# Machine Learning for Molecular Engineering 3/7/10/20.01 (U) 3/7/10/20.C51 (G) Spring 2025

Problem Set #1

**Date:** April 2, 2025

**Due:** April 7, 2025 @ 3:00 pm ET

#### Instructions

- This problem set has two modeling tasks with several sub-questions. Some are marked grad version, which are required for graduate students (X.C51) but optional for others. Points for all students are in blue, while grad-only points are in orange. The total points are 75 for undergraduates and 100 for graduates.
- To get started, open your Google Colab or Jupyter notebook starting from the problem set template file pset1.ipynb (direct Colab link). You will need to use the data files here. Make your own copy of this template to save changes, by selecting "Save a copy in Drive". If you have not used Google Colab, you might find this example notebook helpful.
- Important: This problem set requires a GPU. Before you start in Google Colab, find Notebook Settings under the Edit menu. In the Hardware accelerator drop-down, select a GPU as your hardware accelerator. Changing the runtime resets the notebook, so make this change before starting! Read Part 2.1 for additional help.
- Collaboration is encouraged and AI tools are permitted, but submitting work that is not your own is plagiarism. Any collaboration or assistance from an LLM (including utilties present within Google Colab) should be described at the end of your submission.
- Upon completion, submit your IPython Notebook pset1.ipynb to Gradescope. Ensure your submission includes all necessary code to be run without error, with all plots and outputs. Comments are encouraged; put answers to conceptual questions in Markdown/Text cells.

# Part 1: Preliminary modeling

#### Background

Imagine if all diseases could be diagnosed with from a tiny drop of blood. While that day may still be far off, much progress has been made in searching for what are called *biomarkers*, molecules in the blood that are associated with particular diseases. Many studies use mass spectrometry to search for such diagnostic molecules. Biomarkers can be proteins, nucleic acids, lipids, or any of thousands of other chemical compounds that are found in the blood (see Figure 1).

Because many of these chemical compounds are products of metabolism, they are often called *metabolites*, and the detection of metabolites is called *metabolomics*. Recent studies have shown that metabolites can be predictive of human health conditions [2, 3]. In this problem, we will use two different classification methods to detect breast cancer from patients' metabolite data collected from human plasma/serum, following data processing steps found here [4].

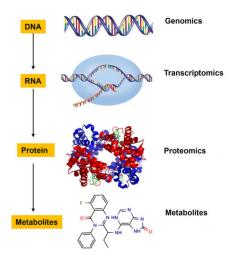


Figure 1: Figure adapted from Ref. [1]

# Part 1.1 (5 points) Load and inspect the raw data

To perform supervised machine learning on vector-valued data, you need labeled examples  $\{(\mathbf{x},y)\}$ , where  $\mathbf{x}$  is a vector of input features and y the known label. Your goal is to train a model  $\hat{f}$  that maps features to labels:  $\hat{f}(\mathbf{x}) \approx y$ . For diagnosing breast cancer from metabolite data, the metabolite signal is  $\mathbf{x}$ , and the binary label (positive or negative) is y, both provided as .csv files.

Task: We provide code utilizing pandas and numpy to load the data. Make sure you understand what each line of code is doing. Briefly explain each line; then, use X.shape to report the number of samples and features per sample.

#### Part 1.2 (5 points) Generate train/test splits

To fairly evaluate the performance, split your data into a training data set and testing data set. Only training data should be used to train the model; testing data are for unbiased evaluations of model performance. During training, the model should not have access to *any* information about the testing dataset, so you should not train (or preprocess!) on the testing data. Use sklearn.model\_selection.train\_test\_split to randomly split your dataset into training and testing data with an 80%:20% ratio (you should get two feature arrays, and two corresponding label arrays).

Task: Show your train\_test\_split code, print the shapes of your four variables, X\_train, X\_test, y\_train, and y\_test and ensure that the dimensions match your expectations.

