1 Lesson 10 Example 2

Two fair, six-sided dice are rolled.

- \bullet Let S be the sum of the two numbers. Calculate and graph the p.m.f. of S
- Let D be the absolute difference between the two numbers. (That is, D is always a positive number). Calculate and graph the p.m.f. of D.

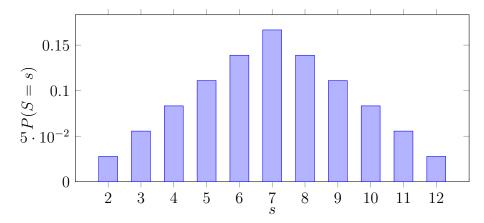
2 Answer

2.1 Part A

The p.m.f. of S, the sum of the numbers rolled on two dice, is as follows:

S	Number of Outcomes	P(S=s)
$\frac{2}{3}$	1	$\frac{1}{36} \approx 0.0278$
3	2	$\frac{2}{36} = \frac{1}{18} \approx 0.0556$
4	3	$\begin{array}{c} \frac{2}{36} = \frac{1}{18} \approx 0.0556\\ \frac{3}{36} = \frac{1}{12} \approx 0.0833\\ \frac{4}{36} = \frac{1}{9} \approx 0.1111 \end{array}$
5	4	$\frac{3}{36} = \frac{1}{9} \approx 0.1111$
6	5	$\frac{5}{36} \approx 0.1389$
7	6	$\frac{\frac{6}{36} = \frac{1}{6} \approx 0.1667}{\frac{5}{36} \approx 0.1389}$
8	5	$\frac{5}{36} \approx 0.1389$
9	4	$\frac{4}{36} \stackrel{36}{=} \frac{1}{9} \approx 0.1111$
10	3	$\begin{array}{c} \frac{4}{36} = \frac{1}{9} \approx 0.1111\\ \frac{3}{36} = \frac{1}{12} \approx 0.0833\\ \frac{2}{36} = \frac{1}{18} \approx 0.0556 \end{array}$
11	2	$\begin{vmatrix} \frac{3}{36} = \frac{1}{12} \approx 0.0833 \\ \frac{2}{36} = \frac{1}{18} \approx 0.0556 \\ \frac{1}{2} \approx 0.0278 \end{vmatrix}$
12	1	$\frac{1}{36} \approx 0.0278$

Graph of the p.m.f. of S



2.2 Part B

To find P(D=d) for each possible value of D, we count the number of outcomes for each d:

- $P(D=0) = \frac{6}{36} = \frac{1}{6} \approx 0.1667$ Outcomes: (1,1), (2,2), (3,3), (4,4), (5,5), (6,6)
- $P(D=1) = \frac{10}{36} \approx 0.2778$ Outcomes: (1,2), (2,1), (2,3), (3,2), (3,4), (4,3), (4,5), (5,4), (5,6), (6,5)
- $P(D=2) = \frac{8}{36} \approx 0.2222$ Outcomes: (1,3), (3,1), (2,4), (4,2), (3,5), (5,3), (4,6), (6,4)
- $P(D=3) = \frac{6}{36} = \frac{1}{6} \approx 0.1667$ Outcomes: (1,4), (4,1), (2,5), (5,2), (3,6), (6,3)
- $P(D=4) = \frac{4}{36} = \frac{1}{9} \approx 0.1111$ Outcomes: (1,5), (5,1), (2,6), (6,2)
- $P(D=5) = \frac{2}{36} = \frac{1}{18} \approx 0.0556$ Outcomes: (1,6), (6,1)

The p.m.f. of D, the absolute difference between the numbers rolled on two dice, is as follows:

D	Number of Outcomes	P(D=d)
0	6	$\frac{6}{36} = \frac{1}{6} \approx 0.1667$
1	10	$\frac{10}{36} \approx 0.2778$ $\frac{8}{36} \approx 0.2222$
2	8	$\frac{8}{36} \approx 0.2222$
3	6	$\frac{6}{36} = \frac{1}{6} \approx 0.1667$
4	4	$ \frac{1}{36} - \frac{1}{6} \sim 0.1111$
5	2	$\begin{vmatrix} \frac{3}{36} = \frac{1}{9} \approx 0.1111 \\ \frac{2}{36} = \frac{1}{18} \approx 0.0556 \end{vmatrix}$

Graph of the p.m.f. of D

