

Kevin Sekuj

CS-225: Discrete Structures in CS

Homework 2, Part 2

Exercise Set 5.1, Problem #15, #16, #57, #60

Canvas Summation Problems

#15.

$$a_n = (-1)^{(n-1)} \cdot \frac{(n-1)}{n} \text{ where } n \geq 1$$

#16.

$$a_n = 3 \cdot 2^{n-1} \text{ where } n \geq 1$$

#57.

$$\sum_{j=0}^{n-2} \frac{j+1}{(n-j-1)^2}$$

#60.

$$\sum_{k=1}^n (16k^2 + 3)$$

----Continued on pg2----

Canvas Summation Problems

#1.

$$\sum_{i=200}^{500} (3i - \frac{7}{2}) =>$$

$$\sum_{i=200}^{500} 3i - \sum_{i=200}^{500} \frac{7}{2} =>$$

$$3(\sum_{i=200}^{500} 1) - \frac{7}{2}(\sum_{i=200}^{500} 1) =>$$

$$3(\sum_{i=1}^{500} i - \sum_{i=1}^{199} i) - \frac{7}{2}(\sum_{i=1}^{500} 1 - \sum_{i=1}^{199} 1) =>$$

$$3\left(\frac{500(500+1)}{2} - \frac{19(19+1)}{2}\right) - \frac{7}{2}(500 - 199)$$

#2.

$$\sum_{j=0}^{20} (3j^2 - (-2)^j) =>$$

$$\sum_{j=0}^{20} 3j^2 - \sum_{j=0}^{20} (-2)^j =>$$

$$3\sum_{j=0}^{20} j^2 - \sum_{j=0}^{20} (-2)^j =>$$

$$3\left(\frac{(20(20+1)) \cdot ((2)(20+1))}{6}\right) - \left(\frac{(-2)^{20+1} - 1}{(-2) - 1}\right)$$

#3.

$$\sum_{j=45}^{70} (4^j - 2^j) =>$$

$$\sum_{j=45}^{70} 4^j - \sum_{j=45}^{70} 2^j =>$$

$$\left(\frac{(4^{70+1}) - (4^{45})}{4 - 1}\right) - \left(\frac{(2^{70+1}) - (2^{45})}{2 - 1}\right)$$