#### Part 1.3 (5 points) Preprocess the data through scaling

Features in your dataset may have different units and magnitudes: for example, an atom's molecular weight (1 - 294 grams/mol) and covalent radius  $(30 - 250 \times 10^{-12} \text{ meters})$  have different ranges. To avoid unfairly weighting features, we *standardize* all features to a consistent scale.

**Standardization:** Let N be the total number of features, and M is the total sample size. Let  $X_{0,j}...X_{i,j}...X_{N-1,j}$  be the feature vector for the  $j^{\text{th}}$  sample (patient), where  $X_{i,j}$  refers to the unnormalized abundance of the  $i^{\text{th}}$  metabolite in the  $j^{\text{th}}$  patient. The mean and standard deviation<sup>1</sup>

<sup>&</sup>lt;sup>1</sup>scikit-learn and numpy use a normalization of M for the population standard deviation, rather than M-1 for the sample standard deviation, which is numpy's default as well. pandas defaults to the sample standard deviation.

of each feature are calculated as:

$$\mu_i = \frac{1}{M} \sum_{j=1}^{M} X_{i,j} \qquad \sigma_i^2 = \frac{1}{M} \sum_{j=1}^{M} (X_{i,j} - \mu_i)^2$$
 (1)

Each feature is transformed under an affine mapping for the feature vectors  $X_{i,j}$ . We call the transformed feature vectors  $X'_{i,j}$ :

$$X'_{i,j} = \frac{1}{\sigma_i} (X_{i,j} - \mu_i) \tag{2}$$

Note that this procedure is invertible (meaning you can get the original feature vector back if you know  $\sigma_i$  and  $\mu_i$ ), meaning no information loss for your data.

Task: Use scikit-learn's preprocessing. StandardScaler to process your input features, X, into X\_train\_scaled, following the feature standardization above. Show the  $\mu_i$  and  $\sigma_i$  of each feature are 0 and 1 respectively after scaling (use np.mean and np.var). Apply the same ScalerTransform to X\_test to produce X\_test\_scaled. Note: the ScalerTransform should *only* be fit upon X\_train and applied to X\_test. Take one sentence to discuss why, and what information leak might occur if one were to fit the scaler upon both X\_train and X\_test.

#### Part 1.4 (10 points) Train and evaluate a Logistic Regression model

Now, you should be ready to train a logistic regression model and evaluate its performance on the test data. We will use simple model modules from scikit-learn, a machine learning library. We will use three handy evaluations for this task:

- Confusion matrices (reference): A visualization to stratify model performance by looking at positive and negative samples separately, and how many are correctly classified (true positives and negatives) vs. misclassified (false positives and negatives).
- ROC Curve (reference): The receiver operating characteristic (ROC) curve plots the true positive rate (TPR) against the false positive rate (FPR) at different decision thresholds. We usually report the area under the curve (AUC) of the ROC (AUC-ROC) for a scalar metric.
- Precision-recall (PR) curve (reference): This plots the precision (proportion of true positives to all predicted positives) against the recall (or true positive rate). We report the area under the PR curve (AUPRC) as a single metric from the PR curve. This evaluation is handy when the dataset is highly imbalanced, i.e. many more positives than negatives or vice versa.

Task: Train a logistic regression model on the scaled training data and evaluate it on testing data with scikit-learn's LogisticRegression class. For both the train and test datasets, generate plots for confusion matrices and the ROC curve with help of plot\_clf, and report the AUC-ROC score. Finally, plot a histogram with matplotlib.pyplot.hist of the model coefficients (you can retrieve model coefficients from model.coef\_, where model is your model) to get an understanding of the parameters learned for the dataset's features.

#### Part 1.5 (5 points) Introduce L1 regularization

In the previous part, you visualized the distribution of model coefficients. Now, we consider how these change after regularizing the model with L1 loss (we'll explore L2 regularization in Part 2).

Task 1: For this part, modify your logistic regression model to include L1 regularization using the keyword arguments penalty='11', solver='saga'. Use the same pre-processed training and

testing data from Part 1.1. Print the AUC-ROC score, plot the ROC curve, and plot the confusion matrix for both training and testing data.

