## CS122APandasDataframes

November 23, 2021

## 1 Dataframes: Another view of tabular data!

This notebook introduces the basics of Pandas and dataframes from a relational/SQL perspective. A Pandas dataframe is essentially a collection of numpy series that share an index. Dataframes can be populated with data from CSV files, JSON files, Parquet files, SQL databases, and other sources.

```
[40]: import pandas as pd
      import numpy as np
      import matplotlib.pyplot as plt
[41]: # first let's populate a dataframe with sailor data from a CSV file
      sailors = pd.read csv("/Users/mikejcarey/SailingClub/Sailors.csv")
[42]: cat /Users/mikejcarey/SailingClub/Sailors.csv
     sid, sname, rating, age, major
     22, Dustin, 7, 45, CS
     29, Brutus, 1, 33, EE
     31, Lubber, 8, 55.5, Econ
     32, Andy, 8, 25.5, Math
     58, Rusty, 10, 35, CS
     64, Horatio, 7, 35, CS
     71, Zorba, 10, 16, CS
     74, Horatio, 9, 35, Math
     85, Art, 4, 25.5, Music
     95,Bob,3,63.5,Econ
     101, Joan, 3, , Math
     107, Johannes, ,35.0,
[43]: sailors
[43]:
           sid
                   sname
                           rating
                                     age
                                           major
            22
                  Dustin
                               7.0
                                   45.0
                                              CS
      0
      1
            29
                  Brutus
                              1.0
                                    33.0
                                              ΕE
      2
            31
                  Lubber
                              8.0
                                    55.5
                                            Econ
      3
            32
                    Andy
                              8.0
                                    25.5
                                            Math
```

```
5
           64
                             7.0
                                  35.0
                                            CS
                Horatio
      6
           71
                   Zorba
                            10.0
                                  16.0
                                            CS
      7
           74
                Horatio
                             9.0
                                  35.0
                                          Math
      8
           85
                     Art
                             4.0
                                  25.5
                                        Music
           95
                                  63.5
                                          Econ
      9
                     Bob
                             3.0
      10
          101
                    Joan
                             3.0
                                   NaN
                                          Math
          107
                                           NaN
      11
               Johannes
                             {\tt NaN}
                                  35.0
[44]: sailors.dtypes
[44]: sid
                   int64
                 object
      sname
      rating
                float64
      age
                 float64
      major
                 object
      dtype: object
[45]: sailors.describe()
[45]:
                     sid
                             rating
                                            age
      count
              12.000000
                          11.000000
                                     11.000000
      mean
              64.083333
                           6.363636
                                     36.727273
      std
              30.010478
                           3.107176
                                     13.583747
      min
              22.000000
                           1.000000
                                     16.000000
      25%
                           3.500000
              31.750000
                                     29.250000
      50%
              67.500000
                           7.000000
                                     35.000000
      75%
                           8.500000
              87.500000
                                      40.000000
             107.000000 10.000000
                                     63.500000
      max
[46]: # now let's populate two more dataframes with boat and reservation data
      boats = pd.read_csv("/Users/mikejcarey/SailingClub/Boats.csv")
      reserves = pd.read_csv("/Users/mikejcarey/SailingClub/Reserves.csv")
[47]: boats
[47]:
         bid
                  bname
                          color
         101
              Interlake
                           blue
      0
      1
        102
              Interlake
                            red
      2 103
                Clipper
                          green
      3 104
                 Marine
                            red
[48]: reserves
[48]:
           sid
                  bid
                              date
      0
          22.0
               101.0 1998-10-10
```

