



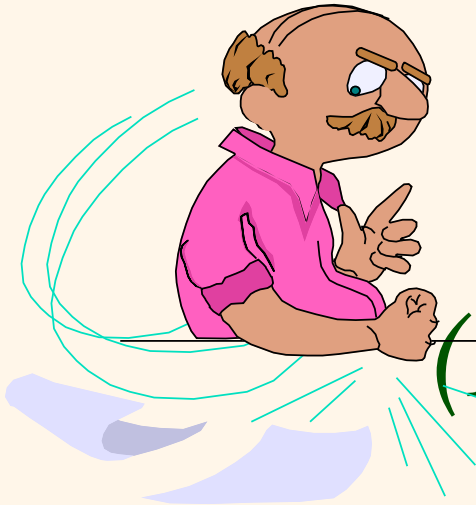
Introduction to Data Management

**** The “Flipped” Edition ****

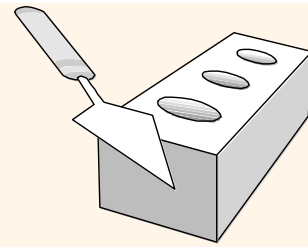
Lecture #8

(Relational Design Theory II)

Instructor: Mike Carey
mjcarey@ics.uci.edu

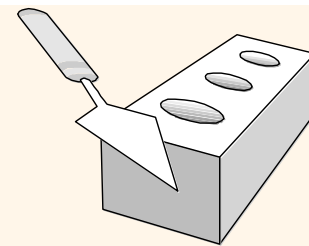


Today's Notices



- ❖ Keep one eye on the wiki page...
 - <http://www.ics.uci.edu/~cs122a/>
 - **Note the *Relational Design Theory* readings addition!**
- ❖ ... and the other eye on Piazza Q&A!
 - piazza.com/uci/fall2021/cs122aeecs116
- ❖ HW #2 should be well underway!
 - Its starting point: Our *HW #1 E-R solution*
 - **Make sure that you're using the very latest version!**





Quick Roadmap Check...

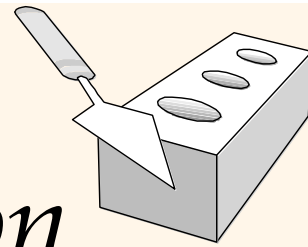
Topic Coverage and Exam Schedule

Syllabus


Topic	Reading (Required!)
Databases and DB Systems	Ch. 1
Entity-Relationship (E-R) Data Model	Ch. 6.1-6.5, 6.8-6.9
Relational Data Model	Ch. 2.1-2.4, 3.1-3.2
E-R to Relational Translation	Ch. 6.6-6.7
Relational Design Theory	Ch. 7.1-7.4.2
Midterm Exam 1	Fri, Oct 22 (during lecture time)
Relational Algebra	Ch. 2.5-2.7
Relational Calculus	⇒ Wikipedia: Tuple relational calculus
SQL Basics (SPJ and Nested Queries)	Ch. 3.3-3.5
SQL Analytics: Aggregation, Nulls, and Outer Joins	Ch. 3.6-3.9, 4.1
Advanced SQL: Constraints, Triggers, Views, and Security	Ch. 4.2, 4.4-4.5, 4.7
Midterm Exam 2	Mon, Nov 15 (during lecture time)
Storage	Ch. 12.1-12.4, 12.6-12.7
Indexing	Ch. 14.1-14.4, 14.5
Physical DB Design	Ch. 14.6-14.7, 15.1-15.3, 15.5.3
Semistructured Data Management (a.k.a. NoSQL)	Ch. 8.1, ⇒ AsterixDB SQL++ Primer , ⇒ Couchbase SQL++ Book
Data Science 1: Advanced SQL Analytics	Ch. 5.5, 11.3
Data Science 2: Notebooks, Dataframes, and Python/Pandas	Lecture notes and Jupyter notebook
Basics of Transactions	Ch. 4.3, Ch. 17
Endterm Exam	Fri, Dec 3 (during lecture time)

Midterm Exam 1

Time: Fri, Oct 22, Lecture Time
Place: SSLH 100





Web Tool for FDs & Normalization


**Griffith**
UNIVERSITY

Griffith Portal


Normalization Tool


 EDIT ATTRIBUTES


 LEARNING RESOURCES


 LOAD EXAMPLE


Functions


 FIND A MINIMAL COVER


 FIND ALL CANDIDATE KEYS

 CHECK NORMAL FORM

 NORMALIZE TO 2NF

 NORMALIZE TO 3NF METHOD 1

 NORMALIZE TO 3NF METHOD 2

 NORMALIZE TO BCNF

Attributes in Table

! Separate attributes using a comma (,)

a, b, c, d, e

Functional Dependencies

a × b ×

→

c ×

Delete

c ×

→

d × e ×

Delete

Add Another Dependency

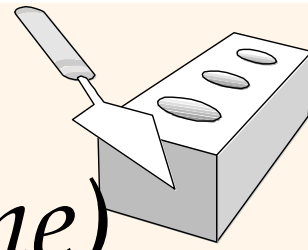
Save This Table

! Save this table to your PC and you can use it next time.

