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8 puzzle - IDA\* . . . . . . . . . . . . . . . . .

recursive to stack . . . . . . . . . . . . . . . . .

## 1 Environment Settings

	1.1	.vimrc
1		
1		et encoding
	set	encoding=utf-8
2	set cot	fileencodings=utf-8,big5 showmode
2	synt	tax on
2	set	hlsearch
		background=dark
	set	laststatus=2
3	set	wildmenu
3	set	scrolloff=5 " keep at least 5 lines above/
		below
		ruler
5	set	cursorline ic " ignore case when searching
5	Set	bs=2 " enable backspace
5	set	number
6		tabstop=4
		shiftwidth=4
		autoindent
8	set	smarttab
8	set	smartindent
8		appr
O	J y 11	tax on
10		enc=utf-8 fencs=utf-8,big5 bs=2
		smd nu bg=dark hls ls=2 wmnu so=5 ru cul
-		ts=4 sw=4 ai sta si
10		list lcs=tab:>\ "# a space after '\'
10	imap	o <f9> <esc>:w<enter><f9></f9></enter></esc></f9>
10	map	<f9> :!g++ "%:t" -o "%:r.out" -Wall -Wshadow -</f9>
10		02 -Im && "./%:r.out"
11	map	<pre><f10> :!g++ "%:t" -o "%:r.out" -Wall -Wshadow</f10></pre>
		-02 -Im
11	aut	ocmd! BufNewFile * silent! Or ~/.vim/skel/ Template.%:e
11		rempiace.%.e
12		
12		
12		
13		

13

13

# 2 Computational Geometry

#### 2.1 Geometry on Plane

```
struct node {
    double x,y;
    node() {}
    node(double _x, double _y) : x(_x),y(_y) {}
    node operator+(const node& rhs)const
        { return node(x+rhs.x,y+rhs.y); }
    node operator-(const node& rhs)const
        { return node(x-rhs.x,y-rhs.y); }
    node operator*(const double& rhs)const
        { return node(x*rhs,y*rhs); }
    node operator/(const double& rhs)const
        { return node(x/rhs,y/rhs); }
    double operator*(const node& rhs)const
        { return x*rhs.x+y*rhs.y; }
    double len2()const{ return x*x+y*y; }
    double len()const{ return sqrt(x*x+y*y); }
    node unit()const{ return *this/len(); }
    \begin{tabular}{ll} \beg
            x*rhs.y-y*rhs.x; }
    node T()const{ return node(-y,x); }
    node rot(double rad)const{ //逆時針旋轉 弧度
        return node(cos(rad)*x-sin(rad)*y, sin(rad)*x
                +cos(rad)*y);
   }
};
node __mirror(node normal, double constant, node
       point){ //2D3D
    double scale=(normal*point+constant)/(normal*
            normal);
    return point-normal*(2*scale);
node mirror(node p1, node p2, node p3){ //2D3D
    return __mirror((p2-p1).T(),(p2-p1).T()*p1*(-1)
            ,p3);
double ori(const node& p1,const node& p2, const
       node& p3){ //平行四邊形面積(帶正負)
    return (p2-p1)^(p3-p1);
bool intersect(const node& p1, const node& p2,
       const node& p3, const node& p4){
    return (ori(p1,p2,p3)*ori(p1,p2,p4)<0 && ori(p3
            ,p4,p1)*ori(p3,p4,p2)<0);
pair<node, node> two_circle_intersect(node p1,
       double r1, node p2, double r2){
    double degree=acos(((p2-p1).len2()+r1*r1-r2*r2)
            /(2*r1*(p2-p1).len()));
    return make_pair(p1+(p2-p1).unit().rot(degree)* }
            r1, p1+(p2-p1).unit().rot(-degree)*r1);
node intersectionPoint(node p1, node p2, node p3,
          node p4){
    double a123 = (p2-p1)^(p3-p1);
    double a124 = (p2-p1)^{(p4-p1)};
    return (p4*a123-p3*a124)/(a123-a124);
2.2 KDTree
struct NODE{
    int x , y;
    int x1 , x2 , y1 , y2;
    NODE *L , *R;
bool cmpx( const NODE& a , const NODE& b ){
    return a.x < b.x;</pre>
```

```
bool cmpy( const NODE& a , const NODE& b ){
  return a.y < b.y;</pre>
NODE* KDTree( int L , int R , int depth ){
  if (L > R) return 0;
  int M = (L + R) >> 1;
  node[M].f = depth % 2;
  nth_element( node+L , node+M , node+R+1 , node[
     M].f ? cmpy : cmpx );
  node[M].L = KDTree( L , M-1 , depth+1 );
  node[M].R = KDTree( M+1 , R , depth+1 );
  node[M].x1 = node[M].x2 = node[M].x;
  node[M].y1 = node[M].y2 = node[M].y;
  if ( node[M].L ){
    node[M].x1 = min(node[M].x1, node[M].L->x1
    node[M].y1 = min(node[M].y1, node[M].L->y1
       );
  if ( node[M].R ){
    node[M].x2 = max(node[M].x2, node[M].L->x2
    node[M].y2 = max(node[M].y2, node[M].L->y2
       );
  return node+M;
inline int mayTouchRectangle( NODE* r , int x ,
   int y , long long d2 ){
  long long d = (long long)(sqrt(d2) + 1);
  return x >= r -> x1 - d & x <= r -> x2 + d & y >=
     r-y1 - d \&\& y <= r-y2 + d;
}
// find the nearest point near p
// r is tree node
void nearest( NODE* r , NODE* p , long long &dmin
    ){
  if ( !r || !mayTouchRectangle( r , p->x , p->y
      , dmin ) ) return;
  if ( p->i != r->i ) dmin = min( dmin , dis( *r
      , *p ) ); // dis returns the dis^2
  int whichFirst = r->f ? p->y < r->y: p->x < r->
     х;
  if ( whichFirst ){
    nearest( r->L , p , dmin );
    nearest( r->R , p , dmin );
  else{
    nearest( r->R , p , dmin );
    nearest( r->L , p , dmin );
```

