Linear Regression (Boston House Pricing)

March 25, 2022

```
[]: from sklearn import linear model
     from sklearn import datasets
     import pandas as pd
     data = datasets.load_boston() ## loads Boston dataset from datasets librar
     print(data['DESCR'])
    .. boston dataset:
    Boston house prices dataset
    **Data Set Characteristics:**
        :Number of Instances: 506
        :Number of Attributes: 13 numeric/categorical predictive. Median Value
    (attribute 14) is usually the target.
        :Attribute Information (in order):
                       per capita crime rate by town
            - CRIM
            - ZN
                       proportion of residential land zoned for lots over 25,000
    sq.ft.
            - INDUS
                       proportion of non-retail business acres per town
            - CHAS
                       Charles River dummy variable (= 1 if tract bounds river; 0
    otherwise)
            - NOX
                       nitric oxides concentration (parts per 10 million)
            - RM
                       average number of rooms per dwelling
                       proportion of owner-occupied units built prior to 1940
            - AGE
            - DIS
                       weighted distances to five Boston employment centres
                       index of accessibility to radial highways
            - RAD
            - TAX
                       full-value property-tax rate per $10,000
            - PTRATIO pupil-teacher ratio by town
                       1000(Bk - 0.63)^2 where Bk is the proportion of black people
    by town
                       % lower status of the population
            - LSTAT
            - MEDV
                       Median value of owner-occupied homes in $1000's
```

:Missing Attribute Values: None

:Creator: Harrison, D. and Rubinfeld, D.L.

This is a copy of UCI ML housing dataset. https://archive.ics.uci.edu/ml/machine-learning-databases/housing/

This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.

The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic prices and the demand for clean air', J. Environ. Economics & Management, vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics ...', Wiley, 1980. N.B. Various transformations are used in the table on pages 244-261 of the latter.

The Boston house-price data has been used in many machine learning papers that address regression problems.

- .. topic:: References
- Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Data and Sources of Collinearity', Wiley, 1980. 244-261.
- Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.

/home/niteesh/.local/lib/python3.10/site-packages/sklearn/utils/deprecation.py:87: FutureWarning: Function load_boston is deprecated; `load_boston` is deprecated in 1.0 and will be removed in 1.2.

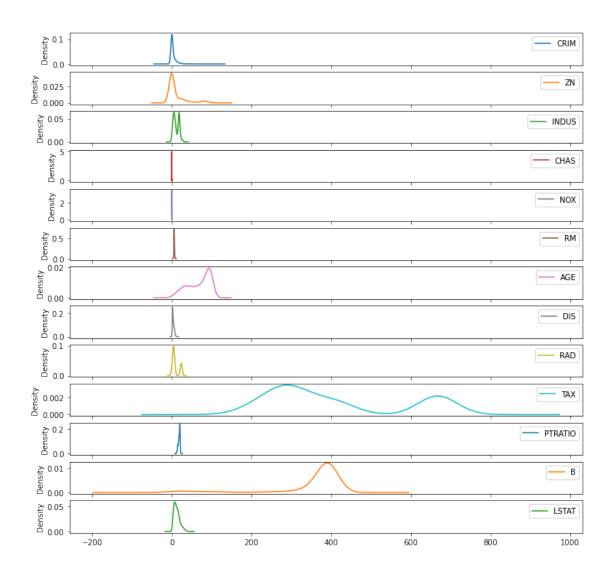
The Boston housing prices dataset has an ethical problem. You can refer to the documentation of this function for further details.

The scikit-learn maintainers therefore strongly discourage the use of this dataset unless the purpose of the code is to study and educate about ethical issues in data science and machine learning.