Filename to Save As:

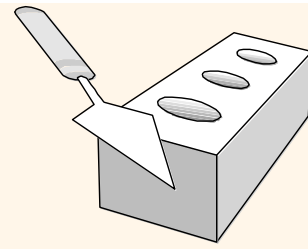
Save

http://www.ict.griffith.edu.au/normalization_tools/normalization/ind.php



Terms & Definitions (From Last Time)

- ❖ If X is part of a (candidate) key, we will say that X is a *prime attribute*.
- ❖ If X (an attribute set) contains a candidate key, we will say that X is a *superkey*.
- ❖ $X \rightarrow Y$ can be pronounced as “ X determines Y ”, or “ Y is functionally dependent on X ”.
- ❖ Some types of dependencies (*on a key*):
 - *Trivial*: $XY \rightarrow X$
 - *Partial*: XY is a key, $X \rightarrow Z$ (note that Y is absent)
 - *Transitive*: $X \rightarrow Y$, $Y \rightarrow Z$, Y is non-prime, $X \rightarrow Z$



Second Normal Form (2NF)

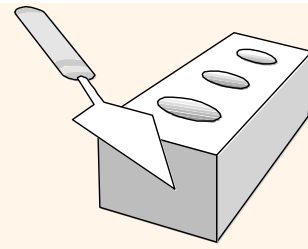
- ❖ Rel'n R is in **2NF** if it is in **1NF** and no non-prime attribute is *partially* dependent on a candidate key of R.
- ❖ Ex: Supplies(sno, sname, saddr, pno, pname, pcolor)
where: $\text{sno} \rightarrow \text{sname}$, $\text{sno} \rightarrow \text{saddr}$, $\text{pno} \rightarrow \text{pname}$, $\text{pno} \rightarrow \text{pcolor}$
 - Q1: What are the candidate keys for Supplies?
 - Q2: What are the prime attributes for Supplies?
 - Q3: Why is Supplies not in 2NF?



A1: (sno, pno)

A2: sno, pno

A3: *Each* of its four
FDs violates 2NF!



Third Normal Form (3NF)

- ❖ Rel'n R is in 3NF if it is in 2NF and it has no *transitive* dependencies to non-prime attributes.
- ❖ Ex: Workers(eno, ename, esal, dno, dname, dfloor)
where: $eno \rightarrow ename$, $eno \rightarrow esal$, $eno \rightarrow dno$, $dno \rightarrow dname$, $dno \rightarrow dfloor$

Q1: What are the candidate keys for Workers?

Q2: What are the prime attributes for Workers?

Q3: Why is Workers not in 3NF?

A1: eno

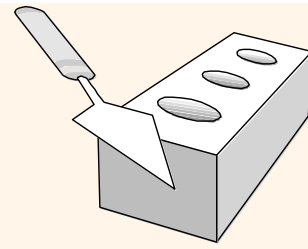
A2: eno

A3: Two inferable FDs,
 $eno \rightarrow dname$ and
 $eno \rightarrow dfloor$, each
violate 3NF.



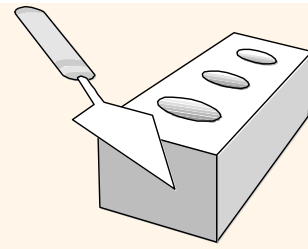
Note: A lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations is *always* possible.

Boyce-Codd Normal Form (**BCNF**)



- ❖ Rel'n R with FDs F is in **BCNF** if, for all $X \rightarrow A$ in F^+
 - $A \in X$ (*trivial* FD), or else
 - X is a *superkey* (i.e., X **contains a key**) for R .
- ❖ In other words, R is in BCNF if the **only** non-trivial FDs that hold over R are **key constraints** ($key \rightarrow attr$)
 - Everything depends on “the key, the whole key, and nothing but the key” (so help me Codd 😊)

Boyce-Codd Normal Form (Cont'd.)



❖ *Ex:* Supply2(sno, sname, pno)

Given FDs: sno \rightarrow sname, sname \rightarrow sno

Q1: What are the candidate keys for Supply2?

Q2: What are the prime attributes for Supply2?

Q3 Is Supply2 in 3NF?

Q4: Why is Supply2 not in BCNF?



Note: Overlapping...!

A1: (sno, pno), (sname, pno)

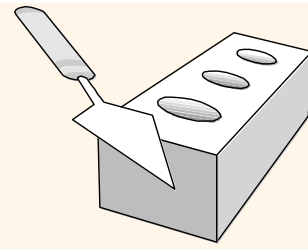
A2: sno, sname, pno

A3: Yes, it is in 3NF.

A4: Each of its FDs has a left-hand-side that isn't a candidate key. (Just a *part* of one.)

Warning: A lossless-join, *dependency-preserving* decomposition of R into a collection of BCNF relations **is not** always possible.

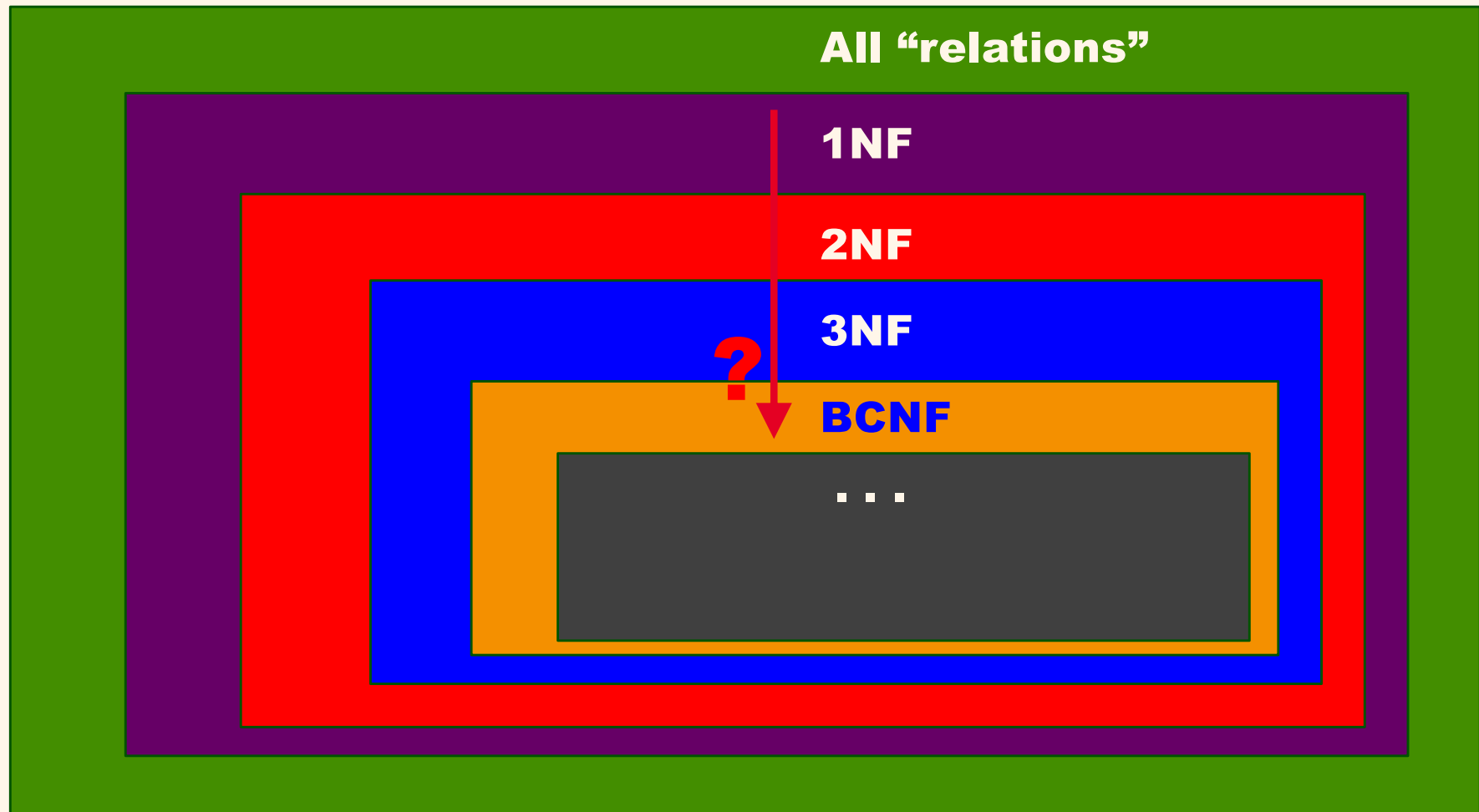
3NF Revisited (Alternative Def'n)



