Homework 3

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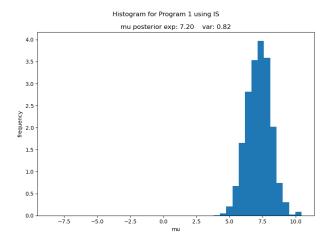
October 27, 2021

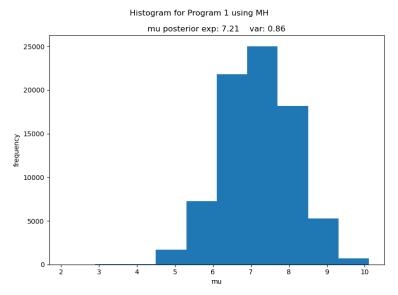
Link to repo:

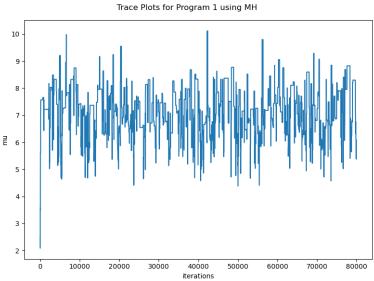
https://github.com/keviny2/CPSC532W-Assignments/tree/main/FOPPL/HW

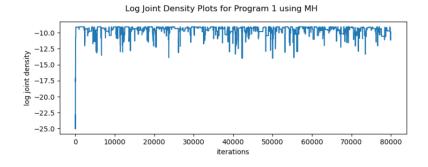
1 Program 1

1.1 Wall-Clock Time

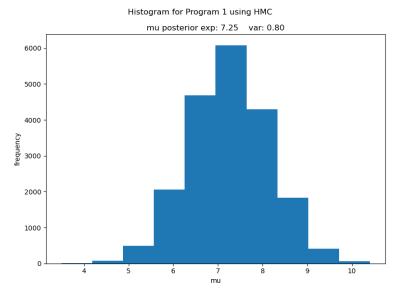




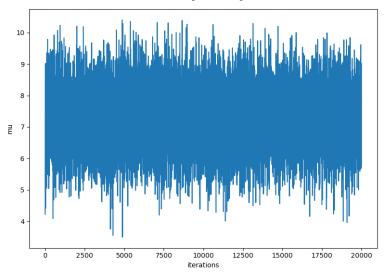




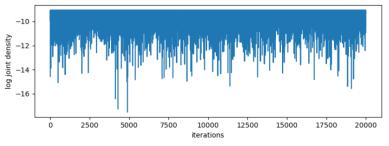
1.4 HMC



Trace Plots for Program 1 using HMC



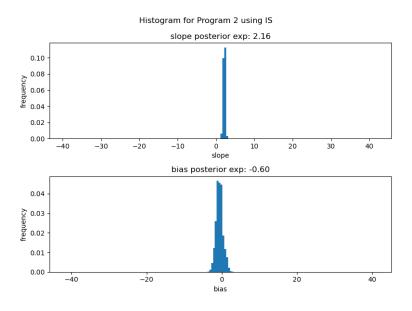
Log Joint Density Plots for Program 1 using HMC

