[i].tar;
      if (edge[i].cap > 0 && d[b] == d[a] + 1){
        int f = DFS(b, std::min(df, edge[i].cap),
             t);
        if (f){
          edge[i].cap -= f, edge[i ^ 1].cap += f;
          return f;
        }
      }
```

```
}
    return 0;
  int BFS(int s, int t){
    memset(d, 0x7f, sizeof(int)*(ncnt + 1));
    memset(visited, 0, sizeof(bool)*(ncnt + 1));
    d[s] = 0; visited[s] = true;
    std::queue<int> Q;
    Q.push(s);
    while (!Q.empty()){
      int a = Q.front(); Q.pop();
      for (int i = path[a]; i; i = edge[i].next){
        int b = edge[i].tar;
        if (visited[b] || edge[i].cap == 0)
           continue;
        visited[b] = true;
        d[b] = d[a] + 1;
        if (b == t) return d[b];
        Q.push(b);
      }
    }
    return d[t];
  }
};
Flow flow( 1001 );
   maximum matching in general graph
//Problem:http://acm.timus.ru/problem.aspx?space
   =1&num=1099
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <iostream>
#include <algorithm>
using namespace std;
const int N=250;
int n;
int head;
int tail;
int Start;
int Finish;
int link[N];
                //表示哪個點匹配了哪個點
                 //這個就是增廣路的Father……
int Father[N];
    但是用起來太精髓了
int Base[N];
                //該點屬於哪朵花
int Q[N];
bool mark[N];
bool map[N][N];
bool InBlossom[N];
bool in_Queue[N];
void CreateGraph(){
  int x,y;
  scanf("%d",&n);
 while (scanf("%d%d",&x,&y)!=EOF)
    map[x][y]=map[y][x]=1;
void BlossomContract(int x,int y){
  fill(mark,mark+n+1,false);
```

fill(InBlossom, InBlossom+n+1, false);

for (i=x;i;i=pre) {i=Base[i]; mark[i]=true; }
for (i=y;i;i=pre) {i=Base[i]; if (mark[i]) {lca

if (Base[pre]!=lca) Father[pre]=link[i]; //

對於BFS 樹中的父邊是匹配邊的點, Father

#define pre Father[link[i]]

for (i=x;Base[i]!=lca;i=pre){

int lca,i;

=Base[i]

```
向後跳
    InBlossom[Base[i]]=true;
                                                   void output(){
    InBlossom[Base[link[i]]]=true;
                                                     fill(mark, mark+n+1, false);
                                                      int cnt=0;
  for (i=y;Base[i]!=lca;i=pre){
                                                      for (int i=1;i<=n;i++)</pre>
    if (Base[pre]!=lca) Father[pre]=link[i]; //
                                                        if (link[i]) cnt++;
        同理
                                                      printf("%d\n",cnt);
    InBlossom[Base[i]]=true;
                                                     for (int i=1;i<=n;i++)</pre>
    InBlossom[Base[link[i]]]=true;
                                                        if (!mark[i] && link[i]){
                                                          mark[i]=true;
  #undef pre
                                                          mark[link[i]]=true;
  if (Base[x]!=lca) Father[x]=y;
                                   //注意不能從
                                                          printf("%d %d\n",i,link[i]);
                                                        }
      Lca這個奇環的關鍵點跳回來
  if (Base[y]!=lca) Father[y]=x;
                                                   int main(){
  for (i=1;i<=n;i++)</pre>
    if (InBlossom[Base[i]]){
                                                     CreateGraph();
      Base[i]=lca;
                                                      Edmonds();
                                                      output();
      if (!in_Queue[i]){
        Q[++tail]=i;
                                                      return 0;
        in_Queue[i]=true; //要注意如果本來連向
            BFS 樹中父結點的邊是非匹配邊的點,
            可能是沒有入隊的
      }
    }
void Change(){
  int x,y,z;
  z=Finish;
  while (z){
    y=Father[z];
    x=link[y];
    link[y]=z;
    link[z]=y;
    z=x;
  }
}
void FindAugmentPath(){
  fill(Father, Father+n+1,0);
  fill(in_Queue,in_Queue+n+1,false);
  for (int i=1;i<=n;i++) Base[i]=i;</pre>
  head=0; tail=1;
  0[1]=Start;
  in Queue[Start]=1;
  while (head!=tail){
    int x=Q[++head];
    for (int y=1;y<=n;y++)</pre>
      if (map[x][y] && Base[x]!=Base[y] && link[x
                 //無意義的邊
          ]!=y)
        if ( Start==y || link[y] && Father[link[y
            ]] ) //精髓地用Father表示該點是否
          BlossomContract(x,y);
        else if (!Father[y]){
          Father[y]=x;
          if (link[y]){
            Q[++tail]=link[y];
            in_Queue[link[y]]=true;
          }
          else{
            Finish=y;
            Change();
            return:
          }
        }
  }
void Edmonds(){
  memset(link,0,sizeof(link));
  for (Start=1;Start<=n;Start++)</pre>
    if (link[Start]==0)
      FindAugmentPath();
```

## String

#### 4.1 **KMP**

