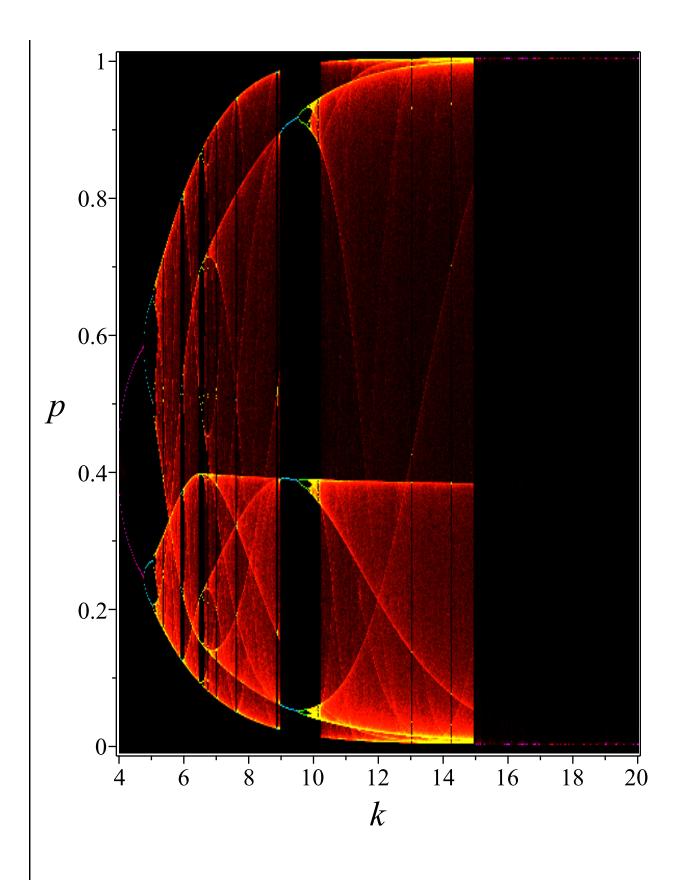
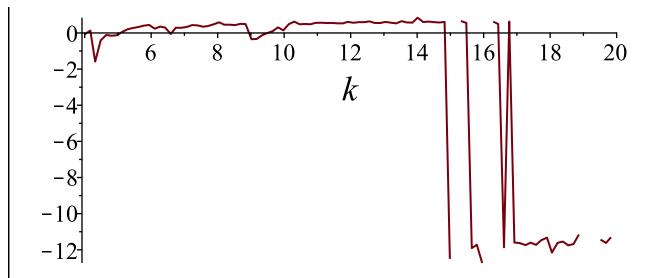
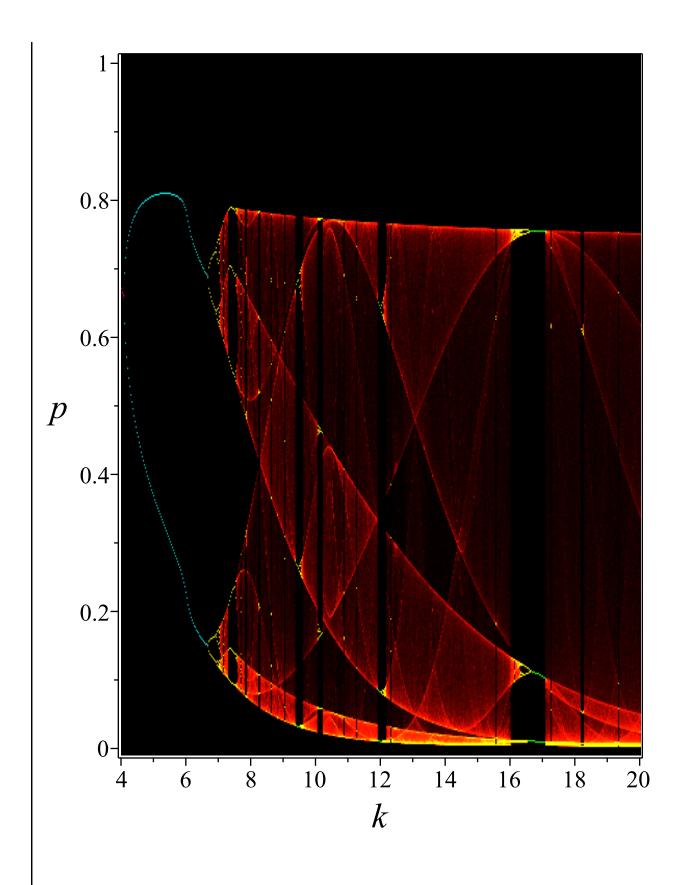
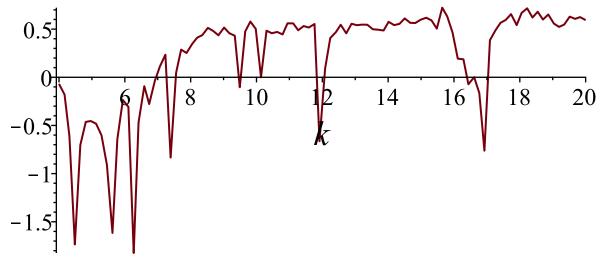
```
> restart
> with (IterativeMaps): with (ImageTools):
 > (r^{-1})^{(r+1)} : (r+1) : (r+1) *x* (1-x) *r: (2r^{-1}) *r* (r+1) *x*2* 
   (1-x)^{(r-1)} \cdot 3r^{(r-1)} \cdot (r-1) \cdot (r-1) \cdot r^{(r+1)} \cdot x^{3} \cdot (1-x)^{(r-2)} \cdot 4r^{(r+1)}
   *(r-1)*r*(r+1)*x^{(r-2)}*(1-x)^3: 5r^:=(1/2)*r*(r+1)*x^{(r-1)}*(1-x)
  (k+1)*x*(1-x)^k: 2k:=(1/2)*k*(k+1)*x^2*(1-x)^(k-1): 3k:=(1/6)*
   (k-1)*k*(k+1)*x^3*(1-x)^(k-2): ^4k := (1/6)*(k-1)*k*(k+1)*x^(k-2)*
   (1-x)^3: 5k: = (1/2)*k*(k+1)*x^(k-1)*(1-x)^2: 6k: = (k+1)*x^k*(1-x)
   : ^7k := x^(k+1):
  1:=.2:m:=4:n:=20:s:=20:
   `firstr`:=`0r`+`1r`+`6r`:
   secondr:=\1r\+\2r\+\3r\+\7r\:
   firstk`:=`0k`+`1k`+`6k`:
   \ensuremath{\text{`secondk'}} := \ensuremath{\text{`1k'+'2k'+'3k'+'7k'}} :
> unassign('k');
> bif:=Bifurcation([x],[firstr],[1],m,n,xmin=-.01,xmax=1.01):
  ColouringProcedures:-HueToRGB(bif):
  Pbif:=plot('k'=m..n,p=-.01..1.01,axes=box,size=[600,600],
  background=bif,labelfont=[times,s],font=[time,s-6]):
  F:=proc(k,x0)
     if not k::numeric and x0::numeric then
       return 'procname'(args);
     LyapunovExponent(unapply(eval(firstr,r=`k`),x),x0,
                      max iter=2^17,epsilon=1e-4);
  end proc:
  Plyap:=plot(F(k,1),'k'=m..n,adaptive=false,numpoints=100,size=
   [600,200], labelfont=[times,s], font=[time,s-6]):
  #plots:-display(Array([[Pbif],[Plyap]]),aligncolumns);
  print(Pbif);print(Plyap);
  bif:=Bifurcation([x],[secondr],[1],m,n,xmin=-.01,xmax=1.01):
  ColouringProcedures:-HueToRGB(bif):
  Pbif:=plot('k'=m..n,p=-.01..1.01,axes=box,size=[600,600],
  background=bif,labelfont=[times,s],font=[time,s-6]):
  F:=proc(k,x0)
     if not k::numeric and x0::numeric then
       return 'procname'(args);
     end if;
     LyapunovExponent(unapply(eval(secondr,r=`k`),x),x0,
                      max iter=2^17,epsilon=1e-4);
  end proc:
  Plyap:=plot(F(k,1),'k'=m..n,adaptive=false,numpoints=100,size=
   [600,200],labelfont=[times,s],font=[time,s-6]):
  print(Pbif);print(Plyap);
  for k from 4 to 20 do:
  expr:=`firstk`*r+`secondk`*(1-r):
  bif:=Bifurcation([x],[expr],[1],-.01,1.01,xmin=-.01,xmax=1.01):
```