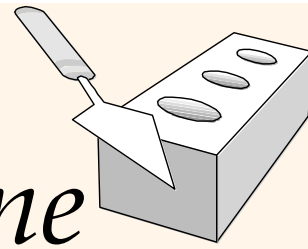
- ❖ Rel'n R with FDs F is in 3NF if, for all $X \rightarrow A$ in F^+
 - $A \in X$ (*trivial* FD), or else
 - X is a superkey (i.e., contains a key) for R , or else
 - A is part of some key for R (i.e., it's a prime attribute).
- ❖ If R is in BCNF, clearly it is also in 3NF.
- ❖ If R is in 3NF, some redundancy is possible. 3NF is a compromise to use when BCNF isn't achievable (e.g., no “good” decomp, or performance considerations).
*Again: A lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations **is always** possible.*



Achieving Normal Forms?



Decomposition of a Relation Scheme

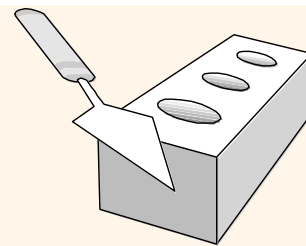


- ❖ Suppose a relation R contains attributes $A_1 \dots A_n$.
A decomposition of R consists of *replacing* R by two or more relations such that:
 - Each new relation contains a subset of the attributes of R (and no attributes that did not appear in R 😊), and
 - Every attribute of R appears as an attribute of at least one of the new relations.
- ❖ Intuitively, decomposing R means we will store instances of the relations that result from our decomposition *instead* of storing instances of R .
- ❖ E.g., decompose **SNLRWH** into **RW** and **SNLRH**...



An Example Decomposition

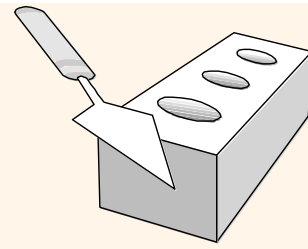
- ❖ Decompositions should be used (only) when needed.
 - Our **SNLRWH** has 2 FDs: $S \rightarrow \text{SNLRWH}$ and $R \rightarrow W$.
 - $R \rightarrow W$ violates 3NF (so W values are repeatedly associated with R values). The fix creates a relation **RW** to store the associations, then removes W from the main schema:
 - I.e.: Decompose **SNLRWH** into **SNLRH** and **RW**.
- ❖ The original information to be stored consisted of **SNLRWH** tuples. **Q:** If we store the “projections” of those tuples onto **SNLRH** and **RW**, are there any potential issues that we should be aware of? ... →



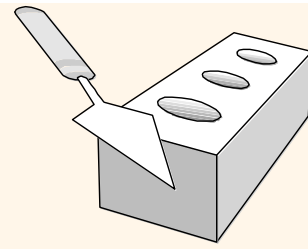
Decompositions: Possible Issues

- ❖ There are three potential “problems” to consider:
 1. Some queries will become more expensive.
 - E.g., how much did sailor Joe earn? ($W*H$ will require a join)
 2. Given instances of the decomposed relations, we may not be able to reconstruct the corresponding instance of the original relation! (If “lossy” ...)
 - Not a problem for the SNLRWH example! (Thanks to **R**)
 3. Checking some dependencies may require joining the instances of the decomposed relations.
 - Fortunately, also not a problem in the SNLRWH example.
- ❖ Tradeoff: Consider these issues *vs.* just tolerating the redundancy.

