FACHHOCHSCHULE NORDWESTSCHWEIZ

MASTER THESIS PROPOSAL

Deep Learning for Anomaly Detection

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Declaration of Authorship

I, Kevin SANER, declare that this thesis titled, “Deep Learning for Anomaly Detection” and the work presented in it are my own. I confirm that:

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"*Your brain does not manufacture thoughts. Your thoughts shape neural networks.*"

Deepak Chopra

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Abstract

School of Business

Master of Science in Business Information Systems

Deep Learning for Anomaly Detection

by Kevin SANER

In the age of Big Data, data analysis becomes ever more important. To analize the data, many researchers nowadays focus on articial intelligence. Artificial intelligence does not rely on labour-intesive feature engineering like the traditional machine learning or statistical models. Therefore the use of AI, such as neural networks, can save a lot of development time. Two widely used architectures of neural networks are the Convolutional Neural Networks and the Recurrent Neural Networks. A Convolutional Neural Network is generally used when a task is related to image recognition, whereas Recurrent Neural Networks are used for the prediction of time series. Recently an approach was proposed to analyze time series data with Convolutional Neural Networks. The strengths and weaknesses of this approach, however, are currently unknown and are further investigated in this paper. To examine the usefulness, the practically relevant use case of anomaly detection was chosen. Within the scope of this work, different approaches on anomaly detection, that employ convolutional or recurrent neural networks are investigated. Further, the influence of transfer learning on both architectures is examined. Since the architectures should be compared regarding their performance, ways to evaluate the performances are assessed. Finally, it is described, how the chosen framework of methodoloy is applied and how the further research is planned out.

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List of Abbreviations

DNN	**D**eep **N**eural **N**etwork
CNN	**C**onvolutional **N**eural **N**etwork
RNN	**R**ecurrent **N**eural **N**etwork
GRU	**G**ated **R**ecurrent **U**nit Network
LSTM	**L**ong **S**hort **T**erm **M**emory
ROC	**R**eceiver **O**perating **C**haracteristics
AUC	**A**rea **U**nder the **C**urve
MAE	**M**ean **A**bsolute **E**rror

Chapter 1

Introduction

With the rise of the Internet of Things (IoT) and ever more sensors, gadgets and smart devices like smartwatches for fall detection or blood pressure monitoring, or fridges for temperature protective control in use, the amount of available data steadily increases (Alansari et al., 2018). Simultaneously, the possibilities to use the data to draw conclusions increases. This data is generally used to draw conclusions such as failure of a system or a medical issue, such as a heart attack. These events typically occur very rarely (Hauskrecht et al., 2007). However, when the number of instances of each class is approximately equal, most machine learning algorithms function best. Problems occur when the number of instances of one class greatly exceeds the number of instances of the other. This issue is very popular in practice, and it can be observed in a variety of fields such as fraud detection, medical diagnosis, oil spillage detection, facial recognition, and so on (Thabtah et al., 2020). The task of identifying the rare item, event or observation is often referred to as anomaly detection. Typically, the anomalous item translates to problems such as bank fraud or medical problems. Often, the anomaly does not adhere to the common statistical definition of an outlier. Therefore, many outlier detection methods (in particular unsupervised methods) fail on such data (Hodge and Austin, 2004)

A special discipline in anomaly detection is to find the anomaly in a time series. The anomaly detection problem for time series is usually formulated as finding outlier data points relative to some standard or usual signal. Time series anomaly detection plays a critical role in automated monitoring systems. It is an increasingly important topic today, because of its wider application in the context of the Internet of Things (IoT), especially in industrial environments. The most popular techniques to find the anomalies are:

- Statistical Methods
- Support Vector Machines
- Clustering
- Density-based Techniques
- Neural Networks

Currently Neural Networks are regarded the cutting-edge research. Although first approaches to use artificial neural networks exist since 1969. They are popular in research for only about 15 to 20 years. Neural networks are well-suited for assisting people in solving complex problems in real-world situations. They can learn and model nonlinear and complex relationships between inputs and outputs; make generalizations and inferences; uncover hidden relationships, patterns, and predictions; and model highly volatile data (such as financial time series data) and variances required to predict rare events (such as fraud detection). Since neural networks do not require time intensive feature engineering, but instead learn the features themselves a lot of time can be saved setting up a model

compared to traditional machine learning approaches. At the moment, there is a lot of research focussing on neural networks, which is why scientist generally expect further improvements on this kind of technology. This promising outlook is why this research paper also purely focusses on Neural Networks for anomaly detection. Convolutional Neural Networks and Recurrent Neural Networks are two neural network topologies that are commonly employed. Convolutional Neural Networks are commonly utilized for image identification tasks, whereas Recurrent Neural Networks are used for time series prediction. Recently, a method for detecting anomalies in time series data with Convolutional Neural Networks was proposed. Therefore especially Recurrent Neural Networks and Convolutional Neural Networks are investigated and compared.

1.1 Definitions

Following, the most important terms in the context of anomaly detection using neural networks are elaborated and defined.

1.1.1 Univariate, Bivariate and Multivariate Data

Time series data investigation poses a special discipline. Generally anomalies in time series are harder to detect for traditional statistical models, since the possibility of long term dependencies exist. Time series data comes in different forms. It is distinguished between univariate, bivariate and multivariate data. Univariate involves the analysis of a single variable while bivariate and multivariate analysis examines two or more variables. One significant difference between time-series and other datasets is that the observations are dependent not only on the components d, but also on the time feature n. Thus, time-series analysis and the statistical methods employed are largely distinct from methods employed for random variables, which assume independence and constant variance of the random variables. Time-series are important to data analysts in a variety of fields such as the economy, healthcare and medical research, trading, engineering, and geophysics. These data are used for forecasting and detecting anomalies.

Univariate Data

There is only one variable in this type of data. Because the information only deals with one variable that changes, univariate data analysis is the simplest type of analysis. It is not concerned with causes or relationships, and the primary goal of the analysis is to describe the data and identify patterns.

Bivariate Data

This type of data involves two different variables. This type of data analysis is concerned with causes and relationships, and the goal is to determine the relationship between the two variables.

Multivariate Data

Multivariate data is defined as data that contains three or more variables. It's similar to bivariate, but there are more dependent variables meaning there is not only one variable that influences the observed behaviour (independent variable) but several. The methods for analysing this data are determined by the objectives to be met. Regression analysis,

path analysis, factor analysis, and multivariate analysis of variance are some of the techniques. Data collected from several sensors installed in a car is an example of a multivariate time-series.

1.1.2 Neural Networks

An Artificial Neural Network (ANN) with several layers between the input and output layers, is known as a Deep Neural Network (DNN). Neural networks come in a variety of shapes and sizes, but they all have the same basic components: neurons, weights and functions. These components work in a similar way as human brains and can be trained just like any other machine learning algorithm.

Neuron

Artificial neurons represent the smallest building blocks of neural networks. A neuron usually receives separately weighted inputs which it sums. The sum is then passed through the activation function to calculate the output of the neuron. When training a neural network, the input weights are adjusted by the optimizer function (see section 1.1.2) to improve accuracy of the given task e.g. classification.

Layer

In neural networks three different kind of layers are distinguished. There are input, output and hidden layers. A layer can be described as a collection of neurons. All layers between the input and output layer are called hidden layers. In the input layer data is fed into the neural network. The output of the hidden layer is calculated by taking the weighted sums of input and passing it through the activation function. Typically, a more complex problem requires more hidden layers to accurately calculate the output. In the output layer the final result e.g. a classification is produced. Figure 1.1 how a simple Neural Network with just one hidden layer could look like.

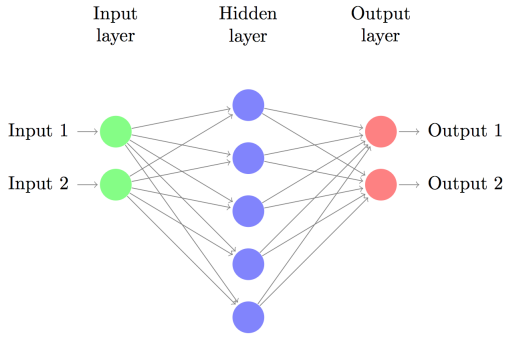

FIGURE 1.1: Input, Hidden and Output Layers (Denny Britz, 2015)

Optimizers

Deep learning has the idea of loss, that tells us how poor the model is performing at the moment. The loss is used the train the network so it performs better. Essentially, a way to decrease the loss needs to be found, because a lower loss indicates that the model is doing better. In mathematics, the process of minimizing an expression is called optimization.

Optimizers are techniques or approaches that are used to adjust the characteristics of the neural network, such as weights, in order to minimise losses.

Supervised vs. Unsupervised Learning

Supervised learning refers to a task, where a machine learning algorithm learns on data that is labelled. A time series that contains an anomaly that is labelled as such would be an example of such a data set. In contrast, when a machine learning algorithm is applied to an unlabelled data set, it is called unsupervised learning. The goal of unsupervised learning is to find hidden patterns (clusters) in the data set.

1.2 Background

Following, it is explained how different kinds of neural networks work and what they are used for.

1.2.1 Neural Networks for Anomaly Detection

Out of the three most popular neural network architectures, convolutional neural networks (CNN), recurrent neural networks (RNN) and deep neural networks (DNN), RNNs are typically used for anomaly detection in time series [e.g (Malhotra et al., 2015), (Verner, 2019)]. RNNs have built-in memory and are therefore able to anticipate the next value in a time series based on current and past data. Classic or vanilla RNNs can theoretically keep track of arbitrary long-term dependencies in input sequences. There, however, is a computational issue: when using back-propagation to train a vanilla RNN, the back-propagated gradients can "vanish" or "explode" due to the computations involved in the process, which use finite-precision numbers. Because Long Short Term Memory (LSTM) units allow gradients to flow unchanged, RNNs using LSTM unit or Gated Recurrent units (GRU) partially solve the vanishing gradient problem and therefore drastically improve accuracy (Hochreiter and Jürgen Schmidhuber, 1997).

Specially to mention in this context are LSTM (Long-Short Term Memory) and GRU (Gated Recurrent Units). Both achieved outstanding performance when used for tasks such as unsegmented, connected handwriting recognition, speech recognition and anomaly detection in network traffic or IDSs (intrusion detection systems) (Chung et al., 2014)

LSTM

LSTM was first proposed in 1997 by Schmidhuber and Hochreiter (Hochreiter and Jürgen Schmidhuber, 1997). The initial version to the LSTM unit consisted of a cells, input and output gates. In 1999, the LSTM architecture was improved by introducing a forget gate and therefore allowing the LSTM to reset its own state (Gers, Jürgen Schmidhuber, and Cummins, 2000). LSTM is used in a supervised training approach, that means it tries to predict a predefined state taking the past and the current state. If the predicted state differs from the expected state, the weights of the different gates are adjusted using an optimizer algorithm such as gradient descent. Figure 1.2 shows how the gates and the cell are arranged. The cell represents the memory of the LSTM. In simple words, the LSTM works as follows to predict a new value:

1. Forget Gate: Obsolete information is removed from the cell state.
2. Input Gate: New information is added to the cell state

3. Output Gate: The new information and the cell state are added to make the new prediction.

4. The new cell state is propagated to the next LSTM unit

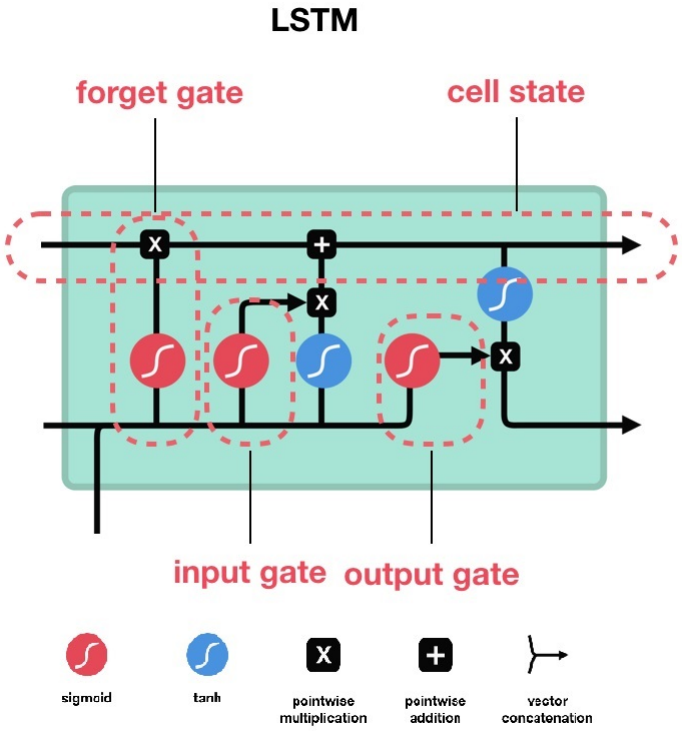

FIGURE 1.2: Gates and Cell of LSTM (Michael Phi, 2018)

CNN

In contrast to RNNs Convolutional Neural Networks are generally used for image classification. CNNs work as feature extractors and are able to recognize patterns . CNNs use layers that are not fully connected, to reduce complexity (compare to 1.2.1). In a CNN, a set number of neurons forms a filter. These filters or kernels are the actual feature extractors. A filter may represent a line or pattern (see Figure 1.3) (LeCun et al., 1998).

