```
In [1]:
          1
             import numpy as np
          2
             import pandas as pd
In [2]:
            from numpy import array
          2
            from numpy import mean
          3
            from numpy import cov
            from numpy.linalg import eig
In [4]:
          1 mat = array([[1,2],[3,4],[5,6]])
          2
             mat
         array([[1, 2],
               [3, 4],
               [5, 6]])
In [5]:
          1 mean(mat)
         3.5
In [6]:
          1 \mid M = mean(mat.T, axis = 1)
          2 M
         array([3., 4.])
In [7]:
          1
            c = mat-M
          2
             C
         array([[-2., -2.],
               [ 0., 0.],
               [ 2., 2.]])
In [8]:
          1 v = cov(c.T)
          2
         array([[4., 4.],
               [4., 4.]])
```

```
In [9]:
             values, vectors = eig(v)
           2
             print(vectors)
           3
             print(values)
          [[ 0.70710678 -0.70710678]
           [ 0.70710678  0.70710678]]
          [8. 0.]
In [10]:
           1 P = vectors.T.dot(c.T)
           2
             print(P.T)
          [[-2.82842712 0.
           [ 0.
                      0.
                               ]
           [ 2.82842712 0.
                               11
In [18]:
           1
              class pca :
                  def __init__(self,n_components):
           2
           3
                      self.n_components = n_components
                      self.components = None
           4
           5
                      self.mean= None
           6
           7
                  def fit(self,x):
                      self.mean = np.mean(x,axis = 0)
           8
                      x = x - self.mean
           9
          10
                      cov = np.cov(x.T)
          11
                      eigenvalues,eigenvectors = np.linalg.eig(cov)
          12
          13
          14
                      eigenvectors = eigenvectors.T
                      idxs = np.argsort(eigenvalues)[::-1]
          15
                      eigenvalues = eigenvalues[idxs]
          16
                      eigenvectors = eigenvectors[idxs]
          17
          18
          19
                      self.components = eigenvectors[0:self.n_components]
          20
          21
                  def transform(self,x):
          22
                      x = x - self.mean
          23
                      return np.dot(x,self.components.T)
          24
```

```
In [14]:
              from sklearn import datasets
           2
              import matplotlib.pyplot as plt
           3
              from sklearn.decomposition import PCA
           4
              import numpy as np
           5
In [16]:
              data = datasets.load_iris()
           2
              x = data.data
           3
              y = data.target
           4
           5
             pca = PCA(2)
           6
              pca.fit(x)
           7
              x_projected = pca.transform(x)
              print("shape of x : ", x.shape)
              print("shape of transformed x : ", x_projected.shape)
           9
              x1 = x_projected[:,0]
          10
              x2 = x_projected[:,1]
          11
          12
              plt.scatter(x1,x2, c=y ,edgecolor = 'none',alpha = 0.8 , cmap = plt.cm.get_cr
              plt.xlabel('PC1')
          13
              plt.ylabel('PC2')
          14
          15
              plt.colorbar()
          16
              plt.show()
          17
          shape of x : (150, 4)
          shape of transformed x: (150, 2)
                                                          2.00
              1.5
                                                         - 1.75
              1.0
                                                         1.50
              0.5
                                                         - 1.25
                                                         - 1.00
              0.0
                                                         0.75
             -0.5
                                                         - 0.50
             -1.0
                                                          0.25
                                                          0.00
                                 PC1
```

```
In [19]:
               from sklearn.datasets import fetch openml
            2
               from sklearn.decomposition import PCA
            3
              from sklearn.preprocessing import StandardScaler
            4
               from sklearn import metrics
            5
               from sklearn.model_selection import train_test_split
               import pandas as pd
In [20]:
               mnist = fetch_openml('mnist_784')
In [21]:
            1
              mnist
           {'data': array([[0., 0., 0., ..., 0., 0., 0.],
                  [0., 0., 0., ..., 0., 0., 0.]