Lossless Join Decompositions

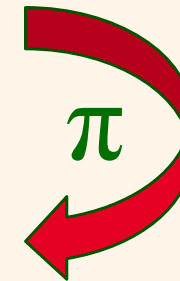


- ❖ Decomposition of **R** into **X** and **Y** is lossless-join w.r.t. a set of FDs **F** if, for every instance *r* that satisfies **F**:
 - $\pi_X(r) \bowtie \pi_Y(r) = r$ (Note: relational algebra 😊)
- ❖ It is always true that $r \subseteq \pi_X(r) \bowtie \pi_Y(r)$
 - In general, the other direction does not hold! If it does, then the decomposition is called *lossless-join*.
 - Must ensure that relations **X** and **Y** *overlap* and the overlap contains a key for *one* of the two relations. Ex: SNLRH + RW
- ❖ The definition extends to decomposition into three or more relations as you would expect.
- ❖ *Decompositions must be lossless! (Avoids Problem (2).)*



Ex: A Lossy Decomposition

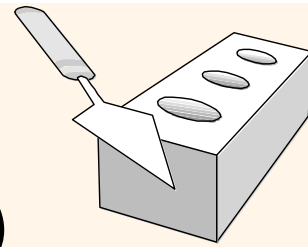
S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40



S	N	L	W	H
123-22-3666	Attishoo	48	10	40
231-31-5368	Smiley	22	10	30
131-24-3650	Smethurst	35	7	30
434-26-3751	Guldu	35	7	32
612-67-4134	Madayan	35	10	40

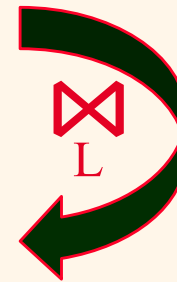
L	R
48	8
22	8
35	5
35	8

Ex: A Lossy Decomposition (cont.)



S	N	L	W	H
123-22-3666	Attishoo	48	10	40
231-31-5368	Smiley	22	10	30
131-24-3650	Smethurst	35	7	30
434-26-3751	Guldu	35	7	32
612-67-4134	Madayan	35	10	40

L	R
48	8
22	8
35	5
35	8

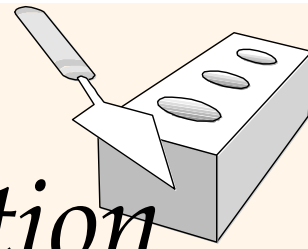


S5	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
131-24-3650	Smethurst	35	8	7	30
434-26-3751	Guldu	35	5	7	32
434-26-3751	Guldu	35	8	7	32
612-67-4134	Madayan	35	5	10	40
612-67-4134	Madayan	35	8	10	40

Whoops!

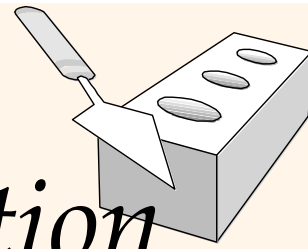
“Satisfaction guaranteed or double your data back...”





Dependency Preserving Decomposition

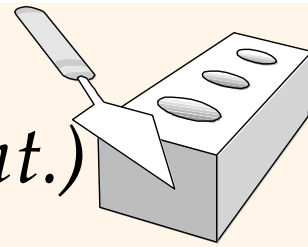
- ❖ Consider CSJDPOV, C is key, $JP \rightarrow C$ and $SD \rightarrow P$.
 - BCNF decomposition: Two tables **Part ID** V and SDP.
 - **Problem:** Checking $JP \rightarrow C$ now requires a join!
- ❖ **Dependency preserving decomposition** (intuitive):
 - I **ContractID** **Project ID** and Z, and we enforce the FDs that hold on R, and on Z, then all FDs that were given to hold on R must also hold. (Avoids Problem (3).)
- ❖ Projection of set of FDs F: If R is decomposed into X, ... projection of F into X (denoted F_X) is the set of FDs $U \rightarrow V$ in F^+ (**closure** of F) where **U, V are both in X**.



Dependency Preserving Decomposition

- ❖ Consider CSJDPQV, C is key, $JP \rightarrow C$ and $SD \rightarrow P$.
 - BCNF decomposition: Two tables, CSJDQV and SDP.
 - **Problem:** Checking $JP \rightarrow C$ now requires a join! (Oops)
- ❖ **Dependency preserving decomposition** (intuitive):
 - If R is decomposed into X, Y and Z, and we enforce the FDs that hold on X, on Y, and on Z, then all FDs that were given to hold on R must also hold. (Avoids Problem (3).)
- ❖ Projection of set of FDs F: If R is decomposed into X, ... projection of F into X (denoted F_X) is the set of FDs $U \rightarrow V$ in F^+ (**closure** of F) where U,V are **both** in X.

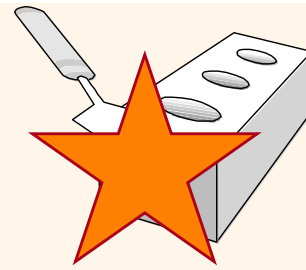
Dependency Preserving Decomp. (Cont.)



- ❖ The decomposition of R into two tables X and Y is dependency preserving if $(F_X \text{ union } F_Y)^+ = F^+$
 - I.e., if we consider only dependencies **in the closure** F^+ that can be checked in X **without** considering Y, and in Y **without** considering X, they *imply* all dependencies in F^+ !
- ❖ Important that we are talking about F^+ , **not** F, here:
 - Ex: EmpDeptMix(eid, email, ename, did, dname) with
 $\text{eid} \rightarrow \text{email}$, $\text{email} \rightarrow \text{eid}$, $\text{eid} \rightarrow \text{ename}$, $\text{email} \rightarrow \text{did}$, $\text{did} \rightarrow \text{dname}$
 - Emp(eid, email, ename) - $\text{eid} \rightarrow \text{email}$, $\text{email} \rightarrow \text{eid}$, $\text{eid} \rightarrow \text{ename}$
 - Dept(did, dname) - $\text{did} \rightarrow \text{dname}$
 - Work(eid, did) - $\text{eid} \rightarrow \text{did}$ (instead of $\text{email} \rightarrow \text{did}$)
- ❖ Dependency preserving does *not* imply lossless join:
 - Ex: ABC with $A \rightarrow B$, if decomposed into AB and C.

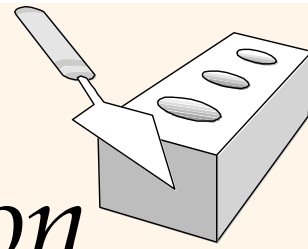
Must check for both!

