

**1.**

$$e^{-\lambda} = 1 - 0.2 = 0.8$$

$$1 - \sum_{i=0}^2 e^{-\lambda} \frac{\lambda^i}{i!} = 0.00157$$

**2.**

$$\begin{aligned} E[X] &= E[X|Y = 0] \cdot P(Y = 0) + E[X|Y > 0] \cdot P(Y > 0) \\ &= E[Y \cdot 8000|Y = 0] \cdot P(Y = 0) + E[(Y - 1) \cdot 8000|Y > 0] \cdot (1 - P(Y = 0)) \\ &= 8000E[Y|Y = 0] \cdot P(Y = 0) + (8000E[Y|Y > 0] - 8000) \cdot (1 - P(Y = 0)) \\ &= 8000 \cdot E[Y] - 8000 \cdot (1 - P(Y = 0)) \\ &= 8000 \cdot 4 - 8000 \cdot (1 - e^{-4}) \\ &= 24146.525 \end{aligned}$$

### 3.

#### a.

We have that the probability that the fire appears in any specific quadrant follows a poisson distribution with mean  $10^{-3} \cdot (10 \cdot 10/4) = 0.025$ . Hence, the probability that fire appears in any quadrant is

$$1 - \frac{0.025^0 e^{-0.025}}{0!} = 1 - e^{-0.025}$$

Hence, the probability that fire appears in three or more quadrant is

$$C_3^4(1 - e^{-0.025})^3(e^{-0.025}) + C_4^4(1 - e^{-0.025})^4 = 0.0000590895$$

#### b.

The number of fires appears in the city follows a poisson distribution with mean  $10^{-3} \cdot 10 \cdot 10 = 0.1$ . Hence, the expected value of fire happens in the city is 0.1

4.

Since the number of jobs arrive in 1 minute follows a poisson distribution with mean 1,  $N$ , the number of jobs arrive in 15 minutes follows a poisson distribution with mean 15.

$$\begin{aligned}P(\text{there will be lost job}) &= 1 - P(\text{there will not be lost job}) \\&= 1 - \sum_{i=1}^{\infty} P(N = i, B > N) \\&= 1 - \sum_{i=1}^{\infty} P(N = i)P(B > i) \\&= 1 - \sum_{i=1}^{\infty} \frac{15^i e^{-15}}{i!} 2^{-i} \\&= 1 - e^{-15/2} \sum_{i=1}^{\infty} \frac{\left(\frac{15}{2}\right)^i e^{-15/2}}{i!} \\&= 1 - e^{-15/2} \\&= 0.999447\end{aligned}$$