In this special case, you can fetch the dataset from the original source::

import pandas as pd
import numpy as np

```
data_url = "http://lib.stat.cmu.edu/datasets/boston"
            raw_df = pd.read_csv(data_url, sep="\s+", skiprows=22, header=None)
            data = np.hstack([raw_df.values[::2, :], raw_df.values[1::2, :2]])
            target = raw_df.values[1::2, 2]
        Alternative datasets include the California housing dataset (i.e.
        :func:`~sklearn.datasets.fetch_california_housing`) and the Ames housing
        dataset. You can load the datasets as follows::
            from sklearn.datasets import fetch_california_housing
            housing = fetch_california_housing()
        for the California housing dataset and::
            from sklearn.datasets import fetch_openml
            housing = fetch_openml(name="house_prices", as_frame=True)
        for the Ames housing dataset.
      warnings.warn(msg, category=FutureWarning)
[]: | # define the data/predictors as the pre-set feature names
     df = pd.DataFrame(data.data, columns=data.feature_names)
     # Put the target (housing value -- MEDV) in another DataFrame
     target = pd.DataFrame(data.target, columns=["MEDV"])
[]: df.plot(kind='kde', subplots=True, figsize=(12,12))
[]: array([<AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>, <AxesSubplot:ylabel='Density'>,
            <AxesSubplot:ylabel='Density'>], dtype=object)
```

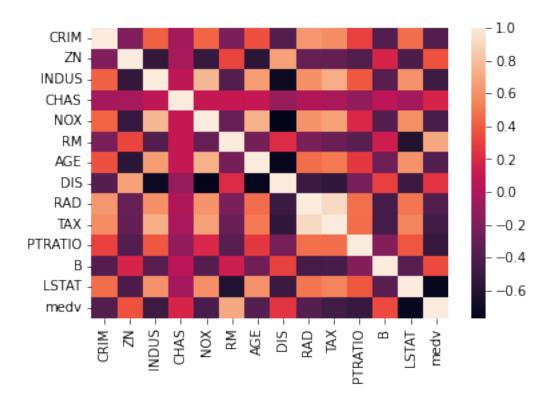


df.corr() []:| []: CRIM ZN **INDUS** CHAS NOX RMAGE CRIM 1.000000 -0.200469 0.406583 -0.055892 0.420972 -0.219247 0.352734 -0.200469 1.000000 -0.533828 -0.042697 -0.516604 0.311991 -0.569537**INDUS** 0.406583 -0.533828 1.000000 0.062938 0.763651 -0.391676 0.644779 CHAS -0.055892 -0.042697 0.062938 1.000000 0.091203 0.091251 0.086518 NOX 0.420972 -0.516604 0.763651 0.091203 1.000000 -0.302188 0.731470 RM -0.219247 0.311991 -0.391676 0.091251 -0.302188 1.000000 -0.240265 0.731470 -0.240265 AGE 0.352734 -0.569537 0.086518 0.644779 1.000000 DIS -0.379670 0.664408 -0.708027 -0.099176 -0.769230 0.205246 -0.747881R.AD 0.625505 -0.311948 0.595129 -0.007368 0.611441 -0.209847 0.456022 TAX $0.582764 \ -0.314563 \ \ 0.720760 \ -0.035587 \ \ \ 0.668023 \ -0.292048$ 0.506456 PTRATIO 0.289946 -0.391679 0.383248 -0.121515 0.188933 -0.355501 0.261515 В -0.385064 0.175520 -0.356977 0.048788 -0.380051 0.128069 -0.273534

```
LSTAT
         0.455621 - 0.412995 \quad 0.603800 - 0.053929 \quad 0.590879 - 0.613808 \quad 0.602339
              DIS
                         RAD
                                   TAX
                                         PTRATIO
                                                         В
                                                                LSTAT
CRIM
        -0.379670
                   0.625505
                             0.582764
                                        0.289946 -0.385064
                                                            0.455621
ZN
         0.664408 -0.311948 -0.314563 -0.391679
                                                  0.175520 -0.412995
INDUS
        -0.708027
                   0.595129
                             0.720760
                                       0.383248 -0.356977
                                                             0.603800
CHAS
        -0.099176 -0.007368 -0.035587 -0.121515 0.048788 -0.053929
NOX
        -0.769230
                  0.611441
                              0.668023
                                        0.188933 -0.380051
                                                             0.590879
RM
         0.205246 -0.209847 -0.292048 -0.355501 0.128069 -0.613808
AGE
        -0.747881
                   0.456022
                             0.506456
                                       0.261515 -0.273534
DIS
         1.000000 -0.494588 -0.534432 -0.232471 0.291512 -0.496996
RAD
        -0.494588
                   1.000000 0.910228 0.464741 -0.444413
                                                            0.488676
TAX
        -0.534432 0.910228
                             1.000000 0.460853 -0.441808
                                                            0.543993
PTRATIO -0.232471 0.464741
                              0.460853
                                       1.000000 -0.177383
                                                            0.374044
         0.291512 -0.444413 -0.441808 -0.177383 1.000000 -0.366087
LSTAT
        -0.496996   0.488676   0.543993   0.374044   -0.366087
                                                             1.000000
```

```
[]: df['medv'] = target
[]: import seaborn as sns
sns.heatmap(df.corr())
```

