

# Lecture 2 - More Python, Remembering statistics



**DTU Management Engineering**Department of Management Engineering

## **Outline**



- Numpy
- Descriptive statistics

# Numpy



- One of your best friends. Does a lot of algebra leg-work for you!
- Important to know:
  - Vector and matrix manipulation
  - Random number generators
  - Mathematical functions
  - Deep VS shallow copy (careful!)

# **Descriptive statistics**



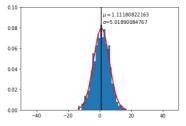
- Mean
- Standard deviation
- Mode
- Quantiles
- Skewness
- Correlation

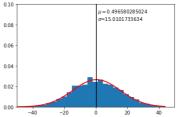
## The mean



$$\bar{x} = \sum_{i=1}^{N} \frac{x_i}{N}$$

$$\sigma = \sqrt{\sum_{i=1}^{N} \frac{(\bar{x} - x_i)^2}{N}}$$



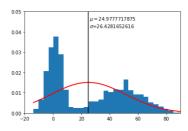


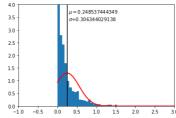
## The mean



$$\bar{x} = \sum_{i=1}^{N} \frac{x_i}{N}$$

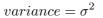
$$\sigma = \sqrt{\sum_{i=1}^{N} \frac{(\bar{x} - x_i)^2}{N}}$$

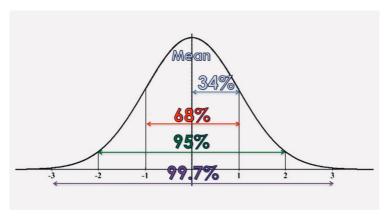




## Variance and standard deviation

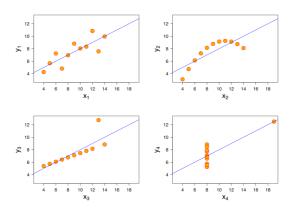






# The Ancombes quartet

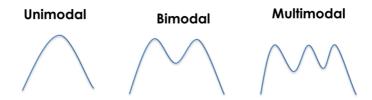




# Modality

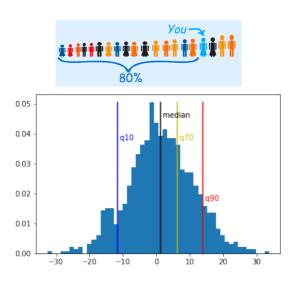


• Mode - Point with high probability



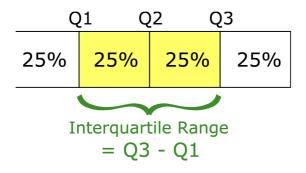
# The quantiles





## Interquartile range

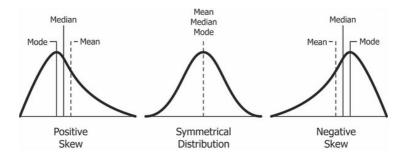




Where the majority of the data lies

## **Skewness**





#### Correlation

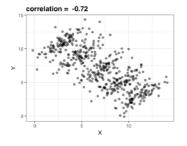


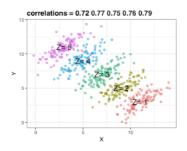
$$cov_{x,y} = \sum_{i=1}^{N} \frac{(\bar{x} - x_i)(\bar{y} - y_i)}{N}$$

$$\rho_{x,y} = \frac{cov_{x,y}}{\sigma_x \sigma_y}$$

# Correlation - Simpson's paradox







#### More to read...



- "Numpy Tutorial Part 1 Introduction to Arrays", https://www.machinelearningplus.com/python/numpy-tutorial-part1-array-python-examples/
- "Numpy Tips and Tricks part 1", http://arogozhnikov.github.io/2015/09/29/NumpyTipsAndTricks1.html
- "Intro to Descriptive Statistics" by Niklas Donges https://towardsdatascience.com/intro-to-descriptive-statistics-252e9c464ac9
- "Python Pandas descriptive statistics", https://www.tutorialspoint.com/python\_pandas/python\_pandas\_descriptive\_statistics.htm
- "Python for Data Science descriptive statistics", https://pythonfordatascience.org/descriptive-statistics-python/