```
int KMP(char pat[5005], char str[5005]) {
  if( strlen(pat)>strlen(str) ) return -1;
  int failure[5005];
  int len=strlen(pat);
  for(int i=1, j=failure[0]=-1; i<len; ++i) {</pre>
    while( j>=0 && pat[j+1]^pat[i] ) j=failure[j
        1;
    if( pat[j+1]==pat[i] ) ++j;
    failure[i]=j;
  for(int i=0, j=-1; str[i]; ++i) {
    while( j>=0 && str[i]^pat[j+1] ) j=failure[j
        ];
    if( str[i]==pat[j+1] ) ++j;
    if( j==len-1 ) {
      return i-len+1; // rec this!!
      j=failure[j];
    }
  }
  return -1;
}
4.2 Z Algorithm
void Z(char G[], int z[]){
  int len = strlen(G);
```

```
z[0] = len;
  int L = 0, R = 1;
  for ( int i = 1 ; i < len ; i++ ) {</pre>
    if ( i >= R || z[i-L] >= R-i ) {
      int x = (i>=R) ? i : R;
      while ( x < len \&\& G[x] == G[x-i] )
        X++;
      z[i] = x - i;
      if (x > i) L = i, R = x;
    else z[i] = z[i-L];
  }
}
```

## 4.3 Suffix Array

```
int rank[LEN], sa[LEN];
int height[LEN];
int y[LEN], cnt[LEN], rr[2][LEN];
inline bool same(int *rank, int a, int b, int 1)
    { return rank[a]==rank[b]&&rank[a+1]==rank[b+
    1]; }
void sa2(char str[], int n, int m) {
  printf("%s!! %d %d\n", str, n, m);
  int *rank1=rr[0], *rank2=rr[1];
  MSET(rr[1], 0);
  int i, p;
  for(i=0; i<m; ++i) cnt[i]=0;</pre>
  for(i=0; i<n; ++i) rank2[i]=str[i], cnt[rank2[i</pre>
      ]]++;
  for(i=1; i<m; ++i) cnt[i]+=cnt[i-1];</pre>
  for(i=n-1; i>=0; --i) sa[--cnt[rank2[i]]]=i;
  for(int j=1; p<n; j<<=1, m=p) {</pre>
    // 表示用第二個key(rank2)排序後 從 y[i]
        開始的後綴排第i名
    for(p=0, i=n-j; i<n; ++i) y[p++]=i;</pre>
    for(i=0; i<n; ++i) if( sa[i]>=j ) y[p++]=sa[i
        ]-j;
    for(i=0; i<m; ++i) cnt[i]=0;</pre>
    for(i=0; i<n; ++i) cnt[ rank2[y[i]] ] ++;</pre>
    for(i=1; i<m; ++i) cnt[i]+=cnt[i-1];</pre>
    for(i=n-1; i>=0; --i) sa[ --cnt[ rank2[y[i]]
        ] ]=y[i];
    for(p=i=1, rank1[sa[0]]=0; i<n; ++i)</pre>
      rank1[sa[i]]=same(rank2, sa[i], sa[i-1], j)
          ?p-1:p++;
    std::swap(rank1, rank2);
  for(int i=0; i<n; ++i) rank[i]=rank2[i];</pre>
void make_height(char str[]) {
  int len=strlen(str);
  height[0]=0;
  for(int i=0, j=0; i<len; ++i, j=height[rank[i</pre>
      -1]]-1) {
    if( rank[i]==1 ) continue;
    if( j<0 ) j=0;
    while( i+j<len && sa[rank[i]-1]+j<len &&
      str[i+j]==str[sa[rank[i]-1]+j] ) ++j;
    height[rank[i]]=j;
  }
}
int main() {
  char str[LEN];
  scanf("%s", str);
  int len = strlen(str);
  sa2(str, len+1, 256);
  make_height(str);
  for(int i=1; i<=len; ++i) printf("%d %d %s\n",</pre>
      i, height[i], str+sa[i]);
}
```

## Longest Palindromic Substring