[]: <AxesSubplot:>



```
[]:
[]:
    target
[]:
          MEDV
          24.0
     0
     1
          21.6
     2
         34.7
     3
          33.4
     4
          36.2
     501
         22.4
    502
         20.6
    503
         23.9
     504 22.0
     505
         11.9
     [506 rows x 1 columns]
[]:
[]: pandas.core.frame.DataFrame
[]: d = pd.DataFrame(df,target['MEDV'])
     d.to_csv("Boston House Prices dataset.csv", index = False)
[]: X = df
     y = target["MEDV"]
[]: lm = linear_model.LinearRegression()
     model = lm.fit(X,y)
[]: predictions = lm.predict(X)
     predictions
[]: array([24., 21.6, 34.7, 33.4, 36.2, 28.7, 22.9, 27.1, 16.5, 18.9, 15.,
            18.9, 21.7, 20.4, 18.2, 19.9, 23.1, 17.5, 20.2, 18.2, 13.6, 19.6,
            15.2, 14.5, 15.6, 13.9, 16.6, 14.8, 18.4, 21., 12.7, 14.5, 13.2,
            13.1, 13.5, 18.9, 20., 21., 24.7, 30.8, 34.9, 26.6, 25.3, 24.7,
            21.2, 19.3, 20., 16.6, 14.4, 19.4, 19.7, 20.5, 25., 23.4, 18.9,
            35.4, 24.7, 31.6, 23.3, 19.6, 18.7, 16. , 22.2, 25. , 33. , 23.5,
            19.4, 22. , 17.4, 20.9, 24.2, 21.7, 22.8, 23.4, 24.1, 21.4, 20. ,
            20.8, 21.2, 20.3, 28., 23.9, 24.8, 22.9, 23.9, 26.6, 22.5, 22.2,
            23.6, 28.7, 22.6, 22. , 22.9, 25. , 20.6, 28.4, 21.4, 38.7, 43.8,
            33.2, 27.5, 26.5, 18.6, 19.3, 20.1, 19.5, 19.5, 20.4, 19.8, 19.4,
```

```
21.7, 22.8, 18.8, 18.7, 18.5, 18.3, 21.2, 19.2, 20.4, 19.3, 22.
20.3, 20.5, 17.3, 18.8, 21.4, 15.7, 16.2, 18., 14.3, 19.2, 19.6,
23. , 18.4, 15.6, 18.1, 17.4, 17.1, 13.3, 17.8, 14. , 14.4, 13.4,
15.6, 11.8, 13.8, 15.6, 14.6, 17.8, 15.4, 21.5, 19.6, 15.3, 19.4,
17. , 15.6, 13.1, 41.3, 24.3, 23.3, 27. , 50. , 50. , 50. , 22.7,
25., 50., 23.8, 23.8, 22.3, 17.4, 19.1, 23.1, 23.6, 22.6, 29.4,
23.2, 24.6, 29.9, 37.2, 39.8, 36.2, 37.9, 32.5, 26.4, 29.6, 50.
32., 29.8, 34.9, 37., 30.5, 36.4, 31.1, 29.1, 50., 33.3, 30.3,
34.6, 34.9, 32.9, 24.1, 42.3, 48.5, 50., 22.6, 24.4, 22.5, 24.4,