#### 3 Data Structure

#### 3.1 PB DS

```
BigInteger & operator = (const int& num) {
#include <ext/pb_ds/assoc_container.hpp>
                                                          int num2=num;
using namespace std;
                                                          memset(arr, 0, sizeof(arr));
using namespace __gnu_pbds;
                                                          len=0, sign=1;
                                                          if( num2<0 ) sign=-1, num2*=-1;</pre>
#include <ext/pb_ds/priority_queue.hpp>
                                                          while( num2 ) arr[len++]=num2%step, num2/=
typedef __gnu_pbds::priority_queue<T, greater<T>,
     pairing_heap_tag> Heap;
                                                          return *this;
 * method: push, pop, modify(iter, val), erase,
                                                        BigInteger & operator = (const char* num0) {
    join
                                                          char num[strlen(num0)];
 * tags: pairing_heap_tag, binary_heap_tag,
                                                          int offset = 0;
     binomial_heap_tag, rc_binomial_heap_tag,
                                                          len = 0;
     thin_heap_tag
                                                          sign = 1;
                                                          if( num0[0] == '-' ) sign = -1, ++offset;
else if( num0[0] == '+' ) ++offset;
                                                          while( num0[offset]=='0' ) ++offset;
#include <ext/pb_ds/tree_policy.hpp>
typedef tree<int, null_type, less<int>,
                                                          strcpy(num, num0+offset);
    rb_tree_tag,
                                                          int tmp = strlen(num);
   tree_order_statistics_node_update> RBTree;
                                                          for(int i=tmp-digit; i>=0; i-=digit) {
typedef tree<int, null_type, less<int>,
                                                            arr[len] = 0;
    splay_tree_tag,
                                                            for(int j=0; j<digit; ++j) arr[len] = arr[</pre>
   tree_order_statistics_node_update> Splay;
                                                                len]*10 + num[i+j]-'0';
                                                            ++len;
 * point_iterator find_by_order(size_type order)
                                                          }
 * size_type order_of_key(const_key_reference
                                                          arr[len] = 0;
     r_key) - number of elements < r_key
                                                          for(int j=0; j<tmp%digit; ++j) arr[len] = arr</pre>
 * void split(const_key_reference r_key, tree &
                                                              [len]*10 + num[j]-'0';
     other) - move elements > r_key
                                                          if( tmp%digit ) ++len;
                                                          return *this;
#include <ext/pb_ds/hash_policy.hpp>
                                                        BigInteger operator + (const BigInteger& b)
typedef cc_hash_table<string, int> Hash;
                                                            const {
typedef gp_hash_table<string, int> Hash;
                                                          if( *this>0 && b<0 ) return *this-(-b);</pre>
                                                          if( *this<0 && b>0 ) return -(-*this-b);
3.2 BigInteger
                                                          BigInteger res=*this;
                                                          int len2=max(res.len, b.len);
#include <cstdio>
                                                          for(int i=0; i<len2; ++i) {</pre>
#include <cstring>
                                                            res.arr[i]+=b.arr[i];
#include <iostream>
                                                            if( res.arr[i]>=step ) res.arr[i]-=step,
#include <iomanip>
                                                                res.arr[i+1]++;
using namespace std;
template < class T>
                                                          res.len=len2;
T abs(const T& n) {return n>=T(0)?n:-n;}
                                                          if(res.arr[len2]) ++res.len;
class BigInteger {
                                                          return res;
public:
  BigInteger(const int& num=0) : len(0), sign(1)
                                                        BigInteger operator - (const BigInteger& b)
                                                            const {
    int num2=num;
                                                          if( *this<b ) return -(b-*this);</pre>
    memset(arr, 0, sizeof(arr));
                                                          if( *this<0 && b<0 ) return -(-*this+b);</pre>
    if( num2<0 ) sign=-1, num2*=-1;</pre>
                                                          if( *this>0 && b<0 ) return *this+(-b);</pre>
    while( num2 ) arr[len++]=num2%step, num2/=
                                                          BigInteger res=*this;
        step;
                                                          int len2=max(res.len, b.len);
  }
                                                          for(int i=0; i<len2; ++i) {</pre>
  BigInteger(const char* num0) : len(0), sign(1)
                                                            res.arr[i]-=b.arr[i];
                                                            if( res.arr[i]<0 ) res.arr[i]+=step, res.</pre>
    *this = num0;
                                                                arr[i+1]--;
  BigInteger(const BigInteger& b) : len(b.len),
                                                          while( len2>0 && res.arr[len2-1]==0 ) --len2;
      sign(b.sign) {
                                                          res.len=len2;
    memset(arr, 0, sizeof(arr));
                                                          return res;
    for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>
                                                        BigInteger operator * (const BigInteger& b)
  ~BigInteger() {}
                                                            const {
  BigInteger & operator = (const BigInteger& b) {
                                                          if( *this==0 || b==0 ) return BigInteger(0);
    len=b.len;
                                                          BigInteger res;
    sign=b.sign;
                                                          for(int i=0; i<len; ++i) {</pre>
    memset(arr, 0, sizeof(arr));
```

