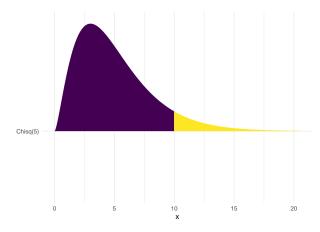
Chapter 4 R Practice

Computing probabilities for continuous distributions in R

The cdf values F(X) = P(X < x) are returned with commands using "p" at the beginning of the R distribution name:

- pnorm(x, mean = mu, sd = sigma) returns F(x) values for a normal random variable $X \sim N(\mu, \sigma^2)$
- punif(x, min = theta1, max = theta2) returns F(x) values for a uniform random variable $X \sim U(\theta_1, \theta_2)$
- pexp(y, rate = lambda) returns F(x) values for an exponential random variable $X \sim exp(\beta = 1/\lambda)$
 - Note our textbook defines exponential distributions in terms of the parameter β , which is the mean wait time, instead of the rate λ .
- pgamma(y, shape = alpha, scale = beta) returns F(x) values for a gamma random variable $X \sim (\alpha, \beta)$ with parameters shape = α and scale = $\beta = 1/\lambda$.
 - Because the gamma function can be parameterized in terms of shape or rate, make sure to name
 the argument inside the pgamma() function to specify which parameter you're defining. If you
 don't specify the name, by default it actually expects rate to be the 3rd argument, not scale.
- pchisq(x, df) returns F(x) values for a chi-square random variable $X \sim \chi^2(\nu)$ where the argument df corresponds to the degrees of freedom parameter \nu
- pbeta(x, shape1 = alpha, shape2 = beta) returns F(x) values for a beta random variable $X \sim Beta(\alpha, \beta)$

There is a hidden argument in each of these functions called lower.tail, and the default is set to lower.tail = TRUE. Meaning, by default, the "p" functions return the probabilities in the lower tail of the density function: F(X) = P(X < x). Sometimes it will be useful to override the default by adding the argument lower.tail = FALSE, which will return values P(X > x). You can think of these two options visually; lower.tail = TRUE represents the dark shaded region P(X < 10), and lower.tail = FALSE represents the light shaded region P(X > 10) in the plot below.



Uniform example

Suppose $X \sim U(0,5)$.

- 1. Sketch the pdf and shade the region X < 2
- 2. Write out the integral and the R code required to calculate P(X < 2). Calculate it using your preferred method.

3. Write out two different lines of code you could use to find P(X > 2) in R. Hint: one should make use of the lower.tail argument. Execute both lines of code in R to verify that they give the value you expect.

4. Suppose we want to find P(2 < X < 3). Sketch a graph with this region shaded.

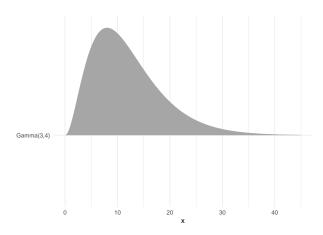
6. Using your visual as a guide, what would you need to subtract from P(X < 3) in order to obtain P(2 < X < 3)?

7. Using your answer to part 6 as a guide, write out R code for computing P(2 < X < 3). Execute your code in R and report the answer.

Gamma example

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Suppose X \sim \Gamma(\alpha = 3, \beta = 4).
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We can plot this distribution with the following code:



8. What's the mean of this distribution? Does this seem reasonable based on the graph above?

- 9. Shade the region X < 5 on the graph above
- 10. Write out the code you need to calculate P(X < 5). Hint: use the pgamma() function.
- 11. Use your code above to compute P(X < 5) and report the answer. Does the value seem reasonable based on the plot above?
- 12. Write out two different lines of code you could use to find P(X > 5) in R. Hint: one should make use of the lower. tail argument. Execute both lines of code in R to verify they give the value you expect.

Chi-squared example

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Suppose X \sim \chi^2(14).
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We can plot this distribution with the following code:

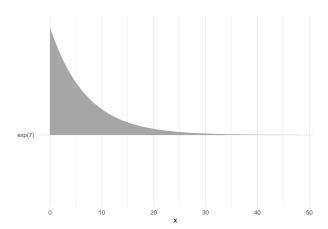


- 13. What's the mean of this distribution? Does this seem reasonable based on the graph above?
- 14. Shade the region X < 10 on the graph above
- 15. Write out the code you need to calculate P(X < 10). Hint: use the pchisq() function.
- 16. Use your code above to compute P(X < 10) and report the answer. Does the value seem reasonable based on the plot above?
- 17. Write out two different lines of code you could use to find P(X > 10) in R. Hint: one should make use of the lower. tail argument. Execute both lines of code in R to verify they give the value you expect.

Exponential example

Suppose $X \sim exp(7)$.

We can plot this distribution with the following code:



- 18. What's the mean of this distribution? Does this seem reasonable based on the graph above?
- 19. Write out the code you need to calculate P(X > 20). Hint: use the pexp() function. How many/what arguments do you need to specify?

- 20. Use your code above to compute P(X > 20) and report the answer. Does the value seem reasonable based on the plot above?
- 21. Shade P(10 < X < 20) on the plot above.
- 22. Write out the code you need to find P(10 < X < 20). Execute the code and report the answer. Does it seem reasonable based on the plot above?

Computing percentiles for continuous distributions in R

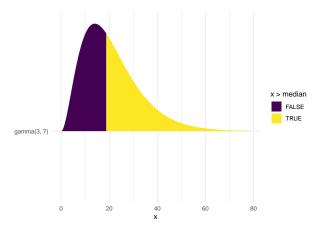
The inverse of the cdf, or the x that solves the equation p = F(x) = P(X < x), are returned with commands using "q" at the beginning of the R distribution name:

- qunif(p, min = theta1, max = theta2) finds x such that P(X < x) = p for a uniform random variable $X \sim U(\theta_1, \theta_2)$
- qexp(p, rate = lambda = 1/beta) finds x such that P(X < x) = p for an exponential random variable $Y \sim exp(\lambda = 1/\beta)$
- qgamma(p, shape = alpha, scale = beta = 1/lambda) finds x such that P(X < x) = p for a gamma random variable $X \sim (\alpha, \beta)$ with parameters shape = α and scale = $\beta = 1/\lambda$
- qchisq(p, df) finds x such that P(X < x) = p for a chi-square random variable $Y \sim \chi^2(\nu)$ where the argument df corresponds to the degrees of freedom parameter \nu.
- qnorm(x, mean = mu, sd = sigma) finds x such that P(X < x) = p for a normal random variable $X \sim N(\mu, \sigma^2)$
- pbeta(x, shape1 = alpha, shape2 = beta) finds x such that P(X < x) = p for a beta random variable $X \sim Beta(\alpha, \beta)$

Again, set lower.tail = FALSE to use upper tail probabilities and find x such that P(X > x) = p.

Gamma example

Suppose $X \sim \Gamma^2(\alpha = 3, \beta = 7)$. Below is a visual of the distribution shaded at the median.



- 23. Write out the code you need to find the median in R. Execute the code and report the value. Does the value seem reasonable based on the plot above?
- 24. Write out the code you need to find the 95th in R. Execute the code and report the value. Does the value seem reasonable based on the plot above?