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1a Generate a vector of integers from 1 to 100. Compute $PX(x)$ (using `mygeometricpmf(p, x)`) for each element in the vector. Use p-values of 0.2, 0.5, and 0.9.

Ans.

```
x = [1:1:100];
```

```
p1 = 0.2;
```

```
p2 = 0.5;
```

```
p3 = 0.9;
```

```
%a
```

```
ai = mygeometricpmf(p1, x);
```

```
ai =
```

Columns 1 through 10

```
0.2000 0.1600 0.1280 0.1024 0.0819 0.0655 0.0524 0.0419 0.0336 0.0268
```

Columns 11 through 20

```
0.0215 0.0172 0.0137 0.0110 0.0088 0.0070 0.0056 0.0045 0.0036 0.0029
```

Columns 21 through 30

```
0.0023 0.0018 0.0015 0.0012 0.0009 0.0008 0.0006 0.0005 0.0004 0.0003
```

Columns 31 through 40

```
0.0002 0.0002 0.0002 0.0001 0.0001 0.0001 0.0001 0.0001 0.0000 0.0000
```

Columns 41 through 50

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 51 through 60

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 61 through 70

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 71 through 80

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 81 through 90

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 91 through 100

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

```
a11 = mygeometricpmf(p1, x);
a12 = mygeometricpmf(p2, x);
a21 = mygeometricpmf(p1, x);
a22 = mygeometricpmf(p2, x);
```

a ii =

Columns 1 through 10

0.5000 0.2500 0.1250 0.0625 0.0313 0.0156 0.0078 0.0039 0.0020 0.0010

Columns 11 through 20

0.0005 0.0002 0.0001 0.0001 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 21 through 30

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 31 through 40

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 41 through 50

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 51 through 60

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 61 through 70

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 71 through 80

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 81 through 90

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

Columns 91 through 100

0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000

```
a_iii = mygeometricpmf(p3, x);  
a_iii =
```

Columns 1 through 10

```
0.9000 0.0900 0.0090 0.0009 0.0001 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 11 through 20

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 21 through 30

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 31 through 40

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 41 through 50

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 51 through 60

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 61 through 70

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 71 through 80

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 81 through 90

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

Columns 91 through 100

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000
```

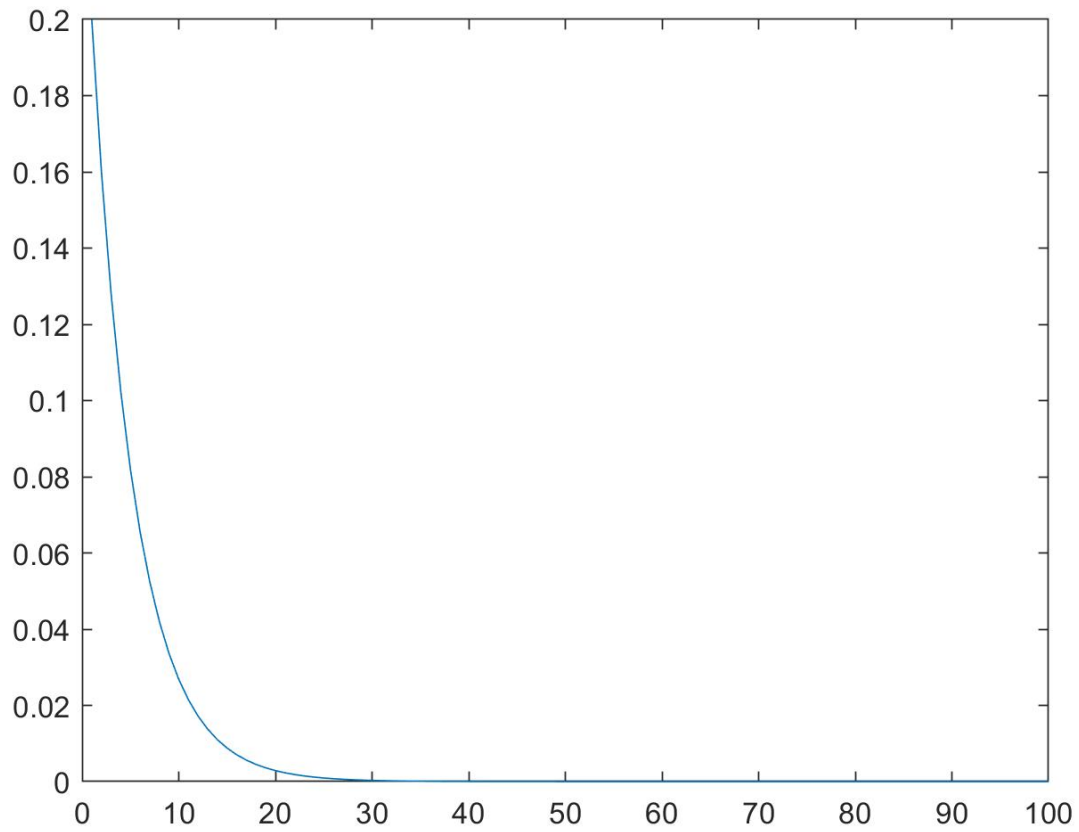
```
function f = mygeometricpmf(p,x)  
    f = p.*(1-p).^(x-1);  
end
```