4

58

Rusty

10.0 35.0

CS

```
2
          22.0 103.0 1998-10-08
          22.0
               104.0 1998-10-07
      3
          31.0 102.0 1998-10-11
      4
      5
          31.0 103.0 1998-11-06
          31.0 104.0 1998-11-12
      6
          64.0 101.0 1998-09-05
      7
          64.0 102.0 1998-09-02
      8
          74.0 103.0 1993-09-08
      10
          NaN
               103.0 1998-09-09
           1.0
      11
                  NaN 2001-01-11
           1.0
                  NaN 2002-02-02
[49]: # now let's work with these three dataframes
      sailors
[49]:
          sid
                  sname rating
                                  age major
           22
                            7.0 45.0
      0
                 Dustin
                                          CS
      1
           29
                 Brutus
                            1.0
                                 33.0
                                          EΕ
      2
           31
                 Lubber
                            8.0 55.5
                                        Econ
                            8.0 25.5
      3
           32
                   Andy
                                        Math
      4
           58
                  Rusty
                           10.0 35.0
                                          CS
                            7.0 35.0
      5
           64
                Horatio
                                          CS
      6
           71
                  Zorba
                           10.0
                                16.0
                                          CS
      7
           74
                            9.0 35.0
                Horatio
                                        Math
      8
           85
                            4.0 25.5
                                       Music
                    Art
      9
           95
                    Bob
                            3.0 63.5
                                        Econ
      10
          101
                   Joan
                            3.0
                                  NaN
                                        Math
                            NaN 35.0
                                         NaN
          107
              Johannes
[50]: sailors.head(3)
[50]:
         sid
                     rating
                               age major
               sname
          22 Dustin
                         7.0 45.0
                                      CS
      0
      1
          29 Brutus
                         1.0
                              33.0
                                      ΕE
                              55.5 Econ
          31 Lubber
                         8.0
[51]: sailors.tail(2)
[51]:
          sid
                  sname rating
                                  age major
      10 101
                   Joan
                            3.0
                                  {\tt NaN}
                                       Math
         107
               Johannes
      11
                            {\tt NaN}
                                 35.0
                                        NaN
[52]: # pandas dataframes are ordered and indexed -- unlike relations
      # in the pure relational model or tables in SQL!
      sailors[10:12]
```