for(int i=0; i<len; ++i) arr[i]=b.arr[i];</pre>

return \*this;

```
for(int j=0; j<b.len; ++j) {</pre>
                                                        if( sign!=b.sign ) return false;
      res.arr[i+j]+=arr[i]*b.arr[j];
                                                        if( len!=b.len ) return false;
                                                        for(int i=len-1; i>=0; --i)
      res.arr[i+j+1]+=res.arr[i+j]/step;
      res.arr[i+j]%=step;
                                                          if( arr[i]!=b.arr[i] ) return false;
                                                        return true;
                                                      bool operator <= (const BigInteger& b) const {</pre>
  res.len=len+b.len-1;
  while( res.arr[res.len] ) ++res.len;
                                                         return *this<b || *this==b; }</pre>
  res.sign=sign*b.sign;
                                                      bool operator > (const BigInteger& b) const {
                                                         return b<*this; }</pre>
  return res;
                                                      bool operator >= (const BigInteger& b) const {
BigInteger operator / (const int& b) const {
                                                         return b<=*this; }</pre>
  if( b==0 ) return 0;
                                                      bool operator != (const BigInteger& b) const {
  BigInteger res;
                                                         return !(*this==b); }
  long long reduce=0;
                                                      BigInteger operator-() const {
  int signb=b>0?1:-1, b2=b*signb;
                                                        BigInteger res = *this;
  for(int i=len-1; i>=0; --i) {
                                                        if( res.len>0 ) res.sign*=-1;
    res.arr[i] = (arr[i]+reduce*step)/b2;
                                                        return res;
    reduce = (arr[i]+reduce*step)%b2;
                                                     template < class T> BigInteger operator + (const
  }
  res.len = len;
                                                          T& b) const {return *this+BigInteger(b);}
  while( res.len>0 && res.arr[res.len-1]==0 )
                                                      template < class T > BigInteger operator - (const
                                                          T& b) const {return *this-BigInteger(b);}
      --res.len;
  if( res.len==0 ) res.sign=1;
                                                      template < class T > bool operator == (const T&
  else res.sign=sign*signb;
                                                         b) const {return *this==BigInteger(b);}
                                                      void print(const char *str="") const {
  return res;
                                                        if( len==0 ) printf("0");
BigInteger operator / (const BigInteger& b)
                                                       else {
                                                          printf("%d", arr[len-1]*sign);
    const {
  BigInteger abs_this=abs(*this);
                                                          for(int i=len-2; i>=0; --i) printf("%04d",
  if( b==0 ) return 0;
                                                              arr[i]);
  BigInteger st=0, ed, md;
                                                       }
                                                       printf("%s", str);
  if( b.arr[0]>0 ) ed=abs this/b.arr[0];
  else if( b.arr[1]*b.step+b.arr[0]>0 ) ed=
      abs_this/b.arr[1]*b.step+b.arr[0];
                                                     bool isInt() const {
  else ed=abs_this;
                                                        if( len>2 ) return false;
  while( st<ed ) {</pre>
                                                        if( len<2 ) return true;</pre>
    md = (st+ed)/2+1;
                                                        long long res=toInt();
    if( md*b<=abs_this ) st=md;</pre>
                                                        return res<(111<<31) && res>=-(111<<31);</pre>
    else ed=md-1;
                                                     friend ostream& operator << ( ostream& out,</pre>
                                                         const BigInteger &rhs ) {
  if( st.len==0 ) st.sign=1;
  else st.sign=sign*b.sign;
                                                        if( rhs.len==0 ) out << '0';</pre>
                                                        else {
  return st;
                                                          out << rhs.arr[rhs.len-1]*rhs.sign;</pre>
                                                          for(int i=rhs.len-2; i>=0; --i) out <<</pre>
BigInteger operator % (const int& b) const {
                                                              setfill('0') << setw(BigInteger::digit)</pre>
  if( b<=0 ) return 0;</pre>
                                                               << rhs.arr[i];
  BigInteger res;
  long long reduce=0;
                                                       return out;
  for(int i=len-1; i>=0; --i)
    reduce = (arr[i]+reduce*step)%b;
                                                      long long toInt() const {return sign*(111*arr
  return reduce*sign;
                                                         [1]*step+arr[0]);}
                                                   private:
BigInteger operator % (const BigInteger& b)
                                                      static const int length = 100;
                                                      static const int digit = 4, step = 10000;
  if( b.isInt() ) return *this%int(b.toInt());
                                                      int arr[length];
  if( b<=0 ) return 0;
                                                      int len, sign;
  return *this-*this/b*b;
                                                   istream& operator >> ( istream& in, BigInteger &
bool operator < (const BigInteger& b) const {</pre>
                                                       rhs ) {
  if( sign!=b.sign ) return sign<b.sign;</pre>
                                                      char s[1000];
                                                      in >> s;
  if( len!=b.len ) return len*sign<b.len*b.sign</pre>
                                                      rhs = s;
  for(int i=len-1; i>=0; --i)
                                                      return in;
    if( arr[i]!=b.arr[i] ) return arr[i]*sign<b }</pre>
        .arr[i]*b.sign;
                                                       Fenwick Tree Range Modify [1, size]
  return false;
                                                   inline int lowbit(int x) { return x&-x; }
bool operator == (const BigInteger& b) const {
                                                   template<class T>
```

```
class fenwick {
                                                      struct TNode {
public:
                                                        TNode<T> *c[2], *fa;
  fenwick(int __size=SIZE) {
                                                        T val, inc, sum;
    size = \__size+10;
                                                        int sz;
    a = new T[size], b=new T[size];
                                                        void down() {
    memset(a, 0, sizeof(T)*size);
                                                          val += inc;
    memset(b, 0, sizeof(T)*size);
                                                          if( lc->fa ) lc->inc += inc;
                                                          if( rc->fa ) rc->inc += inc;
  ~fenwick() { delete[] a, delete[] b;}
                                                          inc = 0:
  inline void add(int 1, int r, long long n) {
                                                        }
    __add(a, r, r*n), __add(a, l-1, (l-1)*-n);
                                                        void up() {
     _add(b, r, n), __add(b, l-1, -n);
                                                          sz = lc -> sz + rc -> sz + 1;
                                                          sum = val;
  inline long long sum(int 1, int r) { return
                                                          if( lc->fa ) sum += lc->sum + lc->inc*lc->sz;
      sum(r) - sum(1-1); }
                                                          if( rc->fa ) sum += rc->sum + rc->inc*rc->sz;
private:
  int size;
                                                      };
  T *a, *b;
                                                      template < class T>
  inline void __add(T *arr, int x, T n) { for(; x class SplayTree {
      &&n&&x<size; x+=lowbit(x)) arr[x]+=n; }
                                                      public:
  inline T __sum(T x) { return __sum(a, x)+(__sum
                                                        void init(const int& n) {
      (b, size)-__sum(b, x))*x; }
                                                          null = &node[0];
  inline T  sum(T *arr, int x) {
                                                          null->fa = NULL;
    T res=0;
                                                          null->val = null->inc = null->sum = null->sz
    for(; x; x-=lowbit(x)) res+=arr[x];
                                                              = 0;
    return res;
                                                          ncnt = 0;
  }
                                                          root = newnode(-1, null);
                                                          root->rc = newnode(-1, root);
};
                                                          root->rc->lc = build(1, n, root->rc);
     Fenwick Tree 2D - [1, size][1, size]
                                                          root->rc->up(), root->up();
int tree[size+1][size+1]={{0}};
                                                        void update(int 1, int r, T val) {
inline int lowbit(const int &x) {return x&(-x);}
                                                          RotateTo(1-1, null);
inline void add(int x, int y, int z) {
                                                          RotateTo(r+1, root);
  for(int i; x<=n; x+=lowbit(x))</pre>
                                                          root->rc->lc->inc += val;
    for(i=y; i<=n; i+=lowbit(i)) tree[x][i]+=z;</pre>
                                                          root->rc->lc->up();
inline int query(short x, short y) {
                                                        11 query(int 1, int r) {
  int res=0;
                                                          if( 1>r ) swap(1, r);
  for(int i; x; x-=lowbit(x))
                                                          RotateTo(1-1, null);
    for(i=y; i; i-=lowbit(i))
                                                          RotateTo(r+1, root);
      res+=tree[x][i];
                                                          TNode<T> *now = root->rc->lc;
  return res;
                                                          now->up();
}
                                                          return now->sum + now->inc*now->sz;
3.5 Skew Heap
                                                      private:
                                                        TNode<T> *root, *null;
                                                        TNode<T> node[MAXN];
 * merge : root = merge(x, y)
                                                        int ncnt;
 * pop
         : root = merge(root.lc, root.rc)
*/
                                                        TNode<T>* newnode(T val, TNode<T> *fa) {
                                                          TNode<T> *x = &node[++ncnt];
const int MAXSIZE = 10000;
                                                          x \rightarrow 1c = x \rightarrow rc = null;
class Node {
                                                          x->fa = fa;
                                                          x\rightarrow val = x\rightarrow sum = val, x\rightarrow inc = 0, x\rightarrow sz = 1;
public:
  int num, lc, rc;
  Node(int _{v=0}) : num(_{v}), lc(-1), rc(-1) {}
                                                        TNode<T>* build(int l, int r, TNode<T> *fa) {
} tree[MAXSIZE];
                                                          if( l>r ) return null;
