



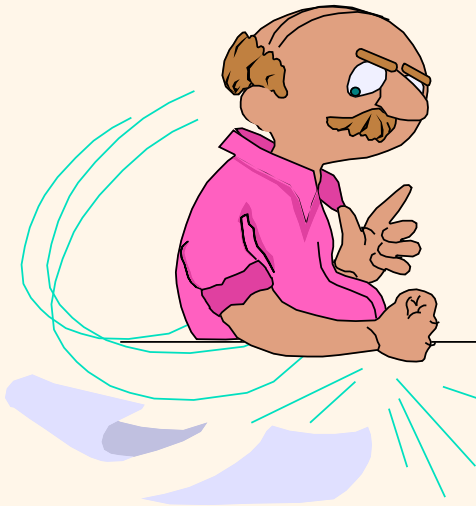
# *Introduction to Data Management*

*\*\*\* The “Flipped” Edition \*\*\**

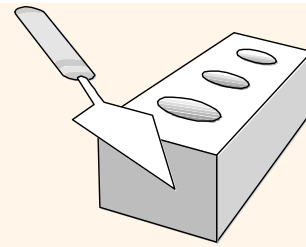
## *Lecture #11*

### *(Relational Languages III)*

Instructor: Mike Carey  
mjcarey@ics.uci.edu

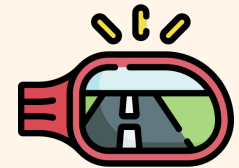


# Today's Notices



## ❖ SWOOSH HW series status

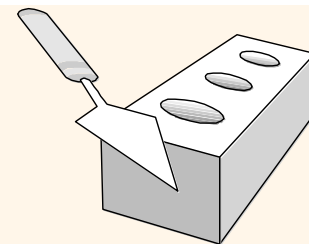
- HW1 is graded, HW2 grading is underway
- HW3 is open for business! (Due Wed at 6 PM)



## ❖ Midterm 1 info:

- See Piazza for the full set of rules (!)
  - In-person exam (using Gradescope)
  - Laptops needed (open *only* to Gradescope)
  - No cell phones or other devices permitted
  - No textbook access allowed
  - 2-sided hardcopy cheat sheet highly recommended





# Pre-Midterm Time Check!

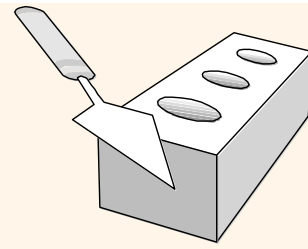
## Topic Coverage and Exam Schedule

### Syllabus

Topic	Reading (Required!)
Databases and DB Systems	Ch. 1
Entity-Relationship (E-R) Data Model	Ch. 6.1-6.5, 6.8-6.9
Relational Data Model	Ch. 2.1-2.4, 3.1-3.2
E-R to Relational Translation	Ch. 6.6-6.7
Relational Design Theory	Ch. 7.1-7.4.2
<b>Midterm Exam 1</b>	<b>Fri, Oct 22</b> (during lecture time)
Relational Algebra	Ch. 2.5-2.7
Relational Calculus	→ <a href="#">Wikipedia: Tuple relational calculus</a>
SQL Basics (SPJ and Nested Queries)	Ch. 3.3-3.5
SQL Analytics: Aggregation, Nulls, and Outer Joins	Ch. 3.6-3.9, 4.1
Advanced SQL: Constraints, Triggers, Views, and Security	Ch. 4.2, 4.4-4.5, 4.7
<b>Midterm Exam 2</b>	<b>Mon, Nov 15</b> (during lecture time)
Storage	Ch. 12.1-12.4, 12.6-12.7
Indexing	Ch. 14.1-14.4, 14.5
Physical DB Design	Ch. 14.6-14.7, 15.1-15.3, 15.5.3
Semistructured Data Management (a.k.a. NoSQL)	Ch. 8.1, → <a href="#">AsterixDB SQL++ Primer</a> , → <a href="#">Couchbase SQL++ Book</a>
Data Science 1: Advanced SQL Analytics	Ch. 5.5, 11.3
Data Science 2: Notebooks, Dataframes, and Python/Pandas	Lecture notes and Jupyter notebook
Basics of Transactions	Ch. 4.3, Ch. 17
<b>Endterm Exam</b>	<b>Fri, Dec 3</b> (during lecture time)

### Midterm Exam 1

Time: Fri, Oct 22, Lecture Time  
Place: SSLH 100



# TRC Formulas

## ❖ Atomic formula:

- $r \in R$ , or  $r \notin R$ , or  $r.a$  *op*  $s.b$ , or  $r.a$  *op* constant
- *op* is one of  $<$ ,  $>$ ,  $\leq$ ,  $\geq$ ,  $\neq$ ,  $=$

