

## Introduction to Data Management



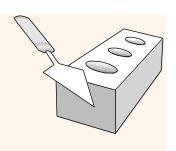
Lecture #7 (Relational Design Theory)

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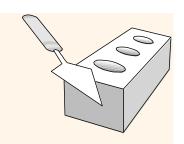


## Today's Notices





- \* Keep one eye on the wiki page...
  - http://www.ics.uci.edu/~cs122a/
- ... and the other eye on Piazza Q&A!
  - piazza.com/uci/fall2021/cs122aeecs116
- ❖ HW #1 is now in the rearview mirror
  - Thursday at 6PM is/was the drop-dead deadline
  - Ask questions in "lecture"/discussions/Piazza
- ❖ HW #2 is your next destination
  - Its starting point is *HW #1's solution (!)*
  - We never want you to be bored in this class...



## Quick Roadmap Check...

#### **Topic Coverage and Exam Schedule**

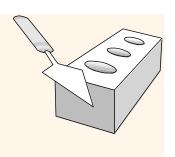
#### **Syllabus**

Topic	Reading (Required!)			
Databases and DB Systems	Ch. 1			
Entity-Relationship (E-R) Data Model	Ch. 6.1-6.5, 6.8-6.9			
Relational Data Model	Ch. 2.1-2.4, 3.1-3.2			
E-R to Relational Translation	Ch. 6.6-6.7			
Relational Design Theory	Ch. 7.1-7.4.1			
Midterm Exam 1	Fri, Oct 22 (during lecture time)			
Relational Algebra	Ch. 2.5-2.7			
Relational Calculus	→ Wikipedia: Tuple relational calculus			
SQL Basics (SPJ and Nested Queries)	Ch. 3.3-3.5			
SQL Analytics: Aggregation, Nulls, and Outer Joins	Ch. 3.6-3.9, 4.1			
Advanced SQL: Constraints, Triggers, Views, and Security	Ch. 4.2, 4.4-4.5, 4.7			
Midterm Exam 2	Mon, Nov 15 (during lecture time)			
Storage	Ch. 12.1-12.4, 12.6-12.7			
Indexing	Ch. 14.1-14.4, 14.5			
Physical DB Design	Ch. 14.6-14.7, 15.1-15.3, 15.5.3			
Semistructured Data Management (a.k.a. NoSQL)	Ch. 8.1, → AsterixDB SQL++ Primer, → Couchbase SQL++ Book			
Data Science 1: Advanced SQL Analytics	Ch. 5.5, 11.3			
Data Science 2: Notebooks, Dataframes, and Python/Pandas	Lecture notes and Jupyter notebook			
Basics of Transactions	Ch. 4.3, Ch. 17			
Endterm Exam	Fri, Dec 3 (during lecture time)			

#### Midterm Exam 1

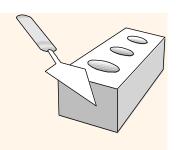
Time: Fri, Oct 22, Lecture Time

Place: SSLH 100



## Reasoning About FDs

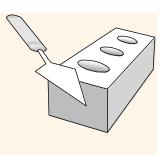
- Given some FDs, we can usually infer additional FDs:
  - $ssn \rightarrow did$ ,  $did \rightarrow lot$  implies  $ssn \rightarrow lot$
  - (Translation: *Matching ssns* imply matching *lots*.)
- \* An FD f is <u>implied by</u> a set of FDs F if f holds whenever all FDs in F hold.
  - $F^+ = closure\ of\ F$  is the set of all FDs that are implied by F.
- \* Armstrong's Axioms (X, Y, Z are *sets* of attributes):
  - Reflexivity: If  $X \subseteq Y$ , then  $Y \to X$
  - Augmentation: If  $X \rightarrow Y$ , then  $XZ \rightarrow YZ$  for any Z
  - <u>Transitivity</u>: If  $X \to Y$  and  $Y \to Z$ , then  $X \to Z$
- \* These are *sound* and *complete* inference rules for FDs!



## Armstrong's Axioms: Examples

pno	name	title	state	zip
1	Sandy	Professor	CA	92697
2	Joe	Jim Gray Professor	CA	94720
3	Anhai	Professor	WI	53706
4	Alex	Associate Professor	CA	92697

- $\clubsuit$  *Reflexivity*: If X⊆Y then Y $\to$ X:
  - $zip \subseteq (zip, name)$ , so  $(zip, name) \rightarrow zip$ .
- $\star \underline{Augmentation}$ : If X $\rightarrow$ Y then XZ $\rightarrow$ YZ for any Z:
  - $zip \rightarrow state$ , so  $(zip, title) \rightarrow (state, title)$ .
- \* *Transitivity*: If  $X \rightarrow Y$  and  $Y \rightarrow Z$  then  $X \rightarrow Z$ :
  - $pno \rightarrow zip$  and  $zip \rightarrow state$ , so  $pno \rightarrow state$ .



