

ASP – Answer Set Programming

An operational formalism (*Baral 2003*)

A program Π is a set of expression ρ

$$\rho : L_0 \text{ or } L_1 \text{ or } \dots L_k \leftarrow L_{k+1}, L_{k+2}, \dots L_m, \text{not } L_{m+1}, \dots, \text{not } L_n$$

where

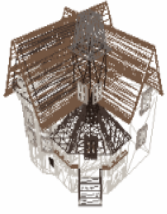
- the L_i are literals (*atoms or atom negations*)
- The « not » is a negation by failure

Intuitive meaning: for all Herbrand interpretation such that



$\{L_{k+1}, L_{k+2}, \dots, L_m\}$ is true

while $\{L_{m+1}, \dots, L_n\}$ failed to be proved

one can derive $\{L_0, L_1, \dots L_k\}$

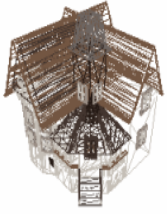


An Artificial Agent

$act(P, S, \mathbf{G}, A) \leftarrow person(P),$
 $situation(S), goal(G), action(A),$
 $will(P, S, \mathbf{G}),$  
 $solve_goal(P, S, G, A).$
 $\leftarrow act(P, S, G, A), act(P, S, G, B), A \neq B.$

Autonomy

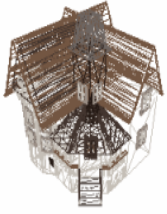
Intelligence



An Ethical Artificial Agent

$act(P, S, G, A) \leftarrow person(P),$
 $situation(S), goal(G), action(A),$
 $will(P, S, G),$
 $solve_goal(P, S, G, A),$
 $moral(P, S, G, A).$

$\leftarrow act(P, S, G, A), act(P, S, G, B), A \neq B.$



An “Aristotelian” Perspective

Predicates:

$csq(A, S, C) : \text{consequence}$

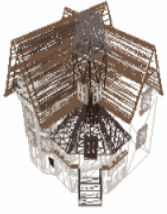
$worse(A, B) : \text{comparison of action}$

$worst_csq(A, S, C) : \text{worst consequence}$

$good(P, S, \mathbf{G}, A) \leftarrow will(P, S, \mathbf{G}),$
 $solve_goal(P, S, G, A), worst_csq(A, S, C),$
 $will(\bar{P}, \bar{S}, U), solve_goal(P, \bar{S}, U, B),$
 $csq(B, S, D), worse(\bar{D}, C).$

$bad(P, S, \mathbf{G}, A) \leftarrow will(P, S, \mathbf{G}),$
 $solve_goal(P, S, G, A), worst_csq(A, S, C),$
 $will(\bar{P}, \bar{S}, U), solve_goal(P, \bar{S}, U, B), A \neq B, csq(B, S, D),$
not $worse(D, C).$

The same action may be both good and bad!

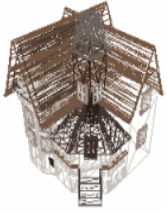


Moral and immoral

*moral(P, S, **G**, A) ← **not** bad(P, S, G, A).*

*moral(P, S, **G**, A) ← good(P, S, G, A),
not immoral(P, S, G, A).*

*immoral(P, S, **G**, A) ← bad(P, S, G, A),
not moral(P, S, G, A).*



The Lying Example

- Three persons: “I”, Peter and Paul
- Two possibilities: tell(P, truth) or tell(P, lie)
- Consequence: tell(“I”, truth) generates a murder

$csq(A, S, A) \leftarrow .$

$csq(A, S, B) \leftarrow csq(A, S, C), csq(C, S, B).$

$csq(tell(\text{“I”}, truth), s0, murder) \leftarrow .$

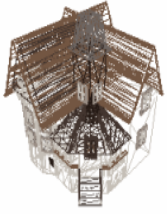
$worse(A, B) \leftarrow better(B, A), \text{not } better(A, B).$

$worse(A, B) \leftarrow worse(A, C), worse(C, B).$

$better(A, tell(P, lie)) \leftarrow .$

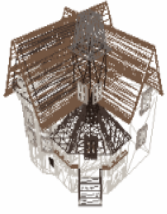
$better(A, murder) \leftarrow .$

$better(A, A) \leftarrow .$



The Lying Example

- Half of the answer sets contain:
act("I", answer("I"),s0, tell("I", truth))
- And half of the answer sets contain:
act("I", answer("I"),s0, tell("I", lie))
- If we add *worse(murder, lie)* then all the answer sets that contain
act("I", answer("I"),s0, tell("I", truth)) are removed.