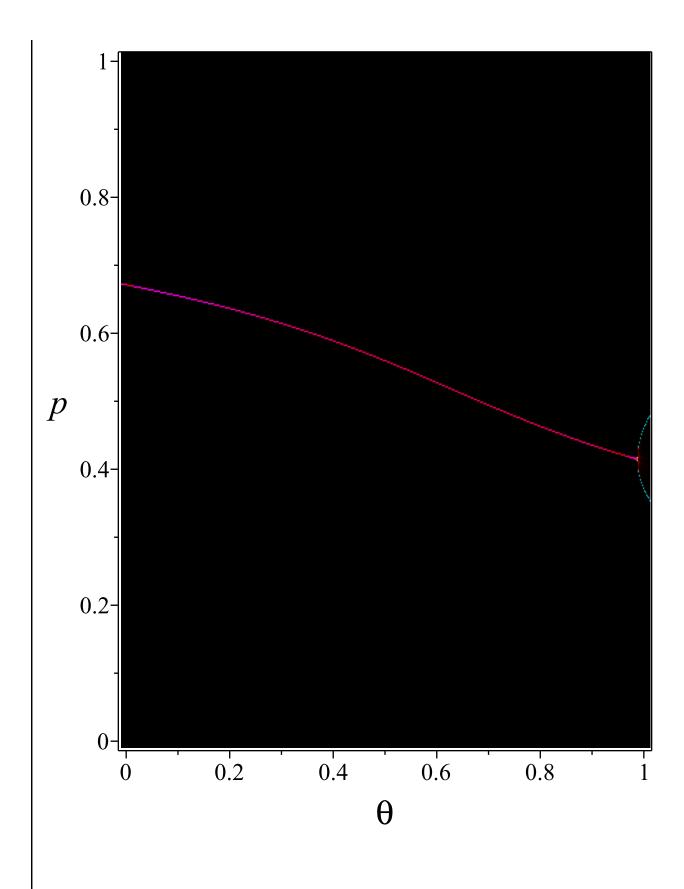


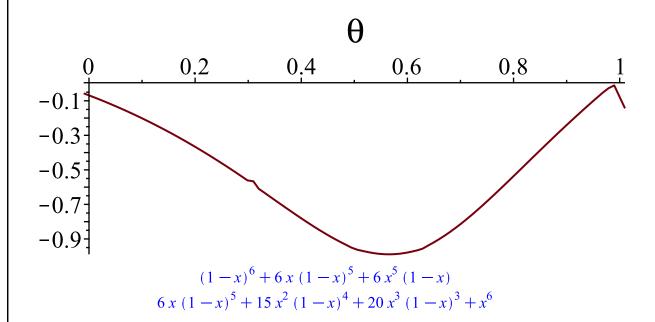


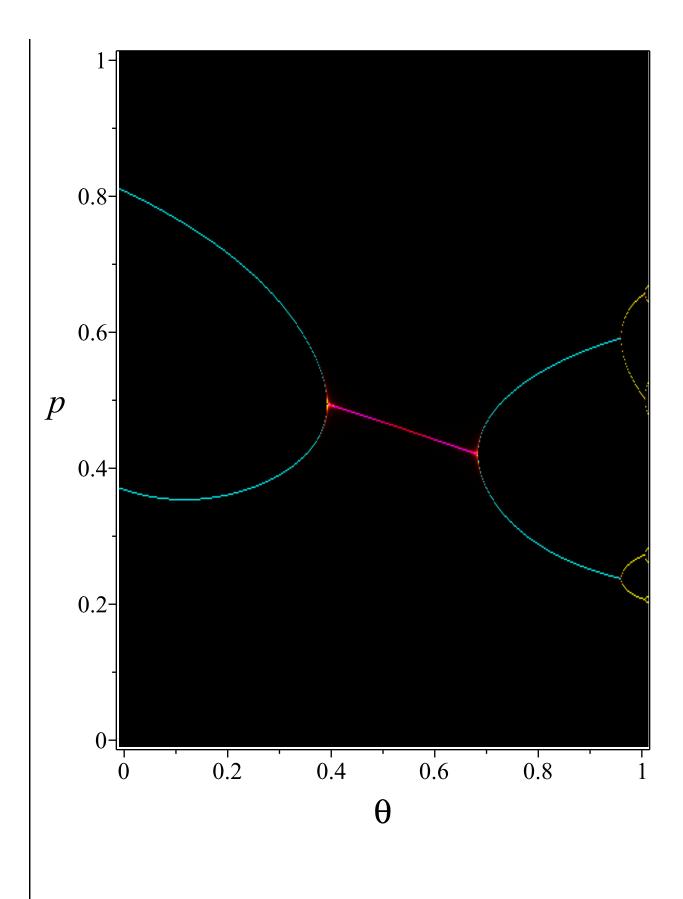


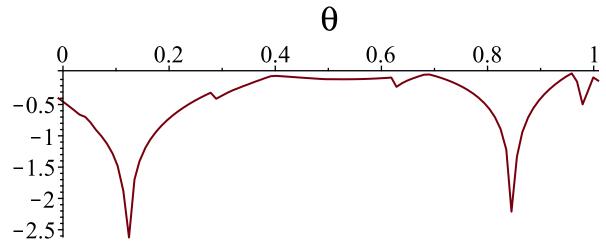


$$(1-x)^5 + 5x(1-x)^4 + 5x^4(1-x)$$
  
5x(1-x)^4 + 10x<sup>2</sup>(1-x)<sup>3</sup> + 10x<sup>3</sup>(1-x)<sup>2</sup> + x<sup>5</sup>



