Homework 4

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Link to repo:

https://github.com/keviny2/CPSC532W-Assignments/tree/main/FOPPL

Program 0

BBVI implementation:

```
for l in range(L):
    # reset sig['logW'] at each iteration
    sig['logW'] = 0
    sig['6'] = {}

# r_tl is the return value of the expression (won't have a value for each parameter)
    r_tl, sig_tl = evaluate_program(ast, sig, self.method)

    @_tl = clone(sig_tl['6'])

# cause all of a sudden we want to keep track of sigma now too in hw4...
    if nom == 1:
        r_tl = torch.FloatTensor([r_tl, next(iter(sig['Q'].values())).scale.clone().detach()])

# add to return list
    samples.append([r_tl, sig_tl['logW'].clone().detach()])

# add to list for self.elbo_gradient and self.optimizer_step functions
    @_t.append(e.tl)
    sig['logW_list'].append(sig_tl['logW'].clone().detach())

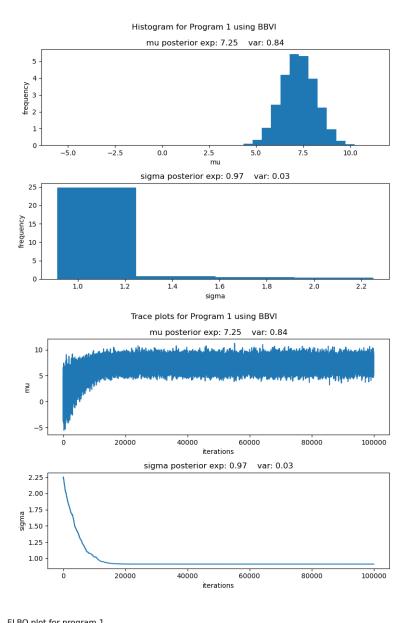
g_hat = self.elbo_gradients(G_t, sig['logW_list'])
    bbvi_loss.append(torch.mean(torch.tensor(sig['logW_list']))) # make a copy of the ELBO

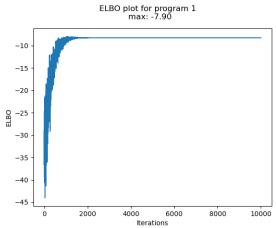
sig['Q'] = self.optimizer_step(sig, g_hat)

print('Variational distribution: {}'.format(sig['Q']))

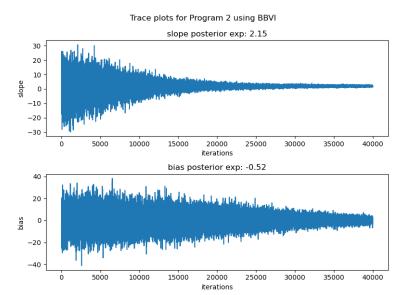
return samples, bbvi_loss
```

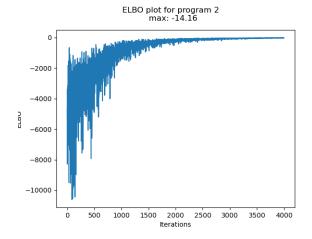
```
def <u>elbo_gradients</u>(self, <u>G</u>, <u>logW</u>):
              # tensors for computing b_hat afterwards
F_one_to_L_v = torch.empty(0)
G_one_to_L_v = torch.empty(0)
                for <u>l</u> in range(L):
              F_one_to_L_v = torch.reshape(F_one_to_L_v, (L, num_params))
G_one_to_L_v = torch.reshape(G_one_to_L_v, (L, num_params))
               parameters = sig['Q'][v].Parameters()
for idx, param in enumerate(parameters):
    if len(param) > 1:
```



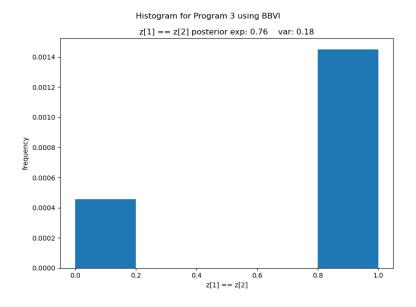


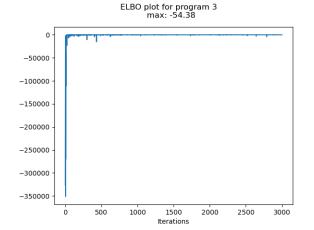
Took 298.65 seconds to finish Program 1
Posterior Expectation mu: tensor(7.2508)
Posterior Variance mu: tensor(0.8383)
Posterior Expectation sigma: tensor(0.9665)
Posterior Variance sigma: tensor(0.0347)