```
// 要處理的字串
char t[1001];
cahr s[1001 * 2]; // 中間插入特殊字元的t。
int Z[1001 * 2], L, R; // Gusfield's Algorithm
// 由a往左、由b往右,對稱地作字元比對。
int match(int a, int b) {
 int i = 0;
 while (a-i)=0 \&\& b+i < N \&\& s[a-i] == s[b+i]) i
 return i;
}
void longest_palindromic_substring()
 int N = strlen(t);
 // 在t中插入特殊字元, 存放到s。
 memset(s, '.', N*2+1);
 for (int i=0; i<N; ++i) s[i*2+1] = t[i];</pre>
 N = N*2+1;
 // modified Gusfield's lgorithm
 Z[0] = 1;
 L = R = 0;
 for (int i=1; i<N; ++i) {
   int ii = L - (i - L);
                          // i的映射位置
   int n = R + 1 - i;
   if (i > R) {
     Z[i] = match(i, i);
     L = i;
     R = i + Z[i] - 1;
   else if (Z[ii] == n) {
     Z[i] = n + match(i-n, i+n);
     R = i + Z[i] - 1;
   else Z[i] = min(Z[ii], n);
 // 尋找最長迴文子字串的長度。
 int n = 0, p = 0;
 for (int i=0; i<N; ++i)</pre>
   if (Z[i] > n) n = Z[p = i];
 // 記得去掉特殊字元。
 cout << "最長迴文子字串的長度是" << (n-1) / 2;
 // 印出最長迴文子字串, 記得別印特殊字元。
 for (int i=p-Z[p]+1; i<=p+Z[p]-1; ++i)</pre>
   if (i & 1) cout << s[i];</pre>
}
```

## 5

```
Math
5.1 Euler's phi function O(n)
1. gcd(x,y) = d \Rightarrow \phi(xy) = \frac{\phi(x)\phi(y)}{\phi(x)}
2. p \text{ is } prime \Rightarrow \phi(p^k) = p^{k-1}\phi(p)
3. p \text{ is prime} \Rightarrow \phi(p^k) = \phi(p^{k-1}) \times p
4. n = p_1^{k_1} p_2^{k_2} \cdots p_m^{k_m}

\Rightarrow \phi(n) = p_1^{k_1-1} \phi(p_1) p_2^{k_2-1} \phi(p_2) \cdots p_m^{k_m-1} \phi(p_m)
const int MAXN = 100000;
int phi[MAXN], prime[MAXN], pn=0;
memset(phi, 0, sizeof(phi));
for(int i=2; i<MAXN; ++i) {</pre>
  if( phi[i]==0 ) prime[pn++]=i, phi[i]=i-1;
  for(int j=0; j<pn; ++j) {</pre>
     if( i*prime[j]>=MAXN ) break;
     if( i%prime[j]==0 ) {
       phi[i*prime[j]] = phi[i] * prime[j];
     phi[i*prime[j]] = phi[i] * phi[prime[j]];
  }
}
5.2 Extended Euclid's Algorithm
  ax + by = gcd(a, b)
int ext_gcd(int a, int b, int &x, int &y){
  int x2;
  if( b==0 ) {
     x=1, y=0;
     return a;
  }
  int gcdn=ext_gcd(b, a%b, x, y), x2=x;
  x=y, y=x2-a/b*y;
  return gcdn;
int ext gcd(int a, int b, int &x, int &y){
  int t, px=1, py=0, tx,ty;
  x=0, y=1;
  while(a%b!=0) {
     tx=x, ty=y;
    x=x*(-a/b)+px, y=y*(-a/b)+py;
     px=tx, py=ty;
     t=a, a=b, b=t%b;
  }
  return b;
```

## 5.3 Möbius function

