## 1. Yes, proof:

$$\begin{array}{lll} f(n) & <= & cg(n) & ; \ \forall n \geq n0 \\ 3n+9 & <= & c \ (n \land 3) & ; \ \forall n \geq n0 \end{array}$$

let 
$$n0 = 1$$
,  $c = 12$ ; then

$$3n + 9 <= 12 (n^3); \forall n \ge 1$$

## 2. No, by definition, we have:

$$\begin{array}{lll} f(n) & >= & cg(n) & ; \ \forall n \geq n0 \\ 3n+9 & >= & c \ (n \land 3) & ; \ \forall n \geq n0 \end{array}$$

Since  $(n^3)$  increases at a faster rate than (3n) as n goes to positive infinity, there is no positive value (c) that will make the above inequality valid.