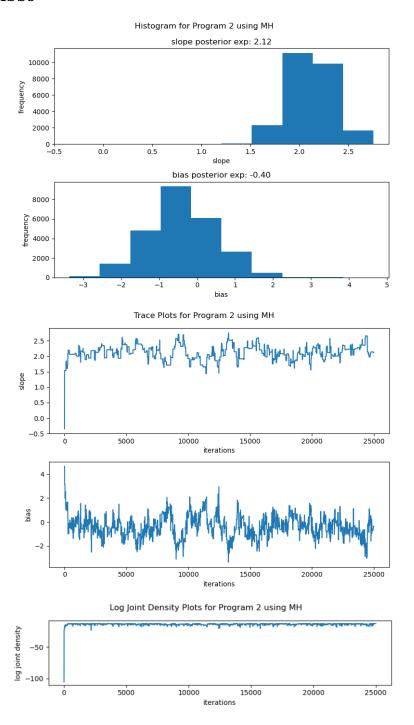


2 Program 2

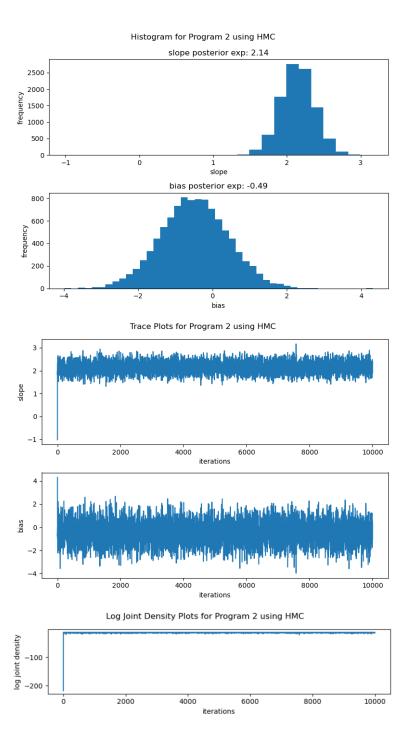
2.1 Wall-Clock Time

```
======= Likelihood Weighting =======
Took 345.71 seconds to finish Program 2
Posterior Expectation slope: tensor(2.1622)
posterior covariance of slope and bias:
[[ 0.05525479 -0.19291554]
[-0.19291554 0.85292497]]
Posterior Expectation bias: tensor(-0.5960)
====== Metropolis within Gibbs =======
Took 231.19 seconds to finish Program 2
Posterior Expectation slope: tensor(2.1177)
posterior covariance of slope and bias:
 [[ 0.04993265 -0.17395253]
[-0.17395253 0.78755741]]
Posterior Expectation bias: tensor(-0.3951)
first attempt
====== Hamiltonian Monte Carlo =======
Took 420.389123916626 seconds to finish Program 2
Posterior Expectation slope: tensor(2.1442)
posterior covariance of slope and bias:
 [[ 0.0529382 -0.19120865]
 [-0.19120865 0.82222667]]
Posterior Expectation bias: tensor(-0.4859)
```