FIGURE 1.3: Example of a Filter used in CNN (Rich Stureborg, 2019)

To detect whether, a feature is occurrent in a picture, the filter is gradually moved over the picture in so called strides. In every step (stride) the dot-product between the filter and the part of the picture is calculated. The results of the operations are stored in activation maps. The greater the dot-product the more alike are the filter and the section of the image. Training the network hereby refers to determining the shapes of these filters. Other typical features of a CNN are the pooling layers. The pooling layers reduce the amount of computation necessary. The most commonly used pooling technique is max-pooling and works as shown in Figure 1.4.

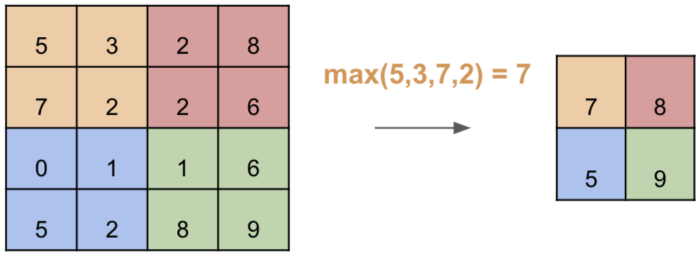

FIGURE 1.4: Example of max-pooling (Rich Stureborg, 2019)

The idea of max-pooling is to only keep the maximum value of an activation map,. In the orange region 7 represents the maximum value, so it is kept while the other values are discarded (Rich Stureborg, 2019). Using this technique the sharpest features are extracted.

In 2019, Wen and Keys proposed to use CNN also for anomaly detection in time series since it shares many common aspects with image segmentation. A univariate time series is therefore viewed as a one-dimensional image.

1.2.2 Transfer Learning

The reuse of a previously trained model on a new problem is known as transfer learning. It is currently very popular in deep learning because it can train deep neural networks with a relatively small amount of data. This is particularly useful in the field of data science, as most real-world problems do not provide millions of labelled data points to train complex models. In transfer learning, the knowledge of an already trained machine learning model is applied to a different but related problem. For example, if a classifier was trained to predict if an image contains a backpack, the model's experience could be applied to recognize other objects such as sunglasses (Niklas Donges, 2020).

1.3 Problem Statement

Defining a ground truth is one of the most difficult aspects of time series anomaly detection. Determining when anomalous behaviour begins and ends in time series is a difficult task, as even human experts are likely to disagree in their assessments. Furthermore, there is the question of what constitutes a useful detection when detecting anomalies in time series. In the past, RNN have successfully been used for anomaly detection (e.g. [(Malhotra et al., 2015); (Fan et al., 2016)]. Therefore, designs for various use cases are well researched. RNN are well suited for the task, however, take a long time to train due to the complexity of how a single unit is designed (see 1.2.1). In comparison CNN are not as complex and therefore, generally take less time to train. However, CNNs are generally used for image recognition and were only very recently used for anomaly detection

in time series. It is therefore mostly unknown what designs are applicable for successful anomaly detection in time series data. While RNN are able to deal with multivariate data by design, a classical CNN requires design changes to be able to deal with multivariate data. Wen and Keys (2019) proposed to use a special kind of U-net, an improved version of a Fully Convolutional Neural Network (Ronneberger, Fischer, and Brox, 2015). Further, a CNN is not capable to analyse streaming data so it relies on segmentation of the data. These data segments are called snapshots. In order to not miss any data points, the frequency of taking these snapshots should be at least as high as the length of snapshot so that every time point is evaluated by the model at least once. However, for better performance it might prove beneficial to use a higher frequency which means every point is evaluated various times by the model (Wen and Keyes, 2019). The proposed design change and the fact that every point is evaluated multiple times, increases complexity and evaluation time and therefore counteract the architectural advantage of CNN compared to a RNN. When designing a neural network many parameters have to be chosen, this applies to both mentioned types of Neural Networks. For example, when designing a CNN, the number of layers, the activation function(s) of a single neuron and the optimizer function have to be chosen. Additionally, when using CNN for time series data the length and frequency of the snapshots have to be determined. Similarly, when designing a RNN also the number of layers and the optimizer function have to be determined. Because the basic building blocks of both networks types are very different it is difficult to fairly compare the complexity of two architecture approaches. Another important parameter which applies to both network types is the number of epochs for which the networks are trained. Through the epochs the training time is determined. In order to compare the two types of neural networks, two networks of similar complexity have to be designed. With equal training time the performance of both can be compared and evaluated. A RNN is therefore only set up as benchmark while the main goal of this research project is to clarify whether CNNs are really useful and propose an advantage over RNNs when applied on time series data for anomaly detection.

1.4 Thesis Statement

Convolutional Neural Networks are superior to Recurrent Neural Networks when looking for anomalies in time series data regarding training time and complexity.

1.4.1 Subquestions

- How does a CNN for univariate and multivariate data need to be designed for successful anomaly detection in time series data?
- What advantages and disadvantages arise when using a CNN compared to a RNN for anomaly detection in univariate and multivariate time series?
- What parameter settings are crucial for a fair performance comparison between RNN and CNN?
- Optional: How does transfer learning affect the performance of CNN compared to RNN in anomaly detection in time series?

1.4.2 Research Objectives

Following the research objectives of this paper are defined.

1. Determine what design changes a CNN requires to detect anomalies in time series data.
2. Determine how the CNN should be designed for the comparison with a RNN
3. State the advantages and disadvantages of the chosen CNN architecture.
4. Define parameters which allow a fair comparison of CNN and RNN

1.4.3 Limitations

Recently there have been approaches that combine CNN and RNN into a hybrid network for tasks such as handwriting recognition or video-based emotion recognition (Dutta et al., 2018) (Fan et al., 2016). However, this paper only compares pure CNN and RNN, and does investigate a hybrid approach.

1.4.4 Significance

Until now, time series data was almost only approached with RNNs. This paper should answer the question whether CNNs propose a valid alternative and even propose some advantages over RNNs. The paper will answer the fundamental question whether research should channel efforts to further investigate CNNs for anomaly detection in time series data or whether no benefits can be discovered and research is better to focus on other areas.

Chapter 2

Related Literature

2.1 Anomaly or Outlier?

Generally, there is no agreement on how to distinguish between anomalies and outliers. The following often used citation proves equality of the term outliers and anomalies.

"*Outliers are also referred to as abnormalities, discordants, deviants, or anomalies in the data mining and statistics literature.*" - Aggarwal (2013)

By others, outliers are regarded as corruption in data, while anomalies are abnormal points with a particular pattern. In the context of this paper, only the term anomaly is used to refer to such irregular behaviour. It is hereby important to provide a clear definition for the concept of anomaly. This is critical since different meanings of abnormalities necessitate different detection methods. As a result, it is important to identify the key characteristics of anomalies and to use the description to highlight the boundaries. Following, two of the most common definitions of anomalies:

"*Anomalies are patterns in data that do not conform to a well defined notion of normal behaviour.*" - Chandola et al. (2009)

Ord (1996), defines anomalies as follows:

"*An observation (or subset of observations) which appears to be inconsistent with the remainder of that set of data.*"

Anomalies have two major features, according to both of these definitions:

- The anomalies' distribution deviates significantly from the data's overall distribution.
- Standard data points make up the vast majority of the dataset. The anomalies make up a very small portion of the overall dataset.

The development of anomaly detection methods is dependent on these two factors. The second property, in particular, prevents the employment of common classification methods that depend on balanced datasets.

2.1.1 Types of Anomalies

Anomalies come in a variety of shapes and sizes. Anomalies can be divided into three categories:

1. **Point Anomalies** - A point anomaly occurs when a single point deviates dramatically from the rest of the data. A point anomaly in a time series is, for example, a temperature peak in an otherwise, over time, steady temperature.

2. **Collective Anomalies** - Individual points may or may not be anomalous, but a series of points may be. A time series example could look as follows: A bank customer withdraws $500 from her account per weekday. Although withdrawing $500 every now and then is common for the consumer, a series of withdrawals is unusual.

3. **Contextual Anomalies** - Some points can appear natural in one context but be identified as anomalous in another: In Germany, a daily temperature of 35 degrees Celsius is considered natural in the summer, but the same temperature in the winter is considered unusual.

Knowing ahead of time what kind of anomaly the data might contain helps the data analyst choose the best detection process. Some methods for detecting point anomalies fail to detect collective or contextual anomalies entirely (Braei and Wagner, 2020).

2.2 Anomaly Detection on Univariate Time Series

First, anomaly detection on univariate time series using deep learning approaches is investigated to gain insight into the used architecture and the overall training and detection process.

2.2.1 LSTM

Because of their ability to retain long term memory, Long Short Term Memory (LSTM) networks have been shown to be especially useful for learning sequences containing longer term patterns. Malhotra et al. (2015) model normal behaviour with a predictor and then use the prediction errors to classify abnormal behaviour. This is especially useful in real-world anomaly detection scenarios where instances of normal behaviour are plentiful but instances of anomalous behaviour are rare. For prediction, multiple time steps into the future are forecasted to ensure that the networks capture the temporal structure of the chain. As a result, each point in the series has multiple corresponding expected values made at various points in the past, resulting in multiple error values. The likelihood of normal behaviour on the test data is calculated using the probability distribution of the errors produced when predicting on normal data. For this approach Malhotra et al. use a deep LSTM neural network. The proposed network architecture with two hidden layers is successfully applied on different univariate time series such Electrocardiograms (ECG), a valve time series and a power demand dataset. The proposed approach on univariate data could easily be adopted with multivariate data, where instead of a univariate in- and output, a multivariate data set is fed into the neural network to predict a multivariate output.

Especially to mention is the training approach used in both papers. To train the LSTM based Recurrent Network the data was divided into four sets. a non-anomalous training set, a non-anomalous validation set, a mixture of anomalous and non-anomalous validation set and test set, also consisting of a anomalous and non-anomalous sequences. This approach was chosen to deal with the rare class problem, which is typical in anomaly detection. Since non-anomalous data is plentiful, the model is trained in an unsupervised fashion, predicting the future but not able to classify if anomalous behaviour was present. The goal of this approach was to establish a baseline of non-anomalous behaviour with

the training set. The learned model was then validated and tested with anomalous and non-anomalous data to evaluate its performance.