1b. Plot $PX(x)$ for this vector of x . Generate plots for each value of p

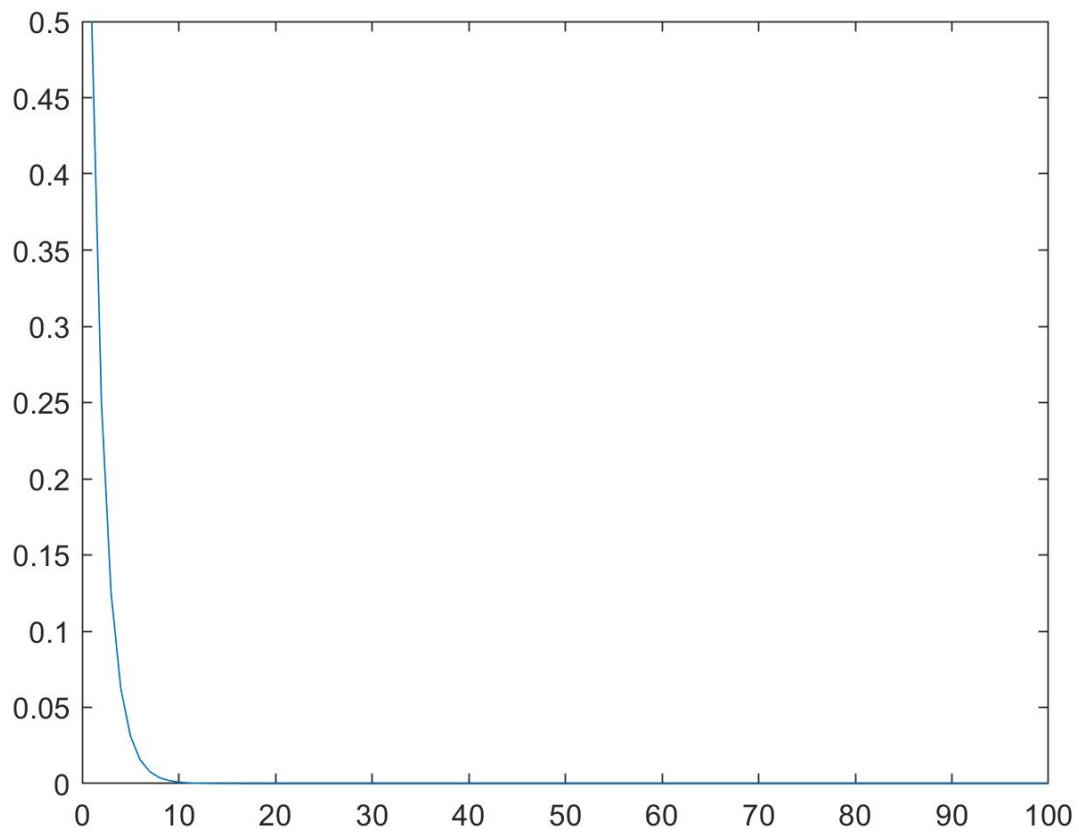
Ans.