## ❖ Formula:

- an atomic formula, or
- $\neg P$ ,  $P \wedge Q$ ,  $P \vee Q$ , where  $P$  and  $Q$  are formulas, or
- $\exists r \in R (P(r))$ , where variable  $r$  is *free* in  $P(\dots)$ , or
- $\forall r \in R (P(r))$ , where variable  $r$  is *free* in  $P(\dots)$ , or
- $P \Rightarrow Q$  (pronounced “implies”, equivalent to  $(\neg P) \vee Q$ )

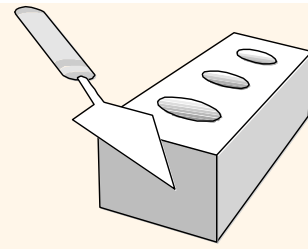
$\exists \forall \in \notin \neg \wedge \vee \Rightarrow = \neq < > \leq \geq$



# Free and Bound Variables

- ❖ The use of a **quantifier** such as  $\exists t \in T$  or  $\forall t \in T$  in a formula is said to bind  $t$ .
  - A variable that is **not bound** is free.
- ❖ Now let us revisit the definition of a **TRC query**:
  - $\{ t(a_1, a_2, \dots) \mid P(t) \}$
- ❖ There is an important restriction: the variable  $t$  that appears to the left of the  $\mid$  (“such that”) symbol must be the **only** free variable in the formula  $P(\dots)$ .
- ❖ Let's look at some examples...

# Find sailors with a rating above 7



Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

$$\{ s \mid s \in \text{Sailors} \wedge s.\text{rating} > 7 \}$$

❖ This is equivalent to the more general form:

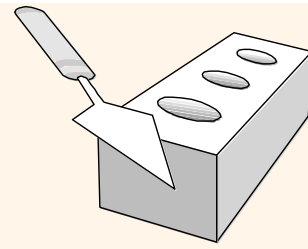
$$\{ t(\text{id}, \text{nm}, \text{rtg}, \text{age}) \mid \exists s \in \text{Sailors} \\ ( t.\text{id} = s.\text{sid} \wedge t.\text{nm} = s.\text{sname} \\ \wedge t.\text{rtg} = s.\text{rating} \wedge t.\text{age} = s.\text{age} \\ \wedge s.\text{rating} > 7 ) \}$$

(Q: See how each one specifies the answer's *schema* and values...?)

Note that the second query's result schema is **different** as we've specified it.

The Wikipedia article uses a very similar notation:  $\{t:\{\text{id}, \text{nm}, \text{rtg}, \text{age}\} \mid \dots\}$ .

*Find ids of sailors who are older than 30.0 or who have a rating under 8 and are named “Horatio”*



Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

$$\{ t(\text{sid}) \mid \exists s \in \text{Sailors} ( (s.\text{age} > 30.0 \\ \vee (s.\text{rating} < 8 \wedge s.\text{sname} = \text{“Horatio”})) \\ \wedge t.\text{sid} = s.\text{sid} ) \}$$

❖ Things to notice:

- Again, how result schema and values are specified
- Use of Boolean formula to specify the query constraints
- *Highly declarative nature of this form of query language!*

# Ex: TRC Query Semantics

## Sailors

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	4	25.5
95	Bob	3	63.5

sid	bid	date
22	101	10/10/98

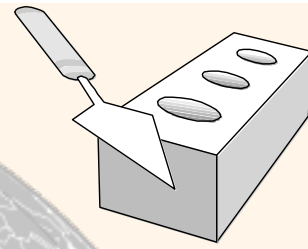
bid	bname	color
101	Interlake	blue

sid	sname	rating	age
22	Dustin	7	45.0

nid	nname	nvalue
1	Pi	3.14159...

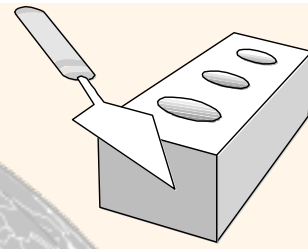
sid	sname	rating	age
66	Donald	0	73.0

⋮





# Ex: TRC Query Semantics



$t(a1, a2, \dots)$

## Sailors

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	4	25.5
95	Bob	3	63.5

sid	bid	date
22	101	10/10/98

bid	bname	color
101	Interlake	blue

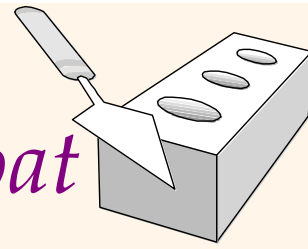
sid	sname	rating	age
22	Dustin	7	45.0

nid	nname	nvalue
1	Pi	3.14159...