2.2.2 CNN

The use of CNNs for time-series analysis has received interest in recent years. Munir et al. (2019) forecast time-series and identify anomalies based on the prediction error using a CNN architecture called deep-learning based anomaly detection method (DeepAnT). DeepAnT uses an architecture that is divided into two modules. The first module is called "Time Series Predictor". The "Time Series Predictor" consists of a CNN. As the name of the module indicates, the CNN is responsible for predicting the future time stamps of a given time series, whereas the "Anomaly Detector" module is responsible for tagging given data point as anomalous. Figure 2.1 represents the architecture of the CNN-based predictor module. It consists of two convolutional layers, each followed by a max-pooling layer. As the last layer, however, a fully connected layer, where all neurons are connected to all neurons of the previous layer, is used. The last is responsible for predicting the next time step. The number of output nodes, hereby, corresponds to the number of predicted time steps. One output node means only the next time step into the future is predicted, whereas three output nodes would imply a sequence of three data points are predicted.

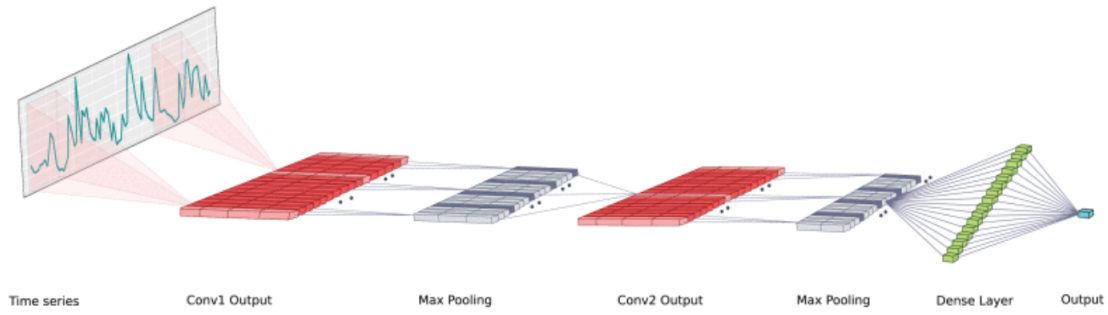

FIGURE 2.1: CNN Architecture for Time Series (Munir et al., 2019)

Once the next time steps are predicted, the values are then passed to the "Anomaly Detector". The detector module calculates the Euclidian distance between the predicted and the actual data point. This measure of discrepancy is used as anomaly score. A high anomaly score indicates a significant anomaly at a given time step. In order to classify the time samples as anomalous and non-anomalous, an anomaly threshold must be specified. The anomaly threshold classifies all data points that lie under the treshold, where the Euclidean distance of predicted and actual value is small, as normal. In contrast all points that exceed the threshold are classified as anomalous. Depending on how low the threshold is set, the sensitivity can be increased. Actually, a lot of anomaly detection algorithms require such a threshold.

2.2.3 Comparison

In an extensive study Braei and Wagner (2020) compared 20 different anomaly detection methods. The anomaly detection methods were divided into the three following categories.

- Statistical Methods

- Classical Machine Learning Methods
- Deep Learning Based Methods (Neural Networks)

Comparison of AUC

The methods were applied on data containing point, collective and contextual anomalies. In order to compare the different approaches, AUC-Values [1] were used. The results showed that the statistical methods generally performed best on point and collective anomalies while deep learning approaches performed rather poorly. On a dataset that contained contextual anomalies, the situation reflected the exact opposite. Deep learning approaches clearly outperformed statistical methods. It was observed that deep learning approaches kept their ability to generalize while statistical methods overfitted on the data (Braei and Wagner, 2020).

Computation Time

The second parameter that was used to compare the different categories was training and inference time. Inference refers to the time used to classify the test data. Compared to statistical methods and classical machine learning, deep learning approaches once again performed rather poorly regarding training time. Looking at inference time deep learning approaches generally perform well, outperforming the other two categories. However, there are huge difference within the deep learning approaches. While CNNs have a very low inference time, and outperform most other algorithms, LSTMs have the highest inference time of all tested algorithms (Braei and Wagner, 2020).

2.3 Anomaly Detection on Multivariate Time Series

In this chapter, anomaly detection on multivariate time series is investigated. Once again, CNNs and LSTMs are examined on the state of the art application possibilities for anomaly detection or time series classification.

2.3.1 LSTM

First, relevant works that use LSTMs are investigated. LSTMs will be used to establish a benchmark.

Anomaly Detection using LSTM

In his dissertation, Alexander Verner (2019), compared different versions of LSTM Neural Networks against traditional machine learning algorithms such as Support Vector Machines (SVM) and Random Forests. The various algorithms were applied to data of sensors that measure blood glucose levels. To measure the blood glucose levels multiple sensors are used for an accurate result, thus a multivariate time series is the outcome. The data set used in Verner's work did not contain anomalies by default, but the anomalies were embedded into the data set artificially. Since the data was also labelled after the type of anomaly it contained, the learning approach can be classified as supervised. Thus, the goal of the study was to correctly classify which anomaly was present. The first approach used a deep or stacked LSTM, with 10 units in the first layer and 35 in the second. The

[1] An ROC curve (receiver operating characteristic curve) is a graph showing the performance of a classification model at all classification thresholds. The AUC measures the entire two-dimensional area underneath the entire ROC curve. See section 2.5.1

resulting accuracy of only 0.4 was, however, rather disappointing. This poor performance was explained with an occurring information loss within the deep network. Next, a single layer architecture, with 100 units was proposed. With just a 10% increase the resulting accuracy was still unacceptable. In a third attempt, the neural network was enriched with an embedding layer. Using this technique, the neural network was able to detect the relationship between the frequencies of measurements that were closely positioned in the time-series. It achieved an accuracy of 98%. The final architecture then used bidirectional LSTMs (BLSTMs). According to Graves (2005), BLSTM outperform LSTM on supervised labelling tasks. A BLSTM can extract even more information from raw data by taking into account the relationship of each measurement to both previous (past) and subsequent (future) measurements in the input time-series. This enhancement resulted in a 99% accuracy. This impressive accuracy, however, comes at a cost. LSTMs are very time consuming and resource intensive to train. Verner used an Amazon Web Service computing instance with 24 CPUs, 4 GPUs and 128 GB of RAM but the training of an LSTM still took about 10 hours.

2.3.2 CNN

In this section CNNs for anomaly detection but also for classification of time series are investigated.

Classification of Time Series Data using CNN

In their research project Zheng et al. (2014) tried to beat the state of the art classification algorithm for time series, which is the k-Nearest Neighbor algorithm(k-NN). k-NN has been empirically shown to be extremely difficult to beat. The typical problem of the k-NN algorithm, however, is its computation time. Zheng et al. proposed to use their own developed architecture, which is called Multi-Channel Deep CNN (MC-DCNN). Each channel, hereby represents a CNN with convolutional and pooling layers. Typically channels in CNN are used to extract features from the different spectra of pictures. A coloured picture for example consists of three channels, red, green and blue. Each channel now works as feature extractor on just one colour. This feature of CNN is now used in time series classification. Every channel learns features independently using a single dimension of the multivariate time series as input. Another difference to image classification is that multivariate time series classification uses multiple 1D subsequences rather than 2D image pixels as data. Because CNN only learn features, no classification can be done. In order to classify, a CNN architecture is combined with a Multilayer Perceptron (MLP) that uses fully connected layers. Figure 2.2 shows the just described architecture. On the left, the different channels are shown, where every channel takes on its own univariate time series. With the denoted feature maps and pooling layers the features of the time series are learned. In the MLP on the right, finally, the classification of the time series is done. It is important to note that this architecture does not predict the next time steps in the series but instead a given time series is directly classified. The classification is hereby for example used to classify the physical activity depending on the heartrate and is not used for anomaly detection. In order to use the proposed architecture for anomaly detection however, only the output layer has to be changed.

Zheng et al. state that the used architecture was superior to the k-NN algorithm regarding accuracy. Further, the experiments show that deeper architecture are able to learn more robust high-level features. Further, the MC-DCNN architecture performs much faster than the k-NN algorithm, especially when a large dataset is present. The above described architecture could be adopted unchanged in order to classify anomalies.

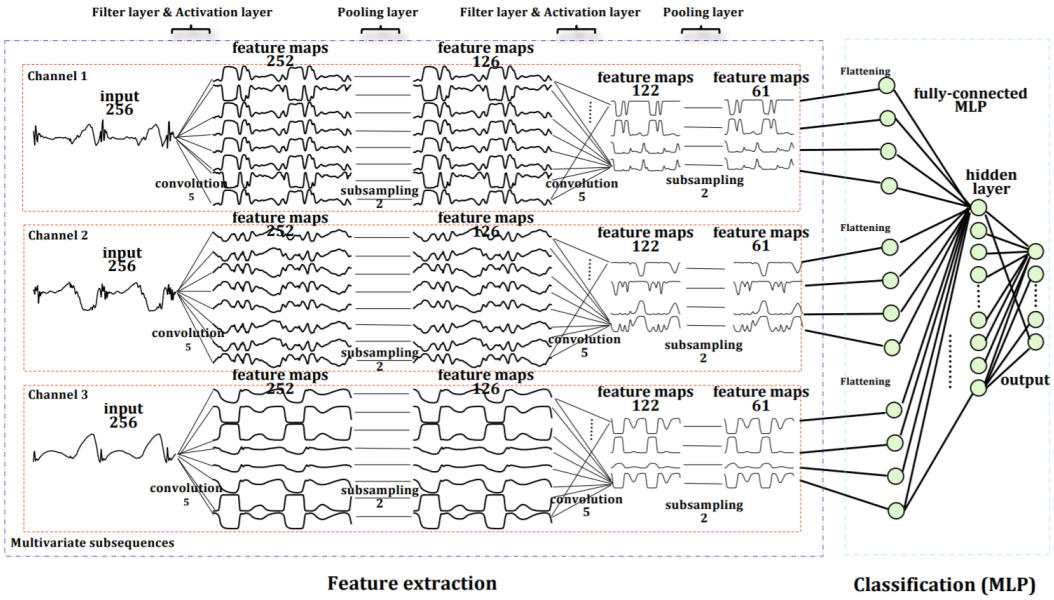

FIGURE 2.2: Architecture of the MC-DCNN (Zheng et al., 2014)

U-Nets for Anomaly Detection

Wen and Keyes (2019) use a special type CNN architecture to detect anomalies. The architecture used is called U-Net. A U-Net consists of so called encoding and decoding layers. The encoding layers work like a standard CNN whereas the decoding layers are used for upsampling. Upsampling refers to restoring the previously condensed feature maps to its original size. In short, the encoding layers extract the most important features of the time series and decoding layers are using these features to assemble a new time series of the same dimensions as the original one. This encoder-decoder-architecture is often referred to as autoencoder architecture. The main weakness of autoencoders is that in the encoding part through downsampling information is permanently lost. To prevent this information loss, U-Nets introduce so called skip channels also called skip connections. A skip connection, as the name implies, is one that connects an earlier part of the network to a later part of the network and transfers data. The idea is simple: skip channels bring back missing knowledge from some earlier layers so that the network can be properly contextualized. This architecture was proven successful when applied to segmentation of neuronal structures in electron microscopic images in the original paper (Çiçek et al., 2016). In order to handle multivariate time series U-Nets also make use multiple channels. Figure 2.3 shows the architecture of the above described U-Net. The left part of the picture shows the encoding layer with five convolutional layers. The encoding layer is followed by the decoding layer, in the right part of the picture. The decoding layer consists of 4 upsampling layers. This symmetric architecture is completed by the yellow lines, that represent the skip channels.

Finally, the model tries to classify what kind of anomaly the multivariate time series contained e.g a seasonal anomaly (contextual) or a point anomaly. Depending on whether the anomaly classes are mutually exclusive or not either a sigmoid or softmax activation is used as last layer activation function.

The proposed U-Net was tested on four scenarios: a univariate task with sufficient data, a multivariate task with sufficient data, a univariate task with insufficient data and transfer learning, and a multivariate task with insufficient data and transfer learning.