%b

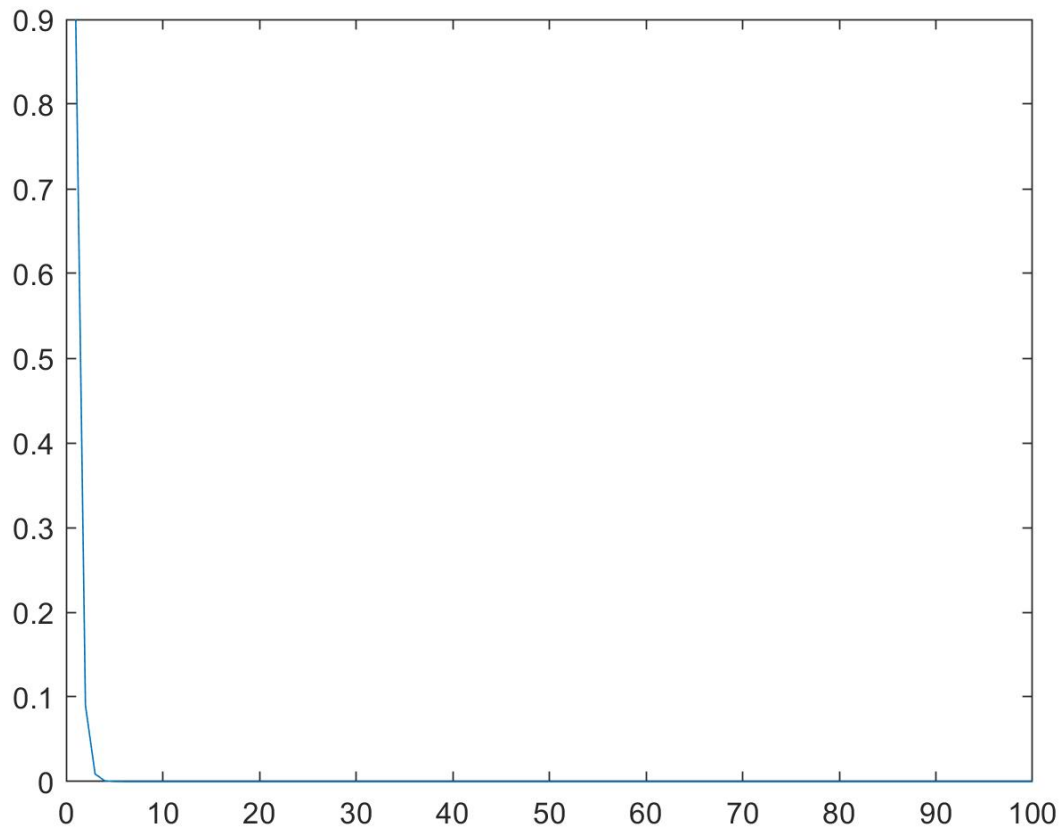
plotAi = plot(ai)



```
plotAii = plot(aii)
```



`plotAiii = plot(aiii)`



1c. Compute $E[X]$ for this vector of integers using the function that you implemented above. Compute $E[X]$ for each value of p

Ans.

```
eAi = sum(x .* ai)
eAi = 5
eAii = sum(x .* aii)
eAii = 2
eAiii = sum(x .* aiii)
eAiii = 1.1111
```

1d. Compute $\text{Var}[X]$ for this vector of integers using the function that you implemented above. Compute $\text{Var}[X]$ for each value of p

Ans.

```
varianceAi = (1-p1)/(p1 ^ 2)
varianceAi = 20
```

$\text{varianceAii} = (1 - p2) / (p2^2)$

$\text{varianceAii} = 2$

$\text{varianceAiii} = (1 - p3) / (p3^2)$

$\text{varianceAiii} = 0.1235$

2a. Generate 1000 samples with the following values for (μ, σ) : (70, 10), (150, 20), (-20, 70)

Ans.