                                                          int md = (1+r)>>1;
int merge(int x, int y){
                                                          TNode<T> *now = newnode(all[md], fa);
    if( x==-1 ) return y;
                                                          now->lc = build(1, md-1, now);
    if( y==-1 ) return x;
                                                          now->rc = build(md+1, r, now);
    if( tree[x].num<tree[y].num ) // key</pre>
                                                          now->up();
        swap(x, y);
    tree[x].rc = merge(tree[x].rc, y);
                                                          return now;
    swap(tree[x].lc, tree[x].rc);
                                                        void RotateTo(int x, TNode<T> *aim) {
    return x;
                                                          // find k-th element
}
                                                          TNode<T> *now = root;
    Splay Tree
                                                          while (now->lc->sz != x) {
                                                            if( now \rightarrow lc \rightarrow sz \rightarrow x ) now = now \rightarrow lc;
template < class T>
```

```
else x -= now->lc->sz+1, now = now->rc;
                                                       ranx += (ranx << 2) + 1;
                                                       return ranx;
    splay(now, aim);
                                                     void New_node(Node *&o, int val) {
  void splay(TNode<T> *now, TNode<T> *aim) {
                                                        if(list == NULL) {
    // make now become aim's child
                                                         Node *tt = new Node[100];
    TNode<T> *fa, *fafa;
                                                          for(int i = 0; i < 100; i ++) {
    while( now->fa != aim ) {
                                                            tt[i].w = ran();
      if( now->fa->fa == aim ) Rotate(now, now->
                                                            tt[i].r = list;
          fa->lc==now);
                                                            list = tt + i;
      else {
                                                         }
        fa = now->fa, fafa = fa->fa;
                                                       }
        int pos = (fafa->c[1] == fa);
                                                       o = list;
        if( fa->c[pos] == now ) Rotate(fa, !pos);
                                                       list = o \rightarrow r;
        else Rotate(now, pos);
                                                       o \rightarrow 1 = o \rightarrow r = NULL;
        Rotate(now, !pos);
                                                       o->v = o->minx = val;
                                                       o \rightarrow size = 1;
      }
    }
                                                       o\rightarrow delta = o\rightarrow rev = 0;
    now->up();
    if( aim == null ) root = now;
                                                     void Reuse(Node *o) { if(o) { o->r = list; list =
                                                          o; } }
  void Rotate(TNode<T> *now, int fl) {
                                                     void cut(Node *o, Node *&p, Node *&q, int num) {
    // fl : 0 - L-Rotate
                                                       if(num == 0) {
            1 - R-Rotate
                                                         p = NULL; q = o;
    TNode<T> *fa = now->fa;
                                                        } else if(num == sz(o)) {
    now->down();
                                                         p = o; q = NULL;
    fa->c[!fl] = now->c[fl];
                                                        } else {
    if( now->c[fl] != null ) now->c[fl]->fa = fa;
                                                         o->down();
    now->fa = fa->fa;
                                                         if(num <= sz(o->1)) {
    if( fa->fa != null ) fa->fa->c[ fa->fa->c
                                                            q = o;
                                                            cut(o->1,p,q->1,num);
        [1]==fa]=now;
    now->c[fl] = fa, fa->fa = now;
                                                            q->up();
    now->inc = fa->inc, fa->inc = 0;
                                                          } else {
    fa->up();
                                                            p = o;
  }
                                                            cut(o->r,p->r,q,num-sz(o->1)-1);
};
                                                            p->up();
SplayTree<11> tree;
                                                       }
3.7 Treap
                                                     void merge(Node *&o, Node *p, Node *q) {
struct Node {
                                                       if(!p || !q) {
  Node *1,*r;
                                                         o = p ? p : q;
  int v,delta,rev,size,minx,w;
                                                        } else {
  void up() {
                                                          if(p->w > q->w) {
    minx = v;
                                                            p->down();
    size = 1;
                                                            o = p;
    if(1) size += 1->size, minx = min(minx, 1->
                                                            merge(o->r,p->r,q);
        minx);
                                                          } else {
    if(r) size += r->size, minx = min(minx, r->
                                                            q->down();
        minx);
                                                            o = a;
                                                            merge(o->1,p,q->1);
  void down() {
    if(delta) {
                                                         o->up();
      if(1) 1->delta += delta, 1->v += delta, 1->
          minx += delta;
      if(r) r->delta += delta, r->v += delta, r->
                                                     void insert(Node *&o, int pos, int val) {
          minx += delta;
                                                       if(o == NULL) {
      delta = 0;
                                                         New_node(o,val);
    }
                                                        } else {
    if(rev) {
                                                         Node *1 , *r , *n;
      swap(1,r);
                                                          New_node( n , val );
      if(1) 1->rev ^= 1;
                                                         cut ( o , l , r , pos );
      if(r) r->rev ^= 1;
                                                          merge( 1 , 1 , n );
      rev = 0;
                                                          merge( root , l , r );
    }
                                                       }
}*root = NULL, *list = NULL;
                                                     void add(int 1, int r, int val) {
inline int sz(Node *o) { return o ? o->size : 0;
                                                       Node *a, *b, *c;
   }
                                                       cut(root,a,b,l-1);
int ran() {
                                                        cut(b,b,c,r-l+1);
  static int ranx = 123456789;
```

```
} else if (tree[c][i] < as[mid]){</pre>
 b->v += val;
 b->minx += val;
                                                       sum[c][i]++;
 b->delta += val;
                                                       tree[c+1][lp++] = tree[c][i];
 merge(a,a,b);
                                                     } else
 merge(root,a,c);
                                                       tree[c+1][rp++] = tree[c][i];
void remove(int pos) {
                                                   if (1 == r)return;
                                                   build(c+1, 1, mid);
 Node *a, *b, *c;
 cut(root,a,b,pos-1);
                                                   build(c+1, mid+1, r);
 cut(b,b,c,1);
                                                 int query(int c, int l, int r, int ql, int qr,
 merge(root,a,c);
 Reuse(b);
                                                    int s;//[l, ql)內將被劃分到左子樹的元素數目
int query(int 1, int r) {
                                                    int ss;//[ql, qr]內將被劃分到左子數的元素數目
 Node *a, *b, *c;
                                                    int mid=(l+r)>>1;
                                                   if (1 == r)
 cut(root,a,b,l-1);
 cut(b,b,c,r-l+1);
                                                     return tree[c][l];
 int ret = b->minx;
                                                   if (1 == q1){//這裡要特殊處理!
 merge(a,a,b);
                                                     s = 0;
 merge(root,a,c);
                                                     ss = sum[c][qr];
  return ret;
                                                   }else{
                                                     s = sum[c][ql 1];
                                                     ss = sum[c][qr]-;
void reverse(int 1, int r) {
                                                    } //假設要在區間[l,r]中查找第k大元素, t為當前節
 Node *a, *b, *c;
  cut(root, a, b, 1-1);
                                                       點, Lch, rch為左右孩子, Left, mid為節點t左
                                                       邊界界和中間點。
  cut(b,b,c,r-l+1);
 b->rev ^= 1;
                                                   if (k <= ss)//sum[r]-sum[l-1]>=k, 查找lch[t],區
                                                       間對應為[ Left+sum[l-1], Left+sum[r]-1 ]
 merge(a,a,b);
                                                     return query(c+1, 1, mid, 1+s, 1+s+ss-1, k);
 merge(root,a,c);
                                                   else
}
                                                     //sum[r]-sum[l-1]<k,查找rch[t], 區間對應為
void revolve(int 1, int m, int r) {
 Node *a, *b, *c, *d;
                                                     [mid+1+l-left-sum[l-1], mid+1+r-left-sum[r]]
 cut(root,a,b,l-1);
                                                     return query(c+1, mid+1, r, mid-l+1+ql-s, mid
 cut(b,b,c,m-l+1);
                                                         -l+1+qr-s-ss, k-ss);
 cut(c,c,d,r-m);
 merge(a,a,c);
                                                 int main(){
 merge(a,a,b);
                                                   int i, j, k;
                                                   while(~scanf("%d%d", &n, &m)){
 merge(root,a,d);
}
                                                     for(i=1; i<=n; i++) {</pre>
                                                       scanf("%d", &a[i]);
3.8 劃分樹
                                                       tree[0][i] = as[i] = a[i];
#include <iostream>
                                                     sort(as+1, as+1+n);
#include <cstdio>
                                                     build(0, 1, n);
#include <algorithm>
                                                     while(m--){
using namespace std;
                                                       scanf("%d%d%d", &i, &j, &k);
#define N 100005
                                                         // i,j分 別 為 區 間 起 始 點 , k 為 該 區 間 第 k 大 的
int a[N], as[N];//原數組,排序後數組
                                                             數。
int n, m;
                                                       printf("%d\n", query(0, 1, n, i, j, k));
int sum[20][N]; // 紀錄第 i 層的 1~j 劃分到左子樹的元素
                                                     }
   個 數 ( 包 括 j )
                                                   }
int tree[20][N];//紀錄第i層元素序列
                                                    return 0;
void build(int c, int l, int r) {
  int i, mid=(l+r)>>1, lm=mid-l+1, lp=l, rp=mid
     +1;
  for (i=1; i<=mid; i++)</pre>
   if (as[i] < as[mid]) lm--;</pre>
     //先假設左邊的(mid-l+1)個數都等于as[mid],然
         后把實際上小于as[mid]的減去
  for (i = 1; i <= r; i++){
   if (i == 1) sum[c][i] = 0;
     //sum[i]表示[l, i]內有多少個數分到左邊,用
         DP 來維護
   else sum[c][i] = sum[c][i-1];
   if (tree[c][i] == as[mid]){
     if (lm){
       lm - -;
       sum[c][i]++;
       tree[c+1][lp++] = tree[c][i];
       tree[c+1][rp++] = tree[c][i];
```