Decomposing a Design into BCNF

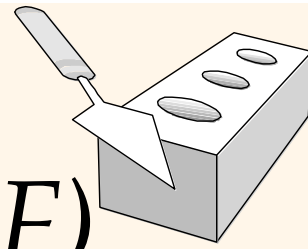


- ❖ Consider a relation R with FDs F . If $X \rightarrow Y$ violates BCNF, decompose R into $R-Y$ and XY . ($R-Y$ has X still!)
 - Repeated application of this idea will yield a collection of relations that are BCNF, a lossless join decomposition, and guaranteed to terminate. (Didn't say dependency preserving...)
- ❖ Ex: CSJDPQV with $C \rightarrow CSJDPQV$, $JP \rightarrow C$, $SD \rightarrow P$, and $J \rightarrow S$.
 - To deal with $SD \rightarrow P$, decompose into SDP, CSJDQV.
 - To deal with $J \rightarrow S$, decompose CSJDQV into JS and CJDQV.
- ❖ In general, several dependencies may violate BCNF. (The order that we process the dependencies in can lead to different decompositions, only some of which may be dependency preserving!)

BCNF and Dependency Preservation



- ❖ In general, there simply may not *be* a dependency preserving decomposition into BCNF.
 - E.g., $R(CSZ)$ with $CS \rightarrow Z$, $Z \rightarrow C$. (Candidate keys: CS , ZS)
 - Can't decompose and preserve the first FD; not in BCNF...
- ❖ Consider again decomposing the relation $CSJDPQV$ into the relations SDP , JS and $CJDQV$:
 - *Not* dependency preserving (*w.r.t.* $JP \rightarrow C$, $SD \rightarrow P$, $J \rightarrow S$).
 - However, it *is* indeed a lossless join decomposition.
 - In this case, *adding* relation JPC to the collection of relations would give us a dependency preserving decomposition.
 - But: JPC data would be used *only* for FD checking! (*Redundancy!*)



Decomposition into 3NF (vs. BCNF)

- ❖ The lossless join decomposition algorithm for BCNF can also be used to obtain a lossless join decomposition into 3NF (and might stop earlier).
- ❖ One idea to ensure dependency preservation:
 - If $X \rightarrow Y$ is not preserved in the resulting BCNF decomposition, add a relation XY .
 - Problem is that XY may violate 3NF (or even 2NF) due to other FDs, so this won't work in general.
- ❖ **The real fix:** Instead of using the *given* set of FDs F to guide the process, use a *minimal cover* for F to synthesize a decomposed schema.



Decomposition into 3NF (cont.)

- ❖ You are *not* going to be held responsible for being able to hand-generate a minimal cover and using it to synthesize a 3NF design...
 - There's an algorithm for that (see book for details)
 - There are tools that can do all this for you (see earlier [URL](#))
- ❖ But – in case you *are* curious, I'll go ahead and "cover" that material (see what I did there? 😊) in an addendum video that you can choose to watch at your own risk!
 - It's fine to skip the extra video if you aren't that curious...
- ❖ Let's instead proceed to apply the BCNF approach from three slides back to some actual examples!
 - In many practical cases this approach will yield a decomposition that turns out to be dependency preserving (and you can check)



Ex: Second Normal Form (2NF)

- ❖ Rel'n R is in **2NF** if it is in **1NF** and no non-prime attribute is *partially* dependent on a candidate key of R.
- ❖ Ex: Supplies(sno, sname, saddr, pno, pname, pcolor)

where: $sno \rightarrow sname$, $sno \rightarrow saddr$, $pno \rightarrow pname$, $pno \rightarrow pcolor$

Q1: What are the candidate keys for Supplies?

Q2: What are the prime attributes for Supplies?

Q3: Why is Supplies **not** in 2NF?

A1: (sno, pno)

A2: sno, pno

A3: *Each* of its four FDs violates 2NF!

Q4: So what's the fix?

Supplier(sno, sname, saddr)

Part(pno, pname, pcolor)

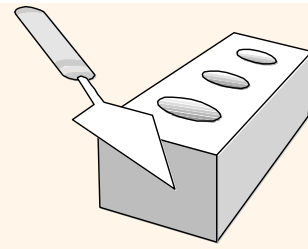
Supply(sno, pno)

Must not forget this!

(Else “lossy join”!)

Notice that...

- We first factored out **Supplier** based on the $sno \rightarrow \dots$ FDs
- We then factored out **Part** based on the $pno \rightarrow \dots$ FDs
- That left us with **Supply** so “all was not lost” ☺



Ex: Third Normal Form (3NF)

❖ Rel'n R is in 3NF if it is in 2NF and it has no *transitive* dependencies to non-prime attributes.

❖ Ex: Workers(eno, ename, esal, dno, dname, dfloor)

where: $\text{eno} \rightarrow \text{ename}$, $\text{eno} \rightarrow \text{esal}$, $\text{eno} \rightarrow \text{dno}$, $\text{dno} \rightarrow \text{dname}$, $\text{dno} \rightarrow \text{dfloor}$

Q1: What are the candidate keys for Workers?

Q2: What are the prime attributes for Workers?

Q3: Why is Workers not in 3NF?

Q4: So what's the fix?

Emp(eno, ename, esal, **dno**)

Dept(**dno**, dname, dfloor)

A1: eno

A2: eno

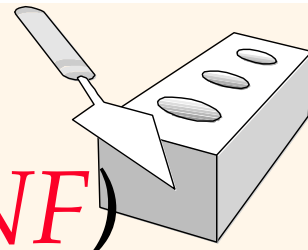
A3: Two inferable FDs, $\text{eno} \rightarrow \text{dname}$
and $\text{eno} \rightarrow \text{dfloor}$, each violate 3NF.

Don't forget this!
(Else "lossy join" !)

Notice that...

