Lab 3

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1.

1a. The two explanatory variables I would remove from the model are INDUS and AGE. Based on p-values alone, it is clear that these are the only two variables that are insignificant in the full model. They have extremely high p-values, as opposed to the other predictors which have very low p-values.

```
reg.picked <- lm(MEDV~CRIM + ZN + CHAS + NOX + RM + DIS + RAD + TAX + PTRATIO + B + LSTAT, data=boston)
summary(reg.picked)
```

```
##
## Call:
##
  lm(formula = MEDV ~ CRIM + ZN + CHAS + NOX + RM + DIS + RAD +
       TAX + PTRATIO + B + LSTAT, data = boston)
##
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
##
  -15.5984 -2.7386
                     -0.5046
                                 1.7273
                                         26.2373
##
##
  Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                            5.067492
                                        7.171 2.73e-12 ***
## (Intercept)
                36.341145
## CRIM
                -0.108413
                             0.032779
                                       -3.307 0.001010 **
## ZN
                 0.045845
                            0.013523
                                        3.390 0.000754 ***
## CHAS
                 2.718716
                            0.854240
                                        3.183 0.001551 **
## NOX
                            3.535243
                                       -4.915 1.21e-06 ***
               -17.376023
## RM
                 3.801579
                             0.406316
                                        9.356 < 2e-16 ***
                                       -8.037 6.84e-15 ***
## DIS
                -1.492711
                            0.185731
                 0.299608
                            0.063402
                                        4.726 3.00e-06 ***
## RAD
## TAX
                -0.011778
                            0.003372
                                       -3.493 0.000521 ***
## PTRATIO
                -0.946525
                             0.129066
                                       -7.334 9.24e-13 ***
                 0.009291
                            0.002674
                                        3.475 0.000557 ***
## B
## LSTAT
                -0.522553
                             0.047424 -11.019 < 2e-16 ***
## ---
                  0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 4.736 on 494 degrees of freedom
## Multiple R-squared: 0.7406, Adjusted R-squared: 0.7348
## F-statistic: 128.2 on 11 and 494 DF, p-value: < 2.2e-16
```

1b. The model improves slightly, with the adjusted r² value improving marginally. However, the F-statistic increases significantly, meaning the model has a better explanatory power.

anova(reg)

```
## Analysis of Variance Table

##

## Response: MEDV

## CRIM

1 6440.8 6440.8 286.0300 < 2.2e-16 ***

## ZN

1 3554.3 3554.3 157.8452 < 2.2e-16 ***
```

