

# Elsevier L<sup>A</sup>T<sub>E</sub>X template<sup>☆</sup>

Elsevier<sup>1</sup>

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## Abstract

This template helps you to create a properly formatted L<sup>A</sup>T<sub>E</sub>X manuscript.

*Keywords:* `elsarticle.cls`, L<sup>A</sup>T<sub>E</sub>X, Elsevier, template

*2010 MSC:* 00-01, 99-00

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## 1. Main

Suppose  $(X_1^T, Y_1), \dots, (X_n^T, Y_n)$  are i.i.d. from  $N_{p+1}(\mu, \Sigma)$ , where  $X_i \in \mathbb{R}^p$  and  $Y_i \in \mathbb{R}$ . Denote  $X = (X_1, \dots, X_n)$ ,  $Y = (Y_1, \dots, Y_n)^T$ .

Write  $Y = \beta_0 \mathbf{1}_n + X^T \beta + \epsilon$ , where  $\mathbf{1}_n$  is  $n$  dimensional vector with all  
5 elements equal to 1.  $\epsilon$  has distribution  $N(0, \sigma^2 I_n)$ .

The problem is to test hypotheses  $H : \beta = 0$ .

The test statistic is

$$T = \frac{(\mathbf{1}_n^T (X^T X)^{-1} Q_n Y)^2}{\hat{\sigma}^2 \mathbf{1}_n^T (X^T X)^{-1} Q_n (X^T X)^{-1} \mathbf{1}_n}.$$

where  $Q_n = I_n - \frac{1}{n} \mathbf{1}_n \mathbf{1}_n^T$  and

$$\hat{\sigma}^2 = \frac{1}{n-2} Y^T Q_n \left[ I_n - \frac{(X^T X)^{-1} \mathbf{1}_n \mathbf{1}_n^T (X^T X)^{-1}}{\mathbf{1}_n^T (X^T X)^{-1} Q_n (X^T X)^{-1} \mathbf{1}_n} \right] Q_n Y$$

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<sup>☆</sup>Fully documented templates are available in the elsarticle package on CTAN.

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<sup>1</sup>Since 1880.

$n$	$p$	$ \beta ^2$	Chen	New
40	310	0.00	0.05	0.04
40	310	0.02	0.15	0.32
40	310	0.04	0.37	0.57
40	310	0.06	0.24	0.48
80	550	0.00	0.05	0.06
80	550	0.02	0.12	0.33
80	550	0.04	0.16	0.47
80	550	0.06	0.65	0.86

Table 1: Non-sparse case,  $T = 10$

$n$	$p$	$ \beta ^2$	Chen	New
40	310	0.00	0.05	0.05
40	310	0.02	0.69	0.60
40	310	0.04	0.97	0.86
40	310	0.06	1.00	0.92
80	550	0.00	0.05	0.04
80	550	0.02	0.99	0.96
80	550	0.04	1.00	1.00
80	550	0.06	1.00	1.00

Table 2: Non-sparse case,  $T = 20$

## References

$n$	$p$	$ \beta ^2$	Chen	New
40	310	0.00	0.05	0.05
40	310	0.02	0.05	0.09
40	310	0.04	0.06	0.08
40	310	0.06	0.08	0.08
80	550	0.00	0.05	0.07
80	550	0.02	0.06	0.04
80	550	0.04	0.06	0.06
80	550	0.06	0.13	0.10

Table 3: Sparse case,  $T = 10$

$n$	$p$	$ \beta ^2$	Chen	New
40	310	0.00	0.05	0.01
40	310	0.02	0.07	0.09
40	310	0.04	0.09	0.08
40	310	0.06	0.18	0.09
80	550	0.00	0.05	0.04
80	550	0.02	0.11	0.07
80	550	0.04	0.25	0.12
80	550	0.06	0.37	0.14

Table 4: Sparse case,  $T = 20$