# 4 Graph 4.1 Dinic

```
class Flow {
public:
  Flow(int _ncnt) :ncnt(_ncnt), ecnt(1), path(new
       int[_ncnt + 2]), d(new int[_ncnt + 2]),
      visited(new bool[_ncnt + 2]){
    memset(path, 0, sizeof(int)*(_ncnt + 1));
  ~Flow(){
    delete[](path);
    delete[](d);
    delete[](visited);
  }
  void Reset(){
    memset(path, 0, sizeof(int)*(ncnt + 1));
    ecnt = 1;
  }
  void AddEdge(int s, int t, int cap){
    edge[++ecnt].tar = t, edge[ecnt].cap = cap,
       edge[ecnt].next = path[s], path[s] = ecnt
    edge[++ecnt].tar = s, edge[ecnt].cap = 0,
       edge[ecnt].next = path[t], path[t] = ecnt
  int MaxFlow(int s, int t){ // Dinic
    int f = 0, df;
    while (BFS(s, t) < ncnt){</pre>
      while (true){
        memset(visited, 0, sizeof(bool)*(ncnt +
        df = DFS(s, INF, t);
        if (!df) break;
        f += df;
      }
    }
    return f;
  }
private:
  static const int eMaxSize = 40002, INF = (int)
     1e9;
  int ecnt, ncnt;
  int *path, *d; // d for Dicic distance
  bool *visited;
  struct Edge{
    int tar, cap, next;
  }edge[eMaxSize];
  int DFS(int a, int df, int t){
    if (a == t) return df;
    if (visited[a]) return 0;
    visited[a] = true;
    for (int i = path[a]; i; i = edge[i].next){
      int b = edge[i].tar;
      if (edge[i].cap > 0 && d[b] == d[a] + 1){
        int f = DFS(b, std::min(df, edge[i].cap),
             t);
        if (f){
          edge[i].cap -= f, edge[i ^ 1].cap += f;
          return f;
        }
      }
    return 0;
```

```
int BFS(int s, int t){
    memset(d, 0x7f, sizeof(int)*(ncnt + 1));
    memset(visited, 0, sizeof(bool)*(ncnt + 1));
    d[s] = 0; visited[s] = true;
    std::queue<int> Q;
    Q.push(s);
   while (!Q.empty()){
     int a = Q.front(); Q.pop();
     for (int i = path[a]; i; i = edge[i].next){
       int b = edge[i].tar;
       if (visited[b] || edge[i].cap == 0)
           continue;
       visited[b] = true;
       d[b] = d[a] + 1;
       if (b == t) return d[b];
       Q.push(b);
     }
   }
   return d[t];
 }
};
Flow flow( 1001 );
4.2 maximum matching in general graph
//Problem:http://acm.timus.ru/problem.aspx?space
   =1&num=1099
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <iostream>
#include <algorithm>
using namespace std;
const int N=250;
int n;
int head;
int tail;
int Start;
int Finish;
               //表示哪個點匹配了哪個點
int link[N];
                 //這個就是增廣路的Father……但
int Father[N];
   是用起來太精髓了
               //該點屬於哪朵花
int Base[N];
int Q[N];
bool mark[N];
bool map[N][N];
bool InBlossom[N];
bool in_Queue[N];
void CreateGraph(){
  int x,y;
  scanf("%d",&n);
 while (scanf("%d%d",&x,&y)!=EOF)
    map[x][y]=map[y][x]=1;
}
void BlossomContract(int x,int y){
  fill(mark,mark+n+1,false);
  fill(InBlossom, InBlossom+n+1, false);
  #define pre Father[link[i]]
  int lca,i;
  for (i=x;i;i=pre) {i=Base[i]; mark[i]=true; }
  for (i=y;i;i=pre) {i=Base[i]; if (mark[i]) {lca
     =Base[i]
  for (i=x;Base[i]!=lca;i=pre){
    if (Base[pre]!=lca) Father[pre]=link[i]; //對
       於BFS樹中的父邊是匹配邊的點,Father向後跳
    InBlossom[Base[i]]=true;
    InBlossom[Base[link[i]]]=true;
  for (i=y;Base[i]!=lca;i=pre){
```

```
if (Base[pre]!=lca) Father[pre]=link[i]; //同
                                                        if (link[i]) cnt++;
                                                      printf("%d\n",cnt);
    InBlossom[Base[i]]=true;
                                                      for (int i=1;i<=n;i++)</pre>
    InBlossom[Base[link[i]]]=true;
                                                        if (!mark[i] && link[i]){
                                                          mark[i]=true;
  #undef pre
                                                          mark[link[i]]=true;
  if (Base[x]!=lca) Father[x]=y;
                                   //注意不能從
                                                          printf("%d %d\n",i,link[i]);
      Lca這個奇環的關鍵點跳回來
                                                        }
  if (Base[y]!=lca) Father[y]=x;
  for (i=1;i<=n;i++)</pre>
                                                   int main(){
    if (InBlossom[Base[i]]){
                                                      CreateGraph();
      Base[i]=lca;
                                                      Edmonds();
      if (!in Queue[i]){
                                                      output();
        Q[++tail]=i;
                                                      return 0;
        in Queue[i]=true; //要注意如果本來連向
            BFS樹中父結點的邊是非匹配邊的點,可能
            是沒有入隊的
      }
    }
}
void Change(){
  int x,y,z;
  z=Finish;
  while (z){
    y=Father[z];
    x=link[y];
    link[y]=z;
    link[z]=y;
    z=x;
  }
}
void FindAugmentPath(){
  fill(Father, Father+n+1,0);
  fill(in Queue, in Queue+n+1, false);
  for (int i=1;i<=n;i++) Base[i]=i;</pre>
  head=0; tail=1;
  Q[1]=Start;
  in_Queue[Start]=1;
  while (head!=tail){
    int x=Q[++head];
    for (int y=1;y<=n;y++)</pre>
      if (map[x][y] && Base[x]!=Base[y] && link[x
                 //無意義的邊
          ]!=y)
        if ( Start==y || link[y] && Father[link[y
            ]] ) //精髓地用Father表示該點是否
          BlossomContract(x,y);
        else if (!Father[y]){
          Father[y]=x;
          if (link[y]){
            Q[++tail]=link[y];
            in_Queue[link[y]]=true;
          }
          else{
            Finish=y;
            Change();
            return;
          }
        }
  }
void Edmonds(){
  memset(link,0,sizeof(link));
  for (Start=1;Start<=n;Start++)</pre>
    if (link[Start]==0)
      FindAugmentPath();
void output(){
  fill(mark, mark+n+1, false);
  int cnt=0;
  for (int i=1;i<=n;i++)</pre>
```

