

CSCE 221 Cover Page
Homework Assignment #3
Due November 30 to CSNet

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Please list all sources in the table below including web pages which you used to solve or implement the current homework. If you fail to cite sources you can get a lower number of points or even zero, read more Aggie Honor System Office <http://aggiehonor.tamu.edu/>

| | | | |
|-------------------------|--|--|--|
| Type of sources | | | |
| People | | | |
| Web pages (provide URL) | | | |
| Printed material | | | |
| Other Sources | | | |

I certify that I have listed all the sources that I used to develop the solutions/codes to the submitted work.

“On my honor as an Aggie, I have neither given nor received any unauthorized help on this academic work.”

Your Name **Kevin Chou**

Date **11/30/15**

Homework 3

due November 30

1. (10 points) R-10.17 p. 493

For the following statements about red-black trees, provide a justification for each true statement and a counterexample for each false one.

(a) A subtree of a red-black tree is itself a red-black tree.

False, if a subtree is rooted at a node that is red, then it does not follow the rule that a red black tree must have a black root.

(b) The sibling of an external node is either external or it is red.

False, if its sibling node is black and has 2 red node children, then it is not a external node.

(c) There is a unique (2,4) tree associated with a given red-black tree.

False, there are different red black trees that can be represented in the same (2,4) tree.

(d) There is a unique red-black tree associated with a given (2,4) tree.

True, there

2. (10 points) R-10.19 p. 493

Consider a tree T storing 100,000 entries. What is the worst-case height of T in the following cases?

(a) T is an AVL tree.

$1.44\log 100,000$

(b) T is a (2,4) tree.

$\log 100,000$

(c) T is a red-black tree.

$2\log 100,000$

(d) T is a binary search tree.

100,000

3. (10 points) R-9.16 p. 418

Draw an example skip list that results from performing the following series of operations on the skip list shown in Figure 9.12: `erase(38)`, `insert(48,x)`, `insert(24,y)`, `erase(55)`. Record your coin flips, as well.

4. (10 points) R-9.7 p. 417

Draw the 11-entry hash table that results from using the has function, $h(k) = (3k + 5) \bmod 11$, to hash the keys 12, 44, 13, 88, 23, 94, 11, 39, 20, 16, and 5, assuming collisions are handled by chaining.

5. (10 points) R-9.8 p. 417

What is the result of the previous exercise, assuming collisions are handled by linear probing?

6. (10 points) R-9.10 p. 417

What is the result of Exercise R-9.7, when collisions are handled by double hashing using the secondary hash function $h_s(k) = 7 - (k \bmod 7)$?

7. (10 points) R-8.2 p. 361

How long would it take to remove $\lceil \log n \rceil$ smallest elements from a heap that contains n entries using the `removeMin()` operation?

8. (10 points) R-8.7 p. 361

An airport is developing a computer simulation of air-traffic control that handles events such as landings and takeoffs. Each event has a *time-stamp* that denotes the time when the event occurs. The simulation program needs to efficiently perform the following two fundamental operations:

- Insert an event with a given time-stamp (that is, add a future event)
- Extract the event with smallest time-stamp (that is, determine the next event to process)

Which data structure should be used for the above operations? Why?

9. (10 points) R-13-3 and R-13-4, p. 654

10. (10 points) R-13.8, p. 655

11. (10 points) R-13.16, p. 656

12. (10 points) R-13.17, p. 656

13. (10 points) You want to help CS/CSE freshman students to prepare their course schedules for the first two years in the lower level division. By building a directed graph suggest order in which they should schedule their courses taking into account their corresponding prerequisites. A set of vertices represents courses and a set of edges represents a dependence of a given course on a course prerequisite.

14. (10 points) R-13.31, p. 656

15. (10 points) Write what the running time, and provide its justification, of the Dijkstra's algorithm is for a sparse and dense graph and the priority queue implemented based on

- (a) a binary heap
- (b) an unsorted list
- (c) a sorted list

16. (10 points) C-13.10, p. 658

17. (10 points) C-13.15, p. 659

18. (10 points) C-13.18, p. 659