                  [0., 0., 0., ..., 0., 0., 0.],
                  [0., 0., 0., \ldots, 0., 0., 0.],
                  [0., 0., 0., ..., 0., 0., 0.],
                  [0., 0., 0., ..., 0., 0., 0.]]),
            'target': array(['5', '0', '4', ..., '4', '5', '6'], dtype=object),
            'frame': None,
            'feature_names': ['pixel1',
             'pixel2',
             'pixel3',
             'pixel4',
             'pixel5',
             'pixel6',
             'pixel7',
             'pixel8',
             'pixel9',
             'pixel10',
             'pixel11',
             'pixel12',
             'pixel13',
             'pixel14',
In [22]:
            1 mnist.data.shape
           (70000, 784)
In [24]:
            1 mnist.target.shape
           (70000,)
In [25]:
            1
               train_img, test_img, train_lbl, test_lbl = train_test_split(
            2
                    mnist.data, mnist.target, test_size=1/7.0, random_state=0)
```

```
In [27]:
             print(train_img.shape)
           2
             print(train_lbl.shape)
           3
             print(test_img.shape)
             print(test_lbl.shape)
          (60000, 784)
          (60000,)
          (10000, 784)
          (10000,)
In [28]:
             from sklearn.preprocessing import StandardScaler
           2
             scaler = StandardScaler()
           3
             scaler.fit(train_img)
             train_img = scaler.transform(train_img)
           4
             test_img = scaler.transform(test_img)
           5
In [29]:
           1
             pca = PCA(.95)
           2
             pca.fit(train_img)
           3
             pca.n_components_
          327
In [30]:
             train_img = pca.transform(train_img)
           2
             test_img = pca.transform(test_img)
In [33]:
             from sklearn.linear_model import LogisticRegression
           1
In [36]:
             logisticRegr = LogisticRegression(solver = 'lbfgs')
```

```
In [37]:
                logisticRegr.fit(train_img, train_lbl)
            C:\Users\hp\anaconda3\lib\site-packages\sklearn\linear_model\_logistic.py:940: ConvergenceWarning: lbfg
            STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
            Increase the number of iterations (max_iter) or scale the data as shown in:
                https://scikit-learn.org/stable/modules/preprocessing.html (https://scikit-learn.org/stable/modules/preprocessing.html)
            Please also refer to the documentation for alternative solver options:
                https://scikit-learn.org/stable/modules/linear model.html#logistic-regression (https://scikit-learn.org/stable/modules/linear m
              extra warning msg= LOGISTIC SOLVER CONVERGENCE MSG)
            LogisticRegression(C=1.0, class_weight=None, dual=False, fit_intercept=True,
                                intercept_scaling=1, l1_ratio=None, max_iter=100,
                                multi_class='auto', n_jobs=None, penalty='12',
                                random_state=None, solver='lbfgs', tol=0.0001, verbose=0,
                                warm_start=False)
In [38]:
                 logisticRegr.predict(test_img[0].reshape(1,-1))
            array(['0'], dtype=object)
In [41]:
                logisticRegr.predict(test_img[0:10])
            array(['0', '4', '1', '2', '4', '7', '7', '1', '1', '7'], dtype=object)
In [39]:
                 score = logisticRegr.score(test_img, test_lbl)
                 print(score)
             2
            0.9201
```

```
In [40]:
           1
              pd.DataFrame(data = [[1.00, 784, 48.94, .9158],
           2
                                      [.99, 541, 34.69, .9169],
           3
                                      [.95, 330, 13.89, .92],
                                      [.90, 236, 10.56, .9168],
           4
                                      [.85, 184, 8.85, .9156]],
           5
                             columns = ['Variance Retained',
           6
           7
                                       'Number of Components',
           8
                                       'Time (seconds)',
           9
                                       'Accuracy'])
            Variance Retained Number of Components Time (seconds) Accuracy
          0 1.00
                               784
                                                      48.94
                                                                      0.9158
          1 0.99
                               541
                                                      34.69
                                                                      0.9169
          2 0.95
                               330
                                                                      0.9200
                                                      13.89
          3 0.90
                               236
                                                      10.56
                                                                      0.9168
          4 0.85
                               184
                                                      8.85
                                                                      0.9156
```