sid	sname	rating	age
66	Donald	0	73.0

⋮

*Find names of sailors who've reserved a **red** boat*



Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

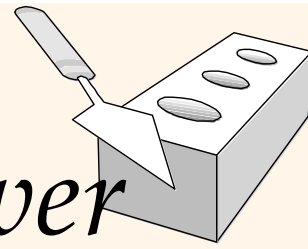
$$\{ t(\text{sname}) \mid \exists s \in \text{Sailors} (t.\text{sname} = s.\text{sname} \wedge \\ \exists r \in \text{Reserves} (r.\text{sid} = s.\text{sid} \wedge \\ \exists b \in \text{Boats} (b.\text{bid} = r.\text{bid} \wedge b.\text{color} = \text{'red'}))) \}$$

❖ Things to notice:

- Again, how result schema and values are specified
- How **joins** appear here as value-matching predicates
- *Highly declarative nature of this form of query language!*

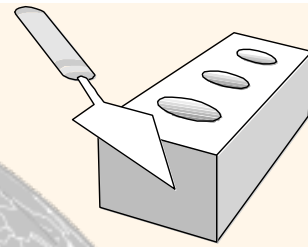
$\exists \forall \in \notin \neg \wedge \vee \Rightarrow = \neq < > \leq \geq$

# Unsafe Queries and Expressive Power



- ❖ It is possible to write syntactically correct calculus queries that have an *infinite* number of answers! Such queries are called unsafe.
  - E.g.,  $s \mid \neg (s \in \text{Sailors})$
- ❖ It is known that *every* query that can be expressed in relational algebra can be expressed as a *safe* query in DRC / TRC; the converse is also true.
- ❖ Relational Completeness: Query language (e.g., SQL) that can express every query that is expressible in the relational algebra/ (safe) calculus.

# Ex: TRC Query Safety



Sailors

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	4	25.5
95	Bob	3	63.5

$t(a1, a2, \dots)$

sid	bid	date
22	101	10/10/98

bid	bname	color
101	Interlake	blue

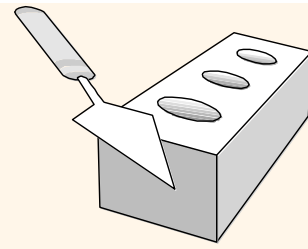
sid	sname	rating	age
22	Dustin	7	45.0

nid	nname	nvalue
1	Pi	3.14159...

sid	sname	rating	age
66	Donald	0	73.0



*Find ids of sailors who've reserved a **red** boat  
and a **green** boat*



Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

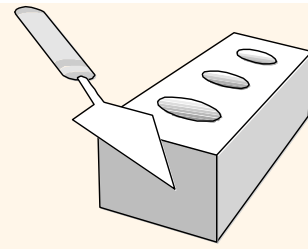
Boats(bid, bname, color)


$$\{ t(sid) \mid \exists s \in \text{Sailors } (t.sid = s.sid \wedge \\ \exists r1 \in \text{Reserves } (r1.sid = s.sid \wedge \\ \exists b1 \in \text{Boats } (b1.bid = r1.bid \wedge b1.color = 'red')) \wedge \\ \exists r2 \in \text{Reserves } (r2.sid = s.sid \wedge \\ \exists b2 \in \text{Boats } (b2.bid = r2.bid \wedge b2.color = 'green')))) \}$$

❖ Things to notice:

- This required *several* more variables! (Q: Why?)
- Q: Could we have done this with just s, **r**, b1, and b2? (And why?)
- Think of tuple variables as “fingers” pointing at the tables’ rows...

# Example: Tuple Variable Bindings



## Sailors

sid	sname	rating	age
22	Dustin	7	45.0
29	Brutus	1	33.0
31	Lubber	8	55.5
32	Andy	8	25.5
58	Rusty	10	35.0
64	Horatio	7	35.0
71	Zorba	10	16.0
74	Horatio	9	35.0
85	Art	4	25.5
95	Bob	3	63.5

(*Bindings at one point in time...*)

## Reserves

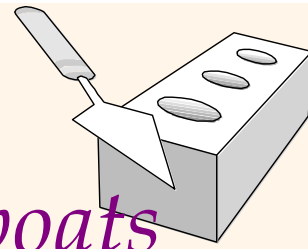
sid	bid	date
22	101	10/10/98
22	102	10/10/98
22	103	10/8/98
22	104	10/7/98
31	102	11/10/98
31	103	11/6/98
31	104	11/12/98
64	101	9/5/98
64	102	9/8/98
74	103	9/8/93