Torture example

- Three persons: “I”, Peter and Paul
- Two possibilities: $\text{interrogate}(P, \text{torture})$ or $\text{interrogate}(P, \text{soft})$
- Consequence: $\text{interrogate}(\text{“I”}, \text{soft})$ generates an attack

$\text{csq}(A, S, A) \leftarrow .$

$\text{csq}(A, S, B) \leftarrow \text{csq}(A, S, C), \text{csq}(C, S, B).$

$\text{csq}(\text{interrogate}(\text{“I”}, \text{soft}), s0, \text{attack}) \leftarrow .$

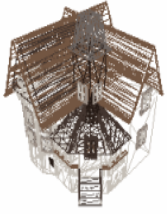
$\text{worse}(A, B) \leftarrow \text{better}(B, A), \text{ **not** } \text{better}(A, B).$

$\text{worse}(A, B) \leftarrow \text{worse}(A, C), \text{worse}(C, B).$

$\text{better}(A, \text{interrogate}(P, \text{torture})) \leftarrow .$

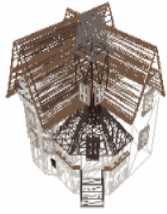
$\text{better}(A, \text{attack}) \leftarrow .$

$\text{better}(A, A) \leftarrow .$



The Torture Example

- Half of the answer sets contain:
act("I", question("I"), s0, interrogate("I", torture))
- And half of the answer sets contain:
act("I", question("I"), s0, interrogate("I", soft))
- If we add *worse(attack, torture)* then all the answer sets that contain
act("I", question("I"), s0, interrogate("I", soft)) are removed.



A Kantian Machine

Requirements for a possible society

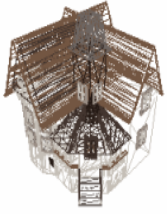


The maxim of my will has to be universalized – “categorical imperative”

- My acts have to obey to a law
- I must act *by the law* – and not just *in accordance to the law*
- My rule of behavior (my maxim) could be universal

If I adopt a right to lie (even in some conditions), I must conceive a world where everybody could act in the same way, which renders impossible to trust anyone.

In the same way, if I decide to suicide, because I am suffering to much, I must conceive a world...



The Kantian Perspective

$act(P, S, G, A) \leftarrow person(P),$

$situation(S), goal(G), action(A),$

$will(P, S, G),$

“Prudence”: pragmatic imperative

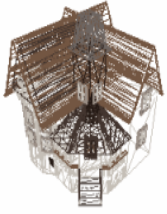
$solve_goal(P, S, G, A),$

“Habilité”:
problematic imperative

$maxim(P, S, A).$

Morality: moral
imperative

$\leftarrow act(P, S, G, A), act(P, S, G, B), A \neq B.$



The Kantian Perspective

$act(P, S, G, A) \leftarrow person(P),$
 $situation(S), goal(G), action(A),$

$will(P, S, G),$

Prudence

$solve_goal(P, S, G, A),$

“Habilité”

$maxim(P, S, A).$

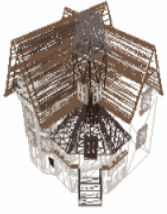
“Moralité”

$\leftarrow act(P, S, G, A), act(P, S, G, B), A \neq B.$

The *categorical imperative (morality)*

$maxim(P, S, A) \leftarrow maxim(“I”, S, B), bind(“I”, B, P, A).$

$bind(P, tell(P, U), Q, tell(Q, U)) \leftarrow .$



The Lying Example

- Categorical Imperative

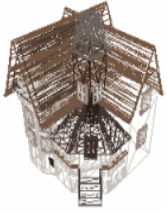
```
maxim_will(P, S, A) :-  
    maxim_will("I", S, B),  
    bind("I", B, P, A),  
    not maxim_will(P, S, C),  
    incompatible(A, C).
```

- Conséquences

```
consequence(A, S, A).  
consequence(tell("I", truth), s0, murder).  
consequence(tell(peter, truth), s0, murder).
```

- Situation

```
maxim_will(peter, S, tell(peter, lie)) :-  
    consequence(tell(peter, truth), S, murder).
```



A Meta-Ethical Requirement

- In a given society, I need to trust at least one person...

$untrust(P) \leftarrow maxim(P, S, tell(P, lie)).$

$trust(P) \leftarrow \textit{not } untrust(P).$

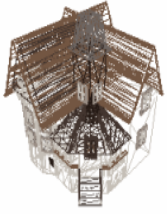
$possible_society \leftarrow trust(P).$

$\leftarrow \textit{not } possible_society.$

- The lying example:

If Paul is lying, there is no real problem

If I lie, there is no acceptable solution...because I cannot trust anyone in the society.



The Torture Example

- Categorical Imperative

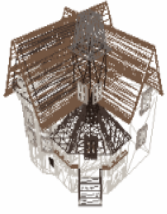
```
maxim_will(P, S, A) :- maxim_will("I", S, B),  
    bind("I", B, P, A),  
    not maxim_will(P, S, C), incompatible(A, C).
```

- Conséquences

```
consequence(A, S, A).  
consequence(interrogate("I", soft), s0, attack).  
consequence(interrogate(peter, soft), s0, attack).
```

- Situation

```
maxim_will(peter, S, interrogate(peter, torture) :-  
    consequence(interrogate(peter, soft), S, attack).
```



A Meta-Ethical Requirement

- If P tortures, the tortured person is not considered as a subject, but as a mean to get the truth...

*instrumentalize_person(P) ←
maxim(P, S, interrogate(P, torture)).*

*confidence(P) ← **not** instrumentalize_person(P).*

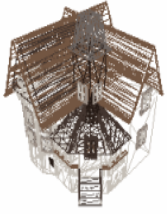
possible_society ← confidence(P).

*← **not** possible_society.*

- The torture example:

If Paul tortures, there is no real problem (?)

If I torture, there is no acceptable solution...because I cannot be in confidence with anyone in the society.



The Suicide Example

- Categorical Imperative

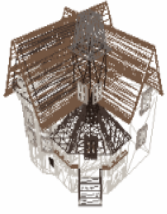
```
maxim_will(P, S, A) :- maxim_will("I", S, B),  
    bind("I", B, P, A),  
    not maxim_will(P, S, C), incompatible(A, C).
```

- Conséquences

```
consequence(A, S, A).  
consequence(take_care("I"), s0, loose_dignity("I").  
consequence(take_care(peter), s0, loose_dignity(peter)).
```

- Situation

```
maxim_will("I", S, take_care("I")).  
maxim_will("I", S, keep_dignity("I")).  
contradictory(keep_dignity(P), loose_dignity(P)).
```



Meta-ethical criteria

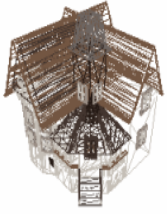
- Once being given Kantian requirements of a possible society, it is possible to define formal criteria, which ensure that a set of ethical axioms characterizing the maxims of will gives one (or more) solution(s).

Examples of such formal criteria: (Baral 2003)

Any stratified AnsProlog Program (*i.e. any program whose dependency graph does not contain any negative cycle*) has a unique answer set

Any signed AnsProlog Program has an answer set

Any order consistent AnsProlog Program has an answer set



B. Constant – System of Principles

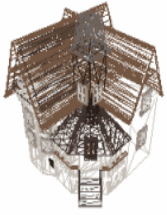
*act(P, S, G, A) ← person(P),
situation(S), goal(G), action(A),
will(P, S, G),
solve_goal(P, S, G, A),
principle(P, S, G, A).*

← act(P, S, G, A), act(P, S, G, B), A ≠ B.

tell become a ternary term

answer a binary term





B. Constant – System of Principles

principle(P, S, answer(P, Q), tell(P, Q, truth)) ←
not *¬principle(P, S, answer(P, Q), tell(P, Q, truth))*.

principle(P, S, answer(P, Q), tell(P, Q, lie)) ←
demerit(Q, tell(P, Q, truth)).

¬principle(P, S, answer(P, Q), tell(P, Q, truth)) ←
principle(P, S, answer(P, Q), tell(P, Q, lie)).

demerit(Q, tell(P, Q, truth)) ←
worst_csq(tell(P, Q, truth), C),
worse(C, tell(P, Q, lie)).

