

Top 6,4, .97

1. Education gain .1245 vs .1245 for Career and .0202 for Experience

1. 1. High School 4,1, Entropy = .722

1. Experience Gain: .322 > Career Gain of 0.171

1. Less than 3: 1,0 Entropy = 0, all low

2. 3 to 10: 2,0 Entropy = 0, all low

3. More than 10, 1,1 Entropy = 1

1. Mgmt 0,1 Entropy = 0, all high

2. Service 1,0 Entropy = 0, all low

2. College 2,3 Entropy = .971

1. Career Gain: .4202 > Experience Gain of .171

1. Mgmt 0,2 Entropy = 0, all high

2. Service 2,1 Entropy = 0.918

Experience Gain .918

Less than 3: 1,0 Entropy = 0, all low

3. 3 to 10: 0,1 Entropy = 0, all high

More than 10, 1,0 Entropy = 0, all low

Step 2: Prune the Tree Using Validation Set

Following Above Tree for Each Instance

Instance 1:

High School → More than 10 → Management → High, Matches Instance's High Salary

Do not prune the High school tree bc there are no validation errors.

Instance 2:

College → Mgmt → High: Does not match Instance's low salary

2 training obs are correct and this 1 testing obs is wrong, keep as is.

Instance 3:

College → Service → 3 to 10 → High, Does not match Instance's low salary

Prune this so that all College → Service are predicted as Low salary.

Doesn't make sense to predict College → service as high just because of this instance.

Final Pruned Tree and # Correct Using all 13 Instances (Training and Test)

1. HS

2. Experience less than 10 years → Low

Correct: 3

Errors: 0

2. Experience More than 10 Years

3. Management → High

Correct: 2

Errors: 0

3. Service → Low

Correct: 1

Errors: 0

1. College

2. Management → High

Correct: 2

Errors: 1

2. Service → Low

Correct: 3

Errors: 1

## 2. PROGRAM KNN in Python, Code Attached

### ReadMe

I was unable to get an arff reader to work on either my mac or at the CS dept computers. Therefore I uploaded the data as a csv and hardcoded the np arrays after reading them in.

To calculate EucDist between two points, use:

EucDist(a,b,length) where length specifies how many numerical variables there are to calculate distance, assuming all non-numeric variables exist after the numbers.

eg for a= [ 6.5, 3. , 5.8, 2.2], and b = [ 5.1, 3.3, 1.7, 0.5]

EucDist(a,b,4)

To find the K-NN of a point, enter in the training set, the test observation, and k to test using:  
NearestNeighbors(train, testobs, k)

To Predict the class of an item using the test observation and the list of Nearest neighbors use:  
PredictClass(test,neighbors)

To retrieve the results for this assignment enter either:

results

or

addColsk(test,train)

To perform the same analysis on a different dataset, enter in the training array 'train' and the testing array test into addColsk(test,train). Or for a single obs:

enter

newobs = np.array([[ 6.7, 3.1, 4.4, 1.4]])

and then test using the same training set:

addColsk(newobs, train)

returning: array([[6.7, '3.1', '4.4', '1.4', 'x0', 'versicolor', 'versicolor',  
'versicolor', 'versicolor', 'versicolor']],  
dtype='|S32')

## 3. WEKA

### 10 Fold CV SMO Classification Results

Run 1: PolyKernel with exponent option 1 129	# Correctly Classified:	717	# Incorrect:
Run 2: PolyKernel with exponent option 2 36	# Correctly Classified:	810	# Incorrect:
Run 3: PolyKernel with exponent option 4 55	# Correctly Classified:	781	# Incorrect:
Run 4: RBFKernel with Gamma set to 0.01 232	# Correctly Classified:	614	# Incorrect:
Run 5: RBFKernel with Gamma set to 1.0 82	# Correctly Classified:	764	# Incorrect:

The RBFKernel with Gamma equal to 1 and the PolyKernel with exponent equal to 1 did not work well. The PolyKernel works better with higher exponents because it allows a higher degree function to map the

data rather than restricting the data to a linear function with exponent 1. You can see that the fourth degree option did not outperform option 2 because it likely overfit the training data with such a high degree function relative to the second option. The RBFKernel gamma parameter defines how far the influence of a single observation reaches. This Kernel worked better with gamma set to 1 rather than .01 because .01 allows a training example's influence to reach farther which does not work well in this classification setting.

#### 4. Kernels

$$K(x,z) = x_1 * z_1 + x_1 * e^{z_2} + z_1 * e^{x_2} + e^{(x_2+z_2)}.$$

Is  $K(x,z)$  an inner product of some  $\Phi(x)$ ? Yes:

$$\Phi(x) = \Phi(x_1, x_2) = [x_1, e^{x_2}]$$

$$\Phi(z) = \Phi(z_1, z_2) = [z_1, e^{z_2}]$$

$$K(x,z) = [x_1, e^{x_2}]' * [z_1, e^{z_2}] = x_1 * z_1 + x_1 * e^{z_2} + z_1 * e^{x_2} + e^{(x_2+z_2)}.$$

It is possible to prove  $K$  is a kernel by showing  $K$  is symmetric and the matrix is positive semi-definite for  $x_1, \dots, x_N$ .

If  $x = (-1, 1)$  and  $z = (1, -1)$

$$K(x,z) = 2.35, k(-x,-z) = 2.35$$

SYMMETRIC,  $K(u) = K(-u)$  for all  $u$ .

Satisfies Mercer's condition.

#### 5. Dual Form SVM

1.

$$w = [2.7, -2, -1.8]$$

$$y_i(w^T x_i + b) = 1$$

Using first row:  $y_i(w^T x_i + b) = 0.9 + b = 1$ , so  **$b = 0.1$**

For alpha 2

$$\text{Sign}(w^T x_i + b) = (2.7 * 1 - 2 * .8 - 1.8 * 1) + 0.1 = \text{sign}(-0.6) = -1$$

**So new observation is predicted to be a -1.**