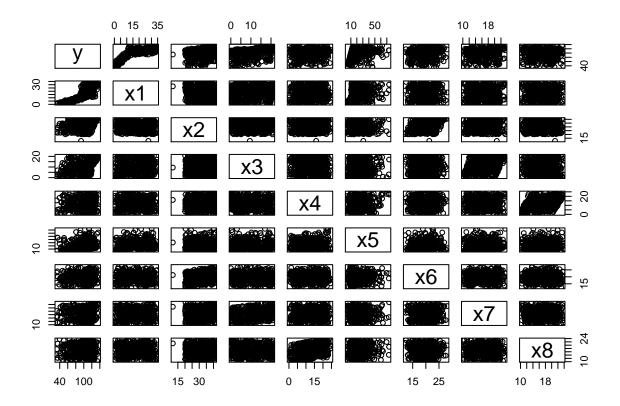
```
## INDUS
               1 2551.2 2551.2 113.2984 < 2.2e-16 ***
                  1529.8 1529.8 67.9393 1.543e-15 ***
## CHAS
               1
## NOX
                    76.2
                            76.2
                                   3.3861 0.0663505 .
               1 10938.1 10938.1 485.7530 < 2.2e-16 ***
## RM
## AGE
               1
                    90.3
                            90.3
                                   4.0087 0.0458137 *
## DIS
                 1779.5
                         1779.5 79.0262 < 2.2e-16 ***
               1
## RAD
               1
                    34.1
                            34.1
                                   1.5159 0.2188325
## TAX
               1
                   329.6
                           329.6 14.6352 0.0001472 ***
## PTRATIO
                  1309.3 1309.3 58.1454 1.266e-13 ***
               1
## B
               1
                   593.3
                           593.3 26.3496 4.109e-07 ***
## LSTAT
               1
                  2410.8
                         2410.8 107.0634 < 2.2e-16 ***
## Residuals 492 11078.8
                            22.5
## ---
                  0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
## Signif. codes:
anova (reg.picked)
## Analysis of Variance Table
##
## Response: MEDV
                  Sum Sq Mean Sq F value
##
                                             Pr(>F)
## CRIM
               1
                  6440.8 6440.8 287.1259 < 2.2e-16 ***
## ZN
               1
                  3554.3
                          3554.3 158.4500 < 2.2e-16 ***
               1 1233.8 1233.8 55.0016 5.282e-13 ***
## CHAS
## NOX
               1 1592.4 1592.4 70.9878 3.947e-16 ***
## RM
               1 12091.0 12091.0 539.0070 < 2.2e-16 ***
## DIS
               1 1122.0 1122.0 50.0186 5.234e-12 ***
## RAD
                    97.5
                            97.5
                                   4.3478
                                            0.03757 *
## TAX
               1
                   669.3
                           669.3 29.8380 7.456e-08 ***
## PTRATIO
                  1519.7
                          1519.7
                                  67.7494 1.666e-15 ***
               1
## B
                           590.6 26.3273 4.149e-07 ***
               1
                   590.6
## LSTAT
               1
                  2723.5
                          2723.5 121.4111 < 2.2e-16 ***
## Residuals 494 11081.4
                            22.4
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
mse.reg <- 11078.8 / 492
mse.reg.picked <- 11081.4 / 494
mae.reg <- sum(abs(reg$residuals)) / 492</pre>
mae.reg.picked <- sum(abs(reg.picked$residuals)) / 494</pre>
print(mse.reg)
## [1] 22.51789
print(mse.reg.picked)
## [1] 22.43198
print(mae.reg)
## [1] 3.363936
print(mae.reg.picked)
```

