

from gurobipy import *

```
#-----#  
#Sets  
d_c=["D0","D1","D2"] # Set for Distribution Centers  
s_m=["S0","S1","S2","S3","S4","S5","S6","S7","S8","S9"] #Set for SuperMarket
```

```
#-----#  
#Data  
  
# Cost of transportation of one truckload from each distribution centre to each store  
cost=[  
    [1938,1424,1407,918,2140,1421,1876,1194,1459,900],  
    [1801,1843,1898,1613,919,912,1063,1553,1453,2220],  
    [3074,2575,857,2171,2800,1942,,2699,1223,2525,2038]  
]  
  
# Districution centre capacity - the maximum capacity of distributon system.  
dc_capacity= [28,58,66]  
  
# Weekly demand at the store, including the surges  
sm_demand=[  
    [8, 12, 12,18, 7, 8, 9, 10, 8, 18],  
    [8, 12, 12, 18, 7, 8, 9, 14, 8, 21],  
    [8, 12, 12, 18, 7, 8, 9, 10, 8, 18],  
    [8, 12, 14, 18, 7, 8, 31, 17, 8, 18],  
    [33, 12, 12, 18, 7, 8, 9, 15, 8, 18],  
    [8, 12, 12, 18, 7, 8, 31, 11, 8, 18]  
]  
  
d_capacity_max = 75
```

```
# Specifying the lenghts of the above arrays  
S_C = range(len(sm_demand))  
S = range(len(s_m))  
D = range(len(d_c))
```

```
#-----#  
# Initialising the model  
m = Model("logistics")
```

Sets:

d_c :Set of distribution centers
 s_m :Set of supermarkets
 s_c :Set of scenarios

Data:

$cost_{dc\ sm}$:Cost to supply to supermarket $sm \in s_m$ from distribution center $dc \in d_c$
 $dc_capacity_{dc}$:Capacity of distribution center $dc \in d_c$
 $sm_demand_{sc\ sm}$:Demand of each supermarket $sm \in s_m$ in each scenario $sc \in s_c$
 $d_capacity_max$:Maximum available capacity in DC_0 and DC_1

Variables:

$X_{dc\ sm}$:Proportion of contribution from distribution center $dc \in d_c$ for the supermarket sm

Objective Function:

$$\min \sum_{sm \in s_m} \sum_{dc \in d_c} X_{dc\ sm} * cost_{dc\ sm}$$

Constraints:

1. The sum of the contribution proportion from all distribution center for each supermarket should not be greater than 1. For all the scenarios, this constrain will be constant because we are using proportions.

$$\sum_{dc \in d_c} X_{dc\ sm} == 1 \quad \forall sm \in s_m$$

2. The total quantity sent out from each distribution center for all supermarkets in each scenario is less than distribution center capacity.

$$\sum_{sm \in s_m} X_{dc\ sm} * sm_demand_{sc\ sm} \leq dc_capacity_{dc} \quad \forall sc \in s_c \quad \forall dc \in d_c$$

3. The total quantity sent out from distribution centres DC_0 and DC_1 for all supermarkets in each scenario is less than 100 which is the labour capacity.

$$\sum_{dc \in \{DC_0, DC_1\}} \sum_{sm \in s_m} X_{dc\ sm} * sm_demand_{sc\ sm} \leq d_capacity_max \quad \forall sc \in s_c$$

Declaring variables for the model

X={}

for d in D:

for s in S:

X[d,s]=m.addVar()

Objective Function

Setting up the objective function of the model- Proportion of contribution of each distribution center for a shopping market

m.setObjective(quicksum(X[d,s]*cost[d][s] for d in D for s in S),GRB.MINIMIZE)

#-----#

Adding Constraints

The sum of proportion for every distribution = 1

sm_demand_constrain={}

for s in S:

sm_demand_constrain[s]=m.addConstr((quicksum(X[d,s] for d in D))==1)

Total capacity of the distribution centres should be maintained for each scenario

cap_c={}

for s_c in S_C:

for d in D:

cap_c[d]=m.addConstr(quicksum(X[d,s]*sm_demand[s_c][s] for s in S)<=dc_capacity[d])

Constrains on D0 + D1 = 75 should be maintained for each scenario

for s_c in S_C:

labour=m.addConstr(quicksum((X[0,s]*sm_demand[s_c][s])+(X[1,s]*sm_demand[s_c][s]) for s in S) <=d_capacity_max)

m.optimize()

Sets:

d_c :Set of distribution centers

s_m :Set of supermarkets

s_c :Set of scenarios

Data:

cost_dc_sm :Cost to supply to supermarket sm ∈ s_m from distribution center dc ∈ d_c

dc_capacity_dc :Capacity of distribution center dc ∈ d_c

sm_demand_sc_sm :Demand of each supermarket sm ∈ s_m in each scenario sc ∈ s_c

d_capacity_max :Maximum available capacity in DC₀ and DC₁

Variables:

X_dc_sm :Proportion of contribution from distribution center dc ∈ d_c for the supermarket sm

Objective Function:

$$\min \sum_{sm \in s_m} \sum_{dc \in d_c} X_{dc\ sm} * cost_{dc\ sm}$$

Constraints:

1. The sum of the contribution proportion from all distribution center for each supermarket should not be greater than 1. For all the scenarios, this constrain will be constant because we are using proportions.

$$\sum_{dc \in d_c} X_{dc\ sm} == 1 \quad \forall sm \in s_m$$

2. The total quantity sent out from each distribution center for all supermarkets in each scenario is less than distribution center capacity.

$$\sum_{sm \in s_m} X_{dc\ sm} * sm_{demand\ sc\ sm} \leq dc_{capacity\ dc} \quad \forall sc \in s_c \quad \forall dc \in d_c$$

3. The total quantity sent out from distribution centres DC0 and DC1 for all supermarkets in each scenario is less than 100 which is the labour capacity.

$$\sum_{dc \in \{DC_0, DC_1\}} \sum_{sm \in s_m} X_{dc\ sc} * sm_{demand\ sc\ sm} \leq d_{capacity_max} \quad \forall sc \in s_c$$