Task 2: Probe the effect of regularization by plotting the histogram of the new model coefficients to find any qualitative changes. Comment on any differences between the two models' distribution of model coefficients, thinking specifically about the *geometric* interpretation of L1 regularization.

# Part 1.6 (optional +2.5 points) Connect model coefficients back to metabolites

**Task:** The column of your feature set X which you loaded in Part 1.1 contains the chemical name for each metabolite. Based on the trained model from Part 1.4, identify the top 5 metabolites that are most correlated the most with a positive diagnosis.

# Part 1.7 (5 points) Hyperparameter tuning the regularization parameter

To optimize your model further, one may tune the hyperparameters, which are parameters whose values are used to control some aspect of the model or the learning process, but is not optimized during the training. These might include the layer widths, the number of layers, the learning rate, optimizer, and more. This is done for a number of reasons: to prevent overfitting, make training most efficient, improve generalization, etc.

**Task:** For this problem, tune the regularization parameter by testing 4 provided values, and selecting the best model based on the *development set* (the internal test set) to select the parameters. Report the hyperparameter with the best validation performance, and that model's performance on the test set.

# Part 1.8 (5 points) Train a Random Forest classifier

Besides Logistic Regression classifiers, another popular classification model architecture is Random Forests, which are ensembles of decision tree classifiers. Ensemble models can be often useful for mitigating overfitting and reducing the variance of your classification method.

To ensure our model's performance isn't just due to luck, we evaluate it on different splits of the data, known as k-fold cross validation. Following Figure 2, we effectively run the same experiment K times, each time using a distinct train/validation split. This yields K different performance values, which can be averaged to yield a more robust reflection of performance.

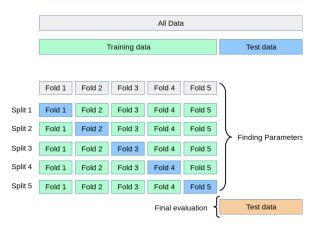


Figure 2: Overview of k-fold cross-validation. Source: scikit-learn.

Task: Initialize a Random Forest classifier using RandomForestClassifier from the scikit-learn library. Use the following parameter set: {max\_depth=2, n\_estimators=20}. Use the function cross\_val\_score to perform a 5-fold cross validation, using scoring='roc\_auc' as the metric to report; report AUC-ROC scores via their mean and standard deviation.

To relearn the scaler transform in each fold, sklearn has the Pipeline API to chain together multiple steps in a machine learning model. Feed cross\_val\_score a Pipeline so that it correctly fits the scaler to only the training set within each cross-validation fold.

# Part 2: Perovskite $E_{hull}$ Regression

# Background

This problem covers neural networks to predict the  $E_{hull}$  of crystalline perovskite materials with varying composition; predicting these properties lets us design new materials with desired function.

#### Structures and properties of perovskites

Natural perovskite is a mineral composed of calcium titanium oxide (CaTiO<sub>3</sub>). It was discovered in Russia by Gustav Rose and named after mineralogist L. A. Perovski. Gernally, any material whose crystalline structure is similar to the perovskite mineral is a *perovskite* (if you're curious, we encourage you to learn more about crystal structure here. Because their structure can support many possible element compositions, perovskites are a quite abundant structural family, and have wideranging properties, applications, and importance, such as in solar cells, piezoelectrics or catalysts.

In perovskites, A is typically a large cation (alkali metal, rare earth, or organic like methylam-monium), B is a transition metal, and X is an anion (oxide, fluoride, nitride, or halide) bonded to both cations. The ideal cubic structure (space group  $Pm\bar{3}m$ ), has B in 6-fold octahedral coordination and A in 12-fold cuboctahedral coordination. However, real materials often deviate from this structure, reducing symmetry. These distortions, such as in BaTiO<sub>3</sub>, lead to properties like piezoelectricity. Many elements can form stable perovskite structures, allowing for a vast possible set of compositions.