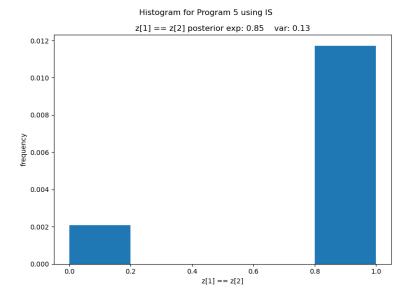


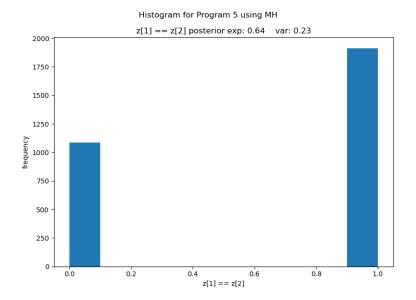
2.4 HMC



3 Program 3

3.1 Wall-Clock Time

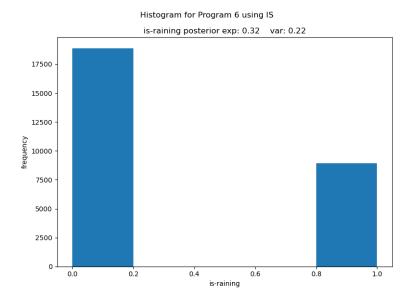


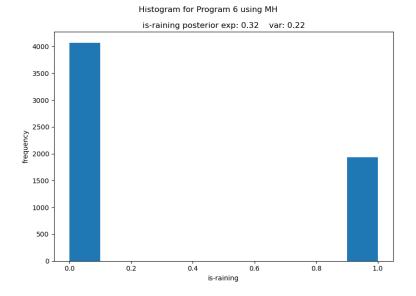


4 Program 4

4.1 Wall-Clock Time

4.2 IS

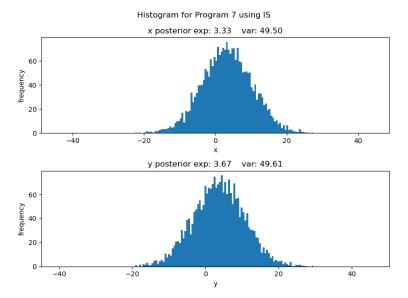


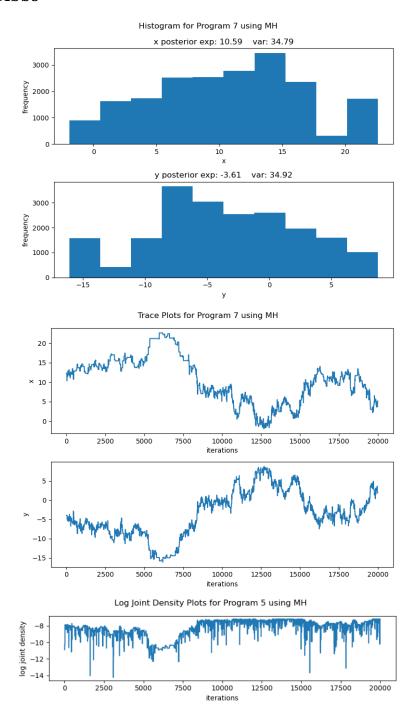


5 Program 5

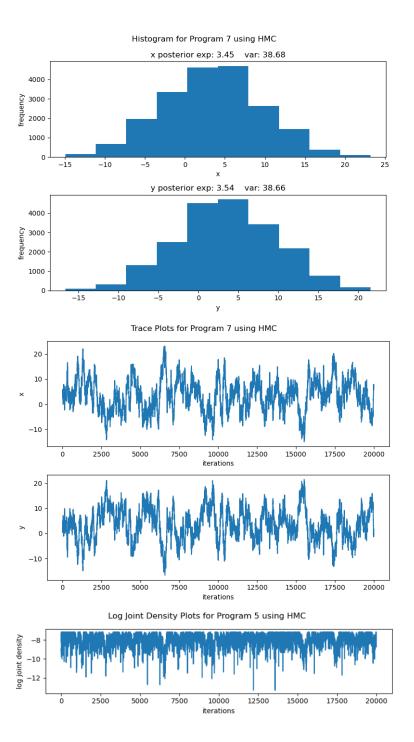
5.1 Wall-Clock Time

```
======= Likelihood Weighting =======
Took 71.46 seconds to finish Program 7
Posterior Expectation x: tensor(3.3320)
Posterior Variance x: tensor(49.5026)
Posterior Expectation y: tensor(3.6669)
Posterior Variance y: tensor(49.6122)
====== Metropolis within Gibbs =======
Took 61.62 seconds to finish Program 7
Posterior Expectation x: tensor(10.5921)
Posterior Variance x: tensor(34.7903)
Posterior Expectation y: tensor(-3.6118)
Posterior Variance y: tensor(34.9180)
first attempt
====== Hamiltonian Monte Carlo =======
second attempt
====== Hamiltonian Monte Carlo =======
third attempt
====== Hamiltonian Monte Carlo =======
fourth attempt
====== Hamiltonian Monte Carlo =======
fifth attempt
======= Hamiltonian Monte Carlo =======
Took 279.50547552108765 seconds to finish Program 7
Posterior Expectation x: tensor(3.4514)
Posterior Variance x: tensor(38.6782)
Posterior Expectation y: tensor(3.5359)
Posterior Variance y: tensor(38.6634)
```





5.4 HMC



6 Code Snippets

```
sample(self, num_samples, num)
        samples = []
for i in range(num_samples):
    r_i, sig_i = evaluate_program(ast, sig, 'IS')
    logw_i = copy.deepcopy(sig['togw'])
    samples.append([r_i, logw_i])
    sig['togw'] = 0
def gibbs_step(self, graph):
        # both transition kernels are the same because we're just sampling from the prior
d_old = deterministic_eval(substitute_sampled_vertices(self.Q[latent_var], graph[]['Y']))
d_new = deterministic_eval(substitute_sampled_vertices(self.Q[latent_var], graph_propose[]['Y']))
        # create variables for the old and new parameter values
old_value = graph[1]['Y'][latent_var]
new_value = graph_propose[1]['Y'][latent_var]
        # compute the ratio of the joint likelihoods variable_bindings = graph[i]['Y'] variable_bindings_propose = graph_propose[i]['Y']
```

```
raw_expression = graph_propose[1]['P'][v]
expression = substitute_sampled_vertices(raw_expression, variable_bindings_propose)
log_alpha += deterministic_eval(expression)
         \label{local_raw_expression} raw_expression = graph[1][ `P'][v] \\ expression = substitute_sampled_vertices(raw_expression, variable_bindings) \\ log_alpha -= deterministic_eval(expression) \\
# likelihood under new model
raw_expression = ['observe*', graph_propose[1]['P'][latent_var][1], graph_propose[1]['Y'][latent_var]]
expression = substitute_sampled_vertices(raw_expression, variable_bindings_propose)
log_alpha += deterministic_eval(expression)
# likelihood under old model
raw_expression = ['observe*', graph[i]['P'][latent_var][1], graph[i]['Y'][latent_var]]
expression = substitute_sampled_vertices(raw_expression, variable_bindings)
log_alpha -= deterministic_eval(expression)
graph_old = copy.deepcopy(graph)
X_old = copy.deepcopy(X)
```

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