In [20]:
```
import pandas as pd
import statsmodels.api as sm
import statsmodels.formula.api as smf
import matplotlib.pyplot as plt
from sklearn import metrics
```

1.) Import Data from FRED

In [2]:
```
data = pd.read_csv("TaylorRuleData.csv", index_col = 0)
```

In [3]:
```
data.index = pd.to_datetime(data.index)
```

In [4]:
```
data.dropna(inplace = True)
```

In [6]:
```
print(data)
```

```
            FedFunds  Unemployment  HousingStarts  Inflation
1959-01-01      2.48           6.0         1657.0     29.010
1959-02-01      2.43           5.9         1667.0     29.000
1959-03-01      2.80           5.6         1620.0     28.970
1959-04-01      2.96           5.2         1590.0     28.980
1959-05-01      2.90           5.1         1498.0     29.040
...              ...           ...            ...        ...
2023-07-01      5.12           3.5         1451.0    304.348
2023-08-01      5.33           3.8         1305.0    306.269
2023-09-01      5.33           3.8         1356.0    307.481
2023-10-01      5.33           3.8         1359.0    307.619
2023-11-01      5.33           3.7         1560.0    307.917

[779 rows x 4 columns]
```

2.) Do Not Randomize, split your data into Train, Test Holdout

In [7]:
```
split1 = int(len(data) * .6)
split2 = int(len(data) * .9)
data_in = data[:split1]
data_out = data[split1:split2]
data_hold = data[split2:]
```

In [8]:
```
X_in = data_in.iloc[:,1:]
y_in = data_in.iloc[:,0]
X_out = data_out.iloc[:,1:]
y_out = data_out.iloc[:,0]
X_hold = data_hold.iloc[:,1:]
y_hold = data_hold.iloc[:,0]
```

In [9]:
```
# Add Constants
X_in = sm.add_constant(X_in)
X_out = sm.add_constant(X_out)
X_hold = sm.add_constant(X_hold)
```

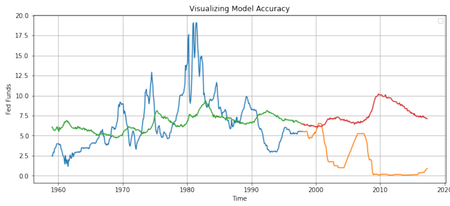
3.) Build a model that regresses FF~Unemp, HousingStarts, Inflation

In [10]:
```
model1 = sm.OLS(y_in, X_in).fit()
```

4.) Recreate the graph fro your model

In [ ]:
```
import matplotlib.pyplot as plt
```

In [11]:
```
plt.figure(figsize = (12,5))

###
plt.plot(y_in)
plt.plot(y_out)
plt.plot(model1.predict(X_in))
plt.plot(model1.predict(X_out))
###

plt.ylabel("Fed Funds")
plt.xlabel("Time")
plt.title("Visualizing Model Accuracy")
plt.legend([])
plt.grid()
plt.show()
```



"All Models are wrong but some are useful" - 1976 George Box

5.) What are the in/out of sample MSEs

In [13]:
```
from sklearn.metrics import mean_squared_error
```

In [14]:
```
in_mse_1 = mean_squared_error(y_in,model1.predict(X_in))
out_mse_1 = mean_squared_error(y_out,model1.predict(X_out))
```

In [15]:
```
print("Insample MSE : ", in_mse_1)
print("Outsample MSE : ", out_mse_1)
```

```
Insample MSE :  10.071422013168641
Outsample MSE :  40.36082783566732
```

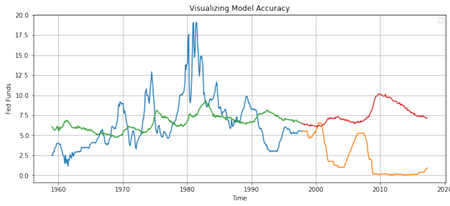
6.) Using a for loop. Repeat 3,4,5 for polynomial degrees 1,2,3

In [16]:
```
from sklearn.preprocessing import PolynomialFeatures
```

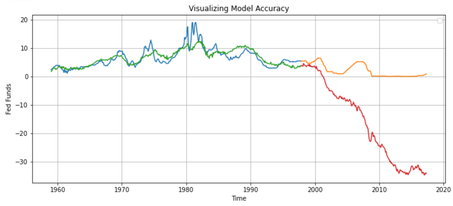
In [18]:
```
max_degrees = 3
```

In [21]:
```
for degrees in range(1, max_degrees+1):
    print('DEGREE : ', degrees)
    poly = PolynomialFeatures(degree = degrees)
    X_in_poly = poly.fit_transform(X_in)
    X_out_poly = poly.transform(X_out)

    model1 = sm.OLS(y_in, X_in_poly).fit()

    plt.figure(figsize = (12,5))

    pred_in = model1.predict(X_in_poly)
    pred_in = pd.DataFrame(pred_in, index = y_in.index)

    pred_out = model1.predict(X_out_poly)
    pred_out = pd.DataFrame(pred_out, index = y_out.index)

    ###
    plt.plot(y_in)
    plt.plot(y_out)
    plt.plot(pred_in)
    plt.plot(pred_out)
    ###

    plt.ylabel("Fed Funds")
    plt.xlabel("Time")
    plt.title("Visualizing Model Accuracy")
    plt.legend([])
    plt.grid()
    plt.show()

    in_mse_1 = metrics.mean_squared_error(model1.predict(X_in_poly), y_in)
    out_mse_1 = mean_squared_error(model1.predict(X_out_poly), y_out)

    print("Insample MSE : ", in_mse_1)
    print("Outsample MSE : ", out_mse_1)
    print('-----------------------------------')
```

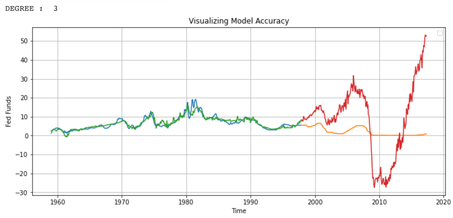
```
DEGREE :  1
```




```
Insample MSE :  10.071422013168641
Outsample MSE :  40.36082783566916
-----------------------------------
DEGREE :  2
```




```
Insample MSE :  3.863477139276069
Outsample MSE :  481.44650991792037
-----------------------------------
DEGREE :  3
```




```
Insample MSE :  1.8723636267594668
Outsample MSE :  371.7677889463972
-----------------------------------
```

7.) State your observations :

The model is overfit, we can see a very samll in cample MSE, but the prediction for out of sample data is not accurate