Because their compositions and thus their properties are extremely tunable, pervoskites are exciting materials for many applications. For example, take solar cells based on organic-inorganic halide perovskites (with an organic cation as A site; lead or a related element as B site; and Cl, Br or I as X): since their discovery about a decade ago, their efficiency has approached that of silicon photovoltaics (around 25%), yet are much cheaper to manufacture and can be made into thin films that are flexible and foldable. Despite their promise, though, perovskite solar cells suffer from stability issues that prevent mass adoption.

#### **Data Generation and Processing**

The data you will be modeling is generated with high-quality Quantum Chemistry calculations using Density Functional Theory (DFT). Each structure takes hundreds of CPU hours to calculate, and thus fairly expensive to obtain. In this question, you are asked to predict  $E_{hull}$  (Energy above hull). It has the unit of eV/Atom. It describes the thermodynamic stability of the crystal structure. If  $E_{hull} = 0.0$ , it means the structure is at its most stable form. Building these predictive models can help theorists reduce their computational cost when designing for more stable materials.

**Energy Above Hull:** The energy of decomposition of this material into the set of most stable materials at this chemical composition, in eV/atom. Stability is tested against all potential chemical

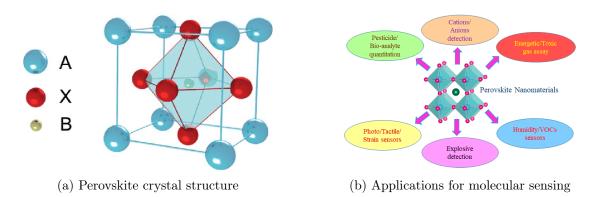


Figure 3: Perovskite structure and applications [5]

combinations that yield that composition. For example, a  $Co_2O_3$  structure (cobalt oxide) would be tested for decomposition against other  $Co_2O_3$  structures, against Co and Co mixtures, and against Co and Co mixtures. Co and Co mixtures. Co and Co mixtures against Co mixtures Co

$$E_{\text{Co}_2\text{O}_3} - \min(2E_{\text{Co}} + \frac{3}{2}E_{\text{O}_2}, 2E_{\text{CoO}} + E_{\text{O}_2}, E_{\text{Co}_2\text{O}_3})$$

Let's start with loading the dataset! You will be asked to use Pandas DataFrames. If you have not used Pandas before, please work through this tutorial.

# Part 2.1 (5 points) Encoding chemical formulae into feature vectors

After loading the pandas dataframe, take a moment to inspect your data by looking at the rows (samples) and columns (features). The important chemical information is stored in columns ['A', 'B', 'X'] and  $E_{hull}$  is stored in the column e\_above\_hull.

First, you will train a model that uses chemical compositions (e.g.  $CaTiO_3$ ) to predict Energy above  $Hull(E_{hull})$  which is a scalar property. How can you map a chemical formula like  $CaTiO_3$  to numeric features for training a model? You need to define a dictionary to encode elements into numerical features so that we can apply programs like linear regressions on these input features. One way to do is to use one-hot encoding to transform elements into bit vectors. For example, if we have elements Fe, Ni, and Mn for A and B sites, we can assign bit vectors of size 3 to fully encode this label information. We do not encode the elements for the X site because Oxygen is the only element available in our dataset for X. We present simple examples on how you should encode perovskite chemistries in table 1.

A site	B site	bit vector representation
'Fe'	'Ni'	[1,0,0,0,1,0]
'Mn'	'Ni'	[0,0,1,0,1,0]
'Fe'	'Mn'	[1,0,0,0,0,1]
'Fe'	'Fe'	[1,0,0,1,0,0]

Table 1: Example bit vector representation of A/B sites in perovskites

Task: After reading the documentation for preprocessing.LabelBinarizer(), use it to transform the features ['A', 'B'] into one-hot encoded arrays with the alphabet for A/B sites from elements.npy. Next, convert the hull energies to a np.array for use in regression. Your code should output X and y. Finally, randomly split these arrays into train/validation with an 80%/20%

ratio. You'll have a separate test set that you should should process separately, and not combine or split further for the first parts of this problem.