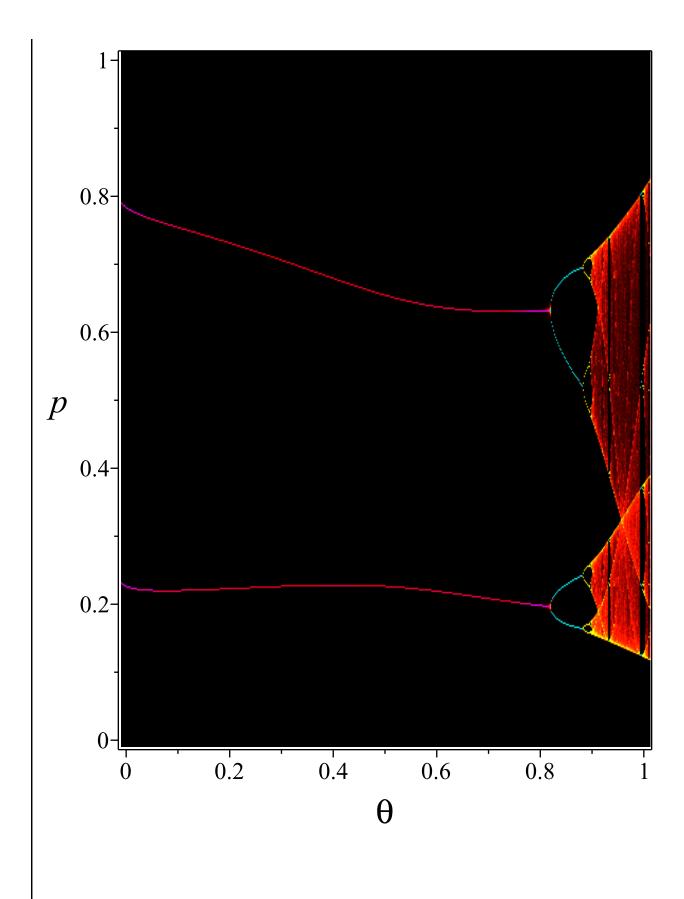


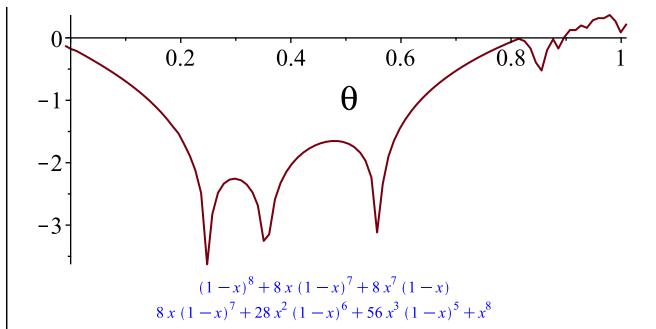


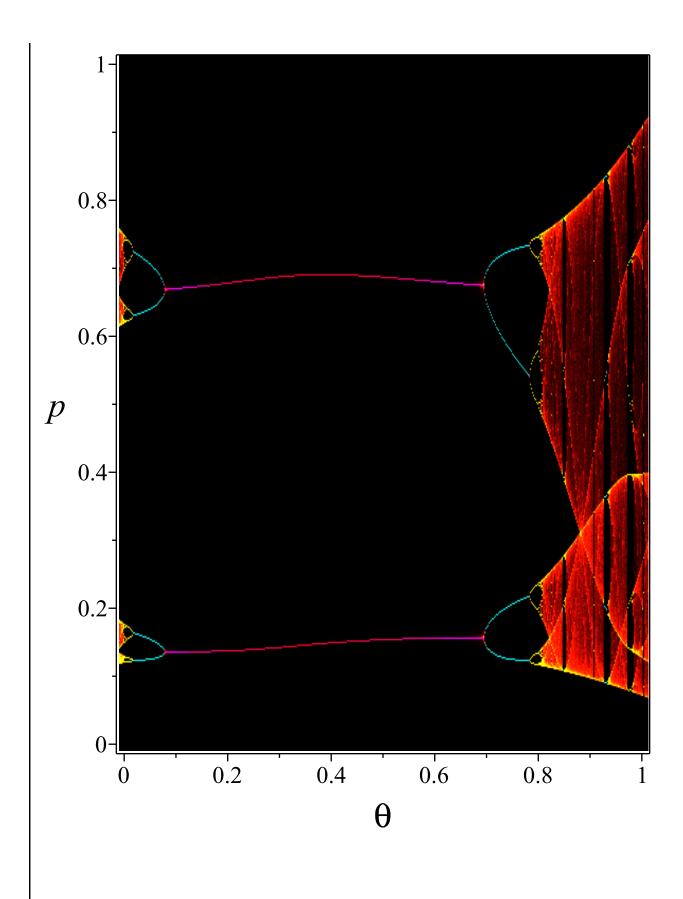


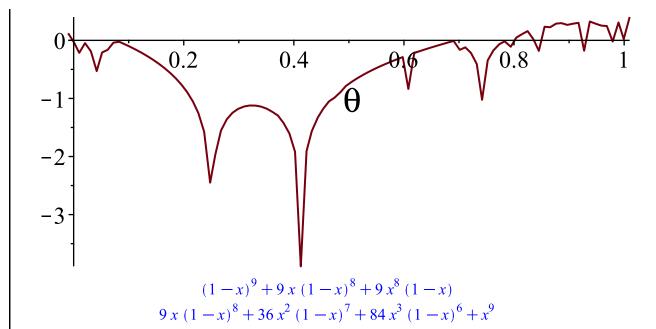
$$(1-x)^{7} + 7x(1-x)^{6} + 7x^{6}(1-x)$$