#### 5 Math

#### 5.1 China remainder theorem

```
ans \equiv a_i \pmod{m_i}
int china_remainder_theorem(int n, int ai[], int
   mi[]) {
  int gcdn, x, y, reduce, tmp;
  for(int i=1; i<n; ++i) {</pre>
    gcdn=ext_gcd(mi[i-1], mi[i], x, y);
    reduce=ai[i]-ai[i-1];
    if( reduce%gcdn!=0 )
      return -1;
    tmp=mi[i]/gcdn;
    x=(reduce/gcdn*x%tmp+tmp)%tmp;
    ai[i] = ai[i-1] + mi[i-1]*x;
    mi[i] = mi[i-1]*tmp;
  }
  return ai[n-1]%mod;
}
```

#### 5.2 Euler's phi function O(n)

```
1. gcd(x,y) = d \Rightarrow \phi(xy) = \frac{\phi(x)\phi(y)}{\phi(d)}
```

- 2.  $p \text{ is } prime \Rightarrow \phi(p^k) = p^{k-1}\phi(p)$
- 3.  $p \text{ is } prime \Rightarrow \phi(p^k) = \phi(p^{k-1}) \times p$
- 4.  $n = p_1^{k_1} p_2^{k_2} \cdots p_m^{k_m}$  $\Rightarrow \phi(n) = p_1^{k_1 - 1} \phi(p_1) \ p_2^{k_2 - 1} \phi(p_2) \cdots p_m^{k_m - 1} \phi(p_m)$

```
const int MAXN = 100000;
int phi[MAXN], prime[MAXN], pn=0;
memset(phi, 0, sizeof(phi));
for(int i=2; i<MAXN; ++i) {
   if( phi[i]==0 ) prime[pn++]=i, phi[i]=i-1;
   for(int j=0; j<pn; ++j) {
      if( i*prime[j]>=MAXN ) break;
      if( i%prime[j]==0 ) {
        phi[i*prime[j]] = phi[i] * prime[j];
        break;
      }
      phi[i*prime[j]] = phi[i] * phi[prime[j]];
   }
}
```

### 5.3 Extended Euclid's Algorithm

```
ax + by = gcd(a, b)
int ext_gcd(int a, int b, int &x, int &y){
  int x2;
  if( b==0 ) {
    x=1, y=0;
    return a;
  int gcdn=ext_gcd(b, a%b, x, y), x2=x;
  x=y, y=x2-a/b*y;
  return gcdn;
int ext_gcd(int a, int b, int &x, int &y){
  int t, px=1, py=0, tx,ty;
  x=0, y=1;
  while(a%b!=0) {
    tx=x, ty=y;
    x=x*(-a/b)+px, y=y*(-a/b)+py;
    px=tx, py=ty;
    t=a, a=b, b=t%b;
  }
  return b;
}
```

#### 5.4 Gaussian Elimination

```
// default for module version, comments for
    double version
// double mmap[row][column];
const 11 modn = 1000000007;
11 mmap[row][column];
11 inv(11 b) {
  return (b==1)?1:inv(modn%b)*(modn-modn/b)%modn;
void gauss(int n,int m) {
  int k=0;
  for(int i=0; i<m; i++)</pre>
    for(int j=k; j<n; j++)</pre>
      if(mmap[j][i]!=0) {
        for(int l=i; l<m; l++)</pre>
          swap(mmap[k][1],mmap[j][1]);
        for(j++; j<n; j++){</pre>
          if(mmap[j][i]==0)
            continue;
          //double scale=mmap[j][i]/mmap[k][i];
          11 scale=mmap[j][i]*inv(mmap[k][i])%
              modn:
          for(int p=i+1; p<n; p++)</pre>
            //mmap[j][p]-=mmap[k][p]*scale;
            mmap[j][p]=(mmap[j][p]-mmap[k][p]*
                scale%modn+modn)%modn;
          mmap[j][i]=0;
        }
        k++;
        break;
}
5.5 Miller Rabin
ll mul(ll a, ll b, ll n) { // a*b%n
  11 r = 0; a \% = n, b \% = n;
  while(b){
    if(b&1) r = (a+r)=n? a+r-n: a+r);
    a = (a+a>=n? a+a-n: a+a);
    b >>= 1;
  }
  return r;
ll powmod(ll a, ll d, ll n) { // a^d%n
  if(d==0) return 111;
  if(d==1) return a%n;
  return mul(powmod(mul(a, a, n), d>>1, n), d%2?a
      :1, n);
bool miller_rabin(ll a, ll n) {
  if (__gcd(a,n) == n ) return true;
  if (__gcd(a,n) != 1 ) return false;
  11 d = n-1, r = 0, res;
  while(d%2==0) { ++r; d>>=1; }
  res = powmod(a, d, n);
  if( res==1 || res==n-1 ) return true;
  while(r--) {
    res = mul(res, res, n);
    if(res==n-1) return true;
  }
  return false;
bool isprime(ll n) {
  ll as[7]={2, 325, 9375, 28178, 450775, 9780504,
       1795265022}; // 2, 7, 61
  for(int i=0; i<7; i++)</pre>
    if( miller_rabin(n, as[i]) == false )
      return false;
  return true;
```

#### }

#### 5.6 Möbius function

```
int* isp;
char fcnt[N+5];
int mobius[N+5];
void make_mobius(int n) {
  isp = mobius;
  memset(mobius, true, sizeof(mobius));
  memset(fcnt, 0, sizeof(fcnt));
  for(int i=2; i<=n; ++i) {</pre>
    if( isp[i] ) {
      fcnt[i] = 1;
      for(int j=i+i; j<=n; j+=i) {</pre>
        isp[j] = false;
        if( fcnt[j]!=-1 ) fcnt[j]++;
      if( i<=10000 )
        for(int ii=i*i, j=ii; j<=n; j+=ii) {</pre>
          fcnt[j] = -1;
    }
  }
  mobius[0] = 0;
  mobius[1] = 1;
  for(int i=2; i<=n; ++i) {</pre>
    if( fcnt[i]==-1 ) mobius[i] = 0;
    else if( fcnt[i]&1 ) mobius[i] = -1;
    else mobius[i] = 1;
 }
}
```