$m = 1000;$

$ui = 70;$

$oi = 10;$

$u_{ii} = 150;$

$o_{ii} = 20;$

$u_{iii} = -20;$

$o_{iii} = 70;$

$b_i = \text{mygaussiansamples}(ui, oi, m)$

$b_{ii} = \text{mygaussiansamples}(u_{ii}, o_{ii}, m)$

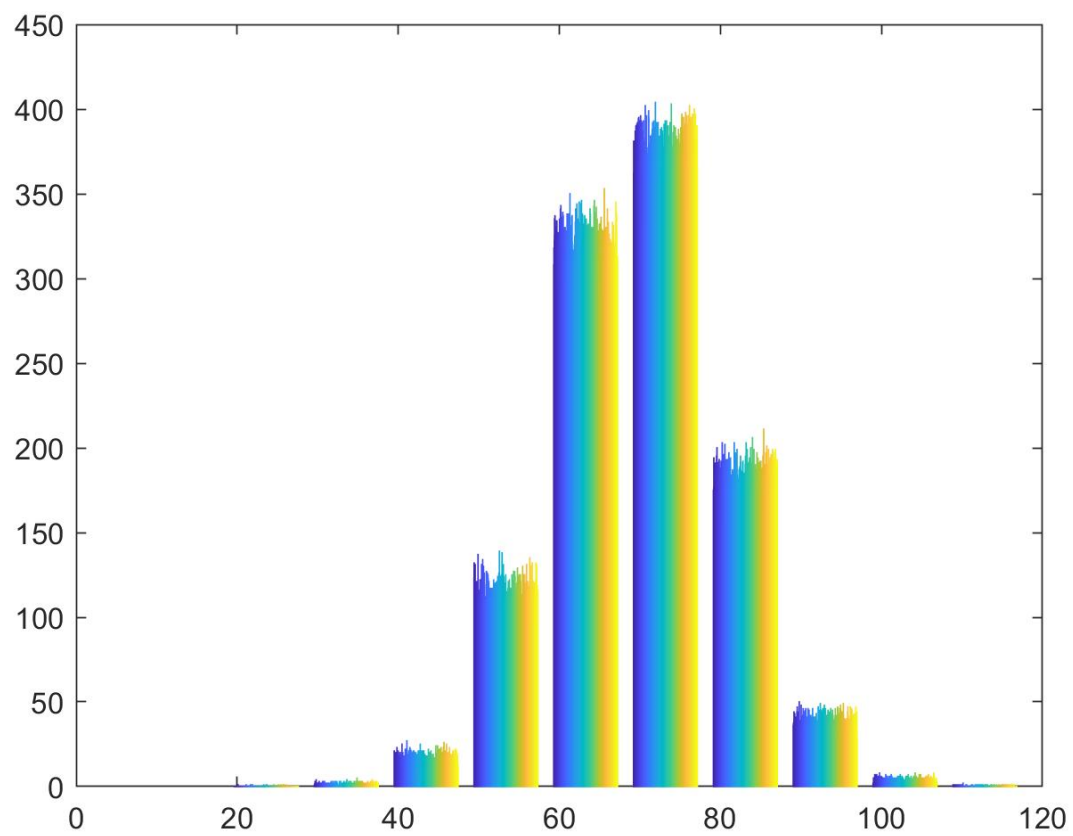
$b_{iii} = \text{mygaussiansamples}(u_{iii}, o_{iii}, m)$

2b. Use the histogram function to plot the samples for each (μ, σ) pair. This should result in 3 plots.