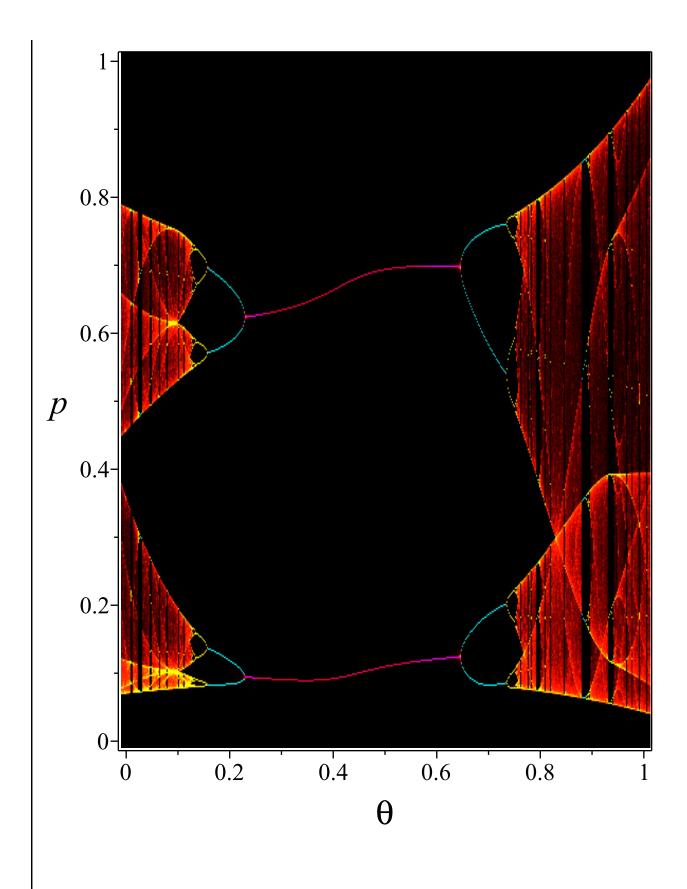
$$7x(1-x)^{6} + 21x^{2}(1-x)^{5} + 35x^{3}(1-x)^{4} + x^{7}$$