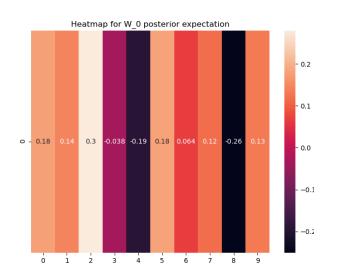
Took 289.66 seconds to finish Program 2
Posterior Expectation slope: tensor(2.1495)
posterior covariance of slope and bias:
[[0.05515892 -0.19639921]
[-0.19639921 0.86761098]]
Posterior Expectation bias: tensor(-0.5225)

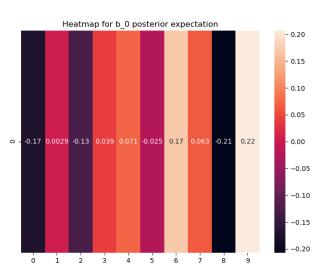


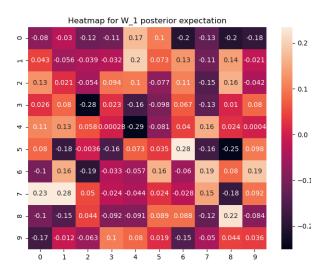


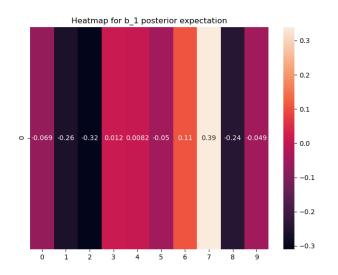
Took 3497.33 seconds to finish Program 3
Posterior Expectation z[1] == z[2]: tensor(0.7606)
Posterior Variance z[1] == z[2]: tensor(0.1821)

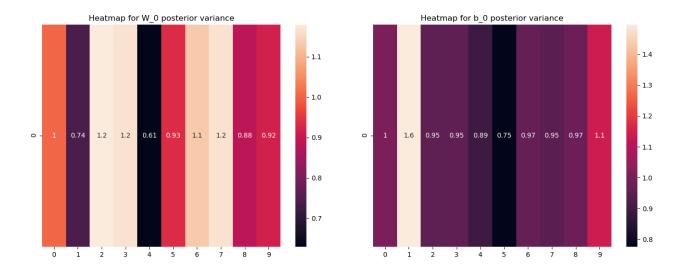
The mode-seeking behavior of VI on models with internal symmetries will find itself climbing different modes in the posterior for independent runs. These internal symmetries render the model unidentifiable, because the model density is invariant under some classes of transformations of the latent parameter (Moore, 2016). This reduces the efficiency of inference procedures. The label switching problem is a well known problem in mixture models, as the latent variables representing class labels are unidentifiable in the sense that the model density does not change if you swap the labels of two classes - hence, *unidentifiable*.

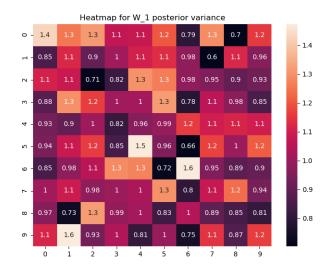


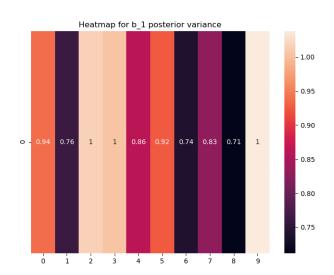


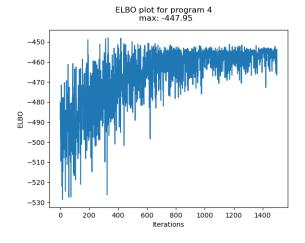










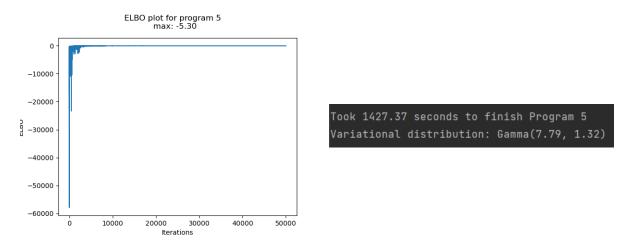


Took 2750.63 seconds to finish Program 4

Black-box variational inference (BBVI) is more generic compared to parameter estimation via gradient descent. In BBVI, we compute an estimate of the gradient of the evidence lower bound (ELBO) using a sampling procedure instead of obtaining the gradient of the ELBO analytically. This renders BBVI applicable to a range of complicated models that parameter estimation via gradient descent will not be able to handle.

Program 5

The variational distribution is a Gamma(7.79, 1.32)



References

Moore, D. A. (2016) *Symmetrized Variational Inference*. NIPS Workshop on Advances in Approximate Inference.