**Hint:** There are many ways to do it. One way to do it is to loop over rows (perovskites) in your dataframe and encode A and B into bit vectors separately, and then stack the two arrays horizontally using np.hstack.

#### Accelerating neural networks with GPUs

Scikit-learn provides common machine learning models but is limited in customization and speed of training. In contrast, PyTorch (along with TensorFlow, JAX, and CNTK) is designed for deep learning, allowing manual expressivity and efficient training through usage of GPU speedup. PyTorch uses reverse-mode automatic differentiation (AD) to compute gradients automatically, making it easier to optimize model weights. It also supports training on a Graphical Processing Unit (GPU), which enables significantly accelerated training.

In this part, you'll call certain functions from PyTorch to construct a Multi-Layer Perceptron, which is composed of alternating linear affine and non-linear transformations (layers), and train it on a GPU in Google Colab (where PyTorch is pre-installed). After this exercise, we hope you will be comfortable building your own machine learning workflow using PyTorch by adapting this and other example code.

Optional reading The PyTorch Tutorial and Quickstart Guide are great companion resources to the functional PyTorch primer we present in this question. Likewise for debugging, we suggest leafing through this guide.

# PyTorch setup: GPU basics, Datasets and DataLoaders

There are no points associated with this part, but spend some time understanding the cells in this section.

Setting up GPU usage: In Google Colab, go to Edit > Notebook Settings, and select T4 GPU under Hardware accelerator. You can also do this via Runtime > Change runtime type or by clicking the three dots in the top right corner. Verify GPU access using the provided code. In PyTorch, the main object is torch. Tensor, similar to np.array. In the second cell, confirm that you can move the sample tensor made to and from the GPU, with .to(device).

Building Datasets and DataLoaders in PyTorch: To organize our data, PyTorch wisely modularizes the data into smaller chunks, or minibatches, that allow the model to process one at a time to avoid memory overhead. In PyTorch, data is stored in torch.utils.data.Dataset and batched with torch.utils.data.DataLoader.

From Part 2.1, you should already have the data featurized and split into a train and validation set, as well as a separate test set loaded from the test file. Take a moment to parse the PerovskiteDataset class construction that implements Dataset for this problem. Also parse the DataLoader instances that wrap each PerovskiteDataset object made, paying attention to the shuffle=True parameter, to avoid overfitting to minibatches; and the size of the minibatch, set with batch\_size=256. You will need to know how to construct your own in PSET 2.

#### Part 2.2 (10 points) Define the MLP in PyTorch

We will now proceed to build a MLP using PyTorch's nn.Module class. The nn.Module class requires two methods: an \_\_init\_\_ method to define components and layers, and a forward class where you define the network's computation, i.e. how to compute a prediction with the layers given input data. Many standard layers, such as nn.Linear affine layers and either the nn.ReLU or nn.Tanh

layer for your activation function, are already made in PyTorch. You can use a nn.Sequential module to stack layers to automatically process your data in order. We ensure all layers are class attributes so PyTorch can handle auto-differentiation properly.

Task: We have provided the skeleton code for implementing your MLP in PyTorch as a nn.Module. Fill in the remainder of the code. Use three hidden layers, of widths 256, 256, 256; and ReLu activation layers after each nn.Linear layer.

#### Part 2.3 (10 points) Implement functions for training and testing

Now with a defined model architecture and DataLoaders, we will set up the training. We initialize a model instance, model, and then an optimizer to perform backpropagation with a variant of stochastic gradient descent. Two options are stochastic gradient descent (torch.optim.SGD) or the Adam optimizer (torch.optim.Adam).

Task 1: Construct the optimizer by using the Adam optimizer, and pass the following as arguments: model.parameters(); a learning rate lr of 1e-3; and L2 regularization with weight\_decay=0.01. Then, define your loss function by using MSE\_loss() to use mean squared error loss.