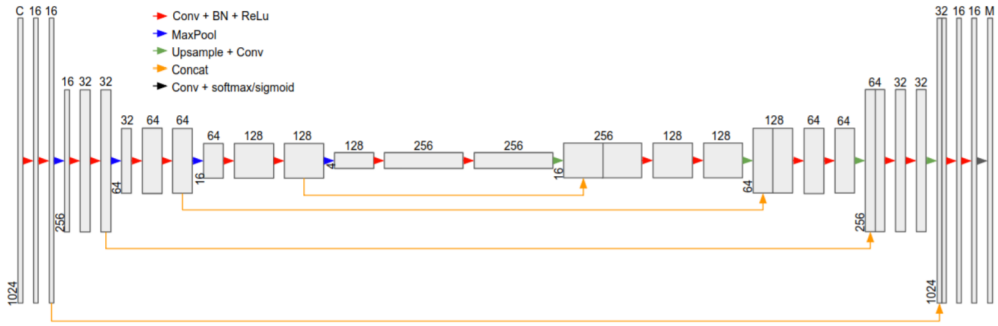

FIGURE 2.3: U-Net Architecture (Wen and Keyes, 2019)

For univariate task the dodgers loop sensor data was used. It involves a 28-week time series of traffic on a ramp near Dodger Stadium with a 5-minute frequency. The goal is to spot unusual traffic patterns caused by sporting events. Out of 39 events, only three could not be detected. The missing detection were attributed to missing values in the data set. Missing values apparently also were the reason for some false positives.

For the multivariate task the gasoil heating loop data set was used. It contains 48 simulated control sequences for a gasoil plant heating loop that was hacked at one stage. There are 19 variables in all time series. A multivariate U-Net with 19 channels was trained. Out the 18, in the test present attacks, only one was missed. However, also 3 false alarms (false positives) were reported.

The tasks that included transfer learning are investigated further in section 2.4.1.

2.4 Transfer Learning

The idea behind transfer learning is to transfer knowledge from one domain to another. For example, the knowledge of a Neural Network that classifies pictures of dogs and cats can be used to classify pictures of rabbits. This is possible because all these animals share some features such as eyes or ears. Transfer learning typically uses a, on a large data set, pre-trained network. Some layers are then retrained on the target data set, that typically is much smaller and might not consist of enough data to train a powerful Neural Network.

2.4.1 Transfer Learning with CNN

Since CNN work as feature extractors, the idea when applying transfer learning is to transfer these features to different domains. In the first few layers a CNN typically learns low level features like corners or edges. The features are typically adopted unchanged, meaning the learned weights of the neurons are frozen. The deeper layers of CNN assemble the low level features to high level features such as an ear. Depending on how related the domain of the pretrained and the new network are, deep layers should be retrained to form other features. If a CNN that is trained to recognize animals should be used to classify furniture, the features possibly can not be adopted one-to-one. Instead, the pretrained weights of the neurons are used as initial weights compared to randomly initialised weights when training a CNN from scratch. Using this approach the CNN is fine tuned to new domain using its previous knowledge. The only part of the neural network that is trained from scratch is the classification layer at the end. This part typically consists

of the fully connected layers and the output layer. These parts need to adopt to the new classes (Chollet and Allaire, 2018).

Transfer Learning in Anomaly Detection

Wen and Keyes (2019) differentiated between transfer learning on univariate and multivariate tasks. For univariate tasks, the architecture, a U-Net, shown in figure 2.3 was used. Only the output layer was changed to match the number of classes in the target task. The pretraining was carried out with various data sets containing different kinds of anomalies such as additive outliers, anomalous temporary changes of volatility, and violations of cyclic patterns as these are the most common anomalies found in univariate time series. In theory, the features learned on these anomalies should be relevant for general anomaly detection. To pretrain the U-Net, synthetic time series were generated. These time series were enriched with the previously mentioned anomalies to create labelled data set for pretraining. Figure 2.4 shows samples from the pretraining data set. In purple, additive outliers, in green changes of volatility and in red violations of cyclic patterns can be observed.

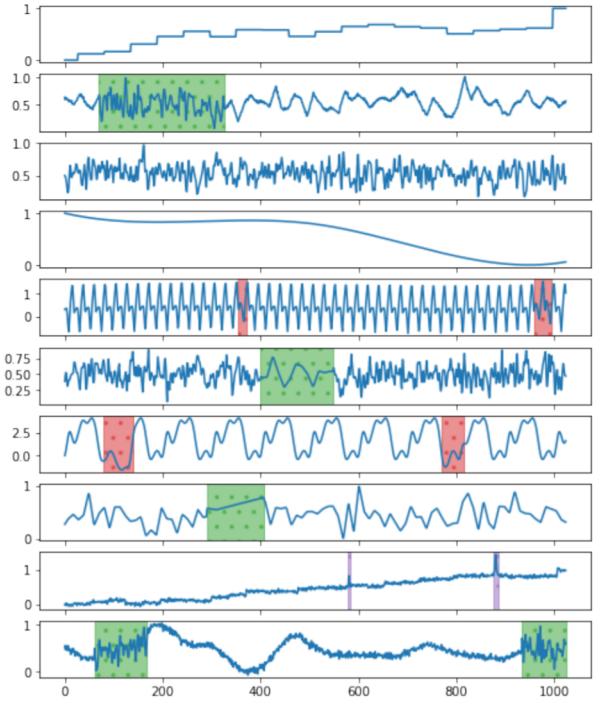

FIGURE 2.4: Synthetic Time Series (Wen and Keyes, 2019)

2.4.2 Transfer Learning with RNN

Although not used as often, transfer learning can also be applied when training RNN. Similar to CNN, RNNs require large labelled data sets for training. Therefore transfer learning is valuable approach when a data set is not large enough to train a powerful RNN. When applying transfer learning, RNNs are typically trained on a related source domain, meaning the resulting weights of the neurons figure as a base. The resulting model is then fine tuned on the target domain. When applying transfer learning using RNN, better accuracy and reduced training efforts on the target domain are the main goals (Gupta et al., 2020).

Transfer Learning for Time Series Analysis

Gupta et al. (2020) used a RNN trained on patient phenotypes [2] to identify previously unseen phenotypes, but also for an unrelated task of in-hospital mortality. The idea was to train a RNN on physiological parameters to classify phenotypes. A phenotype could be the decrease in blood glucose levels. Detecting and classifying a phenotype closely resembles the task of anomaly detection.

To pretrain, Gupta et al. used time series data such as glucose level or heart rate. The goal was to determine, whether a phenotype was present. Since more than one phenotype can be present, the task can be considered as multi-label classification problem. The neural network used consisted of two layers of GRUs. The output layer was designed to represent all possible phenotypes, as activation function the sigmoid function was used. This network was trained on a labelled data set.

The pretrained neural network was then applied to two different target tasks. The target tasks were, hereby, slightly reduced in complexity. Instead of a multi-label classification, the problems were formulated as a binary classification problem, determining in case a), whether or not a phenotype was present and in case b) whether a patient would survive, based on the time series observations after Intensive Care Unit (ICU) admission.

On the target domain, training with different size data sets was done. The pretrained network was tuned on the target task with at lowest just five percent of data. As a benchmark, to compare the obtained results a logistic regression (LR) and a RNN classifier (RNN-C) were used. The two benchmarks, hereby, only operate on the target domain data set. The performances were compared using AUC (see section 2.5.1) for all used algorithms per data set (Case a & Case b).

As expected, the ROC curves of case a) showed that when the training set for the target task is small, the performance gains from transfer learning are greater. Interestingly, in case b) the benchmark RNN is able perform similarly as the two pretrained networks, indicating that better results are obtained the closer related source and target domain are.

2.5 Parameter Settings for fair comparison

In this section it is investigated how CNNs and RNNs can be compared fairly. Since the two's architectures fundamentally differ it is difficult to establish a baseline, where both networks are of similar complexity. In their work Braei and Wagner (2020) chose another approach. Instead of trying to build networks with similar complexity, they fine tuned each evaluated neural network to its full potential and compared their scores as well as their training and inference time. To compare the scores, Braei and Wagner introduced an anomaly threshold (similar as in section 2.2.2). To find out the optimal threshold, it is varied to optimize sensitivity (true positive rate) and specificity (true negative rate). Varying the threshold and drawing the false positives against the true positives results in the so called Receiver Operating Characteristics Curve (ROC-Curve), which is used to find the optimal threshold for a certain model. How the ROC-Curve is used to compare different models is explained in the next section.

2.5.1 ROC and AUC

The receiver operating characteristic curve, ROC-Curve, and the associated metric area under the curve (AUC), together also called AUROC, which is the area under the ROC-Curve, are two metrics that are frequently used to compare models. This metric is highly

[2] A clinical phenotype is the presentation of a disease in a given individual

useful, especially for detecting anomalies. The ROC-Curve depicts the relationship between the true positive rate and the false positive rate at various threshold values. The variables needed for the calculations are:

- TP: True Positives
- FN: False Negatives
- FP: False Positives
- TN: True Negatives

The true positive rate is defined as follows:

$$TPR = TP/(TP + FN)$$

The false positive rate is defines as:

$$FPR = FP/(FP + TN)$$

Typically, lowering the classification threshold, described in section 2.2.2, causes more items to be classified as positive, which increases both False Positives and True Positives. A typical ROC curve is depicted in figure 2.5.

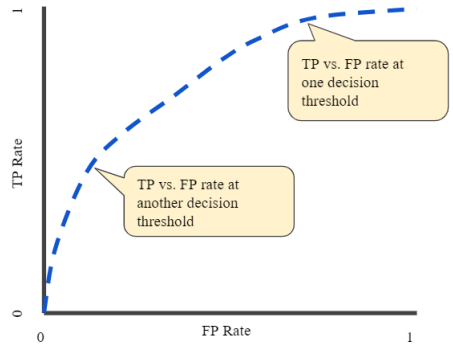

FIGURE 2.5: Example ROC-Curve (Google, 2020)

The area under the above shown curve, however, is classification-threshold-invariant. It measures the quality of the model's predictions irrespective of what classification threshold is chosen. The AUC in anomaly detection expressed the likelihood that the measured algorithm assigns a random anomalous point in the time-series a higher anomaly score than a random normal point. As a result, AUC is a good way to compare different anomaly detection methods (Braei and Wagner, 2020).

2.5.2 F-Score

Another approach to compare models is to use the F-Score. The F-Score describes a model's accuracy on a dataset. It is commonly used to assess binary classification systems, which categorize examples as "positive" or "negative" or in the case of anomaly detection into "anomalous" and "non-anomalous". The F-score is a method of combining the model's precision and recall, per definition it is the harmonic mean of the precision and recall of the model. Precision and recall are calculated as follows from the true and false positive respectively negatives.

$$Precision = TP/(FP + TP)$$

$$Recall = TP/(TP + FN)$$

From precision and recall the F-Score, and in this specific case the F1-Score can be calculated as follows.

$$F1 = 2 * (Precision * Recall)/(Precision + Recall)$$

When applying F-Score, a perfect model has an score of 1. Therefore, different models can also easily compared.

2.5.3 Computation Time

Another approach to compare the performances is to compare the computation times. To compare the computation times Braei and Wagner (2020) looked at the average training and inference time of traditional machine learning models as well as statistical models and neural networks on univariate time series. Generally, neural networks are expected to invest most of their computation time in training and are able to outperform the traditional machine learning on inference time. However, the practical results showed that Recurrent Neural Networks (LSTM & GRU) not only needed a long time to train but also had a large inference time on certain data sets. With LSTM performing second best on the given data set, behind k-means clustering, it can be concluded that this comes with a trade-off. On the same data set a CNN was trained. The CNN achieved an AUC-Value of 0.818, compared to 0,84 of the LSTM, which is not much worse than LSTM. Looking at the training and inference time, the CNN is far superior. The LSTM takes about 1000 seconds for training and also inference. The CNN, however, trains for 50 seconds, with an inference time of under one second, making the CNN the better choice, when relying on small inference times.