# 6 String

#### 6.1 AhoCorasick

```
#define MAXSLEN 5000
#define MAXNUM 5000
#define MAXPLEN 50
class Node {
public:
  Node *fail; // transition when undefined next
      character encountered
  map<char, Node*> _next; // transition to next
     node corresponding to a character
  bool marked; // whether the prefix is "matched"
      sometime
  Node() { fail=NULL; marked=0; }
  ~Node() {
    for(map<char, Node*>::iterator it=_next.begin
        ();it!=_next.end();it++)
    delete it->second;
  }
  Node* build(char ch) {
    if(_next.find(ch)==_next.end()) _next[ch]=new
         Node;
    return _next[ch];
  }
  Node* next(char ch) {
    if(_next.find(ch)==_next.end()) return NULL;
    else return _next[ch];
};
int pn; // number of pattern
char s[MAXSLEN]; // string to be matched
char p[MAXNUM][MAXPLEN]; // patterns
Node* pre[MAXNUM]; // its corresponding node on
   ac-prefix-tree
int ql,qr;
Node* que[MAXNUM*MAXPLEN];
bool appear[MAXNUM];
inline Node* construct(Node *v,char *p) { //
   append a prefix to the tree
  while(*p) { v=v->build(*p); p++; }
  return v;
inline void construct_all(Node *ac) { //
   construct the prefix tree
  for(int i=0;i<pn;i++) pre[i]=construct(ac,p[i])</pre>
inline void find_fail(Node *ac) { // find fail
   function
  Node *v,*u,*f;
  char ch;
  map<char,Node*>::iterator it;
  ql=qr=0;
  ac->fail=ac;
  for(it=ac->_next.begin();it!=ac->_next.end();it
      ++) {
    que[qr]=it->second;
    que[qr]->fail=ac;
    qr++;
  }
  while(ql<qr) {</pre>
    v=que[q1++];
    for(it=v->_next.begin();it!=v->_next.end();it
        ++) {
      ch=it->first; u=it->second;
      que[qr++]=u;
      f=v->fail;
      while(f!=ac&&f->next(ch)==NULL) f=f->fail;
      if(f->next(ch)) u->fail=f->next(ch);
```

```
else u->fail=ac;
                                                      for (int i=0; i<N; ++i) s[i*2+1] = t[i];</pre>
                                                      N = N*2+1;
 }
                                                      // modified Gusfield's lgorithm
                                                      Z[0] = 1;
inline void trace(Node *v) { // marked all
                                                      L = R = 0;
                                                      for (int i=1; i<N; ++i) {</pre>
   contained prefixes
  while(!v->marked) { v->marked=1; v=v->fail; }
                                                        int ii = L - (i - L);
                                                                                // i的映射位置
                                                        int n = R + 1 - i;
inline void ac_match(Node *ac,char *s) { // match
                                                        if (i > R) {
                                                          Z[i] = match(i, i);
    a string s
  Node *v=ac;
                                                          L = i;
  while(*s) {
                                                          R = i + Z[i] - 1;
    while(v!=ac&&v->next(*s)==NULL) v=v->fail;
    if(v->next(*s)!=NULL) v=v->next(*s);
                                                        else if (Z[ii] == n) {
    trace(v);
                                                          Z[i] = n + match(i-n, i+n);
    s++;
                                                          L = i;
  }
                                                          R = i + Z[i] - 1;
}
inline void aho_corasick() {
                                                        else Z[i] = min(Z[ii], n);
                                                      }
  Node ac;
  construct_all(&ac);
                                                      // 尋找最長迴文子字串的長度。
  find_fail(&ac);
                                                      int n = 0, p = 0;
  ac match(&ac,s);
                                                      for (int i=0; i<N; ++i)</pre>
  for(int i=0;i<pn;i++) {</pre>
                                                        if (Z[i] > n) n = Z[p = i];
    if(pre[i]->marked) printf("prefix %d is
                                                      // 記得去掉特殊字元。
                                                      cout << "最長迴文子字串的長度是" << (n-1) / 2;
       matched\n",i);
                                                      // 印出最長迴文子字串,記得別印特殊字元。
    else printf("prefix %d not matched\n",i);
  }
                                                      for (int i=p-Z[p]+1; i<=p+Z[p]-1; ++i)</pre>
}
                                                        if (i & 1) cout << s[i];</pre>
                                                    }
6.2 KMP
                                                    6.4 Suffix Array
int KMP(char pat[5005], char str[5005]) {
                                                    int myrank[LEN], sa[LEN];
  if( strlen(pat)>strlen(str) ) return -1;
                                                    int height[LEN];
  int failure[5005];
                                                    int y[LEN], cnt[LEN], rr[2][LEN];
  int len=strlen(pat);
                                                    inline bool same(int * myrank, int a, int b, int
  for(int i=1, j=failure[0]=-1; i<len; ++i) {</pre>
                                                        1) { return _myrank[a]==_myrank[b]&&_myrank[a
    while( j>=0 && pat[j+1]^pat[i] ) j=failure[j
                                                        +1]==_myrank[b+1]; }
                                                    void make_height(char str[]) {
    if( pat[j+1]==pat[i] ) ++j;
                                                      int len=strlen(str);
    failure[i]=j;
                                                      MSET(height, 0);
                                                      for(int i=0, j=0; i<len; ++i, j=height[myrank[i</pre>
  for(int i=0, j=-1; str[i]; ++i) {
                                                          -1]]-1) {
    while( j>=0 && str[i]^pat[j+1] ) j=failure[j
                                                        if( myrank[i]==1 ) continue;
                                                        if( j<0 ) j=0;</pre>
    if( str[i]==pat[j+1] ) ++j;
                                                        while( i+j<len && sa[myrank[i]-1]+j<len &&</pre>
    if( j==len-1 ) {
                                                          str[i+j]==str[sa[myrank[i]-1]+j] ) ++j;
      return i-len+1; // rec this!!
                                                        height[myrank[i]]=j;
      j=failure[j];
                                                      }
    }
                                                    }
  }
                                                    void sa2(char str[], int n, int MAX = 256) {
  return -1;
                                                      printf("%s!! %d %d\n", str, n, MAX);
}
                                                      int *rank1=rr[0], *rank2=rr[1];
                                                      int *myrank1=rr[0], *myrank2=rr[1]; // rolling
    Longest Palindromic Substring
                                                          array
char t[1001];
               // 要處理的字串
                                                      int *y = myrank; // share memory
cahr s[1001 * 2]; // 中間插入特殊字元的t。
                                                      MSET(rr[1], 0);
int Z[1001 * 2], L, R; // Gusfield's Algorithm
                                                      MSET(cnt, 0);
// 由a往左、由b往右,對稱地作字元比對。
                                                      int i, p=0;
int match(int a, int b) {
                                                      for(i=0; i<n; ++i) myrank2[i]=str[i], cnt[</pre>
  int i = 0;
                                                          myrank2[i]]++;
  while (a-i)=0 \&\& b+i < N \&\& s[a-i] == s[b+i]) i
                                                      for(i=1; i<MAX; ++i) cnt[i]+=cnt[i-1];</pre>
                                                      for(i=n-1; i>=0; --i) sa[--cnt[myrank2[i]]]=i;
     ++;
  return i;
                                                      for(int j=1; p<n; j<<=1, MAX=p) {
    // 表示用第二個key(myrank2)排序後 從 y[i] 開
void longest_palindromic_substring()
                                                            始的後綴排第i名
                                                        for(p=0, i=n-j; i<n; ++i) y[p++]=i;</pre>
                                                        for(i=0; i<n; ++i) if( sa[i]>=j ) y[p++]=sa[i
  int N = strlen(t);
  // 在t中插入特殊字元, 存放到s。
  memset(s, '.', N*2+1);
                                                        for(i=0; i<MAX; ++i) cnt[i]=0;</pre>
```

```
for(i=0; i<n; ++i) cnt[ myrank2[y[i]] ] ++;</pre>
                                                       Others
    for(i=1; i<MAX; ++i) cnt[i]+=cnt[i-1];</pre>
                                                  7.1 8 puzzle - IDA*
    for(i=n-1; i>=0; --i) sa[ --cnt[ myrank2[y[i
        ]] ]=y[i];
                                                  // 一個盤面。其數值1~8代表方塊號碼,0代表空格。
    for(p=i=1, myrank1[sa[0]]=0; i<n; ++i)</pre>
                                                   int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
      myrank1[sa[i]]=same(myrank2, sa[i], sa[i
                                                   // 檢查 permutation inversion。檢查不通過,表示盤
         -1], j)?p-1:p++;
                                                      面不合理。
    std::swap(myrank1, myrank2);
                                                  bool check_permutation_inversion(int board[3][3])
  for(int i=0; i<n; ++i) myrank[i]=myrank2[i];</pre>
                                                     int inversion = 0;
  make_height(str);
                                                     for (int a=0; a<9; ++a)</pre>
                                                       for (int b=0; b<a; ++b) {</pre>
int main() {
                                                        int i = a / 3, j = a % 3;
  char str[LEN];
                                                         int ii = b / 3, jj = b % 3;
  scanf("%s", str);
                                                         if (board[i][j] && board[ii][jj]
  int len = strlen(str);
                                                           && board[i][j] < board[ii][jj])
  sa2(str, len+1);
                                                           inversion++;
  for(int i=1; i<=len; ++i) printf("%d %d %s\n",</pre>
      i, height[i], str+sa[i]);
                                                     int row_number_of_0 = 0;
                                                     for (int i=0; i<3 && !row_number_of_0; ++i)</pre>
6.5 Z Algorithm
                                                       for (int j=0; j<3 && !row_number_of_0; ++j)</pre>
                                                        if (board[i][j] == 0)
void Z(char G[], int z[]){
                                                           row_number_of_0 = i+1;
  int len = strlen(G);
                                                     return (inversion + row_number_of_0) % 2 == 0;
  z[0] = len;
  int L = 0, R = 1;
                                                  for ( int i = 1 ; i < len ; i++ ) {</pre>
                                                   // heuristic function,採用不在正確位置上的方塊個
    if ( i >= R || z[i-L] >= R-i ) {
      int x = (i>=R) ? i : R;
                                                  int h(int board[3][3])
      while ( x < len \&\& G[x] == G[x-i] )
                                                  {
        x++:
                                                     int cost = 0;
      z[i] = x - i;
                                                    for (int i=0; i<3; ++i)</pre>
                                                       for (int j=0; j<3; ++j)</pre>
      if (x > i) L = i, R = x;
                                                         if (board[i][j])
    else z[i] = z[i-L];
                                                           if (board[i][j] != i*3 + j + 1)
 }
                                                             cost++;
                                                     return cost;
                                                  int taxicab_distance(int x1, int y1, int x2, int
                                                      y2)
                                                   {return abs(x1 - x2) + abs(y1 - y2);}
                                                  // heuristic function, 採用taxicab distance。
                                                   int h(int board[3][3]) {
                                                    // 每塊方塊的正確位置。 {0,0}是為了方便編寫程式
                                                        而多加的。
                                                     static const int right_pos[9][2] = {
                                                       {0,0},
                                                       \{0,0\}, \{0,1\}, \{0,2\},
                                                       \{1,0\}, \{1,1\}, \{1,2\},
                                                       \{2,0\}, \{2,1\}
                                                     };
                                                    // 計算每個方塊與其正確位置的 taxicab distance
                                                        的總和。
                                                     int cost = 0;
                                                     for (int i=0; i<3; ++i)</pre>
                                                       for (int j=0; j<3; ++j)</pre>
                                                        if (board[i][j])
                                                           cost += taxicab_distance(
                                                                 right_pos[board[i][j]][0],
                                                                 right_pos[board[i][j]][1]
                                                               );
                                                     return cost;
```