- We first factored out Dept based on the $\text{dno} \rightarrow \dots$ FDs
- That left us with Emp including **dno**, so again "all was not lost" ☺

Ex: Boyce-Codd Normal Form (BCNF)



- ❖ Rel'n R with FDs F is in **BCNF** if, for all $X \rightarrow A$ in F^+
 - $A \in X$ (*trivial* FD), or else
 - X is a superkey (i.e., X **contains a key**) for R.
- ❖ Ex: Supply2(sno, sname, pno)

Given FDs: $\text{sno} \rightarrow \text{sname}$, $\text{sname} \rightarrow \text{sno}$

Q1: What are the candidate keys for Supply2?

Q2: What are the prime attributes for Supply2?

Q3 Is Supply2 in 3NF?

Q4: Why is Supply2 not in BCNF?

Q5: So what's the fix?

Supplier2(sno, sname)

Supplies2(sno, pno)

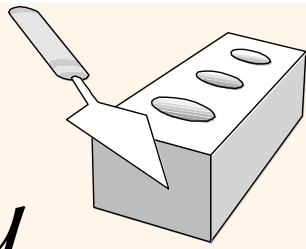
Notice that...

- We first factored out Supplier2 based on $\text{sno} \rightarrow \text{sname}$
- That left us with Supplies2 with sno so “all was not lost” ☺

Note: Overlapping...!

A1: (sno, pno), (sname, pno)
A2: sno, sname, pno
A3: Yes, it is in 3NF.
A4: Each of its FDs has a left-hand-side that isn't a candidate key. (Just a part of one.)

Relational Design Theory Summary



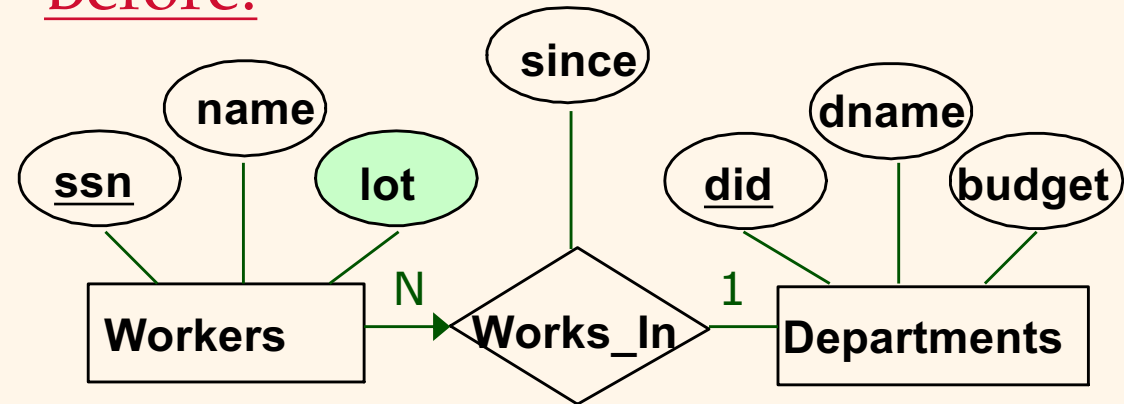
- ❖ If a relation is in **BCNF**, it is free of redundancies that can be detected using FDs. (Trying to ensure that all relations are in BCNF is thus a good goal.)
- ❖ If a relation is not in BCNF, we will decompose it into a lossless-join collection of BCNF relations.
 - Are all FDs preserved? If a lossless-join, dependency-preserving decomposition into BCNF is not possible, consider **3NF** instead.
 - Note: Decompositions should really be carried out while keeping *performance requirements* in mind. (More later!)



On Refining ER Based Designs

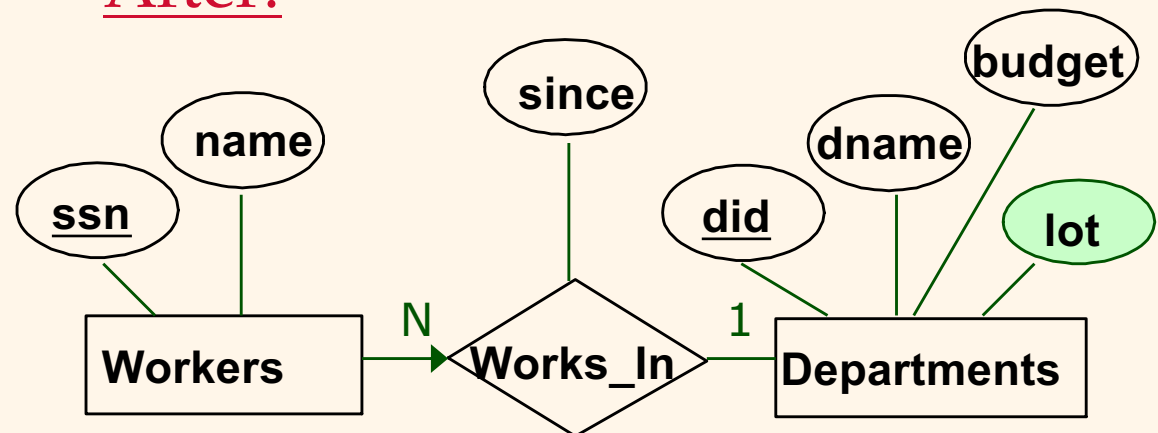
- ❖ 1st diagram translated:
Workers(S,N,L,D,C)
Departments(D,M,B)
(Lots associated with workers.)
- ❖ *Suppose all workers in a dept are assigned the same lot: $D \rightarrow L$ *
- ❖ Redundancy! Fixed by:
Workers2(S,N,D,C)
WorkersLots(D,L)
Departments(D,M,B)
- ❖ Can further fine-tune this:
Workers2(S,N,D,C)
Departments(D,M,B,L)

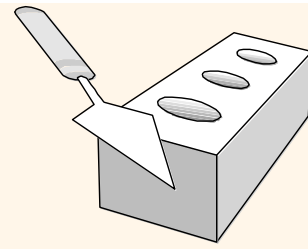
Before:



*Notice: Lot **wasn't** really a “Worker attribute”!*

After:





On Refining ER Based Designs

Before:

- ❖ 1st diagram translated:

Workers(S,N,L,D,C)

Departments(D,M,B)

(Lots associated with workers.)