[1] 3.351519

1c. In both cases, the MSE and the MAE are lower for the model reg.picked, so I would choose that model.

```
library(MASS)
reg.step = step(object=reg, direction='both')
## Start: AIC=1589.64
## MEDV ~ CRIM + ZN + INDUS + CHAS + NOX + RM + AGE + DIS + RAD +
      TAX + PTRATIO + B + LSTAT
##
##
            Df Sum of Sq RSS
## - AGE
                0.06 11079 1587.7
            1
## - INDUS
                   2.52 11081 1587.8
## <none>
                       11079 1589.6
## - CHAS
                218.97 11298 1597.5
## - TAX
                242.26 11321 1598.6
             1
## - CRIM
             1
                 243.22 11322 1598.6
## - ZN
               257.49 11336 1599.3
             1
## - B
             1 270.63 11349 1599.8
## - RAD
                 479.15 11558 1609.1
             1
## - NOX
                 487.16 11566 1609.4
             1
## - PTRATIO 1 1194.23 12273 1639.4
## - DIS
            1 1232.41 12311 1641.0
## - RM
             1 1871.32 12950 1666.6
## - LSTAT
             1 2410.84 13490 1687.3
##
## Step: AIC=1587.65
## MEDV ~ CRIM + ZN + INDUS + CHAS + NOX + RM + DIS + RAD + TAX +
##
      PTRATIO + B + LSTAT
##
            Df Sum of Sq RSS
##
## - INDUS
                    2.52 11081 1585.8
## <none>
                        11079 1587.7
## + AGE
                   0.06 11079 1589.6
## - CHAS
                219.91 11299 1595.6
             1
## - TAX
             1
                 242.24 11321 1596.6
## - CRIM
            1
               243.20 11322 1596.6
## - ZN
                260.32 11339 1597.4
             1
## - B
                272.26 11351 1597.9
             1
## - RAD
                481.09 11560 1607.2
             1
## - NOX
            1 520.87 11600 1608.9
## - PTRATIO 1 1200.23 12279 1637.7
             1 1352.26 12431 1643.9
## - DIS
## - RM
             1 1959.55 13038 1668.0
## - LSTAT
            1 2718.88 13798 1696.7
##
## Step: AIC=1585.76
## MEDV ~ CRIM + ZN + CHAS + NOX + RM + DIS + RAD + TAX + PTRATIO +
##
      B + LSTAT
##
##
            Df Sum of Sq RSS AIC
## <none>
                        11081 1585.8
## + INDUS
                    2.52 11079 1587.7
## + AGE
                  0.06 11081 1587.8
             1
## - CHAS
                227.21 11309 1594.0
             1
## - CRIM
            1 245.37 11327 1594.8
## - ZN
           1 257.82 11339 1595.4
```

```
## - B
                   270.82 11352 1596.0
## - TAX
                   273.62 11355 1596.1
              1
                   500.92 11582 1606.1
## - RAD
## - NOX
                   541.91 11623 1607.9
              1
## - PTRATIO
              1
                  1206.45 12288 1636.0
## - DIS
                  1448.94 12530 1645.9
              1
## - RM
                  1963.66 13045 1666.3
              1
## - LSTAT
                  2723.48 13805 1695.0
              1
anova(reg.step)
## Analysis of Variance Table
## Response: MEDV
##
                  Sum Sq Mean Sq F value
                                              Pr(>F)
## CRIM
                  6440.8 6440.8 287.1259 < 2.2e-16 ***
               1
               1
                  3554.3 3554.3 158.4500 < 2.2e-16 ***
## CHAS
               1 1233.8 1233.8 55.0016 5.282e-13 ***
               1 1592.4 1592.4 70.9878 3.947e-16 ***
## NOX
               1 12091.0 12091.0 539.0070 < 2.2e-16 ***
## RM
## DIS
               1 1122.0 1122.0 50.0186 5.234e-12 ***
## RAD
               1
                    97.5
                             97.5
                                    4.3478
                                             0.03757 *
## TAX
               1
                   669.3
                            669.3 29.8380 7.456e-08 ***
                  1519.7 1519.7 67.7494 1.666e-15 ***
## PTRATIO
               1
## B
                   590.6
                           590.6 26.3273 4.149e-07 ***
               1
                          2723.5 121.4111 < 2.2e-16 ***
## LSTAT
               1
                  2723.5
## Residuals 494 11081.4
                             22.4
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
1d. The model that the stepwise regression picks is the exact same as the model reg.picked, where AGE and
INDUS are taken out. Therefore, the SSE is the exact same for both models.
  2.
lab <- read.csv(file="labdata.txt",head=TRUE,sep="\t")</pre>
labreg <- lm(y~. ,data=lab)</pre>
summary(labreg)
##
## lm(formula = y ~ ., data = lab)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -25.7138 -7.3129 -0.1718
                                 7.4281
                                         23.8909
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            5.10223
                                      3.447 0.000629 ***
## (Intercept) 17.58565
## x1
                1.91936
                            0.05492 34.951 < 2e-16 ***
## x2
                0.89747
                            0.08389
                                     10.699 < 2e-16 ***
## x3
                1.07895
                            0.08370
                                     12.890 < 2e-16 ***
                                      2.721 0.006798 **
## x4
                0.23834
                            0.08759
## x5
                0.10141
                            0.03725
                                      2.723 0.006766 **
                                      1.954 0.051421 .
## x6
                0.29608
                            0.15153
```