}

}

// 上下左右

, "left"};

const string operator[4] = {"up", "down", "right"

```
const int dx[4] = \{-1, 1, 0, 0\}, dy[4] = \{0, 0,
   1, -1};
char solution[30];
 // 正確的推動方式,其數值是方向0~3。
const int reverse_dir[4] = {1, 0, 3, 2};
 // 用表格紀錄每一個方向的反方向。可用於避免來回 type reval; //new
     推動的判斷。
int board[3][3] = {2, 3, 4, 1, 5, 0, 7, 6, 8};
 // 起始狀態。其數值1~8代表方塊號碼,0代表空格。
int sx = 1, sy = 2;
 // 空格的位置。可馬上知道推動方塊的目的地。
bool onboard(int x, int y)
{return x>=0 && x<3 && y>=0 && y<3;}
int IDAstar(int x, int y, int gv, int prev_dir,
   int& bound, bool& ans) {
  int hv = h(board);
  if (gv + hv > bound) return gv + hv;
   // 超過,回傳下次的bound
  if (hv == 0) {ans = true; return gv;}
   // 找到最佳解
  int next_bound = 1e9;
  for (int i=0; i<4; ++i) {</pre>
   // 四種推動方向
   int nx = x + dx[i], ny = y + dy[i];
     // 空格的新位置
   if (reverse dir[i] == prev dir) continue;
     // 避免來回推動
   if (!onboard(nx, ny)) continue;
     // 避免出界
   solution[gv] = oper[i];
     // 紀錄推動方向
   swap(board[x][y], board[nx][ny]);
     // 推動
   int v = IDAstar(nx, ny, gv+1, i, bound, ans);
   if (ans) return v;
   next bound = min(next bound, v);
   swap(board[nx][ny], board[x][y]);
     // 回復原狀態
  }
  return next_bound;
void eight_puzzle() {
 if (!check_permutation_inversion(board)) {
   cout << "盤面不合理,無法解得答案。" << endl;
   return:
 }
 // IDA*
 bool ans = false;
  int bound = 0;
 while (!ans && bound <= 50)</pre>
   bound = IDAstar(sx, sy, 0, -1, bound, ans);
 if (!ans) {
   cout << "50步內無法解得答案。" << endl;
   return;
 // 印出移動方法
 for (int i=0; i<bound; ++i)</pre>
   cout << operation[solution[i]] << ' ';</pre>
  cout << endl;</pre>
}
7.2 recursive to stack
  replace all variable in data into layer[lay].variable
struct data {
```

parameter; local variabla; direction; //new } layer[10000]; int lay=0; //new void go() { // at the beginning start: // call recursive function direction = 1; lay++, parameter = value; goto start; point1: variable = reval; // return reval = value; lay--; goto trans; // at the end trans: switch (direction) { case 1: goto point1; }

## The End