2.6 Research Gap

Anomaly detection on time series data has been widely researched. There are comprehensive comparisons of statistical methods, traditional machine learning approaches and neural networks such as the works of Braei and Wagner (2020) or Verner (2019). Braei and Wager, focus thereby only on univariate time series. Complementary, Verner only investigated multivariate time series. In their work, Braei and Wagner could show that CNN and RNN are able to achieve similar performances, while CNNs are superior in computation time. Verner faced a similar drawback in his research, where the training of the RNN took approximately 10 hours.

Since CNNs are only very recently investigated for anomaly detection in time series, Verner did not include them in his research. The approaches presented by Zheng et al. (2014) and Wen and Keyes (2019), however, show promising results, when using CNNs for time series classification respectively anomaly detection.

As research gap it has been identified that there is currently no research on how well CNNs perform when used in the field of anomaly detection. The works mentioned above do not establish a state of the art baseline, to compare the achieved results. It is therefore currently not assessable, how useful CNNs are for anomaly detection.

Further, since the use of neural networks steadily increases, it can be anticipated that transfer learning approaches that save training time, improve accuracy and are able to

deal with small data sets will become more popular. Both papers, that compare the different methods for anomaly detection do not take advantage of this approach.

Chapter 3

Research Methodology

3.1 Introduction

This section describes which research approach was chosen and why. Further, it elaborates, how the research approach is implemented and what work is done in the corresponding sections.

3.2 Research Design

As research methodology experimental research was chosen. Experimental research typically focuses on systematically testing a hypothesis. It is often applied to research fields such as physics and chemistry but also psychology. In the this research project, the hypothesis to test is formulated as the thesis statement (see section 1.4.

Experimental research knows five process steps. These are:

- Awareness of the Problem
- Design of Experiments
- Experiments
- Evaluation
- Conclusion

Following, it is outlined what will be done in the different process steps and how it is going to help answering the research question and test the thesis statement. Figure 3.1 hereby, graphically illustrates the different steps. The work performed within the framework of the Master Thesis Proposal relates to the part introduction.

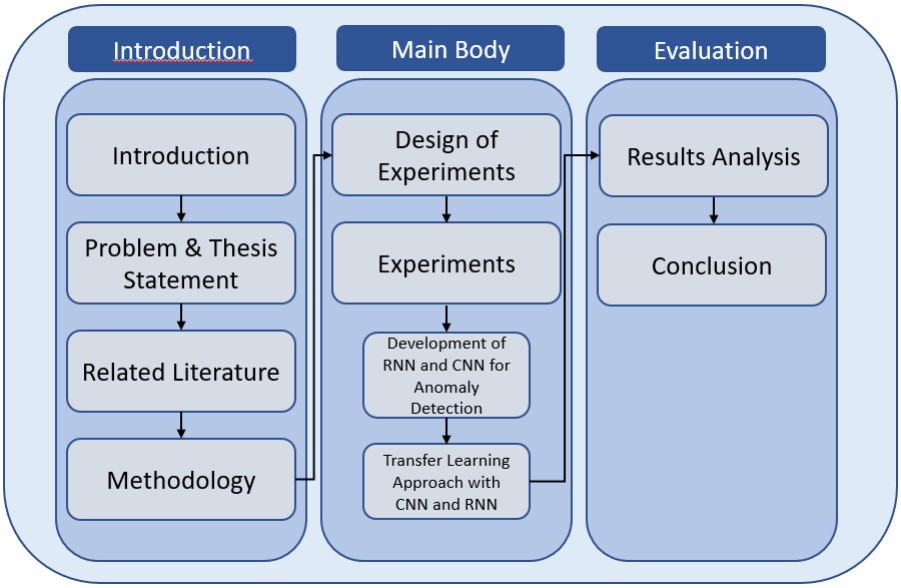

FIGURE 3.1: Thesis Map (**own**)

3.2.1 Awareness of the Problem - Literature Review

In this paper, the literature review consists of two parts, background information presented in section 1.2 and the part Related Literature presented as chapter 2. The reason for this split is to give insight on how neural networks and especially the derived architectures such as CNN and RNN work. A basic understanding of these two architecture is required to comprehend the problem and thesis statement presented in sections 1.3 and 1.4.

Further, the part Related Literature should deliver insights on how CNN and RNN are applied to detect anomalies. Where helpful, the papers investigated not only focus on detecting anomalies but also on related fields such as classification or prediction of time series. The investigated knowledge fields should serve as suggestions on how anomaly detection models can be set up. Next, the possibilities of transfer learning are examined. Since artificial intelligence experiences a boom in recent years, and neural networks are used more frequently, the possibilities offered by transfer learning will increase. Even more important, transfer learning is able to tackle one of the fundamental problems in anomaly detection. It enables to learn a performant model, even on a small data set.

At last, to be able to answer the research question it is investigated how the different architectures, RNN and CNN, can be compared and what measures are important.

3.2.2 Design of Experiments

In the section Design of Experiments, it is outlined how the experiments are designed. It is described how and why datasets are selected as well as which architecture principles are followed when designing the neural networks.

Data Selection

As described in section 2.1 Anomaly or Outlier, there are different kinds of anomalies, which are more or less difficult to detect. Section 2.4 Transfer Learning further shows that the relationship of the source domain and target domain data set is of significant importance for the quality of the results. These two facts indicate that the data sets used

for the experiments need to be carefully selected. In the Section Design of Experiments suitable data sets are proposed. At least, three different data sets are selected to conduct experiments. One of these data sets represents the source domain for transfer learning and another one the target domain. To learn the generic features necessary for transfer learning the data set used as source domain needs to consist of a large amount of data.

Further, the selected data sets have a direct impact on how the experiments have to be designed. Here the decision has to made, whether an unsupervised or supervised approach is applied. A supervised approach hereby requires a data set where the anomalies are labelled. In contrast, an unsupervised approach can investigate any time series data for anomalies but it is difficult to validate the achieved results.

Setup of Experiments

In the section Setup of Experiments the general setup of the experiments is elaborated. Part 2 Related Literature showed that there are various approaches on how to detect anomalies. Anomalies can either be directly classified by the neural network or detected via an anomaly threshold. This decision has to made based on the chosen data set, since only in a supervised approach a network can be designed to directly classify whether an anomaly is present. In the section Setup of Experiments a suitable method to answer the research questions is proposed. In addition, the advantages of the proposed setup, especially with an outlook on how the achieved results can be compared, are elucidated.

3.2.3 Experiments

Finally, in the section Experiments the proposed experimental setup is implemented. The experiments, hereby, focus on multivariate time series, since Braei and Wagner (2020) already issued a comprehensive study comparing different approaches for anomaly detection on univariate time series. Since transfer learning was not part of the referred study, the experiments on transfer learning can, however, also be done on univariate time series.

In the section Experiments, the design of the neural networks is described. It includes the determination of the basic architecture, which is specific to the proposed data set, further, it also includes a lot of tuning work to figure out the best parameters for each neural network. To test the performance of the neural networks, also a baseline classifier is established. The baseline classifier is of a very simple nature. Inspired by the trivial null classifier [1] the established baseline will figure as the benchmark to beat for the deep learning approaches.

3.2.4 Evaluation - Results Analysis

The section Results Analysis is dedicated to the examination of the previously achieved results. The results are compared using predefined metrics such as training time, inference time and F1-Score. Looking at these metrics helps to compare the neural network architectures and to determine whether CNN are actually superior to RNN when applied for anomaly detection. Comparing the neural networks to the baseline algorithm further gives some insight on how useful neural netoworks are in general for anomaly detection.

3.2.5 Conclusion

When comparing the neural networks on an anomaly detection task, it is expected that no architecture is overall superior. For example, the high accuracy of RNN comes with

[1] The trivial null classifier always predicts the majority class and thus represents the minimum precision every useful model should surpass.

the drawback of long training and inference times whereas a CNN with possibly lower accuracy outperforms the RNN escpecially on inference time. Thus, the decision which architecture to use depends on the use case. Therefore, as conclusion a set of recommendations, that shows what architecture is best suited for a certain use case, is compiled.

Chapter 4

Design of Experiments

In the Chapter Design of Experiments the datasets are selected, general design ideas are explained and established and at last the experiments and their goals are described.

4.1 Tools

The following Sections provide insight on what tools, such as software and hardware, is used to conduct the experiments.

4.1.1 Hardware

All experiments are conducted on a HP Probook equipped with a Intel Core i7 with 2.8GHz and 32GB of RAM installed. No additional graphics card was used.

4.1.2 Software

All necessary code is written in R (Version 4.1.0). To design the neural networks, the library Keras (Version 2.4.0) together with the Tensorflow (Version 2.5.0) backend is used.

4.2 Datasets

Following, it is motivated how and why the proposed data sets are used.

4.2.1 Problems of Existing Benchmarks

In order to find out, which Neural Network architecture is better suited for anomaly detection, first, suitable datasets have to be evaluated. Most of the papers on anomaly detection test on one of the popular benchmark datasets such as the ones created by Numenta, Yahoo, NASA, or Pei's Lab. These benchmark datasets are, however, declared as flawed by Wu and Keogh (**YEAR**). Wu and Keogh state that the benchmark datasets suffer from at least one of the following flaws:

1. **Triviality:** Surprisingly, a sizable proportion of the problems in the benchmark datasets are trivial to solve. Triviality is hereby defined as follows: An anomaly can be found with just one line of code.

2. **Unrealistic Density:** This flaw refers to too many anomalies in the dataset or at least in a certain region, whereas in a real world dataset the anomalous data points make up a portion of just above 0 percent.

3. **Mislabeled Ground Truth:** The data in all of the benchmark datasets appears to be mislabeled, with both false positives and false negatives. This is significant for a

number of reasons. The majority of anomaly detectors work by computing statistics for each subsequence of some length. They may, however, place their computed label at the beginning, end, or middle of the subsequence. If caution is not exercised, an algorithm may be penalized for reporting a positive just to the left or right of a labeled region.

4. **Run-to-failure Bias:** Because many real-world systems are run-to-failure, there is often no data to the right of the last anomaly. Therefore, a naïve algorithm that labels the last point as an anomaly has a very good chance of being correct.

In their work, Wu and Keogh, introduced the UCR Time Series Anomaly Datasets as new benchmark, that avoids the problems listed above. However, at the start of this research project the datasets were not publicly available. Because the search for a dataset, that does not suffer from the above mentioned flaws, would be too time-consuming, the decision was taken to partly engineer own datasets.

4.2.2 Anomalies

The neural networks should be used to detect various types of anomalies, in order to test their ability to recognize them. Foorthuis (**YEAR**) compiled, in an extensive literature review, a study on the different types of anomalies. The anomalies were divided into different categories, of which foremost the quantitative multivariate aggregate anomalies are relevant for this research project, especially a) to f) (see figure 4.1). These types of anomalies typically occur in time series data, that is composed by sensor data. Examples of such data could be temperature measurements or Electrocardiograms.

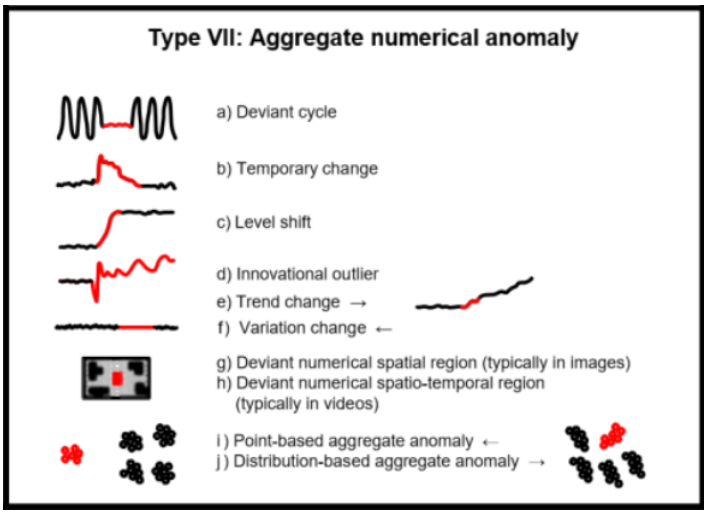

FIGURE 4.1: Quantitative Anomalies (**Foorthuis**)

4.2.3 Dataset Selection

In the following subsections, it is proposed how and why the datasets are selected for the different experiments.