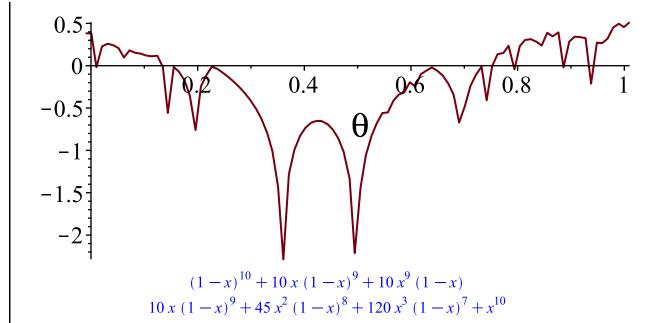


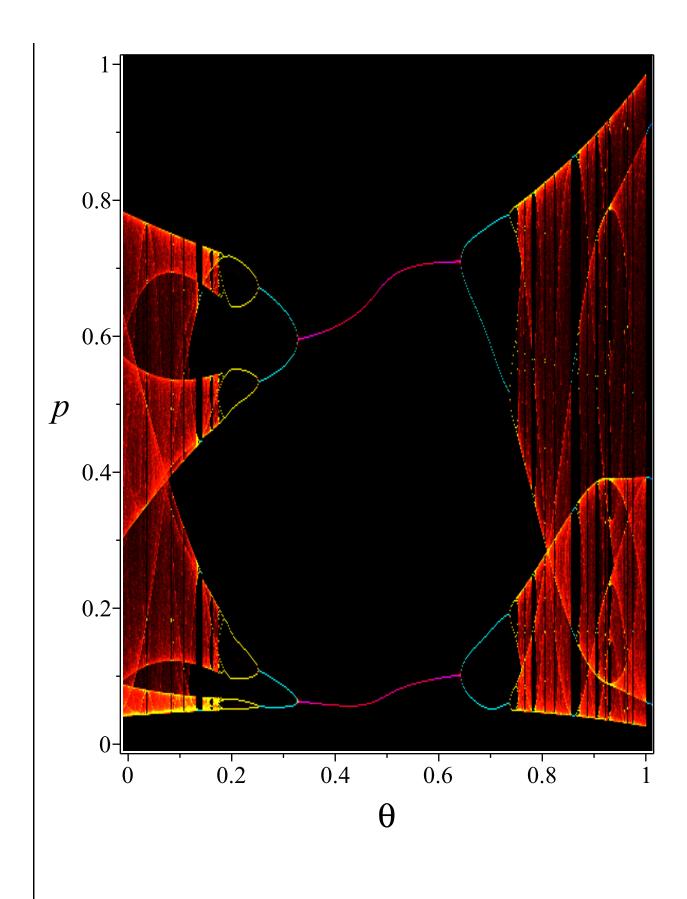


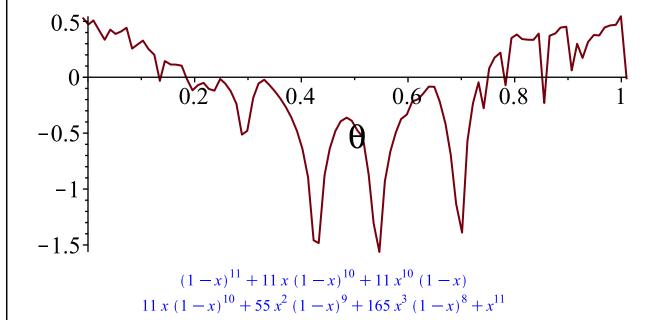


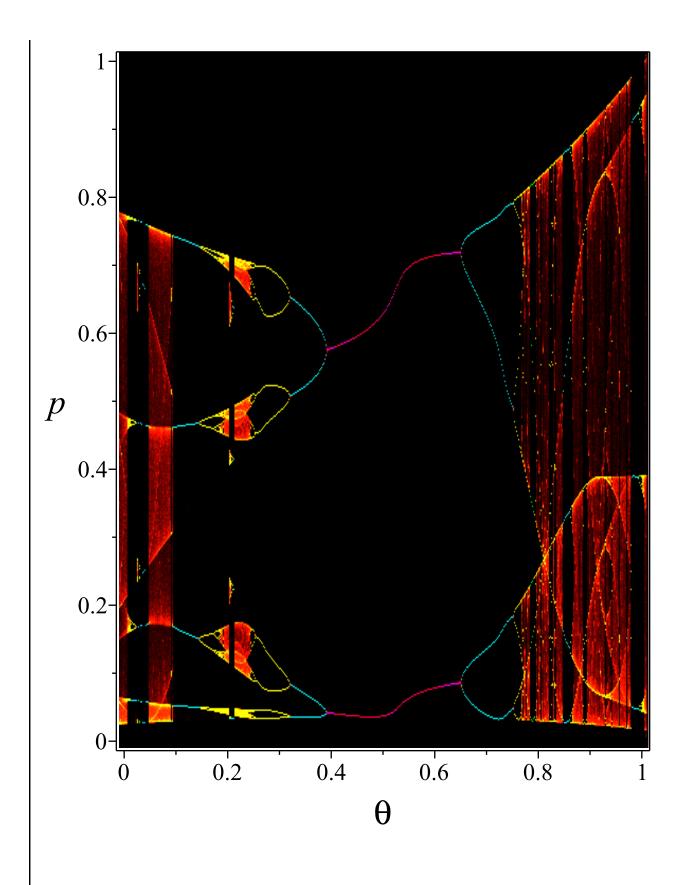


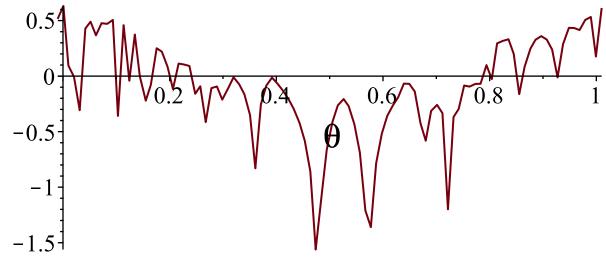






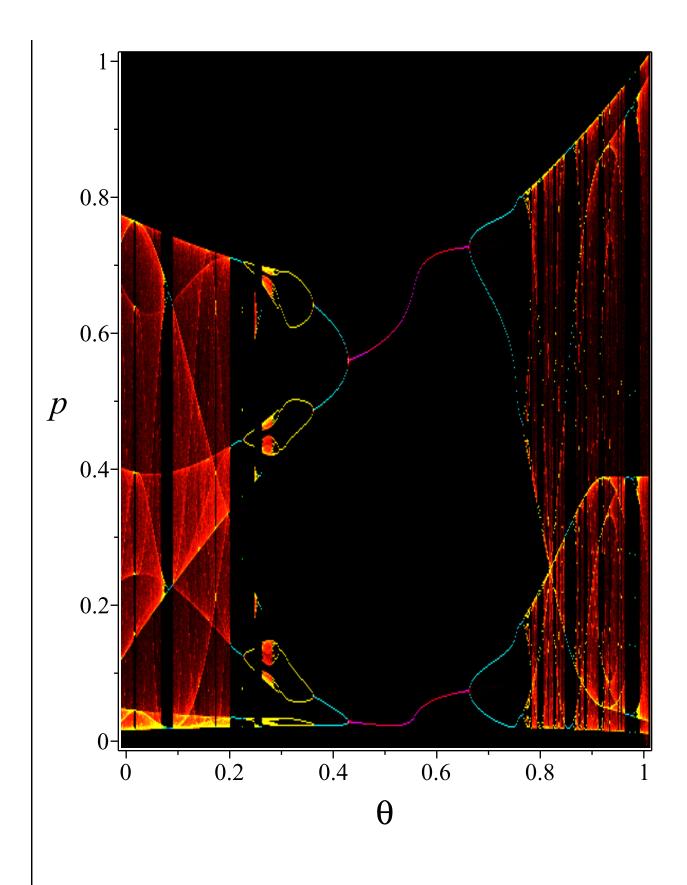


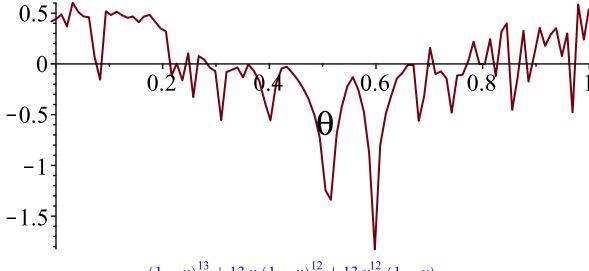




$$(1-x)^{12} + 12 x (1-x)^{11} + 12 x^{11} (1-x)$$

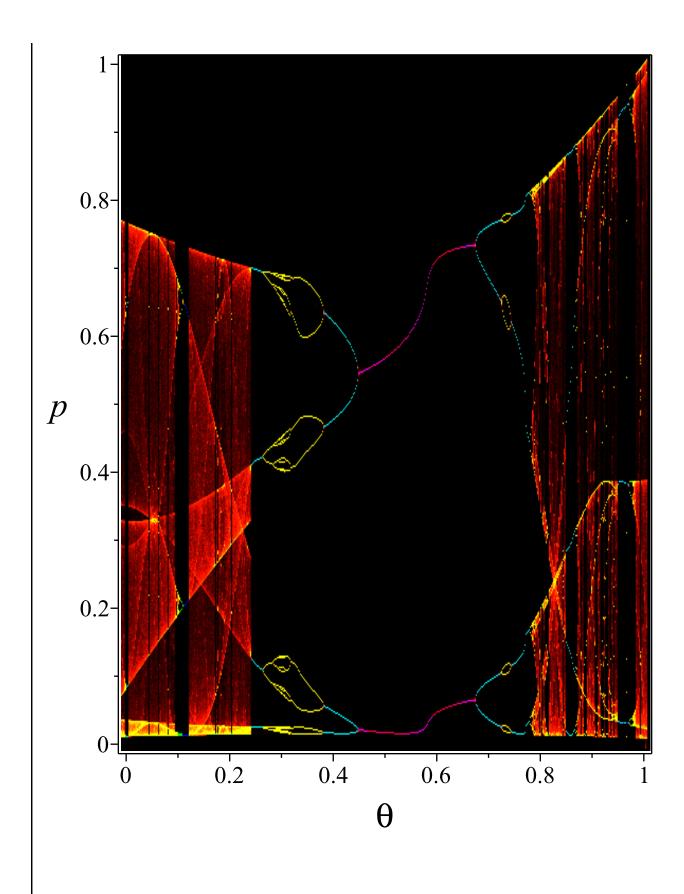
$$12 x (1-x)^{11} + 66 x^{2} (1-x)^{10} + 220 x^{3} (1-x)^{9} + x^{12}$$