- ❖ Note:

In many cases the relational translation of an ER design will take you right to 3NF (even BCNF)....!

- ❖ Redundant

Workers - Entity key \rightarrow attributes for entity sets.

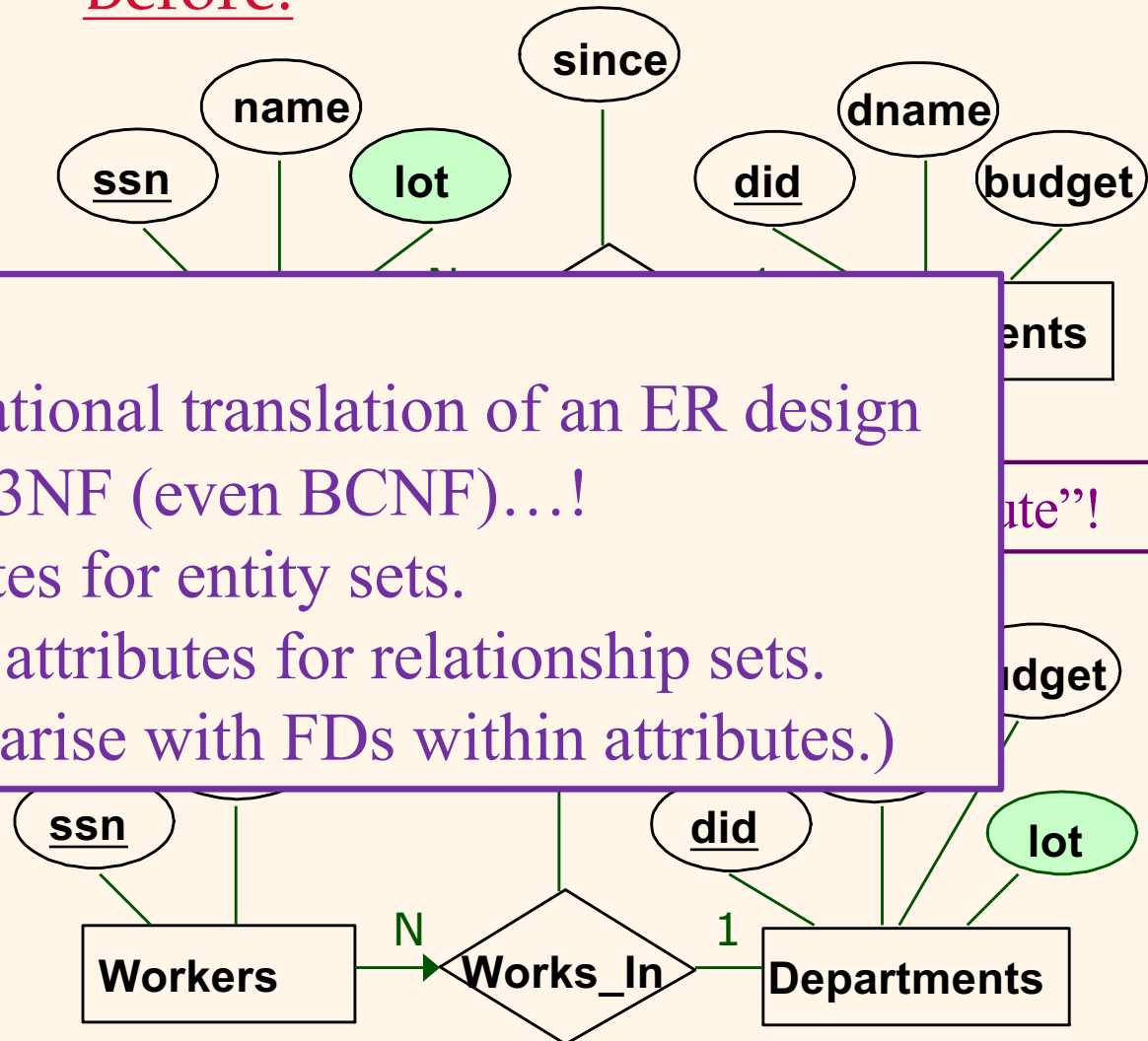
Workers - Relationship key \rightarrow attributes for relationship sets.

Departments (But problems could arise with FDs within attributes.)

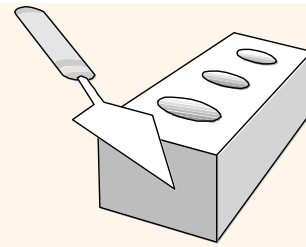
- ❖ Can further fine-tune this.

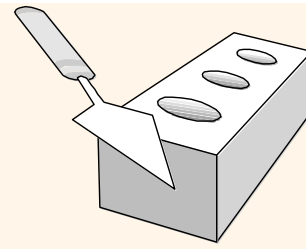
Workers2(S,N,D,C)

Departments(D,M,B,L)



Questions...?



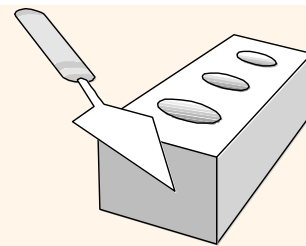


Addendum (3NF Schema Synthesis)



Minimal Cover for a Set of FDs

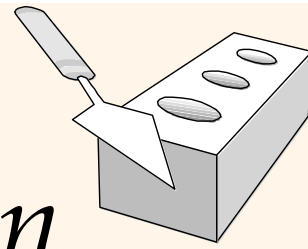
- ❖ Minimal cover **G** for a set of FDs **F**:
 - Closure of **G** = closure of **F**, i.e., $G^+ = F^+$.
 - Right hand side (RHS) of each FD in **G** is a *single* attribute.
 - If we change **G** by deleting any FD *or* deleting attributes from the LHS of any FD in **G**, the closure would change.
- ❖ Intuitively: Every FD in **G** is needed, with **G** being as “*as small as possible*” to have the same closure as **F**.
- ❖ E.g., $A \rightarrow B, ABCD \rightarrow E, EF \rightarrow GH, ACDF \rightarrow EG$ has the following minimal cover (trust me for now):
 - $A \rightarrow B, ACD \rightarrow E, EF \rightarrow G$ and $EF \rightarrow H$
- ❖ **M.C.** \rightarrow lossless-join, dep. pres. 3NF decomposition!



