

1. (4 points) Recall that given a set  $S$ , the power set of  $S$  is denoted  $\mathbb{P}(S)$ . Suppose  $A = \{1, 2\}$  and  $B = \{2, 3\}$ . List all the elements of the following sets:

- (a)  $\mathbb{P}(A \cap B)$   
(b)  $\mathbb{P}(A \times B)$

(a) 1 pt for correctness; 1 pt for work (can get full pts if correct).  
(b) 1 pt for correctness; 1 pt for work (can get full pts if correct).

(please turn page)

2. (4 points) Define  $f : \mathbb{Z} \rightarrow \mathbb{Z}$  by the rule  $f(n) = 2n$ , for all integers  $n$ .
- (a) Is  $f$  one-to-one? Prove or give a counterexample.

1 pt for set up of proof with two arbitrary elements of  $\mathbb{Z}$  that are not equal  
2 pt for steps to show that  $\Rightarrow f(\text{element\_1}) \neq f(\text{element\_2})$   
1 pt for conclusion ( $f$  is one-to-one)