20., 21.7, 19.3, 22.4, 28.1, 23.7, 25., 23.3, 28.7, 21.5, 23.,
26.7, 21.7, 27.5, 30.1, 44.8, 50., 37.6, 31.6, 46.7, 31.5, 24.3,
31.7, 41.7, 48.3, 29., 24., 25.1, 31.5, 23.7, 23.3, 22., 20.1,
22.2, 23.7, 17.6, 18.5, 24.3, 20.5, 24.5, 26.2, 24.4, 24.8, 29.6,
42.8, 21.9, 20.9, 44., 50., 36., 30.1, 33.8, 43.1, 48.8, 31.,
36.5, 22.8, 30.7, 50., 43.5, 20.7, 21.1, 25.2, 24.4, 35.2, 32.4,
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20.3, 22.5, 29., 24.8, 22., 26.4, 33.1, 36.1, 28.4, 33.4, 28.2,
22.8, 20.3, 16.1, 22.1, 19.4, 21.6, 23.8, 16.2, 17.8, 19.8, 23.1,
21., 23.8, 23.1, 20.4, 18.5, 25., 24.6, 23., 22.2, 19.3, 22.6,
19.8, 17.1, 19.4, 22.2, 20.7, 21.1, 19.5, 18.5, 20.6, 19. , 18.7,
32.7, 16.5, 23.9, 31.2, 17.5, 17.2, 23.1, 24.5, 26.6, 22.9, 24.1,
18.6, 30.1, 18.2, 20.6, 17.8, 21.7, 22.7, 22.6, 25., 19.9, 20.8,
16.8, 21.9, 27.5, 21.9, 23.1, 50., 50., 50., 50., 50., 13.8,
13.8, 15., 13.9, 13.3, 13.1, 10.2, 10.4, 10.9, 11.3, 12.3, 8.8,
7.2, 10.5, 7.4, 10.2, 11.5, 15.1, 23.2, 9.7, 13.8, 12.7, 13.1,
12.5,
     8.5, 5., 6.3, 5.6, 7.2, 12.1, 8.3, 8.5, 5., 11.9,
27.9, 17.2, 27.5, 15., 17.2, 17.9, 16.3, 7., 7.2, 7.5, 10.4,
8.8, 8.4, 16.7, 14.2, 20.8, 13.4, 11.7, 8.3, 10.2, 10.9, 11.
9.5, 14.5, 14.1, 16.1, 14.3, 11.7, 13.4, 9.6, 8.7, 8.4, 12.8,
10.5, 17.1, 18.4, 15.4, 10.8, 11.8, 14.9, 12.6, 14.1, 13., 13.4,
15.2, 16.1, 17.8, 14.9, 14.1, 12.7, 13.5, 14.9, 20. , 16.4, 17.7,
19.5, 20.2, 21.4, 19.9, 19. , 19.1, 19.1, 20.1, 19.9, 19.6, 23.2,
29.8, 13.8, 13.3, 16.7, 12. , 14.6, 21.4, 23. , 23.7, 25. , 21.8,
20.6, 21.2, 19.1, 20.6, 15.2, 7., 8.1, 13.6, 20.1, 21.8, 24.5,
23.1, 19.7, 18.3, 21.2, 17.5, 16.8, 22.4, 20.6, 23.9, 22. , 11.9])
```

[]: lm.score(X,y)

[]: 1.0

[]: lm.coef_

```
[]: array([-8.54790267e-17, -2.49800181e-16, -5.85252333e-16, -1.44037004e-14, -5.88240665e-16, 1.13667078e-15, -1.84314369e-16, -4.45715513e-16, -2.58907479e-16, -1.04083409e-17, 7.64633582e-17, -2.98372438e-16, -4.51461785e-16, 1.00000000e+00])
```

[]:	
[]:	