## Boats

bid	bname	color
101	Interlake	blue
102	Interlake	red
103	Clipper	green
104	Marine	red

r1  
r2

b1  
b2



*Find the names of sailors who've reserved all boats*

Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

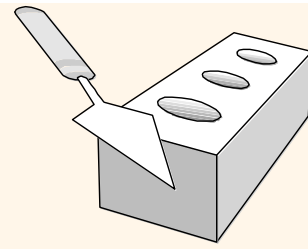
Boats(bid, bname, color)

$$\{ t(\text{sname}) \mid \exists s \in \text{Sailors} (t.\text{sname} = s.\text{sname} \wedge \\ \forall b \in \text{Boats} (\exists r \in \text{Reserves} (r.\text{sid} = s.\text{sid} \wedge \\ b.\text{bid} = r.\text{bid}) ) ) \}$$

*(For all boats  $b$ , sailor  $s$  has a reservation  $r$  for it)*

❖ Things to notice:

- Universal quantification addresses the “all” query use case
- *Highly declarative nature of this form of query language!*



## Find the names of sailors who've reserved all Interlake boats

Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

$\{ t(sname) \mid \exists s \in \text{Sailors}$   
 $(t.sname = s.sname \wedge$

*(For all boats  $b$ , if  $b$  is an 'Interlake' then sailor  $s$  has a reservation  $r$  for it)*

$\forall b \in \text{Boats } (b.bname = \text{'Interlake'} \Rightarrow (\exists r \in \text{Reserves}$   
 $(r.sid = s.sid \wedge b.bid = r.bid) ) ) ) \}$



❖ Or, if you prefer:

$\{ t(sname) \mid \exists s \in \text{Sailors}$   
 $(t.sname = s.sname \wedge$

*(For all boats  $b$ , either  $b$  is not an 'Interlake' or sailor  $s$  has a reservation  $r$  for it)*

$\forall b \in \text{Boats } (b.bname \neq \text{'Interlake'} \vee (\exists r \in \text{Reserves}$   
 $(r.sid = s.sid \wedge b.bid = r.bid) ) ) ) \}$





## Find the names of sailors who've reserved all Interlake boats (Gradescope-friendly version)

Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

{ t(sname) | **some** s **in** Sailors  
(t.sname = s.sname **and**

*(For all boats b, if b is an 'Interlake'  
then sailor s has a reservation r for it)*

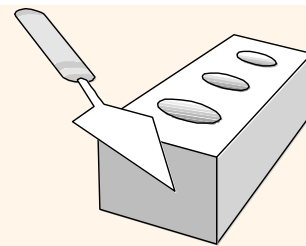
**all** b **in** Boats (b.bname = 'Interlake' **implies** (**some** r **in** Reserves  
(r.sid = s.sid **and** b.bid = r.bid) ) ) ) }

❖ Or, if you prefer:

{ t(sname) | **some** s **in** Sailors  
(t.sname = s.sname **and**

*(For all boats b, either b is not an 'Interlake'  
or sailor s has a reservation r for it)*

**all** b **in** Boats (b.bname **!=** 'Interlake' **or** (**some** r **in** Reserves  
(r.sid = s.sid **and** b.bid = r.bid) ) ) ) }



# Find the names of sailors who've reserved all Interlake boats ( 📱 -friendly version 😊)

Sailors(sid, sname, rating, age)

Reserves(sid, bid, date)

Boats(bid, bname, color)

{ t(sname) | 😊 Sailors s  
(t.sname = s.sname 🐜

*(For all boats b, if b is an 'Interlake' then sailor s has a reservation r for it)*

😊 Boats b (b.bname = 'Interlake' 👉 (😊 Reserves r  
(r.sid = s.sid 🐜 b.bid = r.bid) ) ) ) }



❖ Or, if you prefer:

{ t(sname) | 😊 Sailors s  
(t.sname = s.sname 🐜

*(For all boats b, either b is not an 'Interlake' or sailor s has a reservation r for it)*

😊 Boats b (b.bname 👉 = 'Interlake' 🚣 (😊 Reserves r  
(r.sid = s.sid 🐜 b.bid = r.bid) ) ) ) }

# Relational Calculus Summary



- ❖ Relational calculus is non-operational, so users define queries in terms of *what* they want and not in terms of *how* to compute it.  
(Declarativeness: “*What, not how!*”)
- ❖ Algebra and safe calculus subset have the same expressive power, leading to the concept of *relational completeness* for query languages.
- ❖ Two calculus variants: TRC (tuple relational calculus, which we’ve just studied) and DRC (domain relational calculus, not covered here).