```
int* isp;
char fcnt[N+5];
int mobius[N+5];
void make_mobius(int n) {
    isp = mobius;
    memset(mobius, true, sizeof(mobius));
    memset(fcnt, 0, sizeof(fcnt));
    for(int i=2; i<=n; ++i) {</pre>
        if( isp[i] ) {
             fcnt[i] = 1;
             for(int j=i+i; j<=n; j+=i) {</pre>
                 isp[j] = false;
                 if( fcnt[j]!=-1 ) fcnt[j]++;
             if( i<=10000 )
```

```
for(int ii=i*i, j=ii; j<=n; j+=ii 6</pre>
                                                        Others
                                                   6.1 8 puzzle - IDA*
                    fcnt[j] = -1;
                }
                                                   // 一個盤面。其數值1~8代表方塊號碼,0代表空格。
                                                   int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
    }
                                                   // 檢查 permutation inversion。檢查不通過,
    mobius[0] = 0;
                                                       表示盤面不合理。
    mobius[1] = 1;
                                                   bool check_permutation_inversion(int board[3][3])
    for(int i=2; i<=n; ++i) {</pre>
        if( fcnt[i]==-1 ) mobius[i] = 0;
                                                     int inversion = 0;
        else if( fcnt[i]&1 ) mobius[i] = -1;
                                                     for (int a=0; a<9; ++a)</pre>
        else mobius[i] = 1;
                                                       for (int b=0; b<a; ++b) {</pre>
    }
                                                         int i = a / 3, j = a % 3;
}
                                                         int ii = b / 3, jj = b % 3;
                                                         if (board[i][j] && board[ii][jj]
5.4 China remainder theorem
                                                           && board[i][j] < board[ii][jj])
  ans \equiv a_i \pmod{m_i}
                                                           inversion++;
int china_remainder_theorem(int n, int ai[], int
                                                     int row_number_of_0 = 0;
   mi[]) {
  int gcdn, x, y, reduce, tmp;
                                                     for (int i=0; i<3 && !row_number_of_0; ++i)</pre>
 for(int i=1; i<n; ++i) {</pre>
                                                       for (int j=0; j<3 && !row_number_of_0; ++j)</pre>
    gcdn=ext_gcd(mi[i-1], mi[i], x, y);
                                                         if (board[i][j] == 0)
    reduce=ai[i]-ai[i-1];
                                                           row_number_of_0 = i+1;
    if( reduce%gcdn!=0 )
                                                     return (inversion + row_number_of_0) % 2 == 0;
      return -1;
    tmp=mi[i]/gcdn;
                                                   x=(reduce/gcdn*x%tmp+tmp)%tmp;
                                                   // heuristic function,
                                                       採用不在正確位置上的方塊個數。
    ai[i] = ai[i-1] + mi[i-1]*x;
    mi[i] = mi[i-1]*tmp;
                                                   int h(int board[3][3])
 }
  return ai[n-1]%mod;
                                                     int cost = 0;
}
                                                     for (int i=0; i<3; ++i)</pre>
                                                       for (int j=0; j<3; ++j)
   Gaussian Elimination
                                                         if (board[i][j])
                                                           if (board[i][j] != i*3 + j + 1)
double mmap[100][100];
                                                             cost++;
void gauss(int n,int m) {
                                                     return cost;
  int k=0;
  for(int i=0; i<n; i++)</pre>
                                                   for(int j=k; j<m; j++)</pre>
                                                   int taxicab_distance(int x1, int y1, int x2, int
      if(mmap[j][i]!=0) {
                                                       y2)
        for(int l=i; l<=n; l++)</pre>
                                                   {return abs(x1 - x2) + abs(y1 - y2);}
          swap(mmap[k][1],mmap[j][1]);
        for(j++; j<m; j++) {</pre>
                                                   // heuristic function, 採用taxicab distance。
          if(mmap[j][i]==0)
                                                   int h(int board[3][3]) {
            continue;
                                                     // 每塊方塊的正確位置。 {0,0}
          double scale=mmap[k][i]/mmap[j][i];
                                                         是為了方便編寫程式而多加的。
          for(int p=i+1; p<=n; p++)</pre>
                                                     static const int right_pos[9][2] = {
            mmap[j][p]-=mmap[k][p]*scale;
                                                       {0,0},
          mmap[j][i]=0;
                                                       \{0,0\}, \{0,1\}, \{0,2\},
        }
                                                       \{1,0\}, \{1,1\}, \{1,2\},
        k++:
                                                       \{2,0\}, \{2,1\}
        break;
                                                     };
      }
                                                     // 計算每個方塊與其正確位置的 taxicab distance
}
                                                         的總和。
                                                     int cost = 0;
                                                     for (int i=0; i<3; ++i)</pre>
                                                       for (int j=0; j<3; ++j)</pre>
                                                         if (board[i][j])
                                                           cost += taxicab_distance(
                                                                 right_pos[board[i][j]][0],
                                                                 right_pos[board[i][j]][1]
                                                     return cost;
                                                   // 上下左右
                                                   const string operator[4] = {"up", "down", "right"
                                                       , "left"};
```