22.0 102.0 1998-10-10

1

```
[52]:
          sid
                  sname rating
                                   age major
      10 101
                   Joan
                             3.0
                                   {\tt NaN}
                                        Math
      11 107
                                         NaN
              Johannes
                             NaN 35.0
[53]: # we can do relational-style projection
      sailors['sname']
[53]: 0
              Dustin
              Brutus
      2
              Lubber
      3
                Andy
      4
               Rusty
      5
             Horatio
      6
               Zorba
      7
             Horatio
      8
                 Art
      9
                 Bob
      10
                Joan
      11
            Johannes
      Name: sname, dtype: object
[54]: sailors[['sname', 'rating']]
[54]:
             sname rating
      0
            Dustin
                       7.0
      1
            Brutus
                        1.0
      2
            Lubber
                       8.0
      3
              Andy
                       8.0
      4
             Rusty
                       10.0
      5
                       7.0
           Horatio
      6
             Zorba
                      10.0
      7
                       9.0
           Horatio
      8
                       4.0
               Art
      9
               Bob
                       3.0
      10
              Joan
                       3.0
         Johannes
                       NaN
[55]: # we can do relational-style selection
      sailors[sailors.age < 30.0]</pre>
[55]:
         sid sname rating
                               age major
      3
          32
                         8.0 25.5
                                     Math
               Andy
      6
          71 Zorba
                        10.0 16.0
                                       CS
      8
          85
                Art
                         4.0 25.5 Music
```

```
[58]: # let's break this down - first of all, each
      # column of a dataframe is an indexed serles
      sailors.age
[58]: 0
            45.0
            33.0
      1
            55.5
      2
      3
            25.5
      4
            35.0
      5
            35.0
      6
            16.0
      7
            35.0
            25.5
      8
      9
            63.5
      10
            NaN
      11
            35.0
      Name: age, dtype: float64
[59]: sailors.age < 30.0
[59]: 0
            False
            False
      1
      2
            False
      3
             True
      4
            False
      5
            False
      6
             True
      7
            False
      8
             True
            False
            False
      10
      11
            False
      Name: age, dtype: bool
[60]: sailors[sailors.age < 30.0]
[60]:
         sid sname rating
                              age major
          32
               Andy
                        8.0
                             25.5
                                    Math
      3
      6
          71
              Zorba
                       10.0 16.0
                                       CS
          85
                Art
                        4.0 25.5 Music
[61]: sailors[(sailors.major == 'CS') | (sailors.major == 'EE')]
[61]:
         sid
                sname rating
                               age major
          22
                          7.0 45.0
                                        CS
               Dustin
      0
      1
          29
               Brutus
                          1.0 33.0
                                        ΕE
```

```
10.0 35.0
      4
          58
                Rusty
                                        CS
          64 Horatio
                          7.0 35.0
                                        CS
                         10.0 16.0
                                        CS
          71
                Zorba
[62]: sailors[(sailors.major == 'CS') & (sailors.rating >= 8.0)]
[62]:
         sid sname rating
                              age major
          58 Rusty
                       10.0 35.0
                                      CS
          71
              Zorba
                       10.0 16.0
                                      CS
[64]: sailors
[64]:
          sid
                  sname rating
                                   age
                                        major
           22
                 Dustin
                            7.0 45.0
                                           CS
           29
                 Brutus
                            1.0 33.0
                                           EΕ
      1
      2
           31
                 Lubber
                            8.0 55.5
                                         Econ
      3
           32
                   Andy
                            8.0 25.5
                                         Math
      4
           58
                           10.0 35.0
                                           CS
                  Rusty
      5
           64
                Horatio
                            7.0
                                 35.0
                                           CS
                                           CS
      6
           71
                  Zorba
                           10.0
                                 16.0
      7
                            9.0
           74
                Horatio
                                 35.0
                                         Math
      8
           85
                            4.0 25.5
                                        Music
                    Art
      9
           95
                    Bob
                             3.0 63.5
                                         Econ
      10 101
                             3.0
                                         Math
                   Joan
                                   NaN
      11
          107
               Johannes
                            {\tt NaN}
                                 35.0
                                          NaN
[63]: # and one more time, let's break this down step-by-step
      (sailors.major == 'CS')
[63]: 0
             True
      1
            False
      2
            False
      3
            False
      4
             True
      5
             True
      6
             True
      7
            False
            False
      8
      9
            False
      10
            False
            False
      11
      Name: major, dtype: bool
[65]: (sailors.rating >= 8.0)
```

```
[65]: 0
            False
            False
      1
      2
             True
      3
             True
      4
             True
      5
            False
      6
             True
      7
             True
      8
            False
      9
            False
      10
            False
      11
            False
      Name: rating, dtype: bool
[66]: (sailors.major == 'CS') & (sailors.rating >= 8.0)
[66]: 0
            False
      1
            False
      2
            False
      3
            False
      4
             True
      5
            False
      6
             True
      7
            False
            False
      8
      9
            False
      10
            False
      11
            False
      dtype: bool
[67]: sailors[(sailors.major == 'CS') & (sailors.rating >= 8.0)]
[67]:
         sid
              sname rating
                              age major
          58
                       10.0
      4
             Rusty
                             35.0
                                      CS
      6
          71 Zorba
                       10.0 16.0
                                      CS
[68]: # now let's do some multi-dataframe operations
      boats
[68]:
         bid
                  bname
                         color
      0 101
              Interlake
                          blue
      1 102
              Interlake
                           red
      2 103
                Clipper green
      3 104
                 Marine
                           red
[69]: reserves
```

```
[69]:
           sid
                  bid
                              date
          22.0
                101.0
      0
                      1998-10-10
      1
          22.0
                102.0
                       1998-10-10
      2
          22.0
                103.0
                      1998-10-08
      3
          22.0
                104.0 1998-10-07
      4
          31.0
                102.0 1998-10-11
          31.0
      5
                103.0 1998-11-06
                104.0 1998-11-12
          31.0
      6
      7
          64.0
                101.0 1998-09-05
                102.0
      8
          64.0
                      1998-09-02
      9
          74.0
                103.0 1993-09-08
      10
           NaN
                103.0
                       1998-09-09
           1.0
      11
                  {\tt NaN}
                       2001-01-11
      12
           1.0
                  NaN