# Reasoning About FDs (Cont'd.)

(Recall: "two matching X's always have the same Y")

- \* A few additional rules (which follow from AA):
  - <u>Union</u>: If  $X \to Y$  and  $X \to Z$ , then  $X \to YZ$
  - *Decomposition*: If  $X \to YZ$ , then  $X \to Y$  and  $X \to Z$
- \* Example: Contracts(cid,sid,pjid,did,pid,qty,value), and:
  - The **c**ontract id is the key:  $\mathbb{C} \to \mathbb{C}$
  - A project purchases each part using single contract:  $JP \rightarrow C$
  - A dept purchases at most one part from a supplier:  $SD \rightarrow P$
- \* JP $\rightarrow$ C, C $\rightarrow$  CSJDPQV imply (JP) $\rightarrow$  CSJDPQV
- $\star$  SD  $\to$  P implies SDJ  $\to$  JP (New candidate keys...!)
- $\star$  SDJ  $\to$  JP, JP  $\to$  CSJDPQV imply (SDJ)  $\to$  CSJDPQV

## Reasoning About FDs (Examples)

Let's consider R(ABCDE),  $F = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E\}$ 

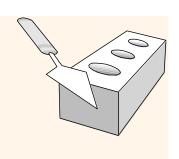
- ❖ Let's work our way towards inferring F+ ...
- (a)  $A \rightarrow B$  (b)  $B \rightarrow C$  (c)  $CD \rightarrow E$
- (d)  $A \rightarrow C$
- BD→CD
- $BD \rightarrow E$
- AD→CD
- (h)  $AD \rightarrow E$
- (j)  $AD \rightarrow D$  $AD \rightarrow C$
- (k) AD→BD
- (1)  $AD \rightarrow B$
- (n)  $AD \rightarrow ABCDE$

Candidate key!

*Note*: If some attribute *X* is not on the RHS of any initial FD, then X must be part of the key!

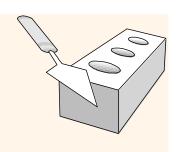
#### (given)

- (a, b, and transitivity)
- (b and augmentation)
- (e, c and transitivity)
- (d and augmentation)
- (g, c and transitivity)
- (g and decomposition)
- (a and augmentation)
- (k and decomposition)
- (a and reflexivity)
- (h, i, j, l, m, and union)



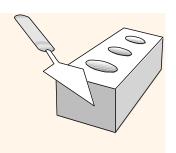
# Reasoning About FDs (Cont'd.)

- Computing the closure of a set of FDs can be very expensive. (Closure size is exponential in # of attrs!)
- \* Typically, we just want to check if a *specific* FD  $X \rightarrow Y$  is *in* the closure of a set of FDs F. An efficient check:
  - **First**: Compute *attribute closure* of *X* (denoted **X+**) w.r.t. *F*:
    - Set of all attributes A such that  $X \rightarrow A$  is in F+ (i.e., all F+ attributes)
    - There is a *linear time algorithm* to compute this (look <u>here</u>): Start with *X* and keep adding attributes that can (now) be inferred via the FDs
  - Then: Check to see if Y is in X+
- ❖ Does  $\mathbf{F} = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E\} \text{ imply } A \rightarrow E$ ?
  - I.e.: Is  $A \rightarrow E$  in the closure F+? Equivalently: Is E in A+?



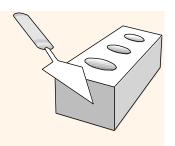
#### FDs & Redundancy

- Role of FDs in detecting redundancy in a schema:
  - Consider a relation R with three attributes, say R(ABC).
    - If **no** (non-trivial) FDs hold: There is *no redundancy* here then. (Think about this ... in fact, think *hard*...!)
      - *Ex:* Prescriptions(doc\_name, patient\_name, drug\_name)
    - Given A → B: Several tuples could have the same A value and if so, then they'll all have the same B value as well! Thus, if A is repeated for some reason, it will always have the same B "tagging along for the ride".
      - Ex: Employee(emp\_name, dept\_no, mgr\_name)
        (Redundancy here if dept\_no → mgr\_name!)

