$$\int_0^\infty y f(y) dy = \int_0^\infty y^2 e^{-y}$$

$$= y^2 e^{-y} \Big|_0^\infty + \int_0^\infty 2y e^y dy$$

$$= 0 - y e^{-y} \Big|_0^\infty + 2 \int_0^\infty e^{-y} dy$$

$$= 2 \left(-e^{-y} \Big|_0^\infty \right) = 2$$

Let the function g be the indicator function $1_{\left(\frac{1}{4},\frac{9}{16}\right)}$. Then we have that

$$\begin{split} P\left(\frac{1}{2} < X < \frac{3}{4}\right) &= E[g(X)] \\ &= \int_{0}^{1} \left(1_{\frac{1}{4} < x^{2} < \frac{9}{16}}\right) dx \\ &= \int_{\frac{1}{2}}^{\frac{3}{4}} 1 dx \\ &= x|_{\frac{1}{2}}^{\frac{3}{4}} \\ &= \frac{1}{4} \end{split}$$

We have that

$$0.8 * 50000 = \int_{D}^{100000} (x - D) \cdot \frac{1}{100000} dx$$
$$= \left(50000 - D + \frac{D^2}{200000}\right)$$

Hence, we have that $D \approx 10557.281$

Since $\lim_{y\to 0.5^-} F_Y(y) = 0.5$ and $\lim_{y\to 0.5^+} F_Y(y) = 1$. We have that P(Y=0.5) = 1-0.5 = 0.5 Therefore,

$$E[Y] = \int_0^{0.5} (y)' \cdot y \, dy + \frac{1}{2} \cdot \frac{1}{2} = \frac{y^2}{2} \Big|_0^{0.5} + \frac{1}{4} = \frac{3}{8}$$