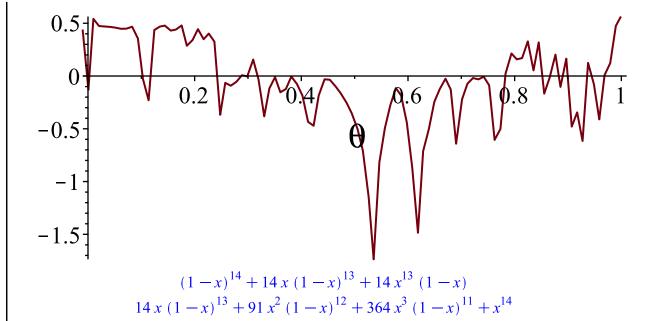


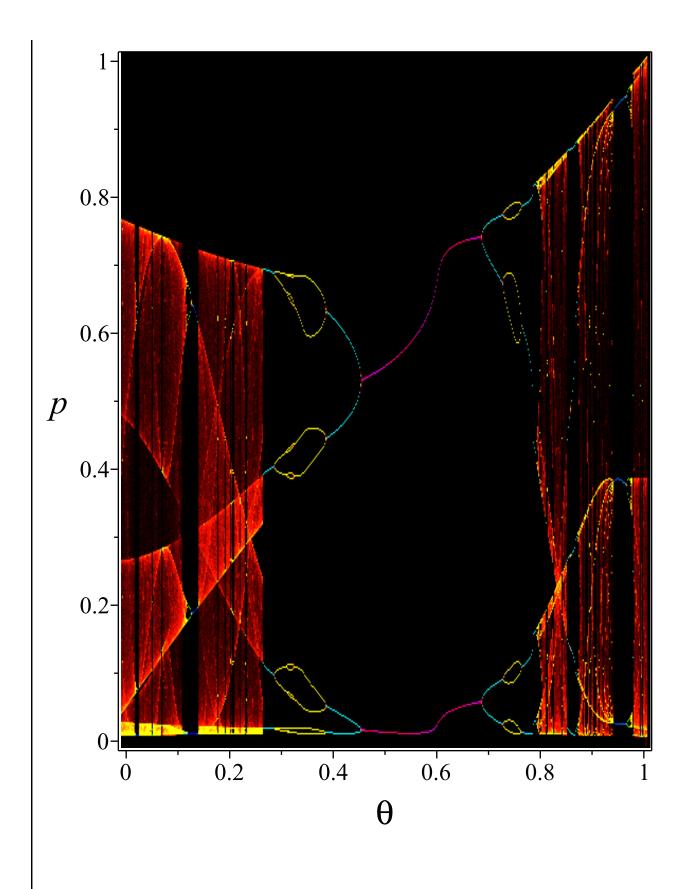


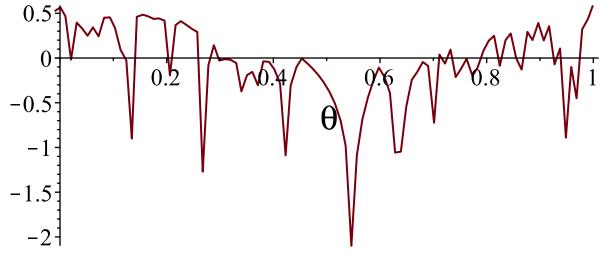
$$(1-x)^{13} + 13 x (1-x)^{12} + 13 x^{12} (1-x)$$

$$13 x (1-x)^{12} + 78 x^{2} (1-x)^{11} + 286 x^{3} (1-x)^{10} + x^{13}$$



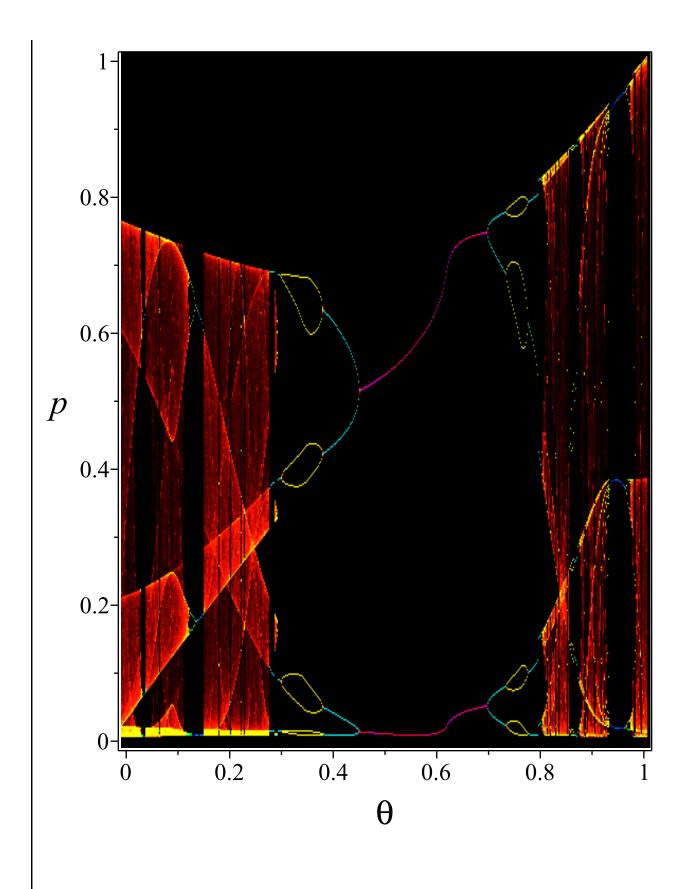


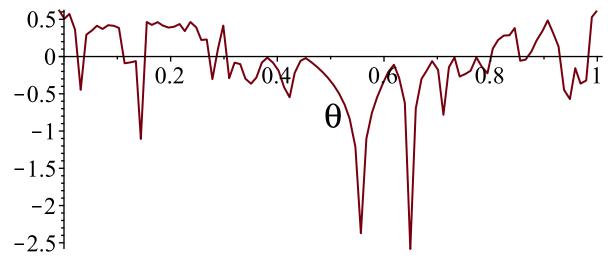




$$(1-x)^{15} + 15 x (1-x)^{14} + 15 x^{14} (1-x)$$

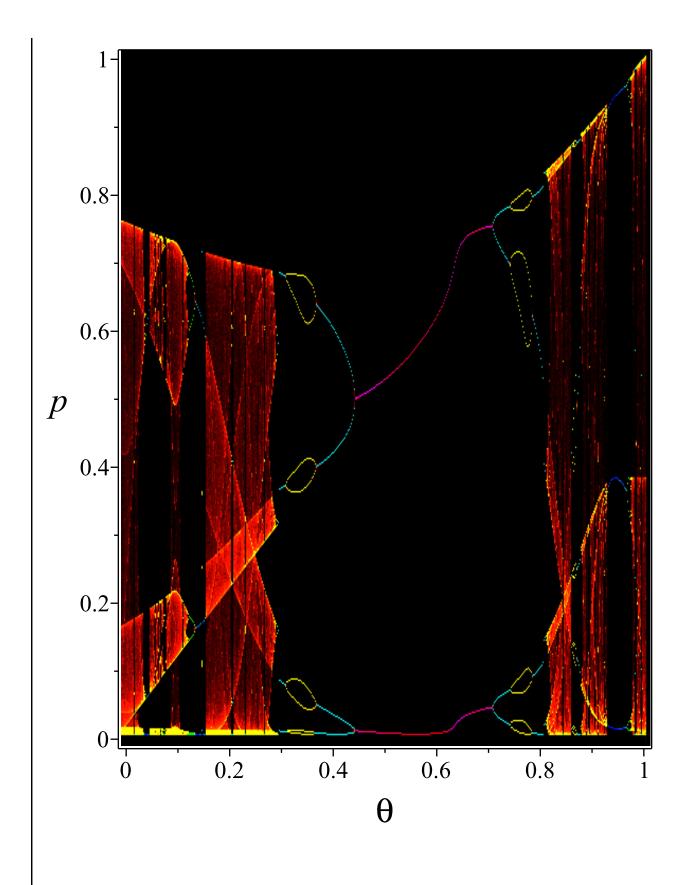
$$15 x (1-x)^{14} + 105 x^{2} (1-x)^{13} + 455 x^{3} (1-x)^{12} + x^{15}$$