Task 2: We have provided the skeleton code for training and validation loops, which is quite standardized for any training task. We use the DataLoader to loop over the training data's minibatches and use the model to predict the  $E_{hull}$  probabilities for each minibatch. Use the loss initialized above to compute a loss on that minibatch; this requires both your model output and the ground-truth values. PyTorch can then compute your gradients with loss.backward(). Model weights are then updated by calling optimizer.step(). Clear the gradients from the previous calculation (minibatch) by calling optimizer.zero\_grad() at the start of each minibatch processing. Complete the train() function following these guidelines. Similarly, complete the validate() function, which uses the validation DataLoader and computes the loss on the validation set, though note: no gradients need be computed or model weights changed.

The train() and validate() functions implemented will operate on only one epoch, and should ultimately return a train loss and validation loss averaged over all minibatches in that one epoch.

#### Part 2.4 (5 points) Train the multi-layer perceptron

For regression tasks, one metric we can use to evaluate model performance is the coefficient of determination, or the  $\mathbb{R}^2$  score. It is defined as:

$$R^{2} = 1 - \frac{\sum_{i}^{N_{\text{data}}} (y_{i} - \hat{f}(\mathbf{x}_{i}))^{2}}{\sum_{i}^{N_{\text{data}}} (y_{i} - \text{mean}(y_{i}))}$$
(3)

where i is the index for each sample,  $y_i$  is the target value,  $\hat{f}$  is the model, and  $\mathbf{x}_i$  is the feature vector. The larger the  $R^2$  score, the more accurate the prediction is. If your prediction is perfect  $R^2 = 1$ . Note that metrics like mean absolute error (MAE) or mean squared error (MSE) can provide more meaningful and interpretable measures of performance.

**Task:** After ensuring you've initialized your model and optimizer with the hyperparameters listed in Table 2, train and validate your model for 250 epochs. Record the average train and validation loss for each epoch and plot these on a single graph (the plotting code is provided). Then, report the  $test\ R^2$  of your trained model on the test data<sup>1</sup>, and visualize your prediction for train and test data with a scatter plot. Finally, briefly comment on the hidden\_layers\_sizes values as they pertain to the MLP's intercepts and coefficients.

1: You'll need to convert your prediction from torch. Tensor to np.array with .cpu().detach().numpy(), then compute the  $R^2$  score with sklearn.metrics.r2\_score.

(hidden lawer giges)	(256, 256, 256)
'hidden_layer_sizes'	
activation	nn.ReLU
'alpha'	0.01
'solver'	Adam
'early_stopping'	False
'epochs'	250

Table 2: Hyperparameters to be used in Part 2.2-Part 2.4

# Part 2.5 Graduate (5 points) Compute model size

Task: Calculate the number of parameters used in your MLP given the provided 'hidden\_layer\_sizes'. You can do this manually or iterate over model.parameters().

# Part 2.6 (5 points) Chemical transferability of one-hot representations

We created a holdout set, which includes elements in new positions not seen in the training set, to test your model's performance.

**Task:** Load the test set (if you haven't already) and featurize the data with the label encoder from Part 2.1. Validate your MLP by computing the  $R^2$  score, and visualize your predictions with a scatter plot. Briefly describe your observations: does your model generalize well to this new data?

# Part 2.7 Graduate (10 points) Featurize elements with physical descriptors

Let's try using a more informative featurization, with physical descriptors of the elements, which should contain more helpful information than a one-hot encoding.

Task: Load the data for atomic properties stored in mendeleev.csv with provided code. Use all the numerical features to construct a new feature matrix (please exclude atomic symbols which are strings). Split the original training data into a training (80%) set and a validation (20%) set; since we have continuous features again, rescale with preprocessing.StandardScalar as seen in Problem 1. Train on the training set with a MLP with the same hyperparameters we provided to you in Part 2.4 (you will need to tweak the number of input features). Plot a scatterplot of predictions on the train and validation datasets.

#### Part 2.8 Graduate (10 points) Chemical transferability of physical descriptors

**Task:** Report the  $R^2$  score on your test set using the model trained in Part 2.7 and visualize your prediction with a scatter plot. Did your holdout predictions improve? Briefly explain why.

#### Acknowledgement

We thank Daniel Schawbe-Koda for helping with the data generation for this problem set.

### References

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