



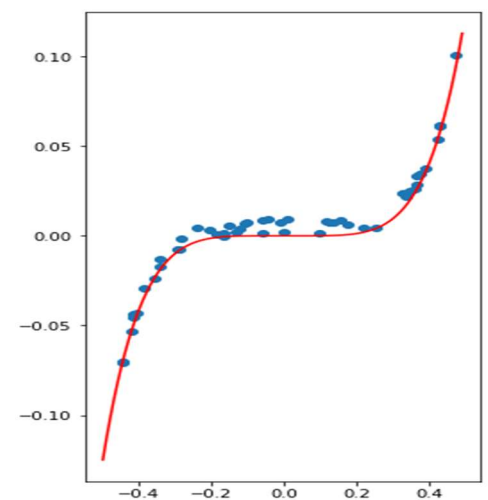
Module : Machine Learning I

Academic Year: 2024/20025

Lab Sheet

Exercise 1:

In this exercise, you will generate a data sample (x,y) as show in the following figure. Additionally, you will use two approaches to tune the value of a : brute-force approach and gradient descent. You will then calculate the average number of iterations required in each approach until achieving the threshold mean squared error (MSE).



1. Generate Data Sample:

- Use NumPy to generate a data sample (x,y) consisting of 20 data points.
- The independent variable x should be generated as random values uniformly distributed between $[-0.5, 0.5]$.
- The dependent variable y should be generated using the formula $y = ax^3 + \text{random noise}$, where a is arbitrary value chosen by you and the random noise is added to simulate real-world data.

2. Brute-Force Approach:

- Randomly sample values of a within the specified range $[0, 100]$ to test.
- Calculate the MSE for each randomly sampled value of a .
- Repeat this process until the MSE falls below a specified threshold=0.015.
- Calculate the average number of iterations needed to reach the threshold MSE.
- How many sampling operations are theoretically required to find the value of a , given that a is sampled from a normal distribution with a mean of 0 and standard deviation of 1? Calculate for the true $a = 0.1$ and $a = 0.31$, assuming values are rounded to two decimals; What are the best and the worst scenario for the value of a ?

3. Gradient Descent to Tune a :

- Initialize a random value for a .

- Perform gradient descent to iteratively update the value of a such that it minimizes the MSE between the predicted and actual values of y .
- Use a learning rate and a predefined number of iterations for gradient descent.
- Calculate the average number of iterations required until achieving the threshold $MSE = 0.015$.

4. Visualize Data Sample and Predictions:

- Plot the generated data sample (x,y) using a scatter plot.
- Plot the final predictions obtained after tuning a using both approaches.

5. Reflection:

- Reflect on the differences between the brute-force approach and gradient descent in terms of computational efficiency and effectiveness in finding the optimal value of a .
- Discuss the implications of the average number of iterations on the performance and scalability of each approach.

Exercise:

In this exercise, you will implement the gradient descent algorithm to solve a linear regression problem. Given a dataset consisting of (x, y) coordinates, your task is to iteratively update the parameter a to minimize the cost function using both Mean Squared Error (MSE) and Mean Absolute Error (MAE) losses. Additionally, you will estimate the configurations (a) for the first two iterations of the gradient descent algorithm.

- **Dataset:** You are provided with a dataset containing 8 samples with the following x and y coordinates:
 - $X = [-0.3, -0.1, -0.4, 0.2, 0.1, -0.0, 0.4, -0.05]$
 - $Y = [-0.9, 0., -4.4, 0.5, 0.3, 0.9, 7.7, 0.6]$
- **Tasks:**
 - Calculate the Cost $J(\theta)$ using both MSE and MAE losses.
 - Define the objective function to be minimized.
 - Solve the linear regression problem iteratively using the gradient descent algorithm.
 - Estimate the configurations (a) for the two first iterations.
 - Transform this solution into Python code.