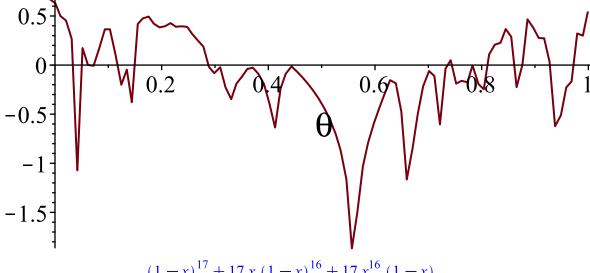




$$(1-x)^{16} + 16x (1-x)^{15} + 16x^{15} (1-x)$$

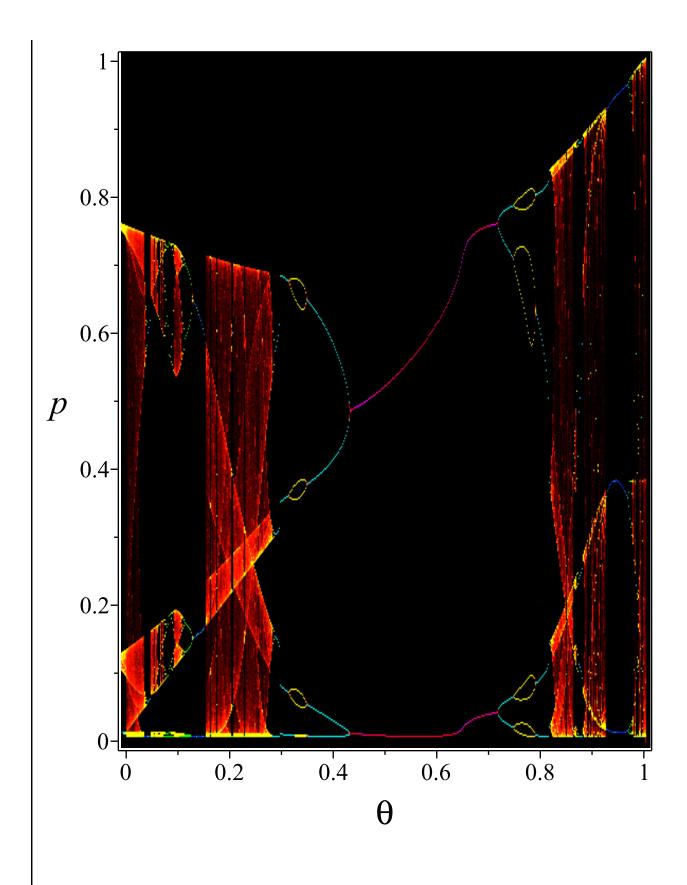
$$16x (1-x)^{15} + 120x^{2} (1-x)^{14} + 560x^{3} (1-x)^{13} + x^{16}$$

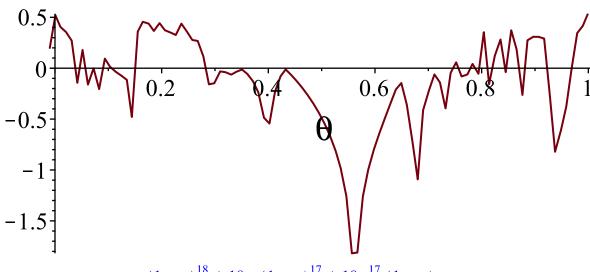




$$(1-x)^{17} + 17x (1-x)^{16} + 17x^{16} (1-x)$$

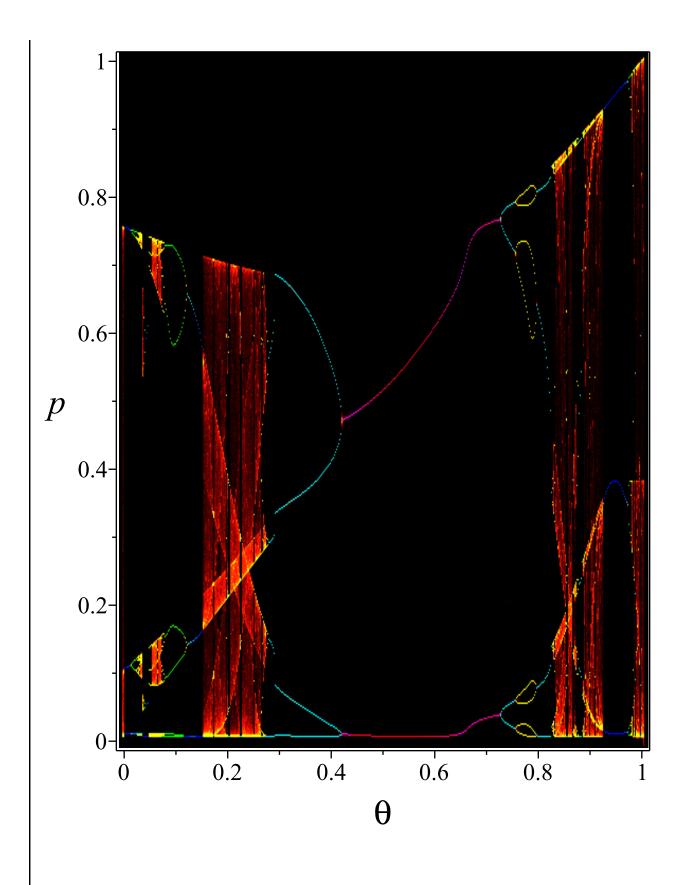
$$17x (1-x)^{16} + 136x^{2} (1-x)^{15} + 680x^{3} (1-x)^{14} + x^{17}$$