cor(lab)

```
x2
                                           xЗ
                                                      x4
                      x1
## y 1.000000000 0.80533240 0.19670658 0.357489045 0.102390521
## x1 0.805332395 1.00000000 -0.08474350 0.078455900 0.044997692
## x2 0.196706581 -0.08474350 1.00000000
                                   0.032190768 0.010550315
## x3 0.357489045 0.07845590 0.03219077 1.000000000 -0.023429594
## x4 0.102390521 0.04499769 0.01055031 -0.023429594
                                              1.000000000
## x5 0.215721371 0.19510364 -0.01520499 -0.018719329 0.110846689
## x6 0.083910285 -0.02965772 0.24679088 -0.001009249 -0.001815613
## x7 0.096340682 0.03255074 0.03925291 0.233860531 0.011634563
## x8 0.004553459 -0.01039468 -0.03037249 -0.012508475 0.392708258
##
             x5
                        x6
                                  x7
     ## x1 0.195103635 -0.029657719 0.032550741 -0.010394675
```

```
## x3 -0.018719329 -0.001009249 0.233860531 -0.012508475

## x4 0.110846689 -0.001815613 0.011634563 0.392708258

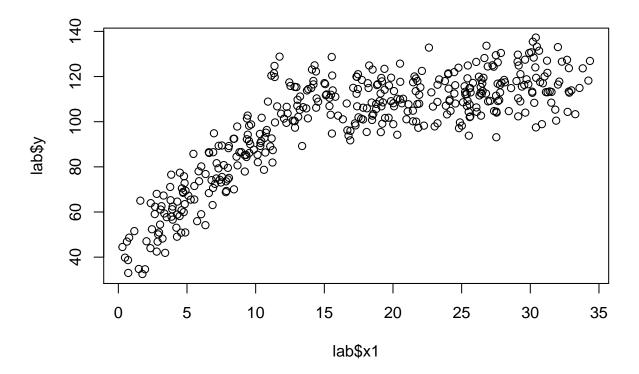
## x5 1.000000000 0.051007118 0.004495165 0.052027308

## x6 0.051007118 1.000000000 0.014613630 -0.057075892

## x7 0.004495165 0.014613630 1.000000000 0.025789695

## x8 0.052027308 -0.057075892 0.025789695 1.000000000

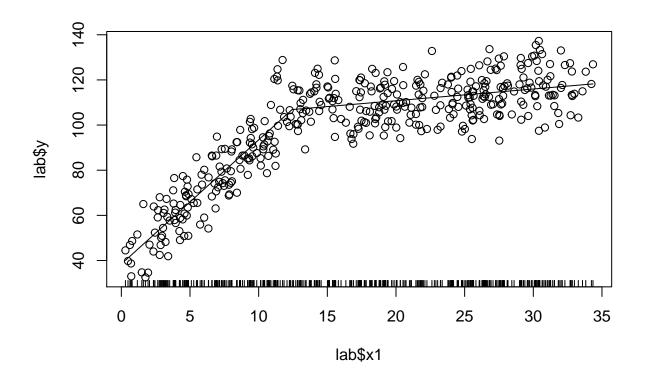
plot(lab$x1,lab$y)
```



2b. Based on the matrix scatter plot and the pairwise correlations, the relationship between y and x1 seems to be the strongest. I would use x1 as the best predictor of y.

```
mean(lab$x1)
## [1] 17.19417
library(segmented)
labreg.x1 = lm(y \sim x1, data=lab)
labreg.piece = segmented(labreg.x1, seg.Z = ~x1, psi=17.19)
anova(labreg)
## Analysis of Variance Table
##
## Response: y
##
              Df Sum Sq Mean Sq
                                   F value
                                               Pr(>F)
               1 134777
                          134777 1343.7867 < 2.2e-16
## x1
## x2
                  14694
                           14694
                                  146.5037 < 2.2e-16 ***
                                  168.3379 < 2.2e-16 ***
## x3
                  16884
## x4
                    1027
                            1027
                                   10.2397 0.001487 **
```

```
## x5
               1
                    810
                             810
                                    8.0783
                                            0.004715 **
                    385
  x6
                             385
                                            0.050784
##
               1
                                    3.8390
                                    0.1590
## x7
                      16
                              16
                                            0.690267
                                    0.0091
                                            0.923860
                       1
## x8
               1
                               1
## Residuals 391
                  39216
                             100
##
## Signif. codes:
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
anova(labreg.piece)
## Analysis of Variance Table
##
## Response: y
##
              Df Sum Sq Mean Sq F value Pr(>F)
## x1
               1 134777
                          134777
                                  1620.8 <2e-16 ***
                  40104
                           40104
                                   482.3 <2e-16 ***
## U1.x1
               1
## psi1.x1
               1
                               0
                                     0.0
## Residuals 396
                  32928
                              83
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
plot(lab$x1, lab$y)
plot(labreg.piece, add=T)
```



At first glance at the SSE, the SSE of the reg.piece model is much lower. It also has a higher DF, meaning the MSE will be much lower for the piecewise model, so I would choose that one.