

## Worksheet 3

Due 10/20

1. During the October 13th lecture, I wrote down many statements equivalent to “ $S$  is a linearly independent set”. Do the same for “ $S$  is a spanning set”. The answer is in the notes but see what you can do from memory.
2. Let  $T : \mathbb{R}^2 \rightarrow \mathbb{R}^3$  be a linear transformation. We know that there exists a matrix  $A$  such that  $T(x) = Ax$ .
  - Suppose we know that  $T(1, 0) = (2, 3, 4)$  and  $T(0, 1) = (-1, 2, 1)$ . Can we determine  $A$ ? If so, what is it? If not, why not?
  - Suppose instead we know that  $T(1, 0) = (2, 3, 4)$  and  $T(2, 0) = (4, 6, 8)$ . Can we determine  $A$ ? If so, what is it? If not, why not?
  - Suppose instead we know that  $T(1, 0) = (2, 3, 4)$  and  $T(1, 1) = (-1, 2, 1)$ . Can we determine  $A$ ? If so, what is it? If not, why not?
  - Suppose instead we know that  $T(x) = u$  and  $T(y) = v$ . Under what conditions on  $x$  and  $y$ , can we determine  $A$ ?
3. Come up with a linear transform that is:
  - One-to-one and onto
  - One-to-one but not onto
  - Onto but not one-to-one
  - Not one-to-one nor onto
4. Is differentiation a linear transformation? The answer is yes. I just want you to think about why this is true.
5. Do a full exam from the exam archive here under test like conditions.