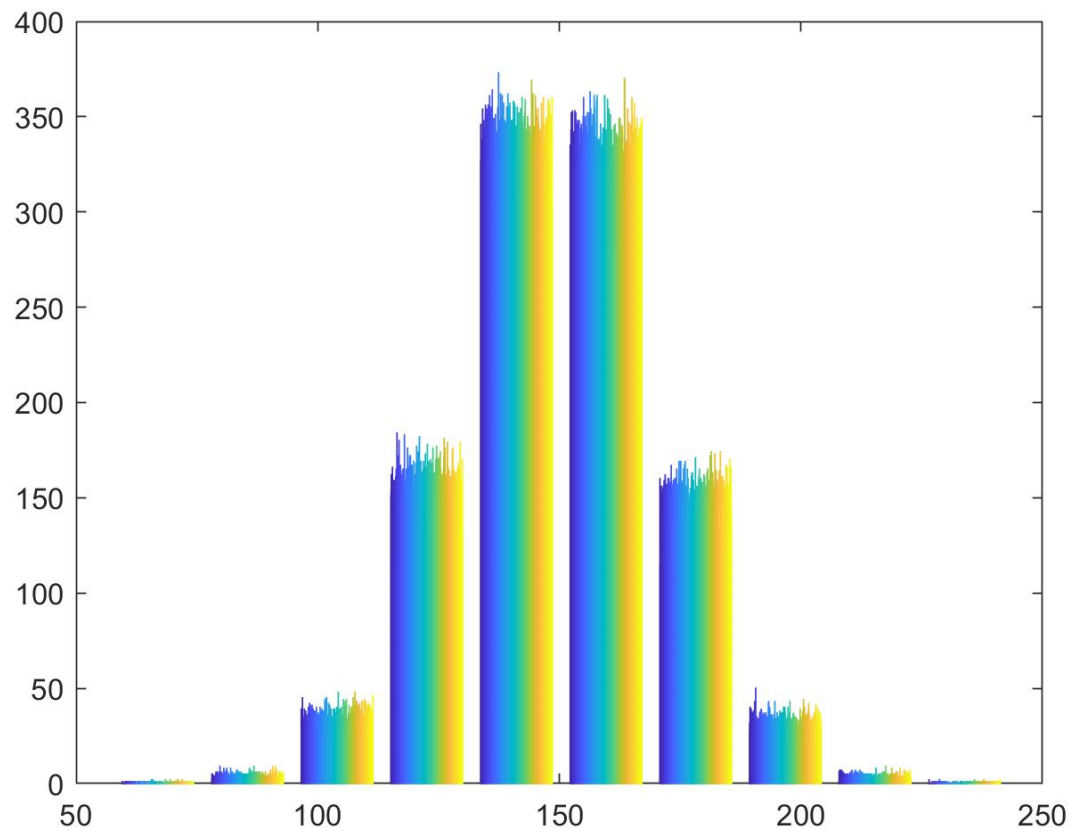
Compare and contrast the three plots, based on what you expect to see

Ans.

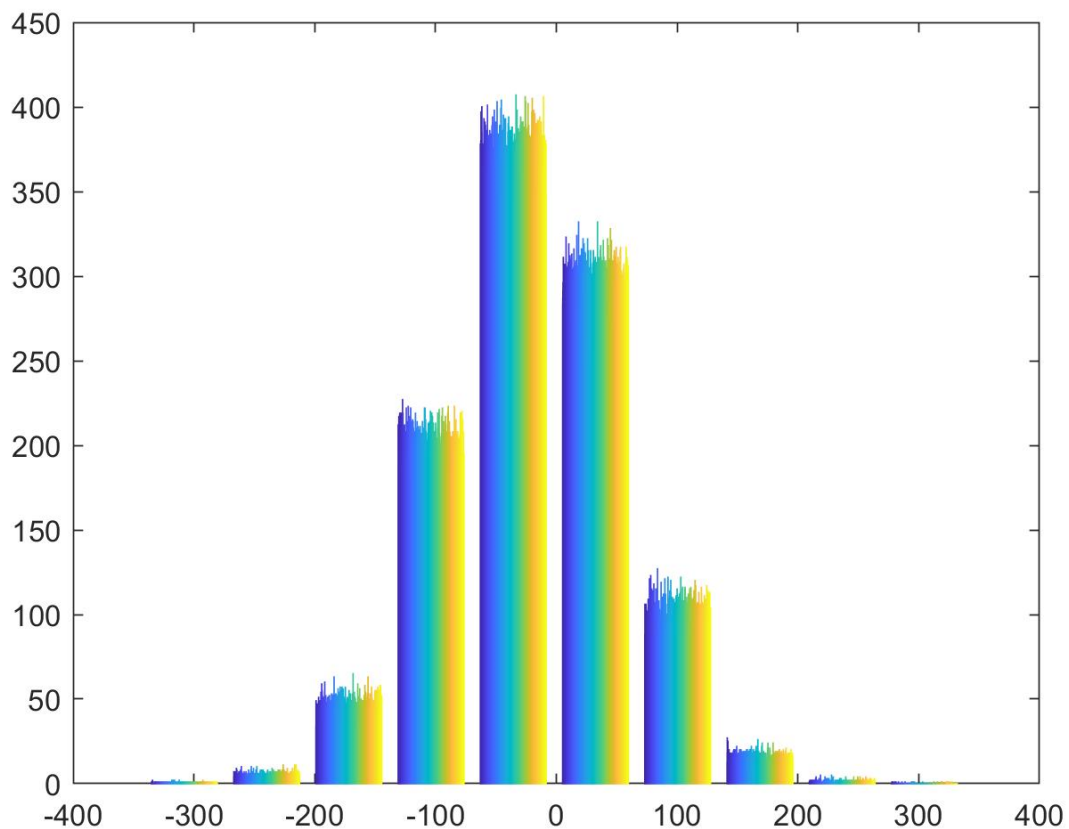
hist(bi) %most data should be around the mean (70), and the data should be focused, but not spread out