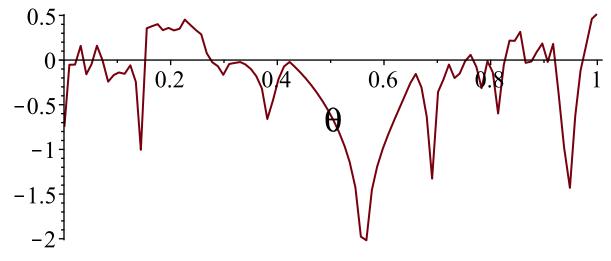




$$(1-x)^{18} + 18x(1-x)^{17} + 18x^{17}(1-x)$$

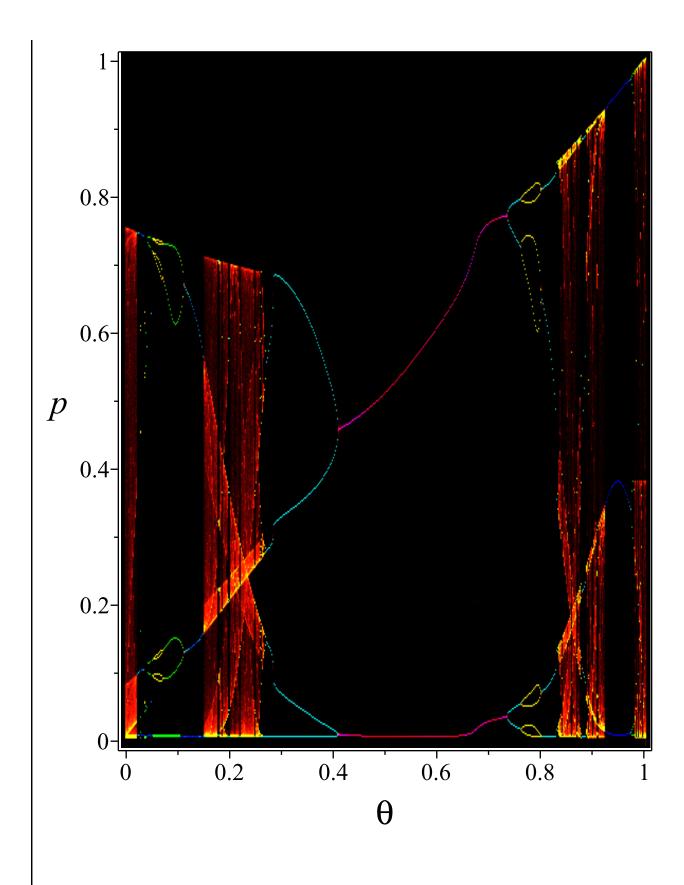
$$18x(1-x)^{17} + 153x^{2}(1-x)^{16} + 816x^{3}(1-x)^{15} + x^{18}$$

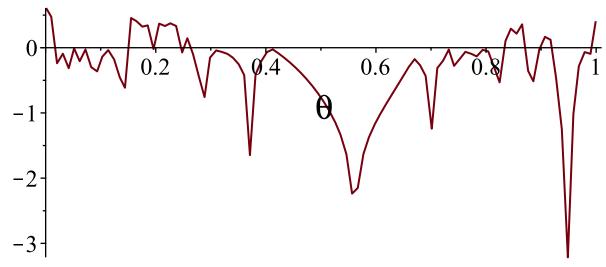




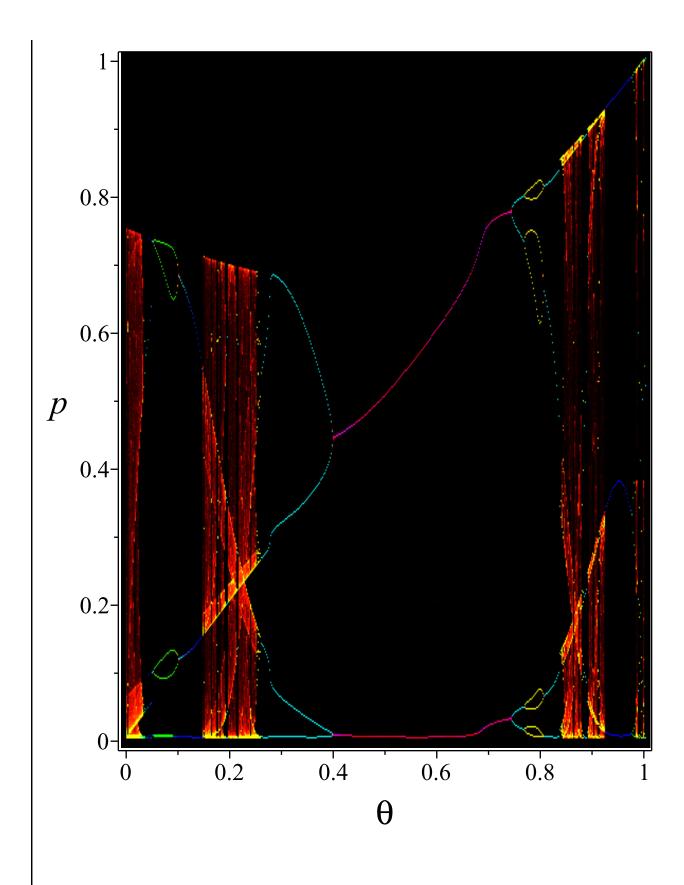
$$(1-x)^{19} + 19x (1-x)^{18} + 19x^{18} (1-x)$$

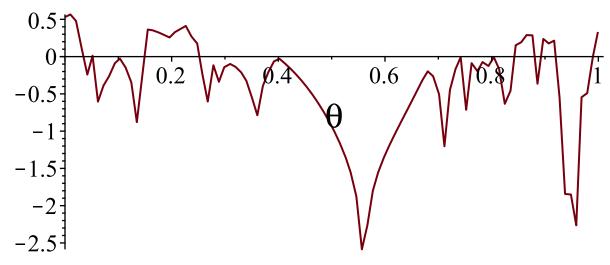
$$19x (1-x)^{18} + 171x^{2} (1-x)^{17} + 969x^{3} (1-x)^{16} + x^{19}$$





$$(1-x)^{20} + 20 x (1-x)^{19} + 20 x^{19} (1-x)$$
  
20 x (1-x)<sup>19</sup> + 190 x<sup>2</sup> (1-x)<sup>18</sup> + 1140 x<sup>3</sup> (1-x)<sup>17</sup> + x<sup>20</sup>





$$(1-x)^{21} + 21 x (1-x)^{20} + 21 x^{20} (1-x)$$
  
21 x (1-x)<sup>20</sup> + 210 x<sup>2</sup> (1-x)<sup>19</sup> + 1330 x<sup>3</sup> (1-x)<sup>18</sup> + x<sup>21</sup>