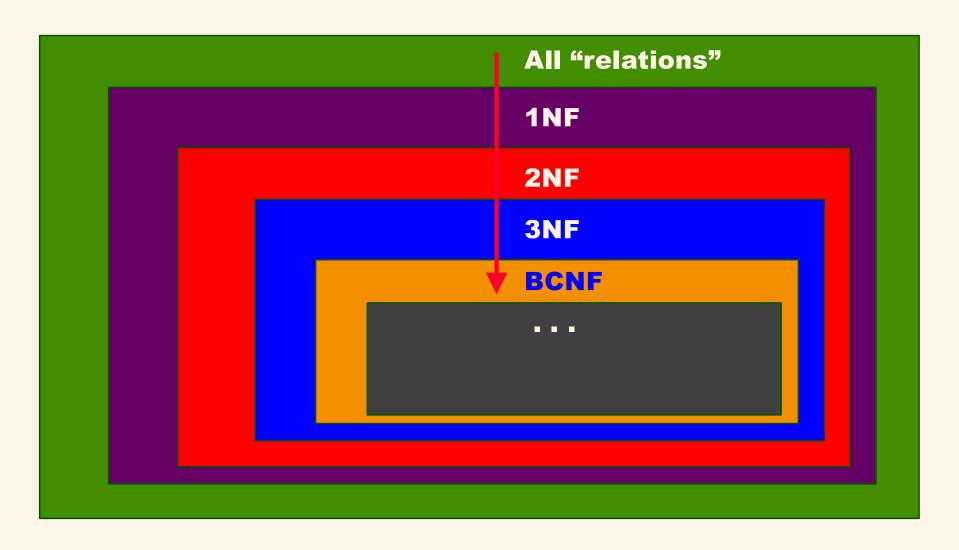


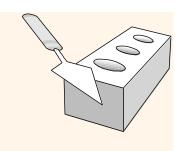
#### Normal Forms

- \* Returning to the issue of schema refinement, the first question to ask is whether any refinement is needed!
- \* We will define various *normal forms* (BCNF, 3NF etc.) based on the nature of FDs that hold.
- Depending upon the normal form a relation is in, it has a different level of redundancy.
  - E.g., a BCNF relation has NO redundancy (as you'll learn).
- Checking which normal form a given relation is in will help us decide if we need to decompose (fix) it.
  - E.g., there's no need to decompose a BCNF relation!



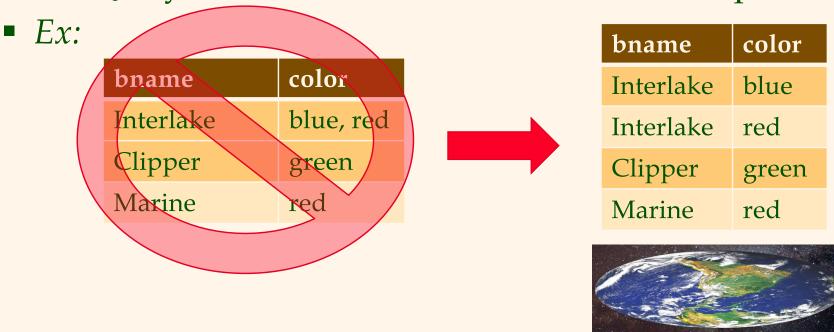
#### Normal Forms





#### First Normal Form (1NF)

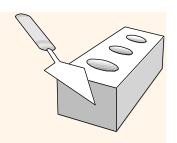
- \* Rel'n R is in 1NF if all of its attributes are atomic.
  - No set-valued attributes! (1NF = "flat" ②)
  - Usually goes *w/o* saying for relational model (but not for *NoSQL* systems, as we'll see at the end of the quarter ©).



(1NF is different than the other normal forms.)

# Some Terms and Definitions (Review)

- \* If X is part of a (candidate) key, we will say that X is a *prime attribute*.
- \* If X (an attribute set) contains a candidate key, we will say that X is a *superkey*.
- \*  $X \rightarrow Y$  can be pronounced as "X determines Y", or "Y is functionally dependent on X".
- \* Some types of dependencies (on a key):
  - Trivial:  $XY \rightarrow X$
  - *Partial*: **X**Y is a key,  $X \rightarrow Z$  (note that Y is absent)
  - *Transitive*:  $X \rightarrow Y$ ,  $Y \rightarrow Z$ , Y is non-prime,  $X \rightarrow Z$



#### To Be Continued....