1. Dataset

The dataset, which should be used for the first experiment will be of synthetic nature. It consists of various cyclic patterns. In a second step, the dataset is enriched with anomalies. This way, two dataset are produced. The dataset without anomalies is used for an unsupervised learning approach whereas the dataset with labelled anomalies is used for a supervised approach. Further information, on how the dataset is created, what it looks like and what the anomalies look like can be found in Section 5.1.1

2. Dataset

The second dataset, which is used for anomaly detection, should consist of real data. To make sure, that the requirements, mentioned in section 4.2.1 are met, the anomalies are embedded manually into the dataset.

3. Dataset

As third dataset, one of the existing benchmark datasets should be used. Despite their obvious flaws, it is still considered useful to validate the previously achieved results on an official benchmark. Further, this gives insights into the overall usefulness of the proposed neural network architectures.

4.2.4 Split of Dataset

With all datasets the classical train, validation and test dataset approach is chosen. For the supervised approach, the training data is enriched with anomalies, whereas for the unsupervised approach a "clean" dataset is used. The final evaluation is done on a test dataset, which is the same for all approaches.

4.3 Setup of Experiments

The following section explains how the different experiments are conducted in detail. When desinging the experiments, the focus is put on comparability rather than optimally tuned neural networks. Further, it is shown how the datasets and anomalies were engineered.

The following subsections give information on the chosen setups of the experiments that apply to all experiments, except where specifically stated otherwise.

4.3.1 Supervised Learning

The supervised learning approach refers to training the neural network on a labelled dataset. The dataset used for training already has the anomalies embedded. The task of finding the anomalies can also be described as a classification task, where the neural networks classifies a sequence as normal or anomalous. In such a case binary crossentropy and a sigmoid activation function are used as loss function and last layer activation fuction. The aforementioned combination means that in the last layer a logistic regression is done, where a threshold is determined to classify the sequences into normal and anomalous.

Supervised classification tasks are used and function well when sufficient samples of all classes are available. In anomaly detection, this is generally not the case, as the anomalous is per definition underrepresented. In the literature (e.g. (Wen and Keyes, 2019)), however, the supervised approach is still successfully used. There are two explanation for

this: First, as explained in Section 4.2.1, the density of anomalies is unrealistic and second, the anomalies are of the same kind and always look very similar, so a neural network is able to learn the pattern of the anomaly. In the experiments it is investigated, how the neural networks react when presented with anomalies that are similar to the ones in the training data, but also to previously unseen anomalies of the same kind (e.g. level shift). It is expected, that any neural network will fail when there are not enough similar anomalies in the training data.

4.3.2 Unsupervised Learning

The unsupervised learning approach refers to the training of a neural network on a dataset that is free of anomalies. The neural network merely learns the cyclic pattern of the data. When learning the pattern the loss function applied is Mean Absolute Error (MAE), so the learning task is a regression, which itself is supervised. The actual anomaly detection hereby is done in a second step. As proposed in section 2.2.2, the anomaly detector module, which is also used in this experiment, calculates the Euclidean distance between predicted and actual value, where a large value corresponds to an anomaly.

A unsupervised approach is the more reliable choice when trying to detect anomalies, because the model does not need to know what anomalies might look like. However, setting up this approach is more time consuming, especially when dealing with multivariate time series, as for every variable, a separate detector module and corresponding threshold needs to be set up. It is yet to be expected, that both neural network architectures, CNN and RNN, will outperform their supervised counterparts.

4.3.3 Neural Networks

The following Sections describe principles that will be generally used in the design of the neural networks.

Activation Function

When designing the neural networks, as activation function generally "ReLu" (Rectified Linear Unit) is used. The function is non-linear and basically just returns the input if it is bigger than 0 and otherwise 0. This function is widely used, because of its simplicity and generally yields good results with little computation expenses.

Optimizer

As optimizer, the often used default choice in machine learning, ADAM (Adaptive Moment Estimation), with the proposed default values, is applied (**AUTHOR**; **YEAR**). ADAM updates the learning rate when training, making it faster than other optimizers such a Gradient Descent. On the downside, however, ADAM uses a lot memory for a given batch size and is found to generalize poorly in late stages of training.

4.3.4 Experiments

In the following, it is suggested how the experiments on the 3 different datasets are conducted.

1. Experiment

In a first experiment the learning abilities of RNN and CNN are compared. It is investigated how useful the architectures are in a supervised and in an unsupervised setup.

This experiment gives general insight on which setups and approaches work under which conditions. As the anomalies embedded are similar in the training and test set, the supervised approaches should yield good results, whereas the unsupervised approaches, given the simplicity of the dataset, are not expected to miss any anomalies.

2. Experiment

The second experiment is conducted on a more challenging dataset. Also the embedded anomalies are of a more challenging nature. All approaches that have been found successful in Experiment 1, are investigated further on the new dataset. Since the dataset consists of more, partially dependent, variables, and more challanging cyclic patterns the architectures used in Experiment 1 have to be extended for example by adding additional layers.

4.3.5 Results

As results three metrics are reported. First and most important, is the F1-Score which gives insight on the models ability to recognize anomalies. Second and third, the training and inference time are reported.

Chapter 5

Experiments

5.1 Experiment 1

The first experiment was conducted on a fully synthetic dataset. Supervised and unsupervised learning approaches were used to detect the anomalies.

5.1.1 Dataset

The dataset, that was created for this first task consisted of five variables. The dataset was created under the assumption, that one measurement was drawn per hour on totally 2000 days, resulting in 48000 datapoints. The variables all follow a cyclic pattern shown in figure 5.1 but are not dependent on each other.

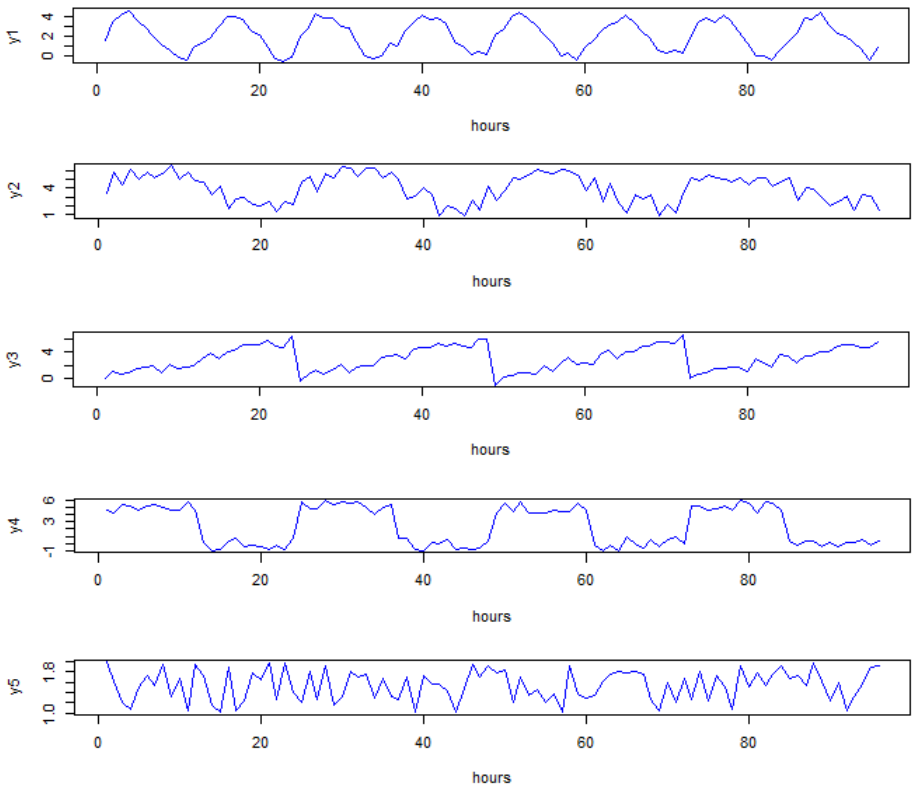

FIGURE 5.1: Synthetic Dataset (**own**)

In a second step the dataset was enriched with six different kinds of anomalies. The anomalies embedded into the dataset are of type deviant cycle, temporary change and level shift. Figure 5.2 shows examples of the embedded anomalies. The same kind of anomalies were embedded into the training and the test dataset.

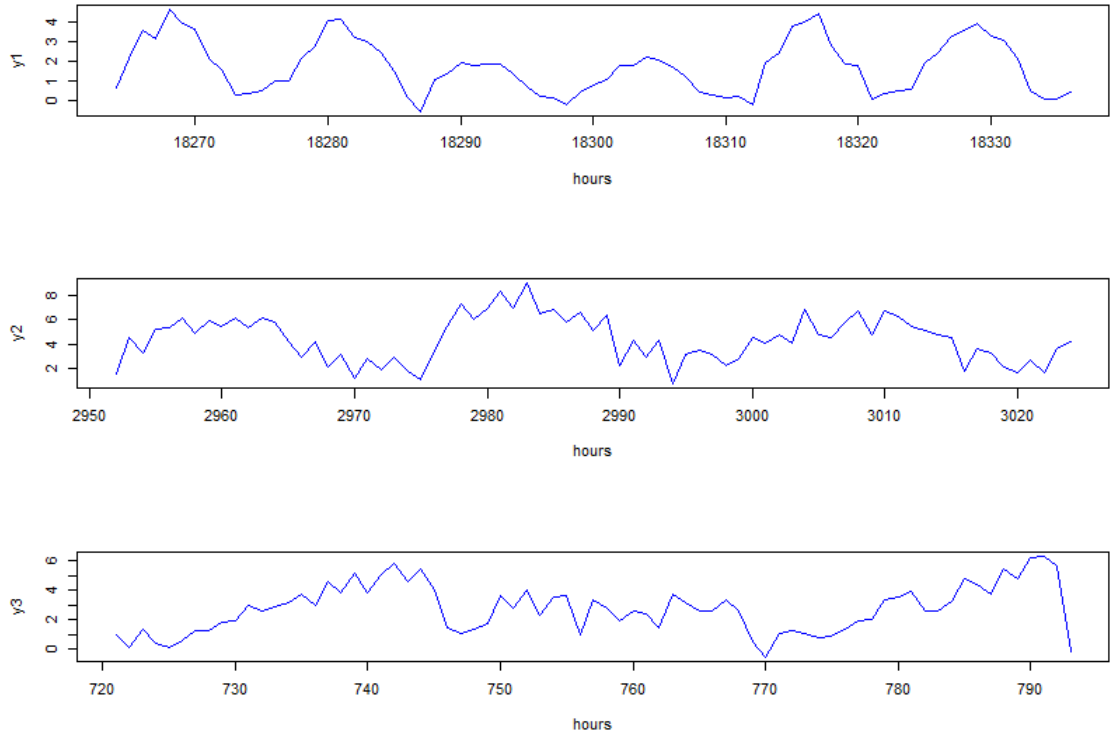

FIGURE 5.2: Synthetic Anomalies (**own**)

For the supervised learning approach the dataset was also labelled. In each case the whole day was marked as an anomaly. In total 30 anomalous days were embedded into the dataset, this corresponds to 1.5 percent of anomalous datapoints.

5.1.2 Neural Networks

In the first experiment, a CNN was tested against a RNN in a supervised and also in an unsupervised fashion. As RNN, the type GRU was chosen. As some first attempts showed, that it showed sufficient results with improved computation time compared to the more complex LSTM.