```
const int dx[4] = \{-1, 1, 0, 0\}, dy[4] = \{0, 0, 0\}
   1, -1};
char solution[30];
 // 正確的推動方式, 其數值是方向 0~3。
const int reverse_dir[4] = {1, 0, 3, 2};
 // 用表格紀錄每一個方向的反方向。
     可用於避免來回推動的判斷。
int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
 // 起始狀態。其數值1~8代表方塊號碼,0代表空格。
int sx = 1, sy = 2;
 // 空格的位置。 可馬上知道推動方塊的目的地。
bool onboard(int x, int y)
{return x \ge 0 \&\& x < 3 \&\& y \ge 0 \&\& y < 3;}
int IDAstar(int x, int y, int gv, int prev_dir,
   int& bound, bool& ans) {
  int hv = h(board);
  if (gv + hv > bound) return gv + hv;
   // 超過,回傳下次的bound
  if (hv == 0) {ans = true; return gv;}
   // 找到最佳解
  int next_bound = 1e9;
  for (int i=0; i<4; ++i) {</pre>
   // 四種推動方向
   int nx = x + dx[i], ny = y + dy[i];
     // 空格的新位置
   if (reverse dir[i] == prev dir) continue;
     // 避免來回推動
   if (!onboard(nx, ny)) continue;
     // 避免出界
   solution[gv] = oper[i];
     // 紀錄推動方向
   swap(board[x][y], board[nx][ny]);
     // 推動
   int v = IDAstar(nx, ny, gv+1, i, bound, ans);
   if (ans) return v;
   next bound = min(next bound, v);
   swap(board[nx][ny], board[x][y]);
     // 回復原狀態
  }
  return next_bound;
void eight_puzzle() {
 if (!check_permutation_inversion(board)) {
   cout << "盤面不合理, 無法解得答案。" << endl;
   return;
 }
 // IDA*
 bool ans = false;
  int bound = 0;
 while (!ans && bound <= 50)</pre>
   bound = IDAstar(sx, sy, 0, -1, bound, ans);
  if (!ans) {
   cout << "50步內無法解得答案。" << endl;
   return;
 }
 // 印出移動方法
 for (int i=0; i<bound; ++i)</pre>
   cout << operation[solution[i]] << ' ';</pre>
  cout << endl;</pre>
```

## The End