                       2002-02-02
[70]: # we can do relational-style joins
      pd.merge(reserves, boats, on='bid')
[70]:
           sid
                  bid
                              date
                                        bname
                                               color
          22.0
                101.0
                       1998-10-10
                                    Interlake
                                                blue
      0
      1
          64.0
                101.0
                       1998-09-05
                                    Interlake
                                                blue
          22.0
                102.0
                      1998-10-10
                                    Interlake
      2
                                                  red
          31.0
                102.0 1998-10-11
      3
                                    Interlake
                                                  red
      4
          64.0
                102.0 1998-09-02
                                    Interlake
                                                  red
          22.0
                103.0 1998-10-08
      5
                                      Clipper
                                               green
      6
          31.0
                103.0 1998-11-06
                                      Clipper
                                               green
      7
          74.0
                103.0 1993-09-08
                                      Clipper
                                               green
      8
           {\tt NaN}
                103.0 1998-09-09
                                      Clipper
                                               green
      9
          22.0
                104.0
                       1998-10-07
                                       Marine
                                                  red
          31.0
               104.0 1998-11-12
      10
                                       Marine
                                                  red
[71]: pd.merge(reserves, boats, left_on='bid', right_on='bid')
[71]:
           sid
                  bid
                              date
                                        bname
                                               color
      0
          22.0
                101.0
                       1998-10-10
                                    Interlake
                                                blue
      1
          64.0
                101.0
                       1998-09-05
                                    Interlake
                                                blue
      2
          22.0
                102.0
                       1998-10-10
                                    Interlake
                                                  red
          31.0
                102.0
      3
                      1998-10-11
                                    Interlake
                                                  red
      4
          64.0
               102.0 1998-09-02
                                    Interlake
                                                  red
      5
          22.0
                103.0 1998-10-08
                                      Clipper
                                               green
          31.0
               103.0 1998-11-06
      6
                                      Clipper
                                               green
      7
          74.0
                103.0 1993-09-08
                                      Clipper
                                               green
                103.0 1998-09-09
      8
           {\tt NaN}
                                      Clipper
                                               green
      9
          22.0
                104.0 1998-10-07
                                       Marine
                                                  red
          31.0
                104.0 1998-11-12
      10
                                       Marine
                                                  red
```

```
[72]: # relational-style joins can be inner joins (the default)
      # or outer joins (left, right, outer)
      pd.merge(sailors, reserves, on='sid', how='left')
[72]:
          sid
                   sname
                           rating
                                     age
                                          major
                                                    bid
                                                                date
      0
            22
                  Dustin
                              7.0
                                   45.0
                                             CS
                                                  101.0
                                                         1998-10-10
      1
            22
                  Dustin
                              7.0
                                  45.0
                                             CS
                                                  102.0
                                                         1998-10-10
      2
            22
                              7.0 45.0
                                                  103.0
                  Dustin
                                             CS
                                                         1998-10-08
      3
            22
                  Dustin
                              7.0 45.0
                                             CS
                                                  104.0
                                                         1998-10-07
      4
            29
                  Brutus
                              1.0
                                   33.0
                                             EΕ
                                                    NaN
                                                                 NaN
      5
                              8.0
                                   55.5
            31
                  Lubber
                                           Econ
                                                  102.0
                                                         1998-10-11
      6
            31
                  Lubber
                              8.0
                                   55.5
                                           Econ
                                                  103.0
                                                         1998-11-06
      7
                                   55.5
            31
                  Lubber
                              8.0
                                           Econ
                                                  104.0
                                                          1998-11-12
      8
            32
                    Andy
                              8.0
                                   25.5
                                           Math
                                                    NaN
                                                                 NaN
      9
            58
                             10.0
                                   35.0
                                             CS
                   Rusty
                                                    NaN
                                                                 NaN
      10
            64
                 Horatio
                              7.0
                                   35.0
                                             CS
                                                  101.0
                                                         1998-09-05
      11
            64
                 Horatio
                              7.0
                                   35.0
                                             CS
                                                  102.0
                                                         1998-09-02
      12
            71
                             10.0
                                   16.0
                   Zorba
                                             CS
                                                    NaN
                                                                 NaN
      13
            74
                 Horatio
                              9.0
                                   35.0
                                           Math
                                                  103.0
                                                         1993-09-08
      14
            85
                     Art
                              4.0
                                   25.5
                                          Music
                                                    NaN
                                                                 NaN
      15
            95
                     Bob
                              3.0
                                   63.5
                                           Econ
                                                    NaN