hist(bii) %most data should be around the mean (150), and the data is more spread out than bi.



hist(biii))%most data should be around the mean (-20), but the data is spread out, because the standard deviation is high



3a. Create two random variables X and Y , where X = [800, 1200, 1600] and Y = [400, 800, 1200].

Ans.

X = [800,1200,1600];

Y = [400,800,1200];

3b. Using the table shown below, create variable P xy, which stores the joint PMF between X and Y .

Ans.

jPmf = [0.2,0.05,0.1;0.05,0.2,0.1;0,0.1,0.2]

3c. Compute values for the marginal PMF of X (e.g. $P_X(x)$) and the marginal PMF of Y (e.g. $P_Y(y)$).

Ans.

%PX(800) = 0.2 + 0.05 + 0.1 = 0.35

%PX(1200) = 0.05 + 0.2 + 0.1 = 0.35

%PX(1600) = 0 + 0.1 + 0.2 = 0.3

Px = [0.35, 0.35, 0.3]

```

%PY(400) = 0.2 + 0.05 + 0 = 0.25
%PY(800) = 0.05 + 0.2 + 0.1 = 0.35
%PY(1200) = 0.1 + 0.1 + 0.2 = 0.4
Py = [0.25,0.35,0.4]

```

3d. Write a MATLAB function called myexpvalue(x, P x) that computes the expected value of a discrete random variable x, using its PMF, P x. Hint: use x(:) and P x(:) in the calculation

Ans.

```

function f = myexpvalue(x, Px)
    f = sum(x .* Px)
end

```

3e. Compute the expected values for X and Y , using myexpvalue(x, P x).

Ans.

```

xExp = myexpvalue(X, Px)
xExp = 1180

```

```

yExp = myexpvalue(Y, Py)
yExp = 860

```

3f. Use the ndgrid function to generate a grid of the two random variables. Store the grids as Sx and Sy.

Ans.

```

[Sx, Sy] = ndgrid(X, Y)
Sx =

```

800	800	800
1200	1200	1200
1600	1600	1600

Sy =

400	800	1200
400	800	1200
400	800	1200

3g. Write a MATLAB function called mycovariance(Sx, Sy, P xy, Ex, Ey) that computes the covariance between a grid of random variables (Sx and Sy) using the joint PMF (e.g. P xy) and marginal expected values (e.g. Ex, Ey).

Ans.

```

function g = mycovariance(Sx, Sy, Pxy, Ex, Ey)
    g = sum(sum(Sx .* Sy .* Pxy)) - Ex * Ey
end

```

3h. Use `mycovariance(Sx, Sy, P xy, Ex, Ey)` to compute the covariance between X and Y

Ans.

```
covar = mycovariance(Sx, Sy, jPmf, xExp, yExp)
```

```
covar = 49200
```