For the supervised learning approach, the chosen architecture can be seen in table 5.1. The architecture with two hidden layers, first presented in Section 2.2, served as example for the RNN. Supplementary, the CNN was built to match the number of layers used for the RNN, where each convolutional layer was followed by a max-pooling layer (explained in Section 1.2.1.

The architecture used for the unsupervised learning approach, displayed in table 5.2, looked very similar to the architecture of the supervised approach. The main difference between the two architectures was that the CNN was not built as a sequential model, because the used software does not support such an architecture. Instead of having one output layer, the CNN had to be designed with five parallel output layers, each predicting

TABLE 5.1: Supervised Learning

	Input	NN-Architecture	Output
CNN	120 past datapoints	2 1D-Convolutional Layers 2 Max-Pooling Layers 1 Dense Layer	1 Dense Layer with Sigmoid Activation
RNN	120 past datapoints	2 GRU Layers 1 Dense Layer	1 Dense Layer with Sigmoid Activation

one time series [1]. In comparison, the RNN has just one output layer with 5 neurons, each used to predict a time series.

TABLE 5.2: Unupervised Learning

	Input	NN-Architecture	Output
CNN	120 past datapoints	2 1D-Convolutional Layers 2 Max-Pooling Layers	5 Dense Layers with 1 regression outputs
RNN	120 past datapoints	2 GRU Layers	1 Dense Layers with 5 regression outputs

Learning

The learning on the data was done using a so called generator function, which iterates over the dataset in predefined steps. The generator function takes the following parameters:

- Lookback - How many data points are considered
- Step - How the data is sampled
- Delay - How many time steps in the future is the target
- Batch Size - The number of samples per batch

For this experiment, the parameter lookback was set to 120 data points in the past, which represent the last 5 days. The parameters step and delay were set to one and as batch size 128 was chosen. This setup can be described as follows: There are 128 ordered samples taken from the the whole dataset. Each of these samples consist of 120 data point of past data. With the step parameter set to one, there is not further subsampling done. With delay set to one, the task for the neural network is to predict the next data point in the future per sample for each variable in the data set. This task is done simultaneously for all samples of batch, which speeds up training.

[1] More detailed summaries of the models can be found in appendix A

5.1.3 Results

Inference time and F1-Score are, for all models, calculated on the same test dataset. As the initial dataset, it consists of 48000 datapoints, with 30 anomalous days embedded. For the supervised approach using a RNN, no F1-Score is reported, as the model, just like the trivial null classifier, always predicted no anomaly. Since the anomalies span over a whole day, for all approaches, the results were averaged per day. Resulting in normal or anomalous days. The reported F1-Score was finally calculated on this data.

TABLE 5.3: Results

	F1-Score	**Training Time**	**Inference Time**
CNN Supervised	0.991388	169s	422s
RNN Supervised	-	967s	952s
CNN Unsupervised	0.9989817	129s	435s
RNN Unsupervised	0.9979613	300s	793s

From the table 5.3, it can be seen that the supervised learning approach takes longer to train. This can be explained by the fact that a CNN must first learn the patterns and only then begins to recognise the anomalies. Further, it shows that despite promising results when training, the trivial null classifier achieves a higher F1-Score than the supervised CNN approach. The best score was achieved with a CNN applied in an unsupervised fashion. The CNN reported just one false negative and a false positive, compared to one false negative and two false positives of the RNN.

5.2 Experiment 2

In a second experiment, a real dataset was used as base. The anomalies were embedded manually. Since, the unsupervised approach with RNN in Experiment 1 proved useless it was not included in the second experiment. Since the anomalies in training and test set were looked very similar in Experiment 1, the supervised approach with the CNN was able to recognize some of the anomalies. In the second approach, it should be investigated if this is approach could be of any use, if the anomalies consist of a hitherto unknown pattern.

5.2.1 Dataset

The dataset used was derived from the "Appliances Energy Prediction Dataset" available on the UCI Machine Learning Repository. The dataset consists of 9 room temperatures (T1 to T9) and corresponding humidity levels, energy in use of ligth and appliances, two random variables for testing regression models as well as six variables containing weather information. The dataset consists of 19735 datapoints, where 6 datapoints are drawn per hour. Of the available variables only 10 variables were used for the anomaly detection task. The variables used are 5 room temperatures, energy use, outside temperature, air pressure and wind speed. The variables were selected because they show a dependency. For example, a high outside temperature and energy use result in high temperatures in the different rooms. Figure 5.3 provides an insight on the used dataset.

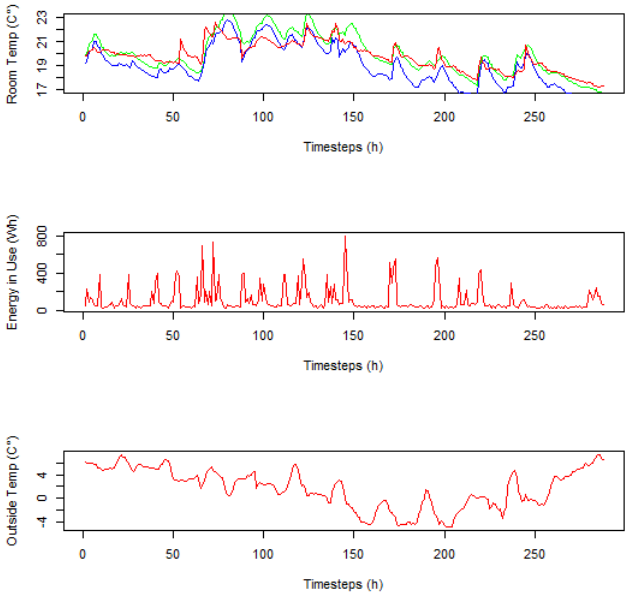

FIGURE 5.3: Appliances Energy Prediction Dataset (**Own or UCI???**)

Sampling

The data set contains datapoints measured between November and May. During this time period, it is observed, that the base temperature steadily rises. This poses the problem, that if the model is trained on data from November to March, with April as validation and May as test period, it is biased on the prevailing colder temperatures. To overcome this

problem a special sampling technique was applied. In total six samples of the data set were created. A sample was created by randomly drawing one data point per hour over all datapoints. Four of these sample are then used for training, one for validation and one for testing. Using this sampling technique, the model is no longer biased on certain weather conditions but with the drawback, that the test set is not independent of the test and validation set.

Anomalies

Again, the anomalies were embedded manually into the dataset. The anomalies are of type level shift, deviant cycles, variaton change and distribution-based aggregate anomaly. The anomalies were embedded into the room temperature variables (T1, T2, and T3) and the energy use variable. Figure 5.4 shows examples of the mentioned anomalies.

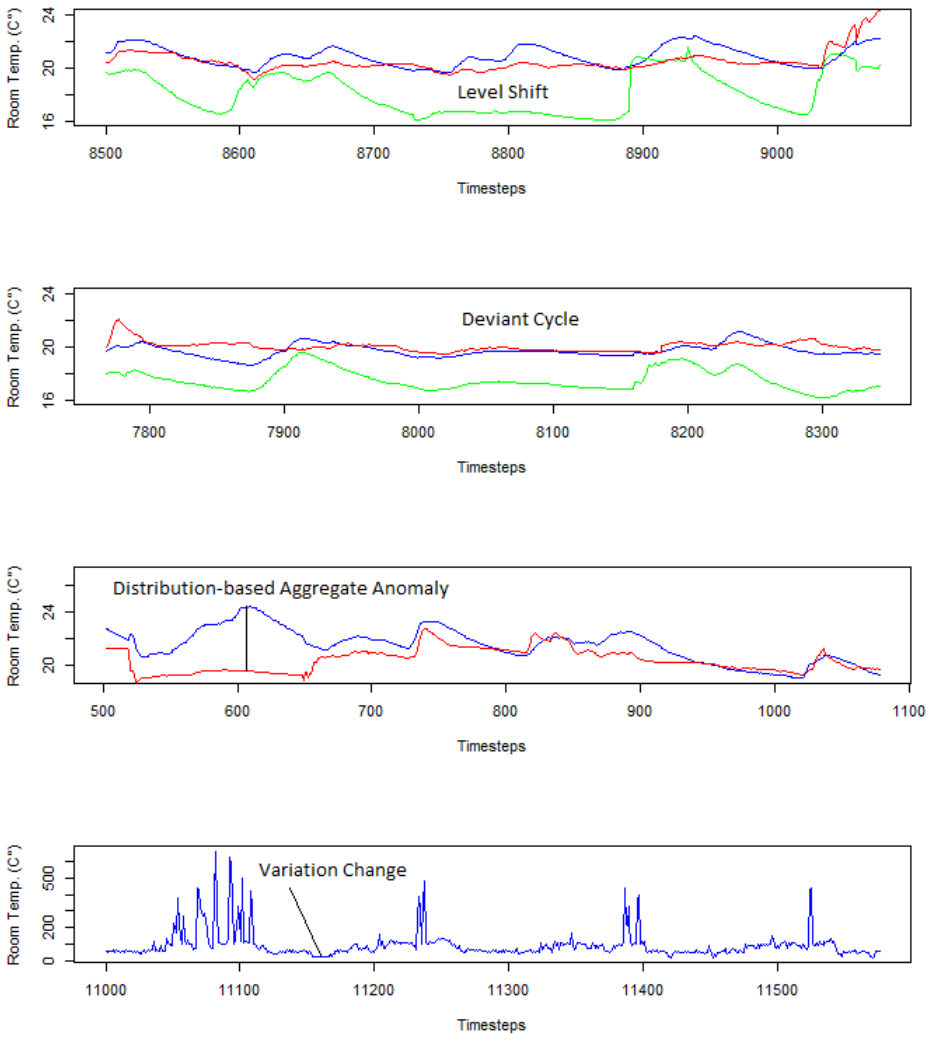

FIGURE 5.4: Examples of Embedded Anomalies (**Own**)

Since the test dataset only consists of around 3000 data points. It was used 3 times so that it does not have an unusual high density of anomalies. In the first instance, anomalies that only affected one variable were embedded. In the second instance, anomalies, that affected all 3 temperature variables, such as a deviant cycle, were embedded. On

top, in the energy use variable, variation change anomalies were embedded. In the third instance, distribution based anomalies, which affected T1 and T2, were embedded.

5.2.2 Neural Networks

Since the RNN did not show sufficient results in Experiment 1 when given a classification task, it was excluded from Experiment 2. The CNN, however, which had probably learned the patterns of the anomalies, was tested again. Since the anomalies in the training and test set are not as similar anymore as in Experiment 1, it is expected that the CNN classifier performs very poorly.

TABLE 5.4: Unupervised Learning

	Input	**NN-Architecture**	**Output**
CNN	288 past datapoints	3 1D-Convolutional Layers 1 Max-Pooling Layers	4 Dense Layers with 1 regression outputs
RNN	288 past datapoints	3 LSTM Layers	1 Dense Layers with 4 regression outputs

Because of the complexity of the dataset, in the second experiment it was decided to use LSTM units instead of GRU in the RNN architecture. LSTM units generally provide more accurate results but use more memory and therefore more computation time. The designed neural network architecture consisted of 3 sequential layers of LSTM layers and one dense layer with four neurons.

The CNN was designed as follows, three layers of one-dimensional convolutional layers were used. After the first layer, a max-pooling layer was added, to reduce the feature space and improve computation time. Since the CNN is expected to predict a time series, the feature space was not further reduced through max-pooling layers, since it would negatively affect the accuracy.

Learning

The generator function for this experiment was configured as follows:

- Lookback - 288 past data points: 12 days in the past
- Step - 1: no further subsampling is done
- Delay - 1: the next time step in the future is predicted
- Batch Size - 128 samples per batch

First experiments were done only using data from T1, T2, T3, energy use and outside temperature to predict T1 to T3 and energy use. However as the result were not satisfactory to predict accurate enough results to find the embedded anomalies, further variables were added for training. Finally, the following variables were used to make predictions: T1 to T5, Appliances and Ligths, Outside Temperature, Air Pressure and Windspeed. As the anomlies, however, were only embedded into 4 out of the 10 variables, only the affected 4 were predicted.