Computing the Minimal Cover

1. Put the set of given FDs in a Standard Form.
 - This turns F into a set G of equivalent FDs with a *single attribute* on the right-hand side of each FD.
2. Minimize the left-hand side of each FD in G .
 - For each FD in G , check each LHS attribute to see if it can be *deleted* without breaking the equivalence $G^+ = F^+$.
3. Delete redundant FDs.
 - For any FDs that remain, check to see if this FD can be *deleted* without breaking the equivalence $G^+ = F^+$.

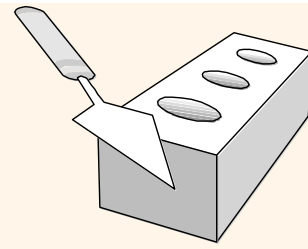
And voila – you now have a minimal cover for F ...!



Obtaining that 3NF Decomposition

- I. Compute F 's minimal cover G (which is also sometimes denoted as F^-).
- II. Search for dependencies in F^- that have the same attribute set on their left hand side, α :
 - a. $\alpha \rightarrow Y_1, \alpha \rightarrow Y_2, \dots, \alpha \rightarrow Y_k$
 - b. Construct one relation as $(\alpha, Y_1, Y_2, \dots, Y_k)$
 - c. Repeat this process for all of the FDs' α 's
 - d. If none of the relations from above contains a candidate key for the original relation R , add one more relation with (just) the attributes of a candidate key for R .

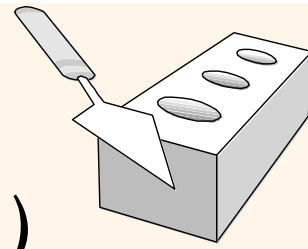
(Q: Why...?)



Testing Your Understanding...

- ❖ Now that you now how to compute BCNF and 3NF decompositions, try it on our earlier examples!
 - $\neq 2NF$: Supplies(sno, sname, saddr, pno, pname, pcolor)
with: $sno \rightarrow sname$, $sno \rightarrow saddr$, $pno \rightarrow pname$, $pno \rightarrow pcolor$
 - $\neq 3NF$: Workers(eno, ename, esal, dno, dname, dfloor)
with: $eno \rightarrow ename$, $eno, ename \rightarrow esal$, $eno \rightarrow dno$, $dno \rightarrow dname, dfloor$
 - $\neq BCNF$: Supply2(sno, sname, pno)
with: $sno \rightarrow sname$, $sname \rightarrow sno$

Note: I changed the $\neq 3NF$ example's FDs to be equivalent to our earlier FDs but messier to better illustrate the nature of the minimal cover algorithm's operation.



Testing Your Understanding (cont.)...

❖ $\neq 3NF$:

Workers(eno, ename, esal, dno, dname, dfloor)

with: $eno \rightarrow ename$, $eno, ename \rightarrow esal$, $eno \rightarrow dno$, $dno \rightarrow dname, dfloor$

3NF M.C. step 1: 3NF M.C. step 2:

$eno \rightarrow ename$

$eno, ename \rightarrow esal$ \rightarrow $eno \rightarrow esal$

$eno \rightarrow dno$

$dno \rightarrow dname$

$dno \rightarrow dfloor$

3NF step II:

Emp(eno, ename, esal, **dno**)

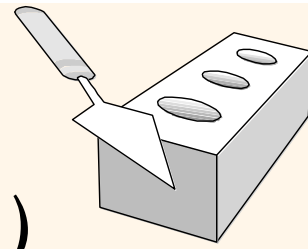
Dept(**dno**, dname, dfloor)

Q1: What is the attribute closure of eno – and what does that mean...?

We got lucky!
(No **lossy join**!)



Q2: What if the Emp-Dept relationship had been M:N?



Testing Your Understanding (cont.)...

❖ $\neq 3NF$:

Workers(eno, ename, esal, dno, dname, dfloor)

with: $eno \rightarrow ename$, $eno, ename \rightarrow esal$, $eno \rightarrow dno$, $dno \rightarrow dname, dfloor$

$eno \rightarrow ename$

$eno, ename \rightarrow esal \rightarrow eno \rightarrow esal$

$eno \rightarrow dno$

$dno \rightarrow dname$

$dno \rightarrow dfloor$

$\{eno\}$

$\{eno, ename\}$

$\{eno, ename, esal\}$

$\{eno, ename, esal, dno\}$

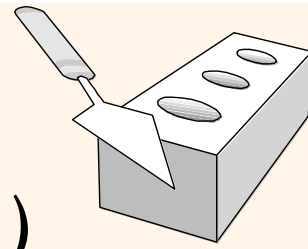
$\{eno, ename, esal, dno, dname\}$

$\{eno, ename, esal, dno, dname, dfloor\}$

Q1: What is the attribute closure of eno – and what does that mean...?

\rightarrow That's everything in Workers! (*Thus...?*)





Testing Your Understanding (cont.)...

❖ $\neq 3NF$ (modified to $M:N$):

Workers(eno, ename, esal, dno, dname, dfloor)

with: $eno \rightarrow ename$, $eno, ename \rightarrow esal$, ~~$eno \rightarrow dno$~~ , $dno \rightarrow dname, dfloor$

$eno \rightarrow ename$

$eno, ename \rightarrow esal \rightarrow eno \rightarrow esal$

~~$eno \rightarrow dno$~~

$dno \rightarrow dname$

$dno \rightarrow dfloor$

Q2: What if the Emp-Dept relationship had been $M:N$?

Without Works we'd have a **lossy join...**!



Emp(eno, ename, esal, ~~dno~~)

Dept(~~dno~~, dname, dfloor)

Works(eno, ~~dno~~)

Questions...?