                                                                 NaN
      16
          101
                    Joan
                              3.0
                                     NaN
                                           Math
                                                    NaN
                                                                 NaN
      17
          107
                                   35.0
                Johannes
                              NaN
                                            NaN
                                                    NaN
                                                                 NaN
[73]: pd.merge(sailors, reserves, left_on='sid', right_on='sid', how='outer')
[73]:
             sid
                     sname
                             rating
                                       age
                                            major
                                                      bid
                                                                  date
            22.0
      0
                    Dustin
                                7.0
                                     45.0
                                               CS
                                                    101.0
                                                           1998-10-10
      1
            22.0
                    Dustin
                                7.0
                                      45.0
                                               CS
                                                    102.0
                                                            1998-10-10
            22.0
      2
                    Dustin
                                7.0
                                     45.0
                                               CS
                                                    103.0
                                                           1998-10-08
                                      45.0
      3
           22.0
                    Dustin
                                7.0
                                               CS
                                                    104.0
                                                           1998-10-07
      4
            29.0
                                      33.0
                                               ΕE
                                                      NaN
                    Brutus
                                1.0
                                                                   NaN
      5
            31.0
                    Lubber
                                8.0
                                      55.5
                                             Econ
                                                   102.0
                                                           1998-10-11
      6
           31.0
                    Lubber
                                8.0
                                      55.5
                                             Econ
                                                   103.0
                                                            1998-11-06
                                                   104.0
      7
           31.0
                                      55.5
                    Lubber
                                8.0
                                             Econ
                                                            1998-11-12
            32.0
      8
                                8.0
                                      25.5
                                                      NaN
                      Andy
                                             Math
                                                                   NaN
      9
            58.0
                     Rusty
                               10.0
                                      35.0
                                               CS
                                                      NaN
                                                                   NaN
      10
            64.0
                   Horatio
                                7.0
                                      35.0
                                               CS
                                                    101.0
                                                            1998-09-05
            64.0
                                7.0
                                      35.0
                                               CS
                                                    102.0
                                                            1998-09-02
      11
                   Horatio
      12
           71.0
                     Zorba
                               10.0
                                      16.0
                                               CS
                                                      NaN
                                                                   NaN
      13
           74.0
                   Horatio
                                9.0
                                      35.0
                                             Math
                                                   103.0
                                                            1993-09-08
      14
           85.0
                        Art
                                4.0
                                      25.5
                                            Music
                                                      NaN
                                                                   NaN
      15
            95.0
                        Bob
                                3.0
                                      63.5
                                             Econ
                                                      NaN
                                                                   NaN
      16
          101.0
                       Joan
                                3.0
                                       NaN
                                             Math
                                                      NaN
                                                                   NaN
      17
          107.0
                  Johannes
                                NaN
                                      35.0
                                               NaN
                                                      NaN
                                                                   NaN
                                                           1998-09-09
      18
             NaN
                       NaN
                                NaN
                                       NaN
                                              NaN
                                                    103.0
```

```
19
            1.0
                      {\tt NaN}
                              {\tt NaN}
                                    {\tt NaN}
                                           {\tt NaN}
                                                   NaN
                                                        2001-01-11
      20
            1.0
                                                        2002-02-02
                      NaN
                              NaN
                                    {\tt NaN}
                                           NaN
                                                   NaN
[75]: # we can also do relational-style unions (and more) - but first
      # let's get some additional data, this time from a JSON file
      moreboats = pd.read_json("/Users/mikejcarey/SailingClub/MoreBoats.json",
       →lines='true')
[76]: boats
[76]:
         bid
                  bname color
      0 101
             Interlake
                          blue
      1 102
             Interlake
                           red
      2 103
                Clipper green
      3 104
                 Marine
                           red
[77]: moreboats
[77]:
         bid
                bname color
      0 201 Sunfish
                        blue
      1 202 Sunfish
                         red
      2 203
                Yacht green
      3 204
                Barge
                         red
[78]: pd.concat([boats, moreboats])
[78]:
         bid
                  bname color
      0 101
             Interlake
                          blue
      1 102 Interlake
                           red
      2 103
                Clipper green
      3 104
                 Marine
                           red
      0 201
                Sunfish
                          blue
      1 202
                Sunfish
                           red
      2 203
                  Yacht green
      3 204
                  Barge
                           red
[79]: # to do a more relational-style union (actually union all) we
      # should fix the rather odd indexing that we got above (:-))
      pd.concat([boats, moreboats], ignore_index=True)
[79]:
         bid