5.2.3 Results

Because the dataset was much more challenging, the reported scores are clearly inferior to Experiment 1. In total there were 13 anomalies to be detected in the test sets. The difference in F1-Score between the CNN and the RNN results from one anomaly which was not recognized by the CNN. However, training the RNN takes over 30 times longer than the CNN.

TABLE 5.5: Results

	F1-Score	**Training Time**	**Inference Time**
CNN Unsupervised	0.666666	172s	24s*
RNN Unsupervised	0.727272	5420s	93s*

* the inference time reported is on just one instance of the test dataset

The above reported results show the overall performance. Since the dataset was more complex than in the first experiment, the results are investigated further to show how the different architecture performed on the various anomalies and how accurate the predictions were on the different variables. First of all, the average error of the predicted variables are investigated further. The below results are reported from the first test set.

TABLE 5.6: Results

	CNN	**RNN**
T1	0.2712066° C	0.1741582° C
T2	0.5236905° C	0.9009765° C
T3	0.3210329° C	0.7244096° C
Appliances	29.64146 Wh	72.91079 Wh

From Table 5.6, it can be seen that the CNN outperforms the RNN on all variables except T1. The RNN, however, performs exceptionally well on T1. Comparing these results to the performance of the different architectures on the first test set

5.3 Experiment 3

Dataset

The first three variables are the sensors of RT level , RT temperature and HT temperature. The last two variables correspond to gasoil source on/off and heater on/off control signals.

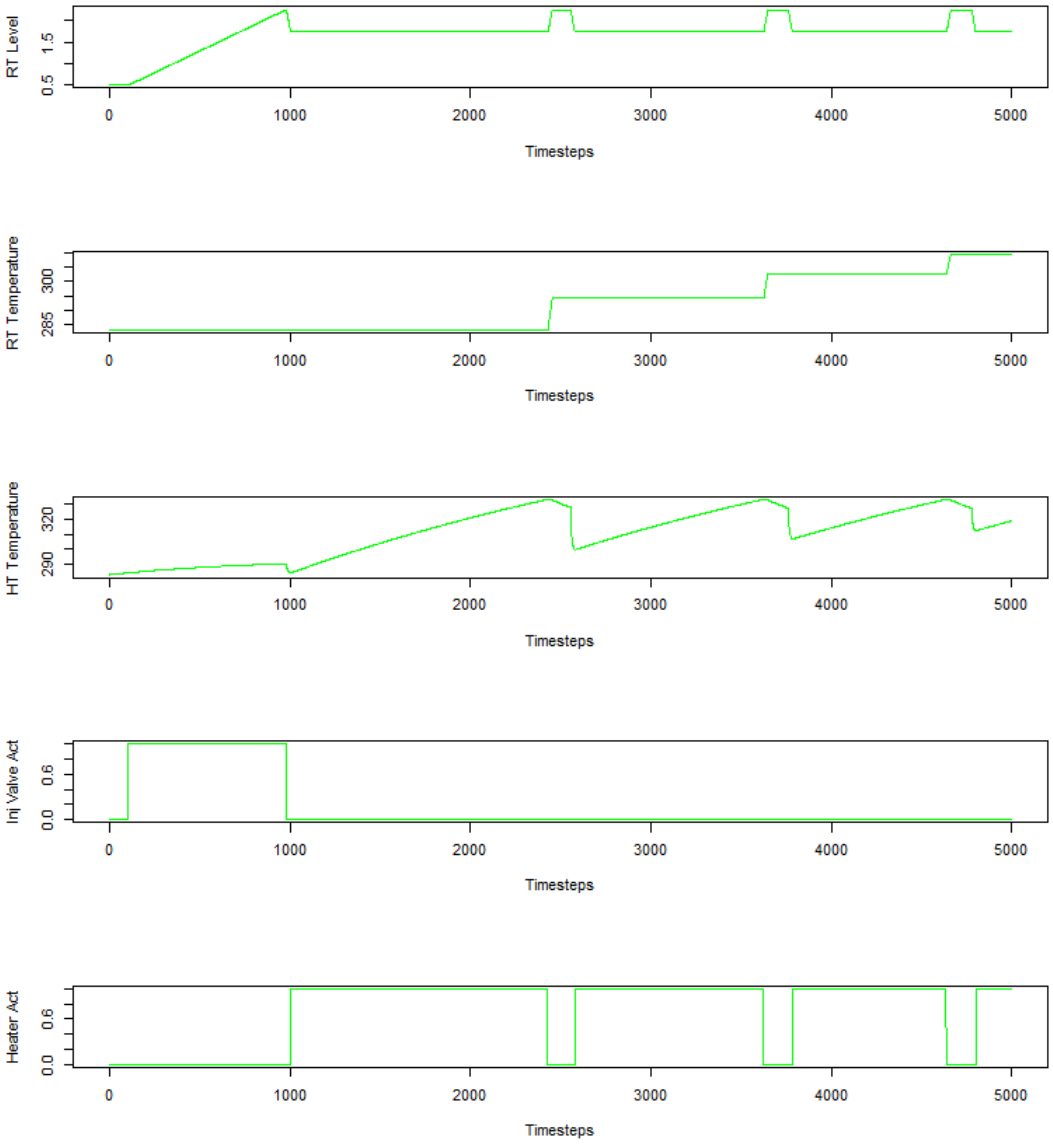

FIGURE 5.5: Examples of Embedded Anomalies (**Own**)

Appendix A

Model Summaries

A.1 Summary of Models of Experiment 1

A.1.1 Supervised Learning

```
## Model: "sequential_9"
##
_________________________________________________________________________
## Layer (type)                 Output Shape              Param
#
##
=========================================================================
## conv1d_23 (Conv1D)           (None, 118, 32)           512
##
_________________________________________________________________________
## max_pooling1d_23 (MaxPooling1D)  (None, 59, 32)        0
##
_________________________________________________________________________
## conv1d_22 (Conv1D)           (None, 59, 32)            3104
##
_________________________________________________________________________
## max_pooling1d_22 (MaxPooling1D)  (None, 29, 32)        0
##
_________________________________________________________________________
## flatten_11 (Flatten)         (None, 928)               0
##
_________________________________________________________________________
## dense_25 (Dense)             (None, 16)                14864
##
_________________________________________________________________________
## dense_24 (Dense)             (None, 1)                 17
##
=========================================================================
## Total params: 18,497
## Trainable params: 18,497
## Non-trainable params: 0
##
_________________________________________________________________________
```

FIGURE A.1: Summary of CNN (**own**)

```
## Model: "sequential_13"
##
_________________________________________________________________________________
## Layer (type)                 Output Shape              Param
#
##
=================================================================================
## gru_7 (GRU)                  (None, 120, 32)           3648
##
_________________________________________________________________________________
## gru_6 (GRU)                  (None, 120, 32)           6240
##
_________________________________________________________________________________
## dense_33 (Dense)             (None, 120, 16)           528
##
_________________________________________________________________________________
## dense_32 (Dense)             (None, 120, 1)            17
##
=================================================================================
## Total params: 10,433
## Trainable params: 10,433
## Non-trainable params: 0
##
_________________________________________________________________________________
```

FIGURE A.2: Summary of GRU (**own**)

A.1.2 Unsupervised Learning

A.2 Summary of Models of Experiment 2

A.2.1 Supervised Learning

A.2.2 Unsupervised Learning

```
## Model: "model_3"
_________________________________________________________________________________
## Layer (type)              Output Shape      Param #  Connected to
##
=================================================================================
===
## input_4 (InputLayer)      [(None, 120, 5)]  0
##
_________________________________________________________________________________
## conv1d_7 (Conv1D)         (None, 118, 32)   512      input_4[0][0]
##
_________________________________________________________________________________
## max_pooling1d_7 (MaxPooli (None, 59, 32)    0        conv1d_7[0][0]
##
_________________________________________________________________________________
## conv1d_6 (Conv1D)         (None, 59, 32)    3104     max_pooling1d_7[0][0]
##
_________________________________________________________________________________
## max_pooling1d_6 (MaxPooli (None, 29, 32)    0        conv1d_6[0][0]
##
_________________________________________________________________________________
## flatten_3 (Flatten)       (None, 928)       0        max_pooling1d_6[0][0]
##
_________________________________________________________________________________
## dense_13 (Dense)          (None, 1)         929      flatten_3[0][0]
##
_________________________________________________________________________________
## dense_14 (Dense)          (None, 1)         929      flatten_3[0][0]
##
_________________________________________________________________________________
## dense_15 (Dense)          (None, 1)         929      flatten_3[0][0]
##
_________________________________________________________________________________
## dense_16 (Dense)          (None, 1)         929      flatten_3[0][0]
##
_________________________________________________________________________________
## dense_17 (Dense)          (None, 1)         929      flatten_3[0][0]
##
=================================================================================
===
## Total params: 8,261
## Trainable params: 8,261
## Non-trainable params: 0
##
_________________________________________________________________________________
```

FIGURE A.3: Summary of CNN (**own**)

```
## Model: "sequential_1"
##
_________________________________________________________________________
## Layer (type)                 Output Shape              Param
#
##
=========================================================================
## gru_3 (GRU)                  (None, None, 32)          3648
##
_________________________________________________________________________
## gru_2 (GRU)                  (None, 32)                6240
##
_________________________________________________________________________
## dense_6 (Dense)              (None, 5)                 165
##
=========================================================================
## Total params: 10,053
## Trainable params: 10,053
## Non-trainable params: 0
##
_________________________________________________________________________
```

FIGURE A.4: Summary of GRU (**own**)

```
## Model: "model_5"
## _________________________________________________________________________________________
## Layer (type)                 Output Shape              Param #   Connected to
## =========================================================================================
## input_11 (InputLayer)        [(None, 288, 11)] 0
## _________________________________________________________________________________________
## conv1d_47 (Conv1D)           (None, 286, 48)   1632      input_11[0][0]
## _________________________________________________________________________________________
## max_pooling1d_34 (MaxPool (None, 143, 48)   0         conv1d_47[0][0]
## _________________________________________________________________________________________
## conv1d_46 (Conv1D)           (None, 143, 32)   4640    max_pooling1d_34[0][0]
## _________________________________________________________________________________________
## conv1d_45 (Conv1D)           (None, 143, 16)   1552      conv1d_46[0][0]
## _________________________________________________________________________________________
## flatten_13 (Flatten)         (None, 2288)      0         conv1d_45[0][0]
## _________________________________________________________________________________________
## dense_24 (Dense)             (None, 1)         2289      flatten_13[0][0]
## _________________________________________________________________________________________
## dense_25 (Dense)             (None, 1)         2289      flatten_13[0][0]
## _________________________________________________________________________________________
## dense_26 (Dense)             (None, 1)         2289      flatten_13[0][0]
## _________________________________________________________________________________________
## dense_27 (Dense)             (None, 1)         2289      flatten_13[0][0]
## =========================================================================================
## Total params: 16,980
## Trainable params: 16,980
## Non-trainable params: 0
## _________________________________________________________________________________________
```

FIGURE A.5: Summary of CNN (**own**)

```
## Model: "sequential"
##
_________________________________________________________________________________
## Layer (type)                        Output Shape                    Param
#
##
=================================================================================
## lstm_2 (LSTM)                       (None, None, 64)                19456
##
_________________________________________________________________________________
## lstm_1 (LSTM)                       (None, None, 32)                12416
##
_________________________________________________________________________________
## lstm (LSTM)                         (None, 16)                      3136
##
_________________________________________________________________________________
## dense (Dense)                       (None, 4)                       68
##
=================================================================================
## Total params: 35,076
## Trainable params: 35,076
## Non-trainable params: 0
##
_________________________________________________________________________________
```

FIGURE A.6: Summary of GRU (**own**)

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