                  bname color
      0 101
             Interlake
                          blue
      1 102
             Interlake
                           red
      2 103
                Clipper
                        green
      3 104
                 Marine
                           red
```

```
4 201
                Sunfish
                          blue
      5 202
                Sunfish
                           red
      6 203
                  Yacht green
      7 204
                  Barge
                           red
[80]: # we can also do relational-style grouping and aggregation (and more)
      bymajor = sailors.groupby('major')
      bymajor
[80]: <pandas.core.groupby.generic.DataFrameGroupBy object at 0x7f8c20536e50>
[81]: bymajor.size()
[81]: major
      CS
               4
      ΕE
               1
               2
      Econ
     Math
               3
      Music
               1
      dtype: int64
[82]: bymajor.count()
[82]:
             sid sname rating age
     major
      CS
               4
                      4
                              4
                                    4
      ΕE
               1
                                    1
                      1
                               1
               2
                      2
                               2
                                    2
      Econ
      Math
               3
                      3
                               3
                                    2
     Music
               1
                      1
                                    1
[84]: bymajor.rating.max()
[84]: major
      CS
               10.0
      ΕE
                1.0
                8.0
      Econ
                9.0
      Math
     Music
                4.0
     Name: rating, dtype: float64
[85]: bymajor.max()[['rating','age']]
[85]:
             rating
                      age
     major
      CS
               10.0 45.0
```

```
EΕ
                1.0 33.0
      Econ
                8.0 63.5
      Math
                9.0
                     35.0
      Music
                4.0 25.5
[86]: bymajor.agg({'rating': ['min', 'max'], 'age': ['count', 'mean', 'std']})
[86]:
            rating
                           age
               min
                     max count
                                             std
                                 mean
      major
      CS
                             4 32.75
               7.0 10.0
                                      12.120919
      ΕE
               1.0
                     1.0
                             1 33.00
                                             NaN
               3.0
                                        5.656854
      Econ
                     8.0
                             2 59.50
      Math
               3.0
                     9.0
                             2 30.25
                                        6.717514
     Music
               4.0
                     4.0
                             1 25.50
                                             NaN
[87]: # we can do relational-style ordering and limiting as well
      bymajor.rating.max().sort_values(ascending=False)[:3]
[87]: major
      CS
              10.0
               9.0
      Math
               8.0
     Econ
      Name: rating, dtype: float64
[88]: # we can also extend a dataframe with a new column, e.g., dogage
      sailors.age / 7
[88]: 0
            6.428571
      1
            4.714286
      2
            7.928571
      3
            3.642857
      4
            5.000000
      5
            5.000000
      6
            2.285714
      7
            5.000000
      8
            3.642857
      9
            9.071429
      10
                 NaN
            5.000000
      11
      Name: age, dtype: float64
[89]: sailors.assign(dogage = sailors.age / 7)
```

```
[89]:
          sid
                   sname rating
                                          major
                                                    dogage
                                    age
           22
                              7.0
                                   45.0
                                             CS
                                                 6.428571
      0
                  Dustin
      1
           29
                  Brutus
                              1.0
                                   33.0
                                             ΕE
                                                 4.714286
      2
           31
                  Lubber
                              8.0
                                   55.5
                                           Econ
                                                 7.928571
      3
                                   25.5
           32
                    Andy
                              8.0
                                           Math
                                                 3.642857
      4
           58
                   Rusty
                             10.0
                                   35.0
                                             CS
                                                 5.000000
      5
                              7.0
                                   35.0
           64
                 Horatio
                                             CS
                                                 5.000000
           71
                   Zorba
                             10.0
                                   16.0
                                                 2.285714
      6
                                             CS
      7
           74
                 Horatio
                              9.0
                                   35.0
                                                 5.000000
                                           Math
                              4.0
                                   25.5
                                          Music
      8
           85
                     Art
                                                 3.642857
                                   63.5
      9
           95
                     Bob
                              3.0
                                           Econ
                                                 9.071429
      10
          101
                    Joan
                              3.0
                                    NaN
                                           Math
                                                       NaN
                                   35.0
                                                 5.000000
      11
          107
                Johannes
                              {\tt NaN}
                                            {\tt NaN}
[90]: # and remember, Python and dataframes are actual functional in nature, so no
      # no dataframes were harmed by the running of this Notebook's operations (:-))
      sailors
[90]:
          sid
                   sname
                          rating
                                    age
                                          major
                                   45.0
           22
                                             CS
                  Dustin
                              7.0
      0
                                             ΕE
      1
           29
                  Brutus
                              1.0
                                   33.0
      2
                              8.0
                                   55.5
           31
                  Lubber
                                           Econ
      3
           32
                    Andy
                              8.0
                                   25.5
                                           Math
      4
           58
                                             CS
                   Rusty
                             10.0
                                   35.0
      5
           64
                 Horatio
                              7.0
                                   35.0
                                             CS
      6
           71
                   Zorba
                             10.0
                                   16.0
                                             CS
      7
           74
                 Horatio
                              9.0
                                   35.0
                                           Math
                              4.0
                                   25.5
      8
           85
                     Art
                                          Music
      9
           95
                     Bob
                              3.0
                                   63.5
                                           Econ
      10
          101
                    Joan
                              3.0
                                    NaN
                                           Math
          107
                Johannes
                              NaN 35.0
                                            NaN
```

[]: