

The Ancient Secrets



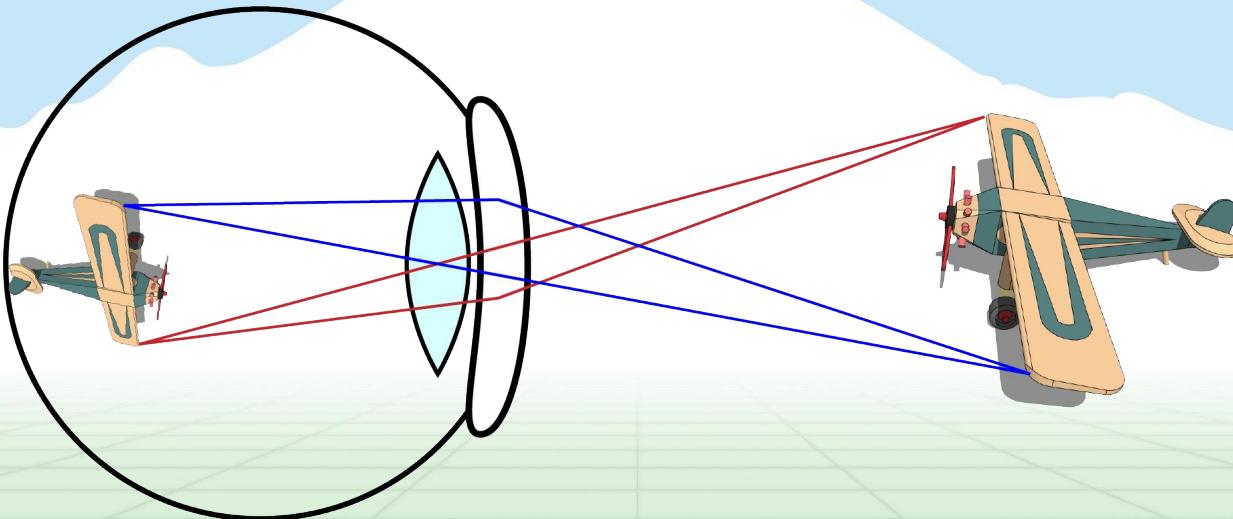
Computer Vision

Previously
On



Ancient Secrets
of Computer Vision

Eyes: projection onto retina



Camera: projection onto sensor array

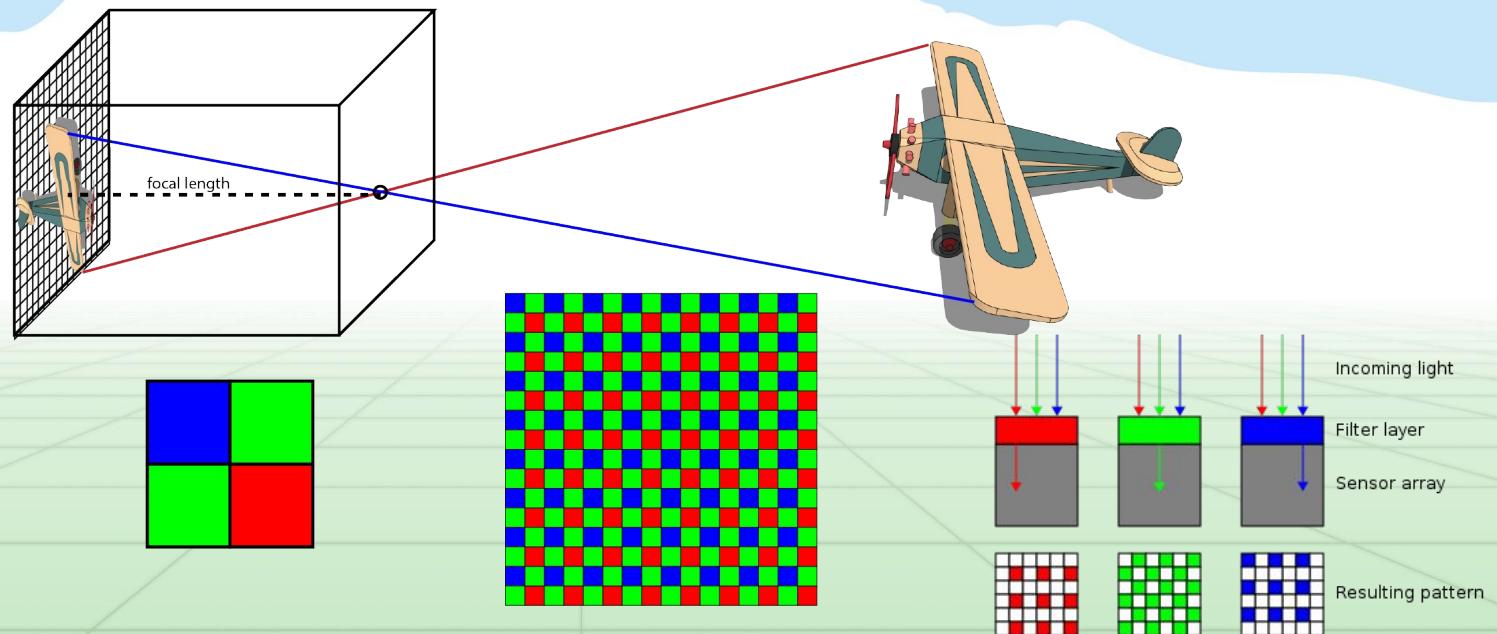
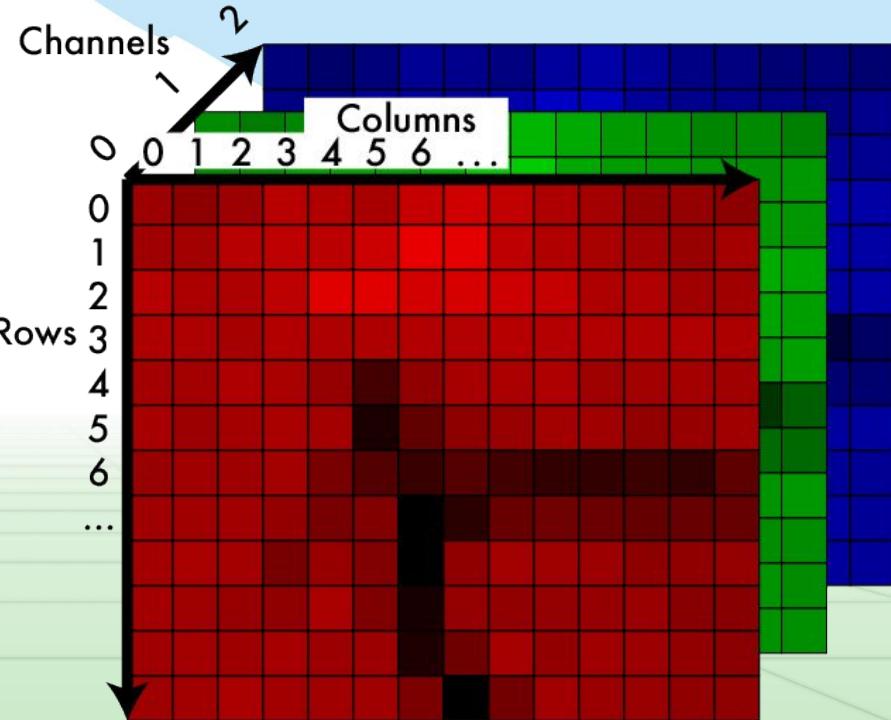


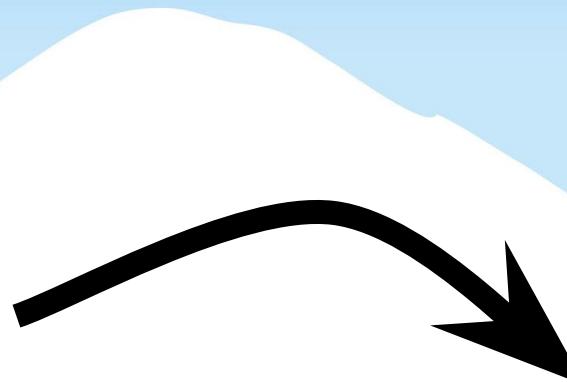
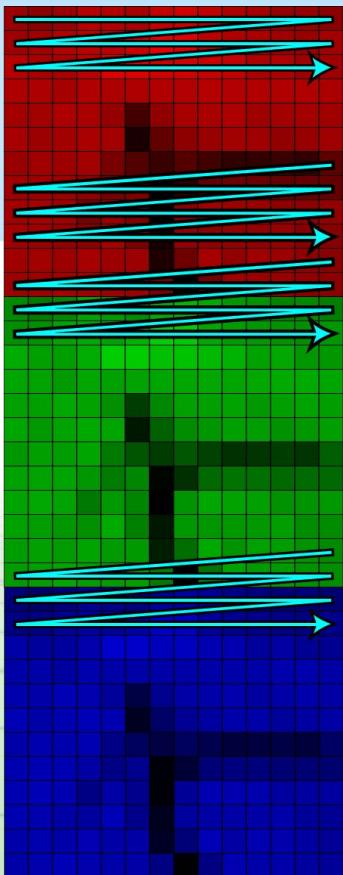
Image: tensor of light values

Addressing pixels:

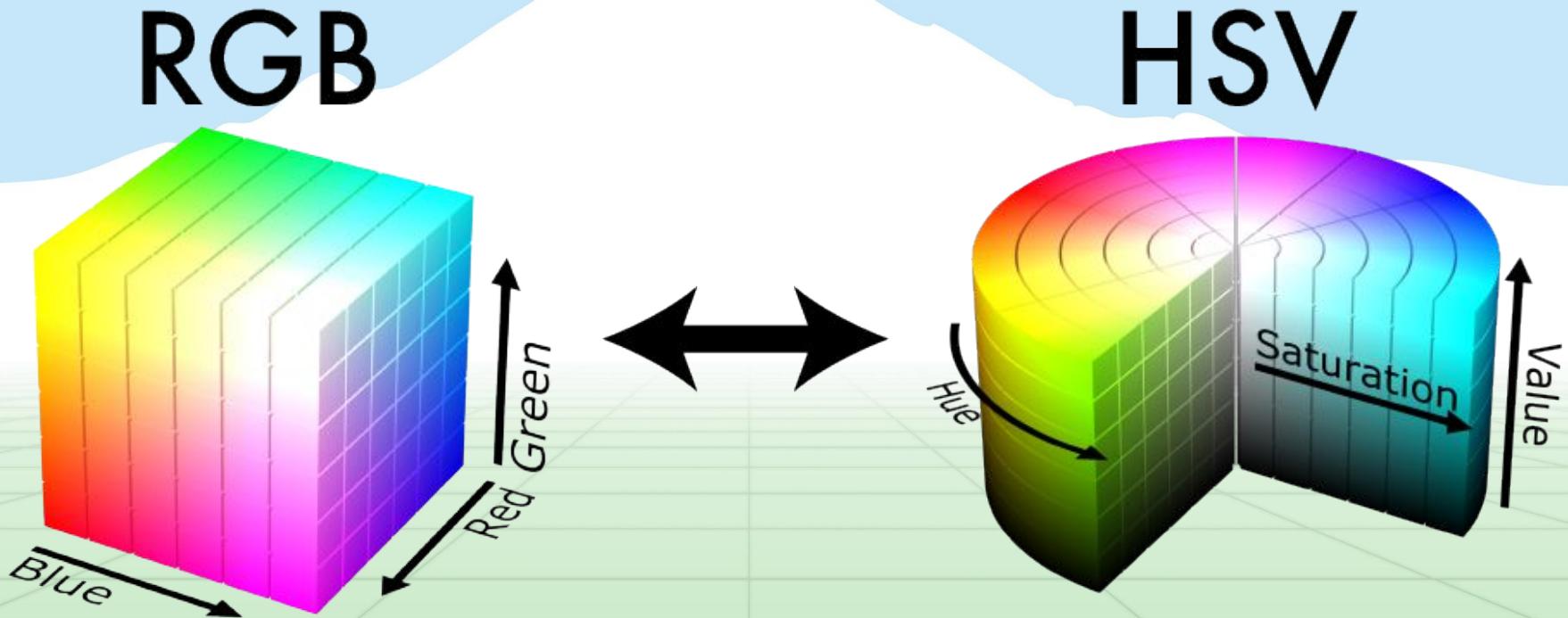
- Size: $W \times H \times C$
- Index: (x, y, z)
 - Column x , row y , chan z
- Like cartesian but flipped



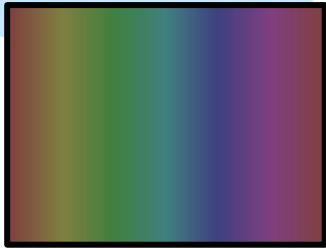
CHW for storing in 1d array



Other colorspaces are fun!



Or pattern...



Nearest neighbor: what it sounds like

$f(x,y,z) = \text{Im}(\text{round}(x), \text{round}(y), z)$

- Looks blocky
- Common pitfall:
Integer division
rounds down in C
- Note: z is still int

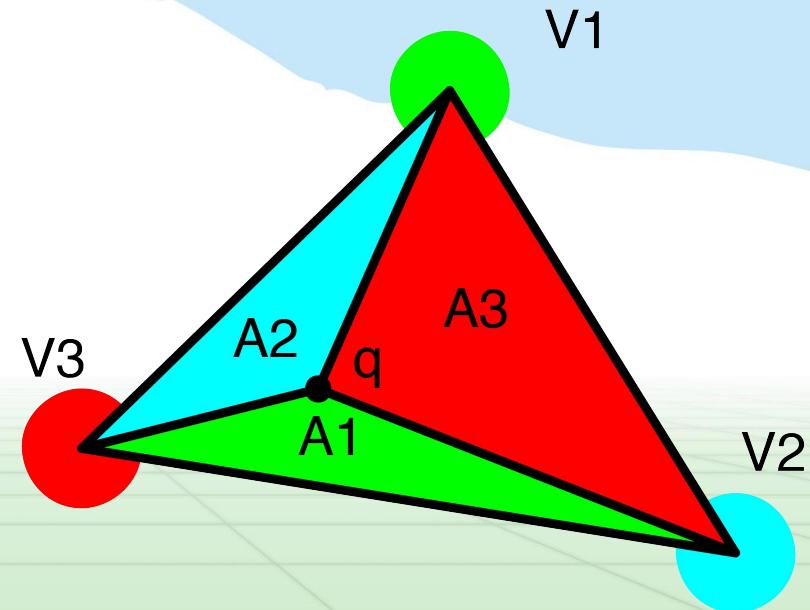


Triangle interpolation: for less structured image

Weighted sum using of triangles:

$$Q = V1 * A1 + V2 * A2 + V3 * A3$$

Should normalize this based on total area



Bilinear interpolation: for grids, pretty good

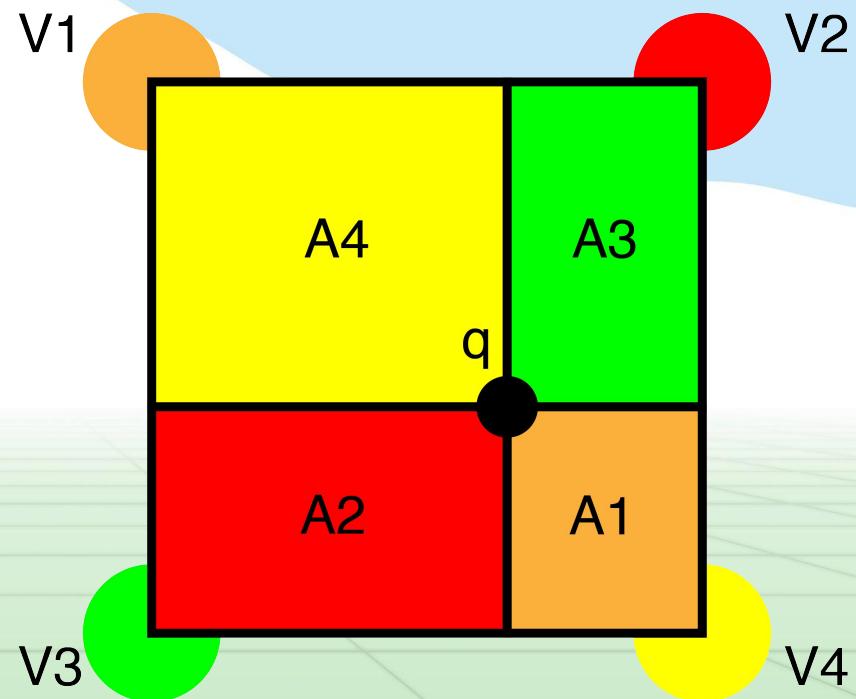
This time find the closest pixels in a box

Same plan, weighted sum based on area of opposite rectangle

$$Q = V1*A1 + V2*A2 + V3*A3 + V4*A4$$

Still need to normalize!

Or do we?



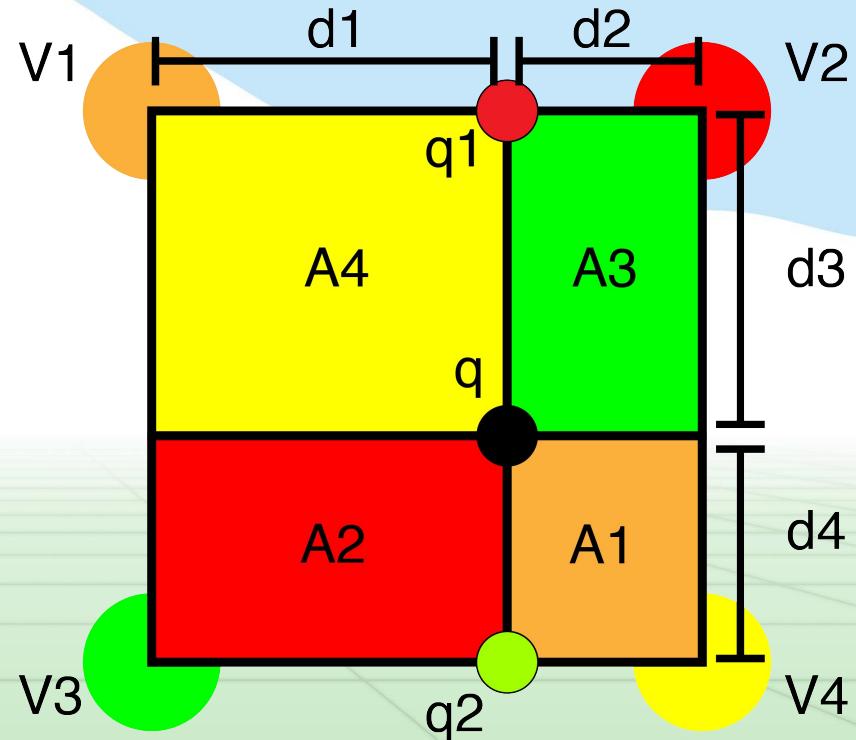
Bilinear interpolation: for grids, pretty good

Alternatively, linear
interpolation of linear
interpolates

$$q_1 = V_1 \cdot d_2 + V_2 \cdot d_1$$

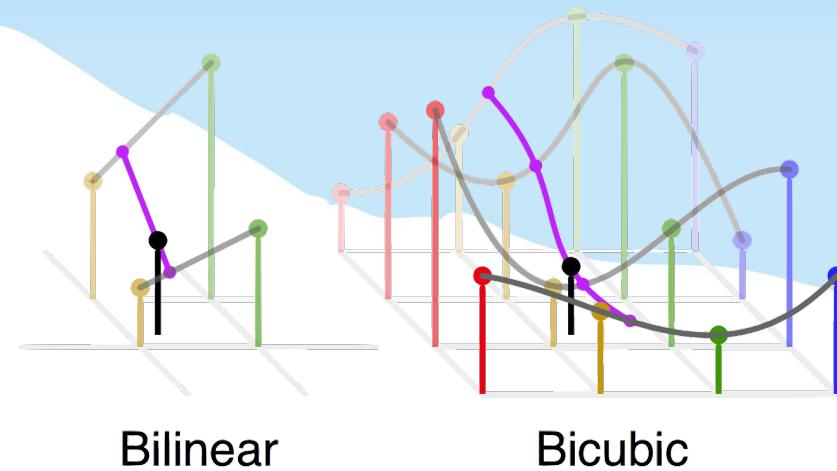
$$q_2 = V_3 \cdot d_2 + V_4 \cdot d_1$$

$$q = q_1 \cdot d_4 + q_2 \cdot d_3$$



Bicubic sampling: more complex, maybe better?

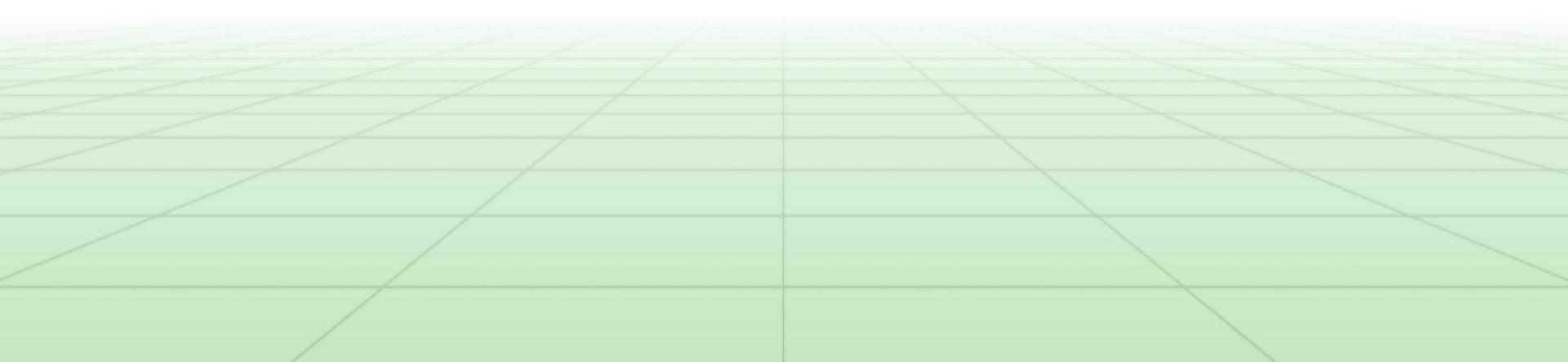
- A cubic interpolation of 4 cubic interpolations
- Smoother than bilinear, no “star”
- 16 nearest neighbors
- Fit 3rd order poly:
 - $f(x) = a + bx + cx^2 + dx^3$
- Interpolate along axis
- Fit another poly to interpolated values



Chapter Four



Convolutions!



So what is this interpolation
useful for?

Image resizing!

Say we want to increase
the size of an image...

This is a beautiful
image of a sunset... it's
just very small...

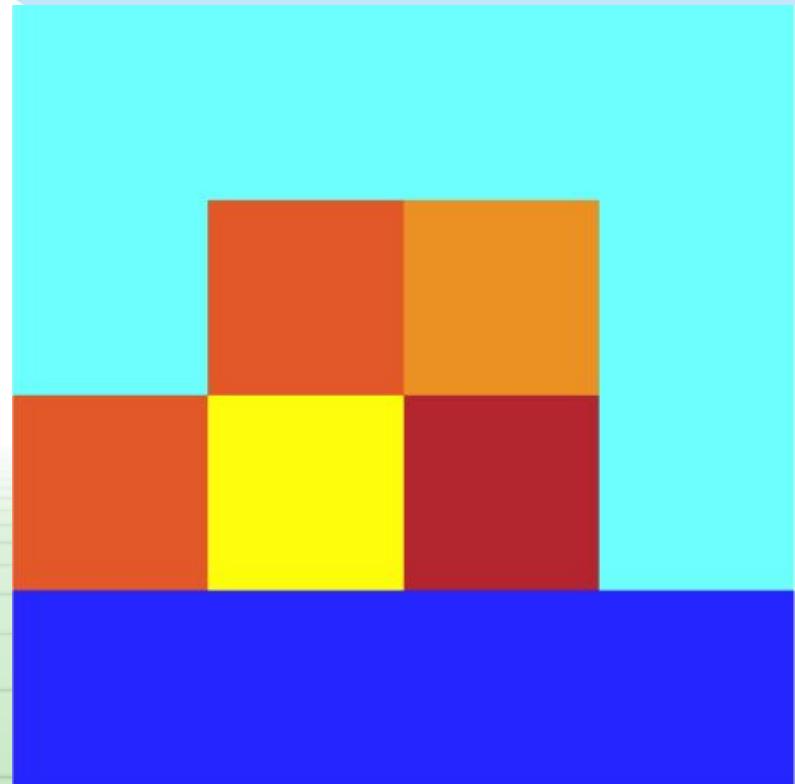
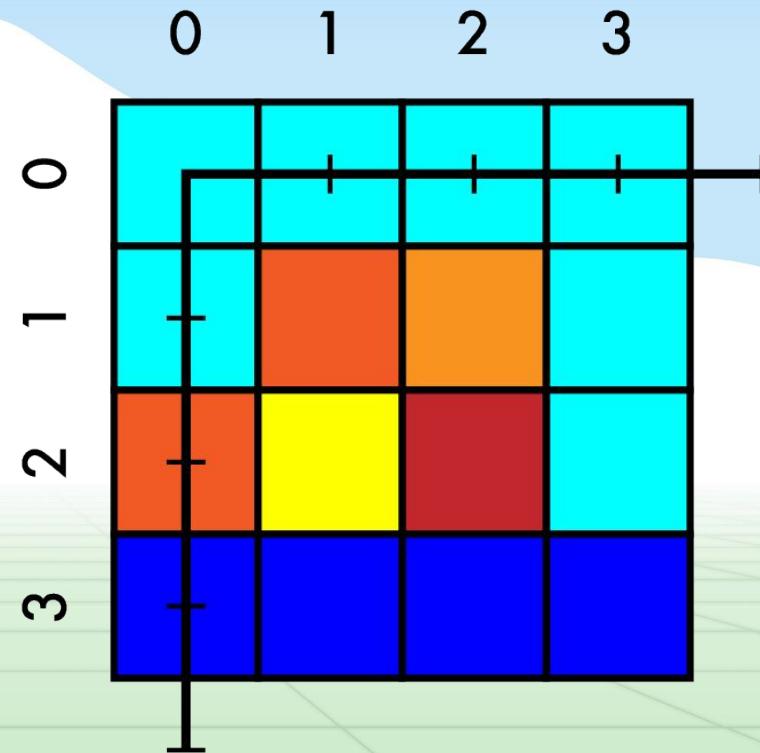


Image resizing!

Say we want to increase
the size of an image...

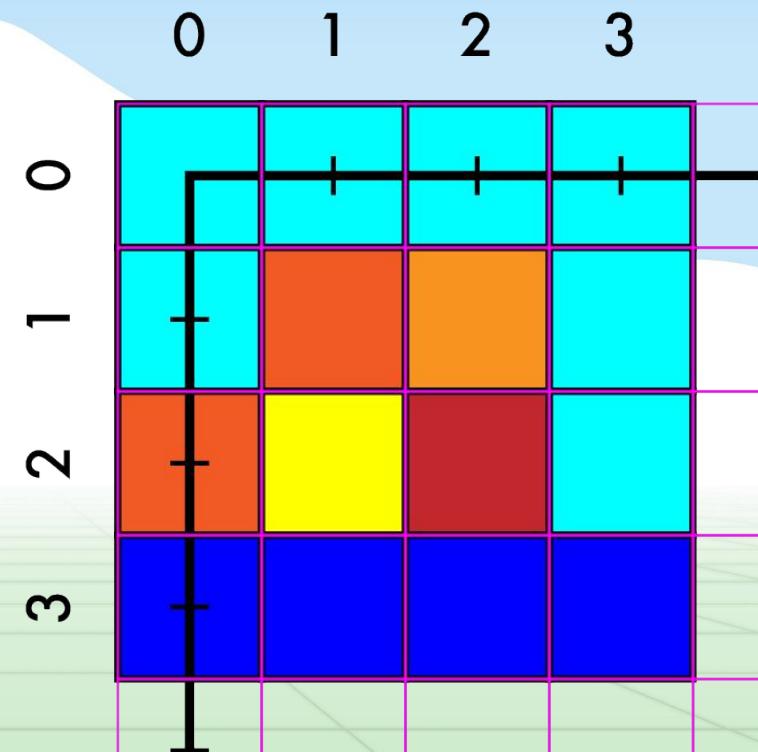
This is a beautiful
image of a sunset... it's
just very small...

Say we want to increase
size $4 \times 4 \rightarrow 7 \times 7$



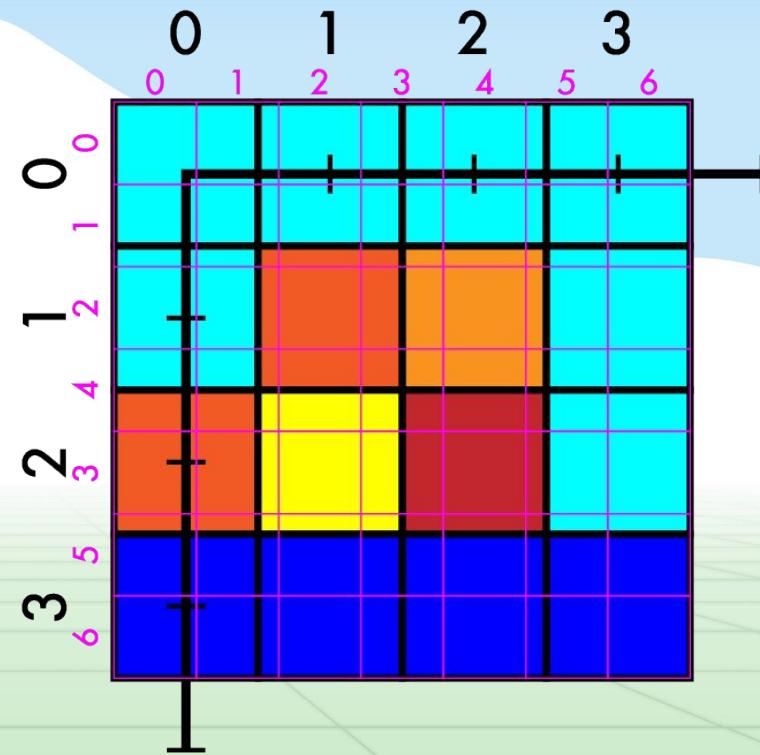
Resize 4x4 -> 7x7

- Create our new image



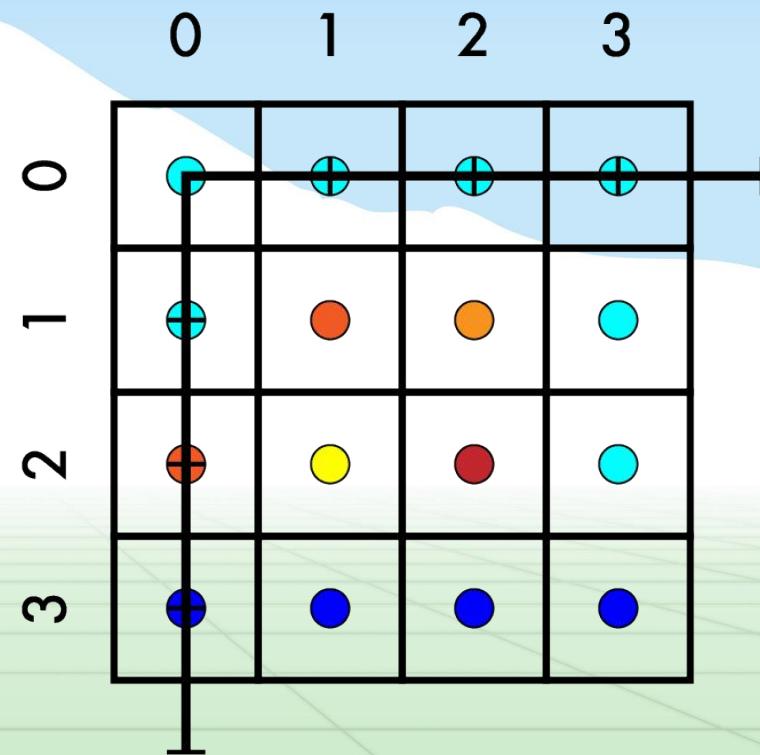
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates



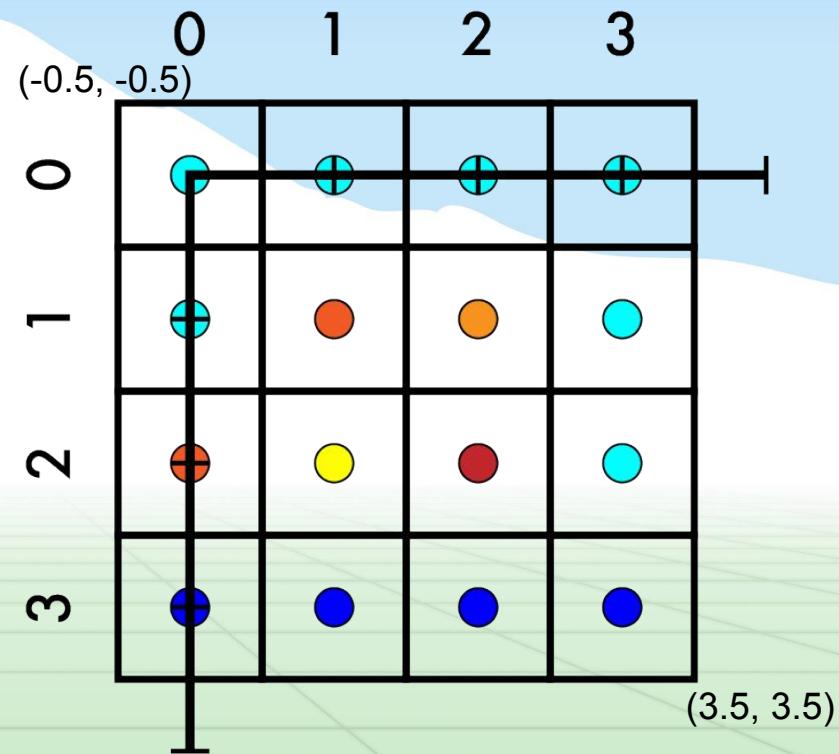
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates



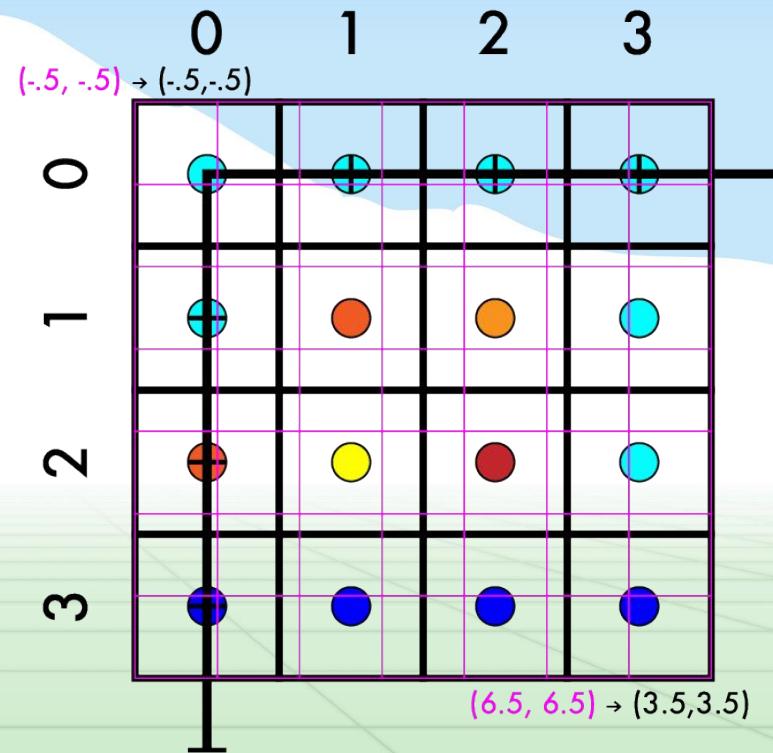
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates



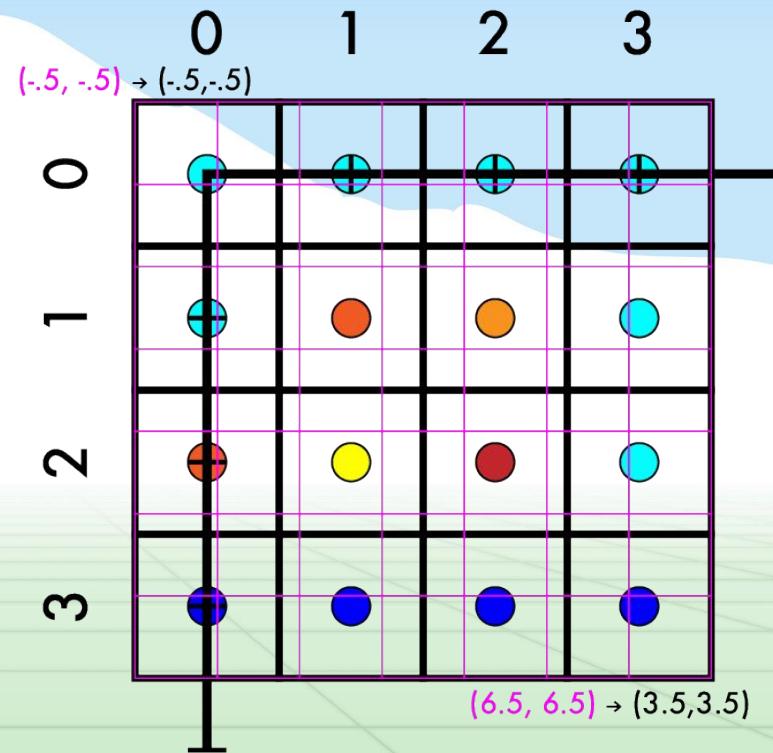
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$



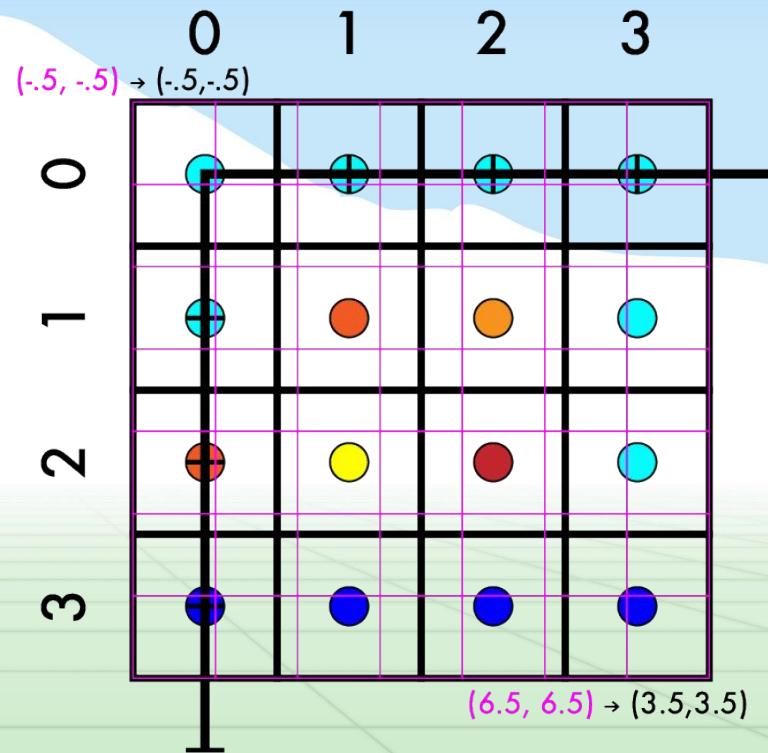
Resize 4x4 -> 7x7

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- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a * 7 = 4$



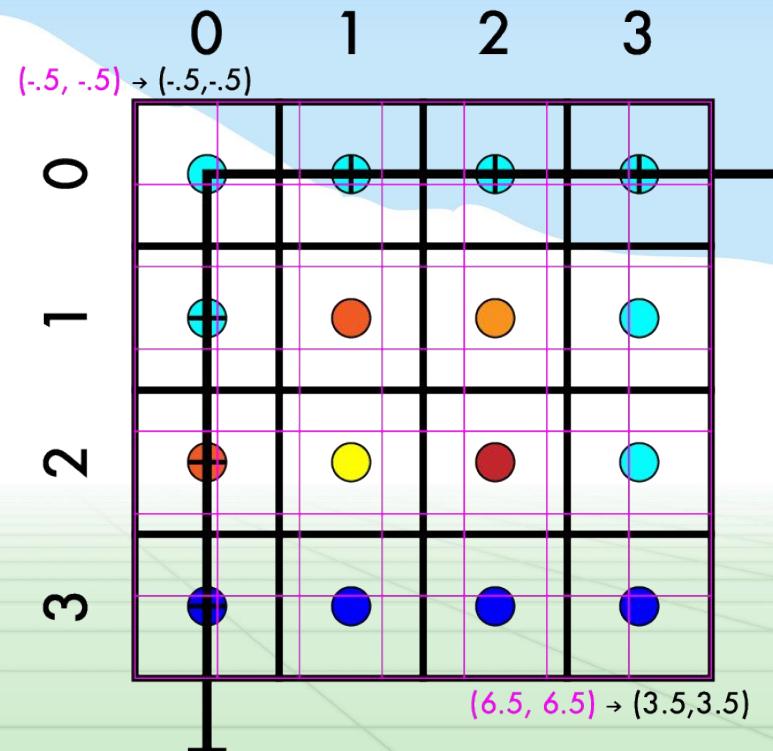
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a * 7 = 4$
 - $a = 4/7$



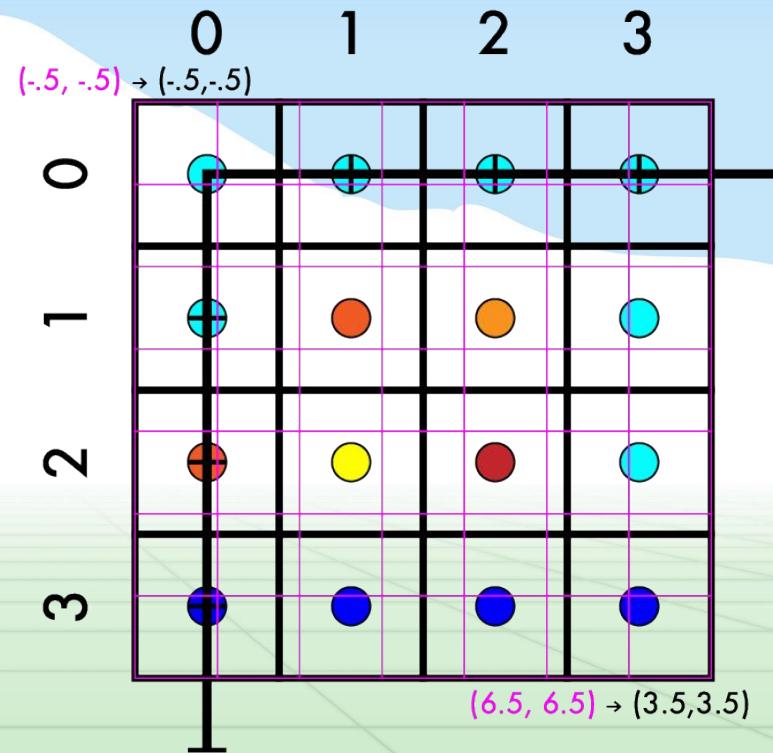
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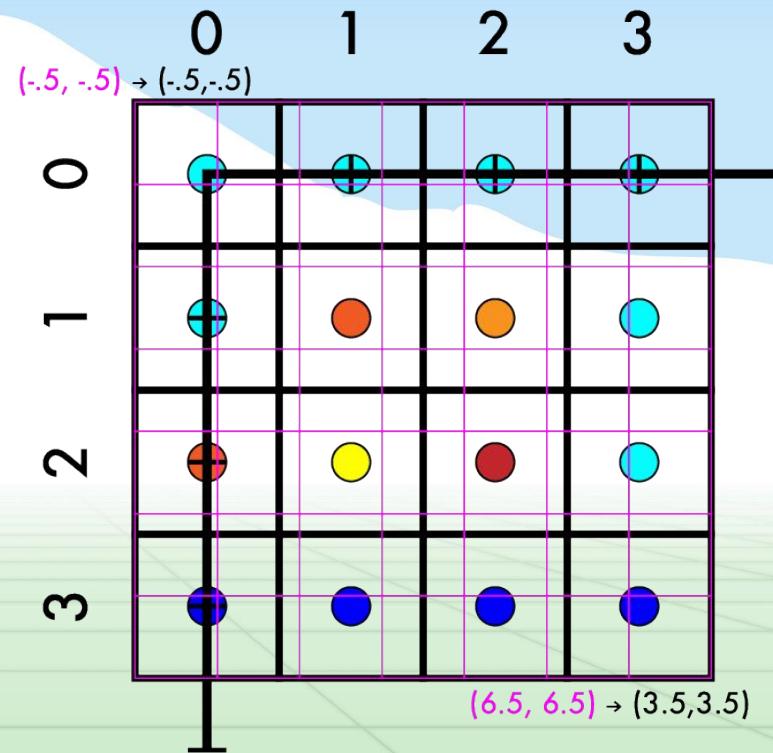
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- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a = 4/7$
 - $a * -.5 + b = -.5$



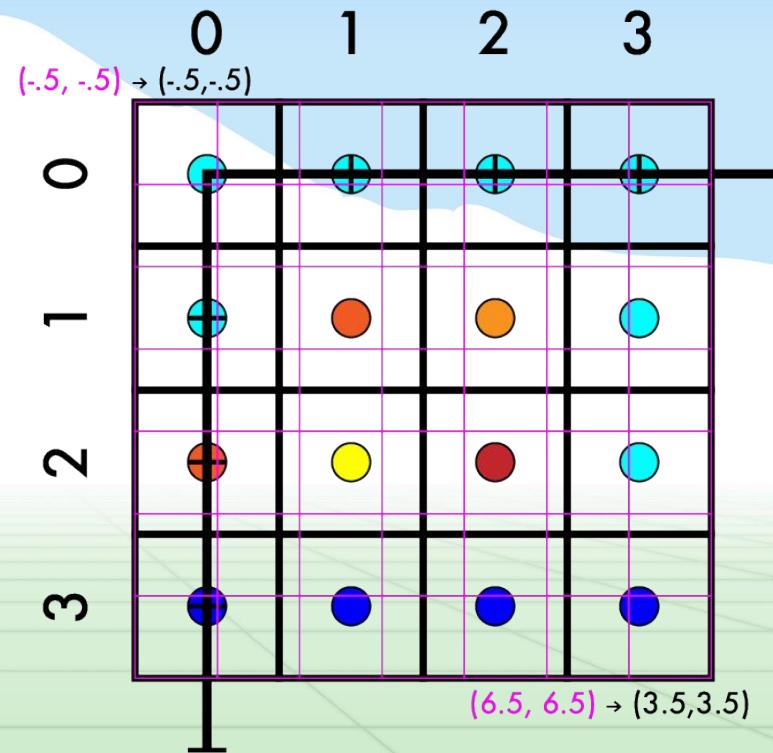
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a = 4/7$
 - $a * -.5 + b = -.5$
 - $4/7 * -1/2 + b = -1/2$



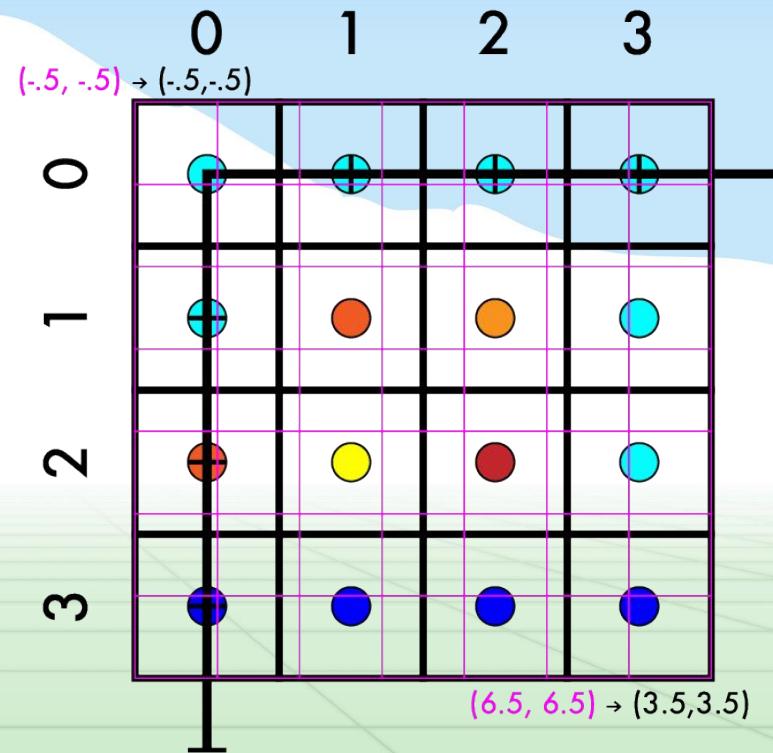
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a = 4/7$
 - $a * -.5 + b = -.5$
 - $4/7 * -1/2 + b = -1/2$
 - $-4/14 + b = -7/14$



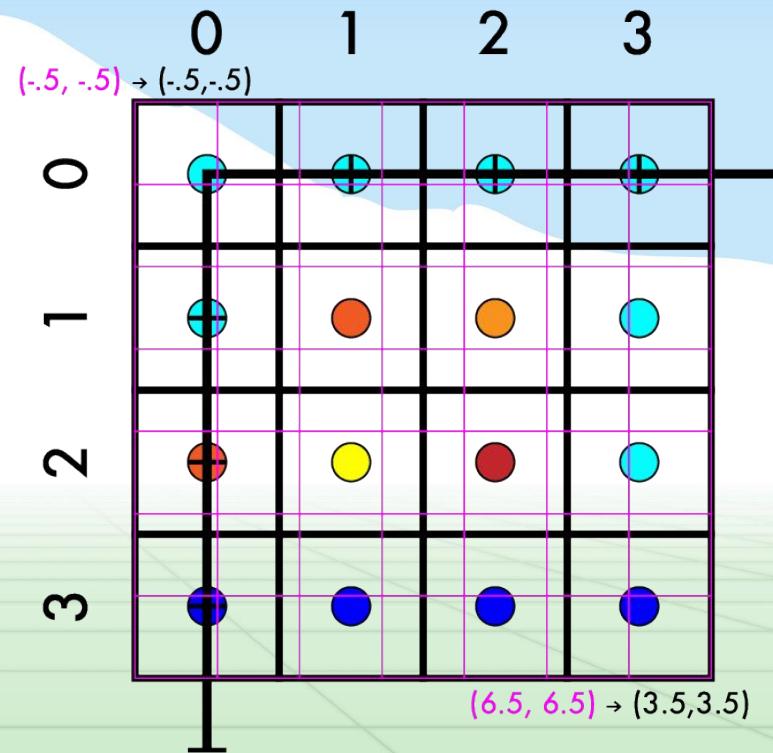
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a = 4/7$
 - $a * -.5 + b = -.5$
 - $4/7 * -1/2 + b = -1/2$
 - $-4/14 + b = -7/14$
 - $b = -3/14$



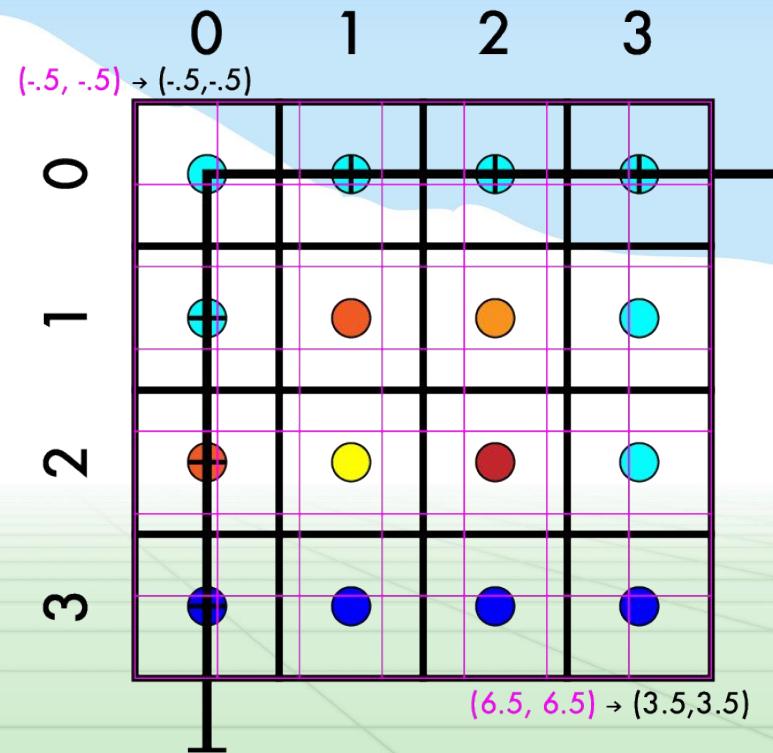
Resize 4x4 -> 7x7

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- Match up coordinates
 - System of equations
 - $aX + b = Y$
 - $a * -.5 + b = -.5$
 - $a * 6.5 + b = 3.5$
 - $a = 4/7$
 - $b = -3/14$



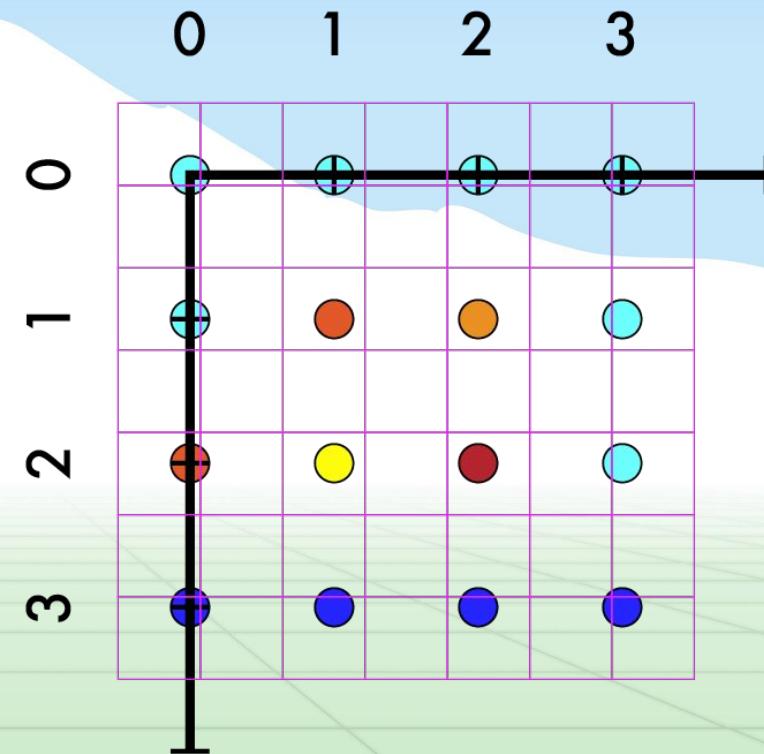
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$



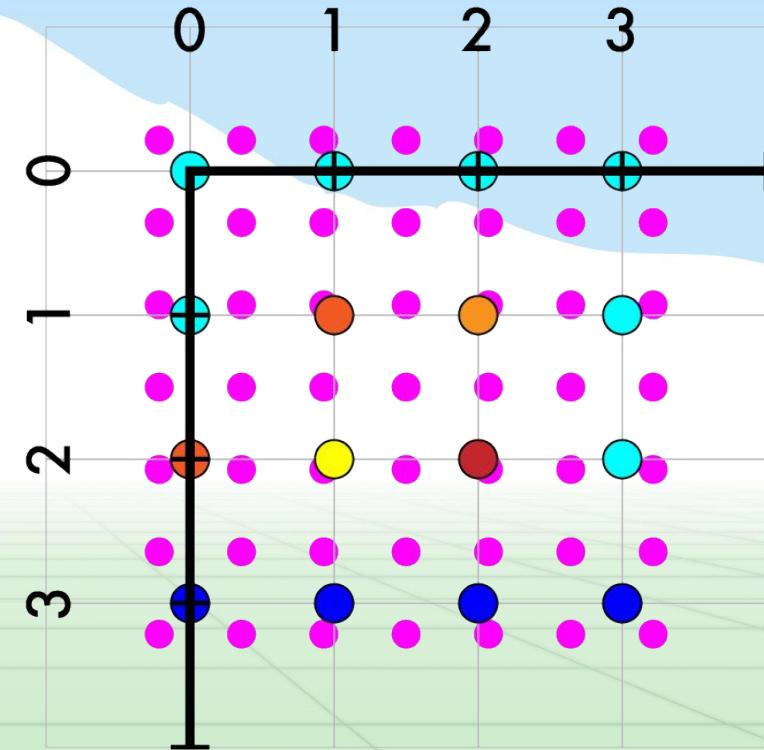
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$



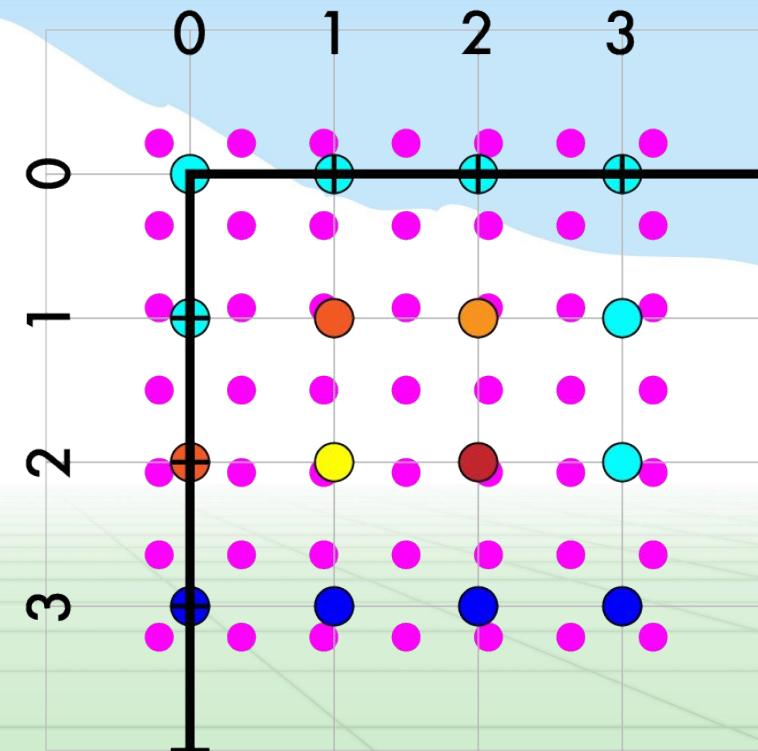
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts



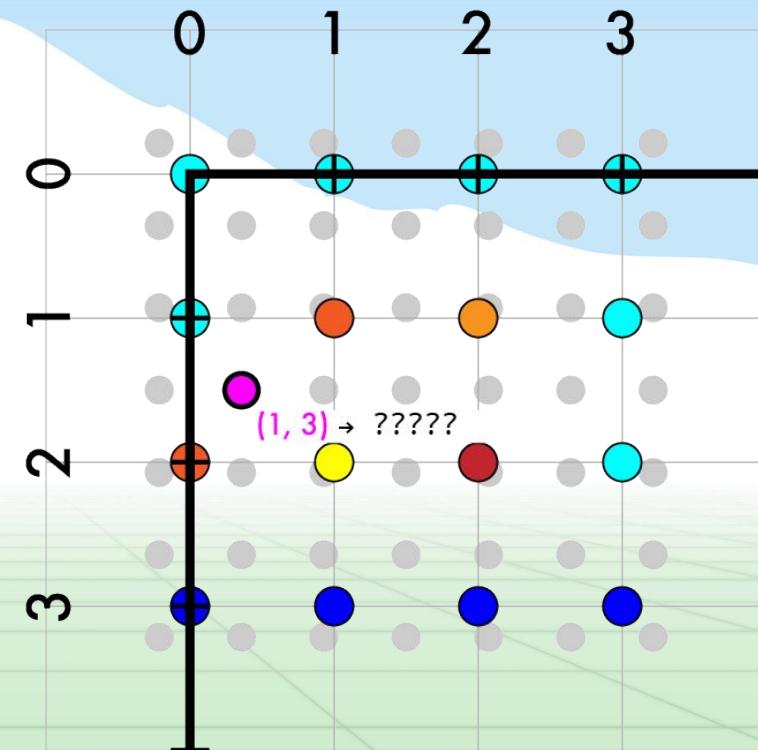
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords



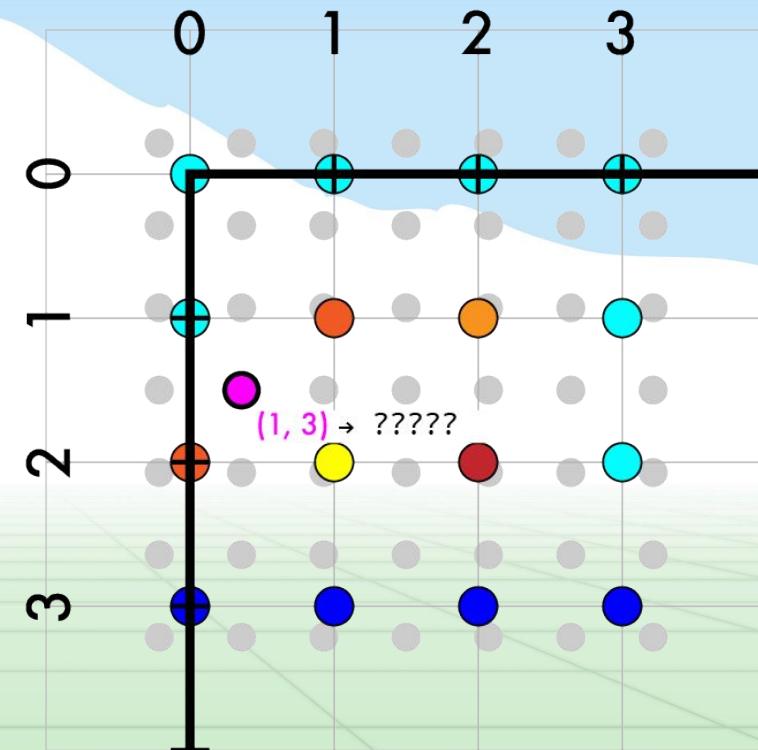
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - (1, 3)



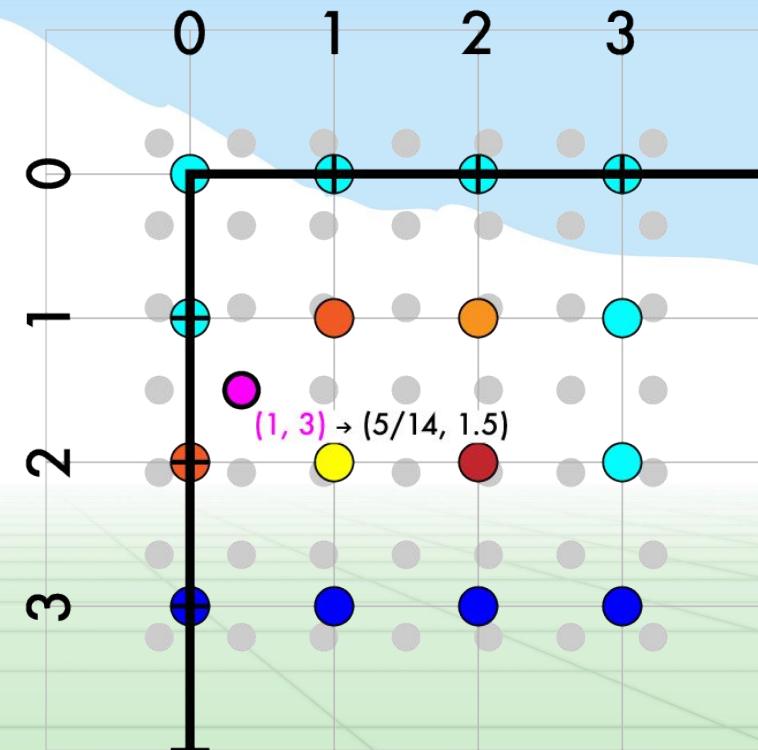
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3)$
 - $4/7 * 1 - 3/14$
 - $4/7 * 3 - 3/14$



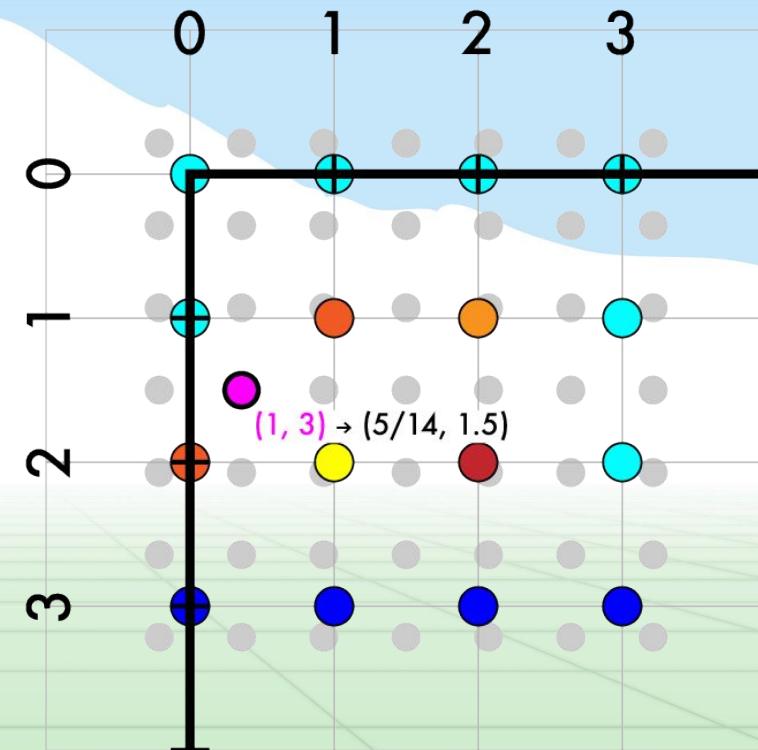
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - (1, 3)
 - $4/7 * 1 - 3/14$
 - $4/7 * 3 - 3/14$
 - $(5/14, 7/14)$



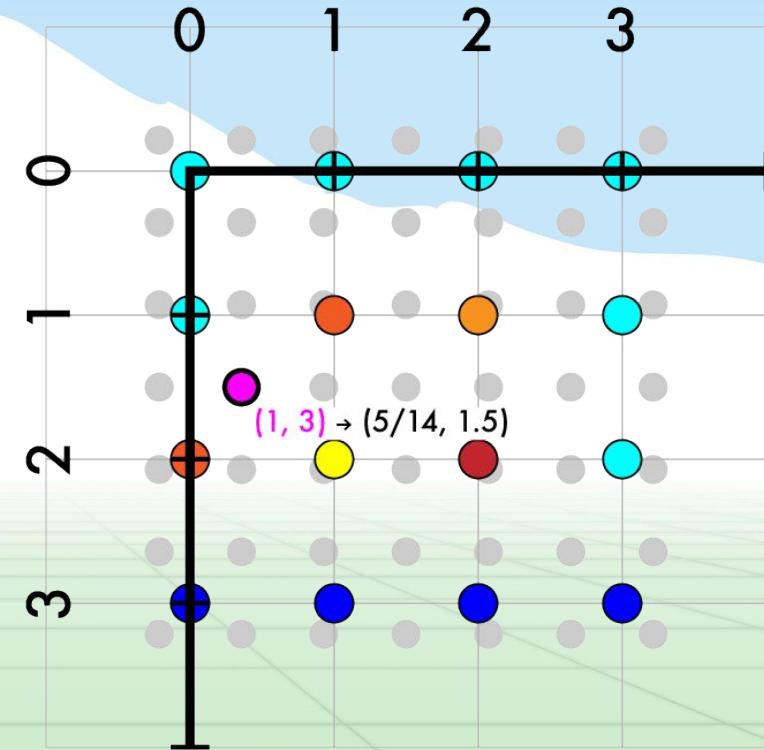
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$



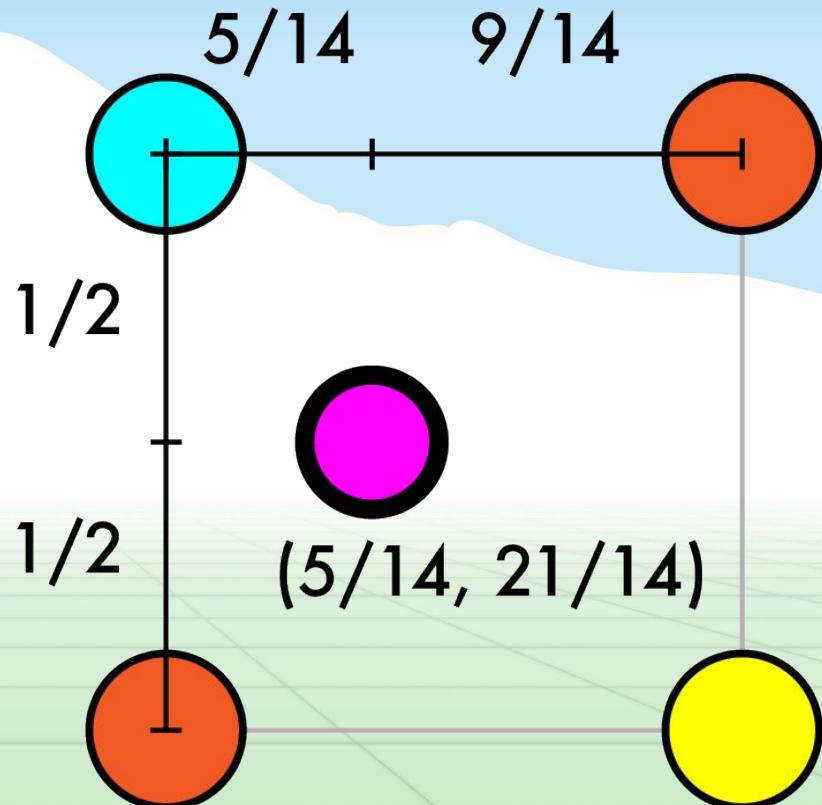
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values



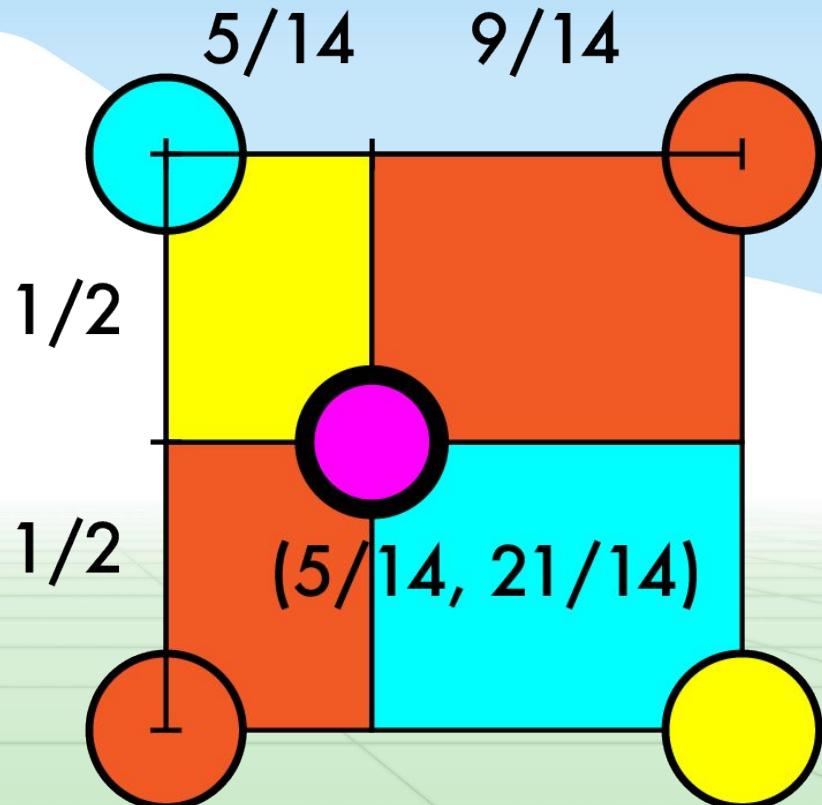
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values



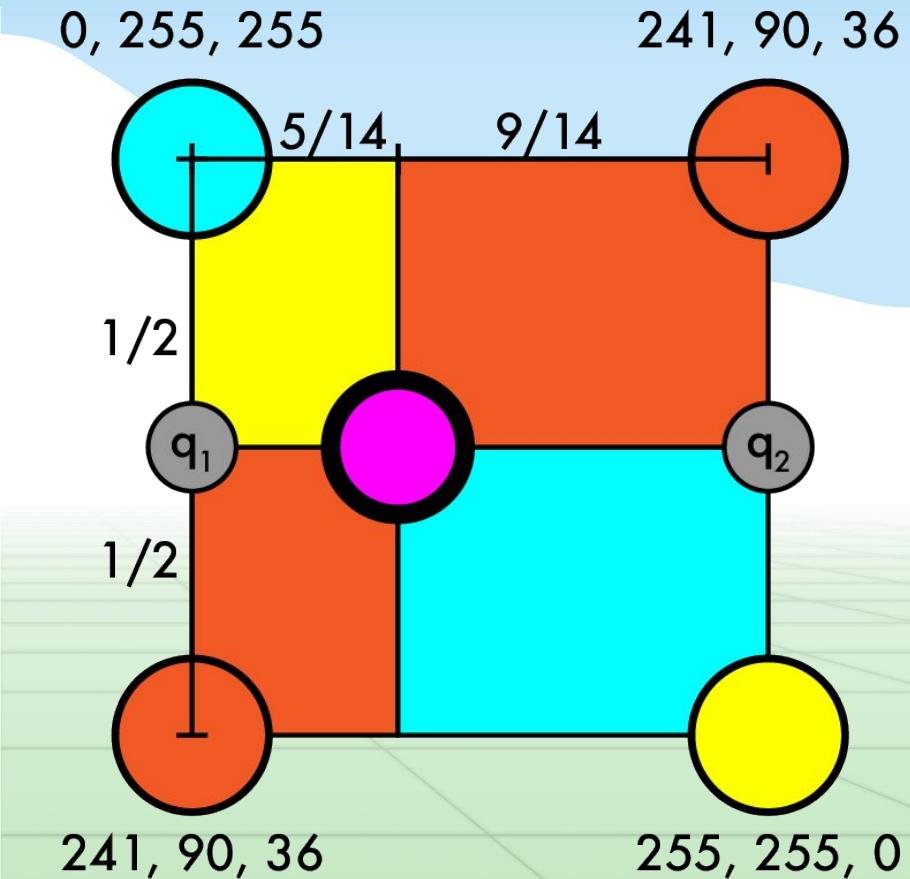
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - Size of opposite rects



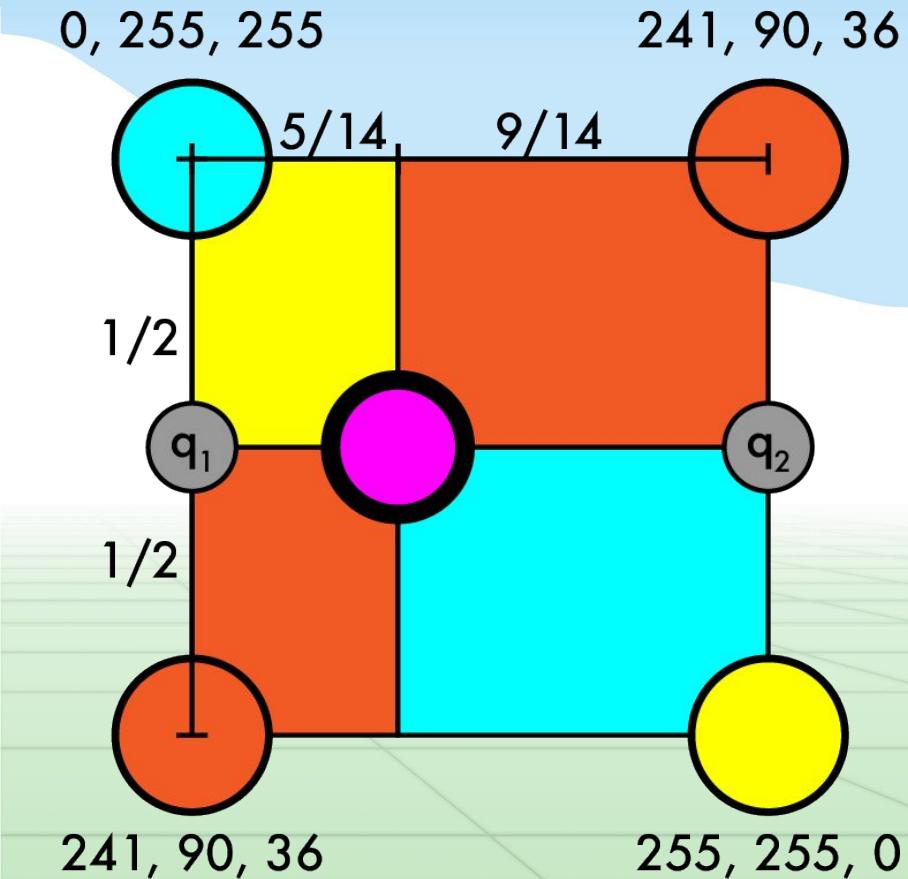
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - Size of opposite rects
 - OR find q_1 and q_2 , then interpolate between them



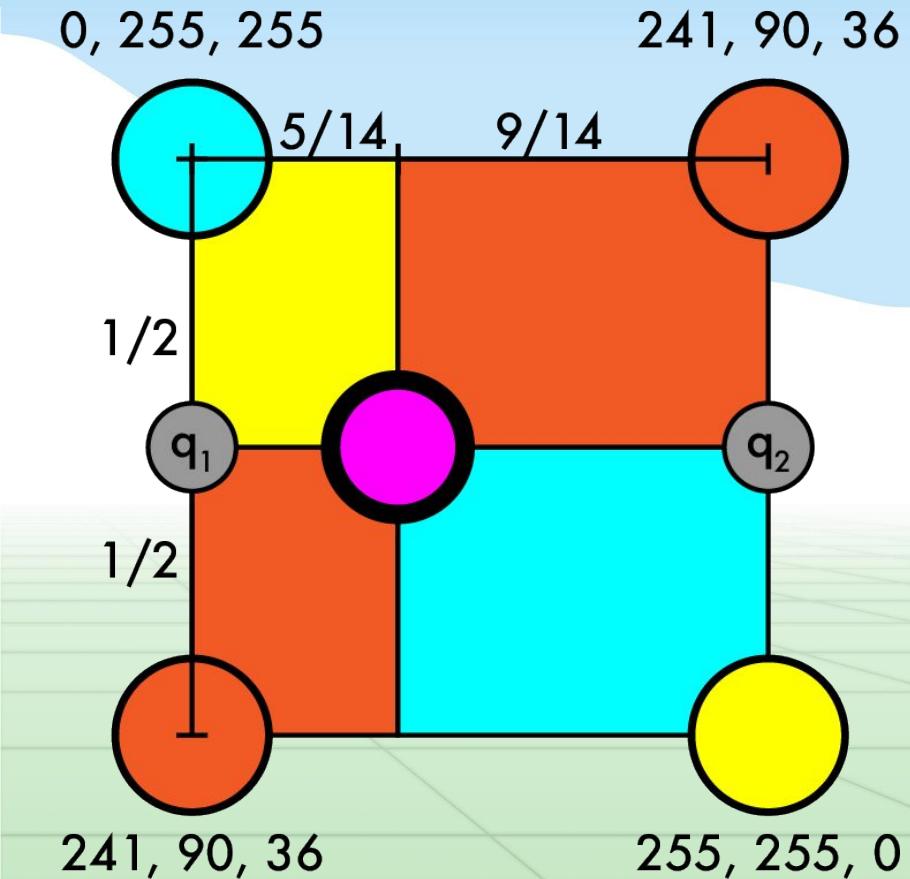
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = r_1, g_1, b_1$
 - $r_1 = .5*0 + .5*241$
 - $g_1 = .5*255 + .5*90$
 - $b_1 = .5*241 + .5*36$



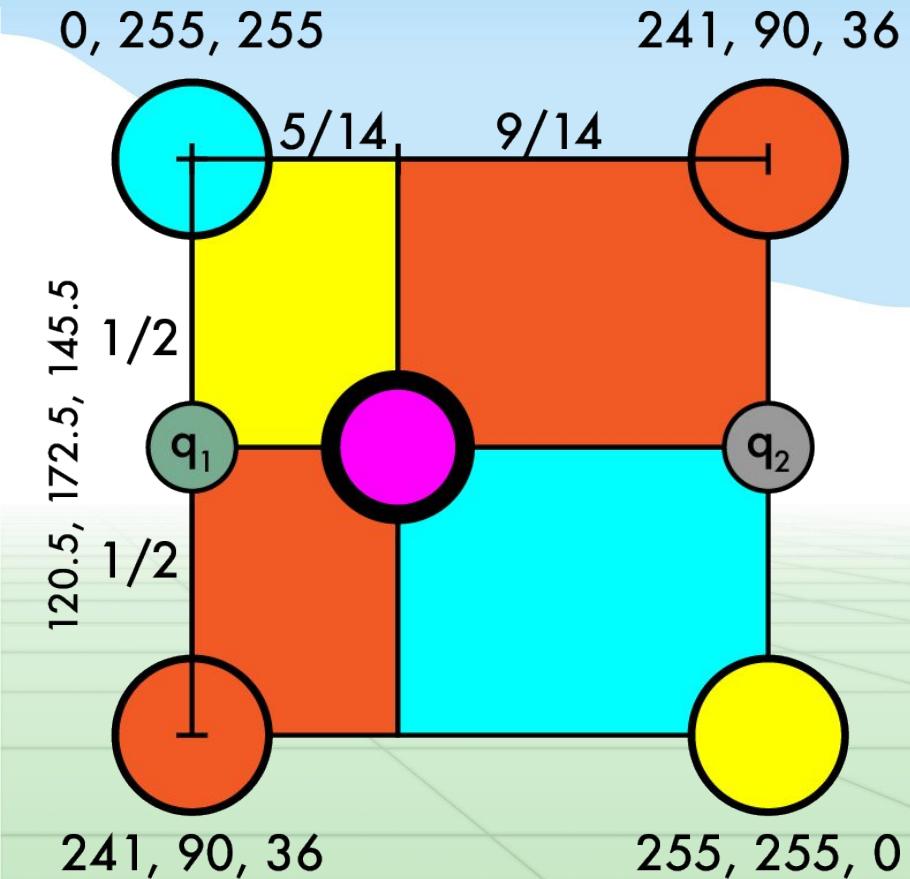
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = r_1, g_1, b_1$
 - $r_1 = .5*0 + .5*241$
 - $g_1 = .5*255 + .5*90$
 - $b_1 = .5*241 + .5*36$



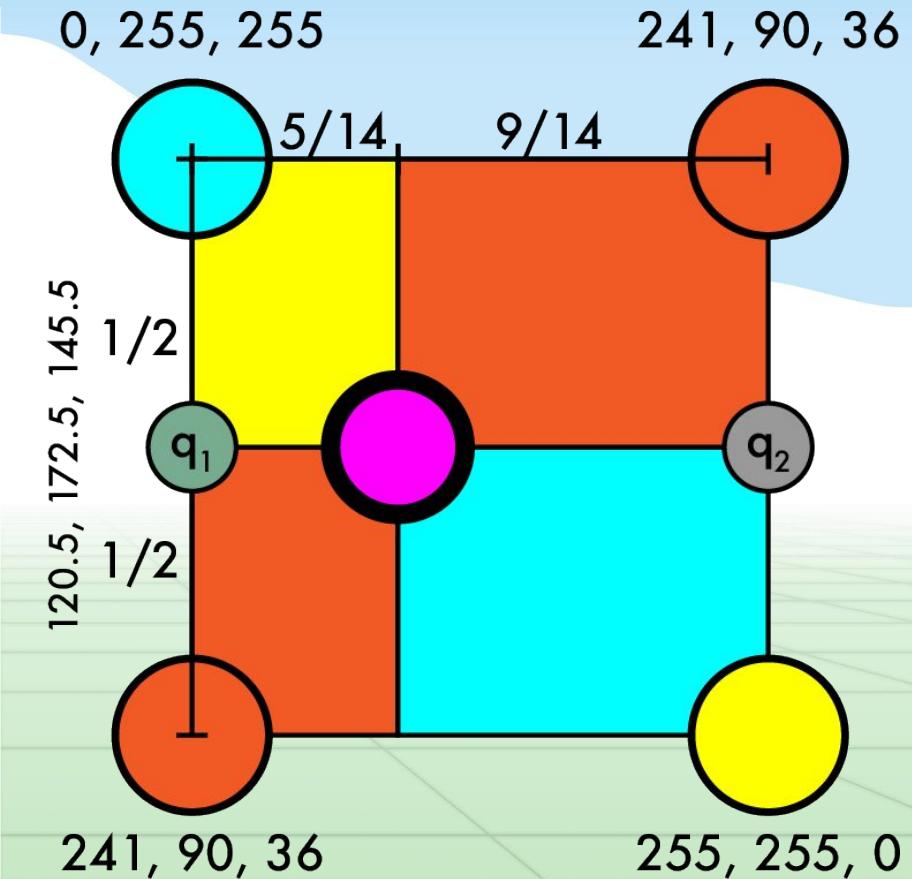
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = r_2, g_2, b_2$



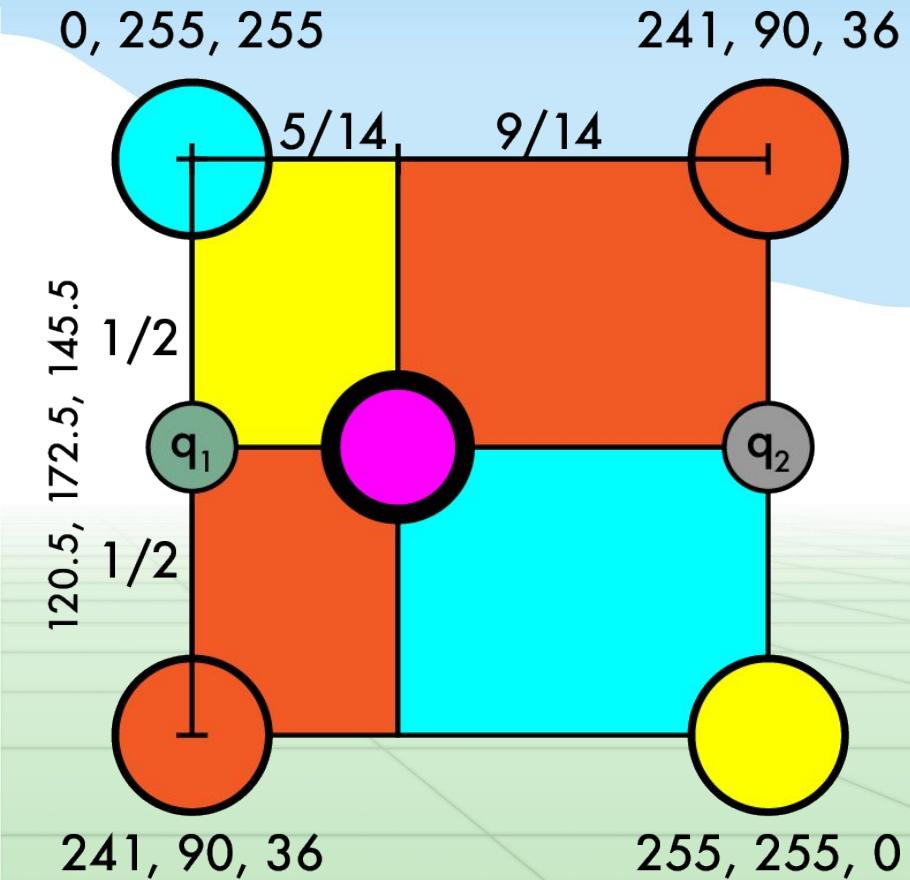
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
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 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
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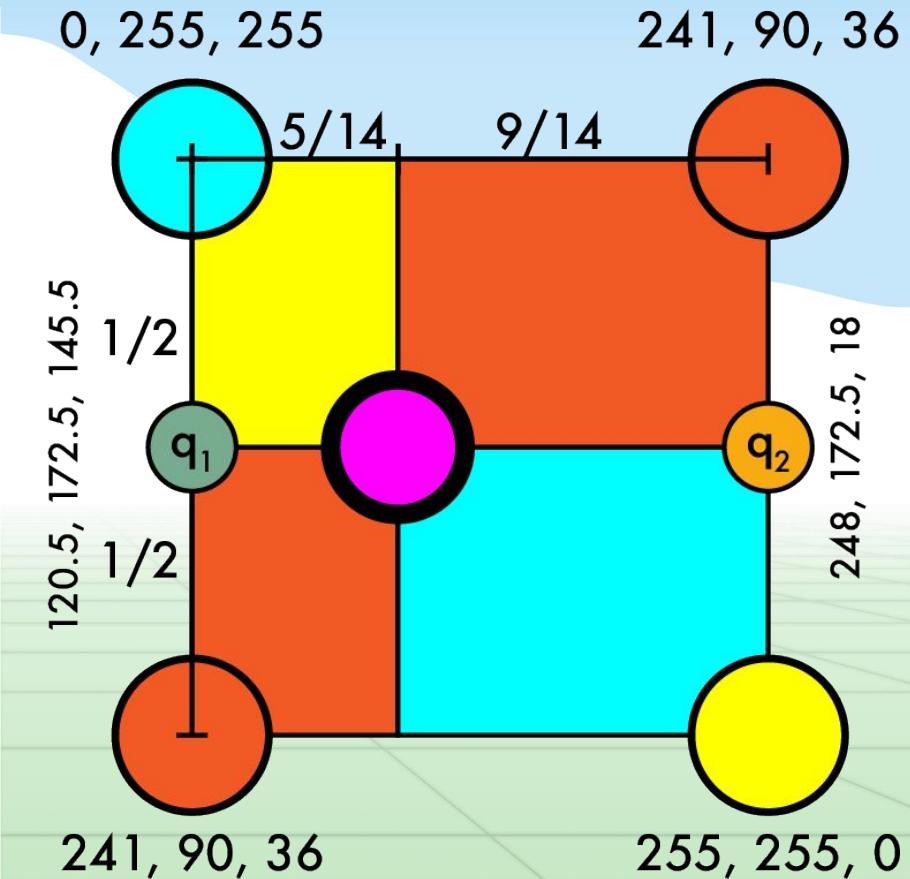
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = r_2, g_2, b_2$
 - $r_2 = .5*241 + .5*255$
 - $g_2 = .5*90 + .5*255$
 - $b_2 = .5*36 + .5*0$



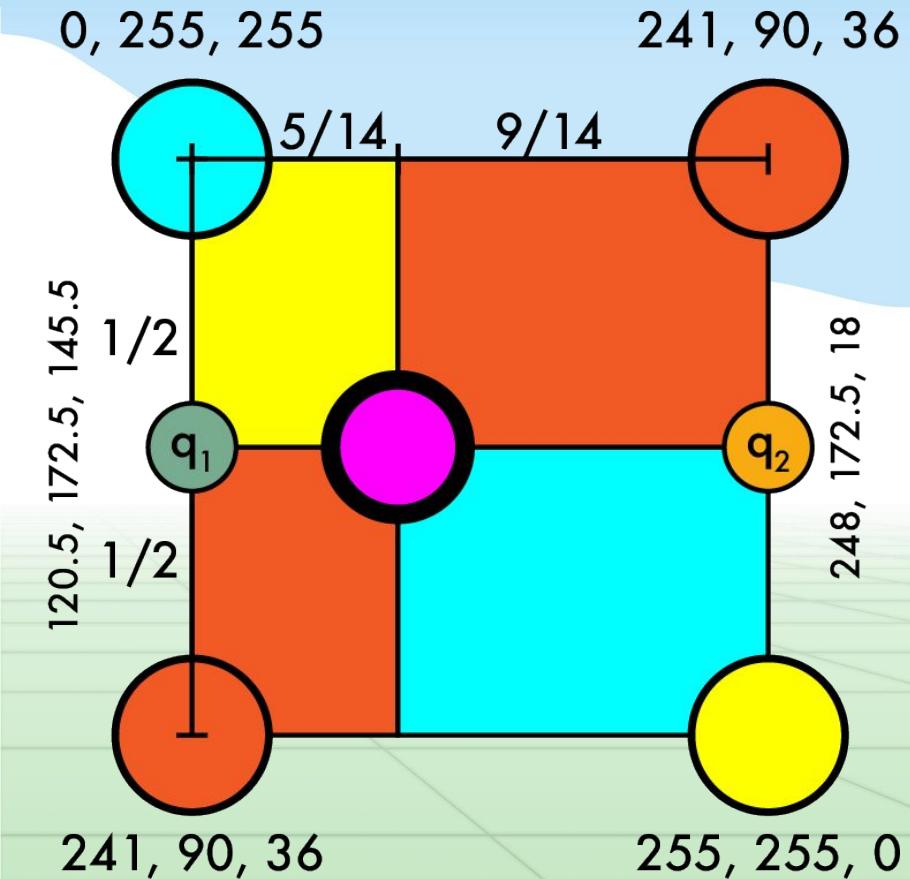
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = (248, 172.5, 18)$



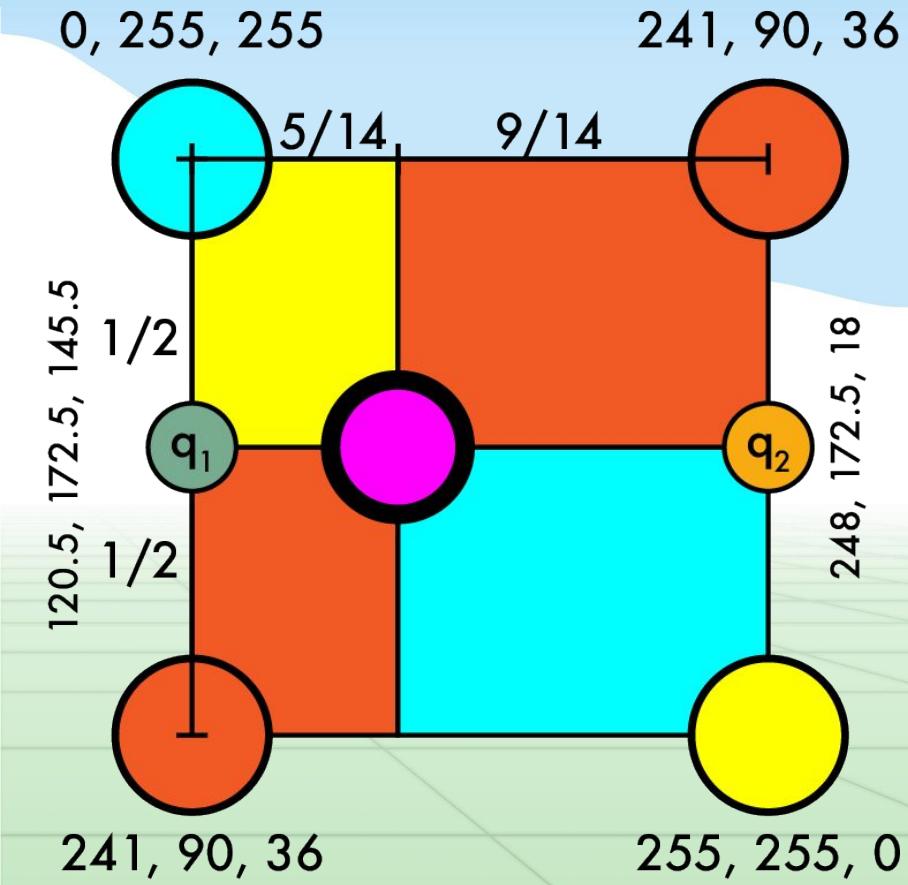
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 \times - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = (248, 172.5, 18)$
 - $q = r, g, b$
 - $w = 9/14 * w_1 + 5/14 * w_2$



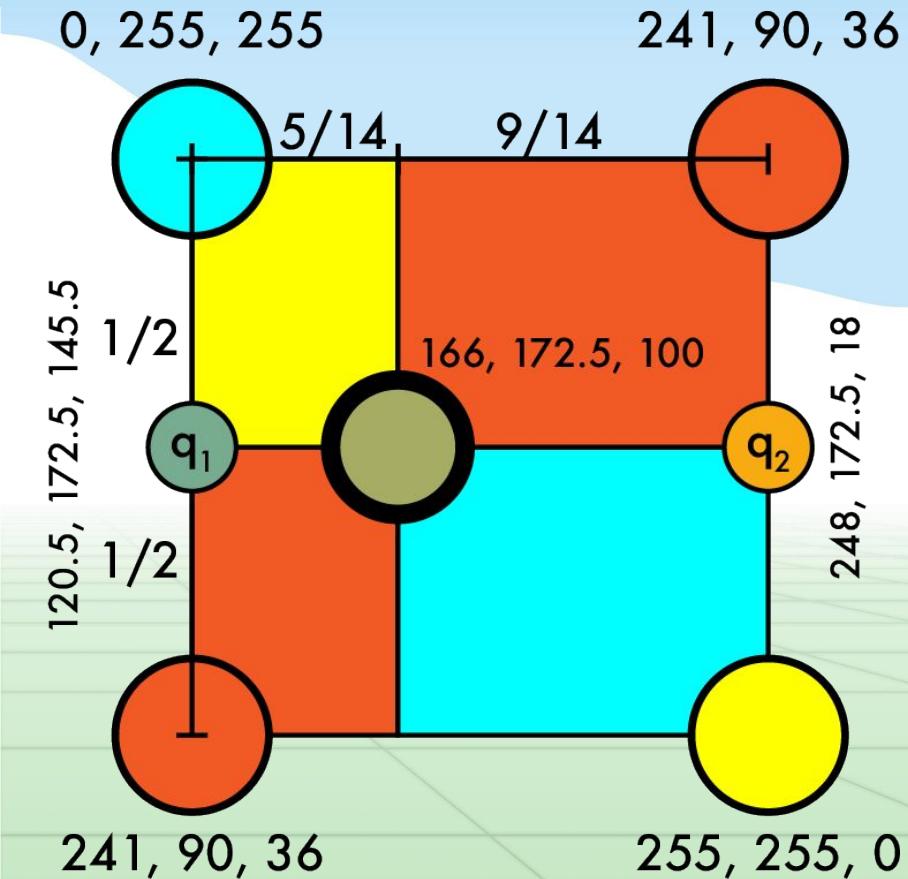
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = (248, 172.5, 18)$
 - $q = r, g, b$
 - $w = 9/14 * w_1 + 5/14 * w_2$
 - $r = 9/14 * 120.5 + 5/14 * 248$
 - $g = 9/14 * 172.5 + 5/14 * 172.5$
 - $b = 9/14 * 145.5 + 5/14 * 18$



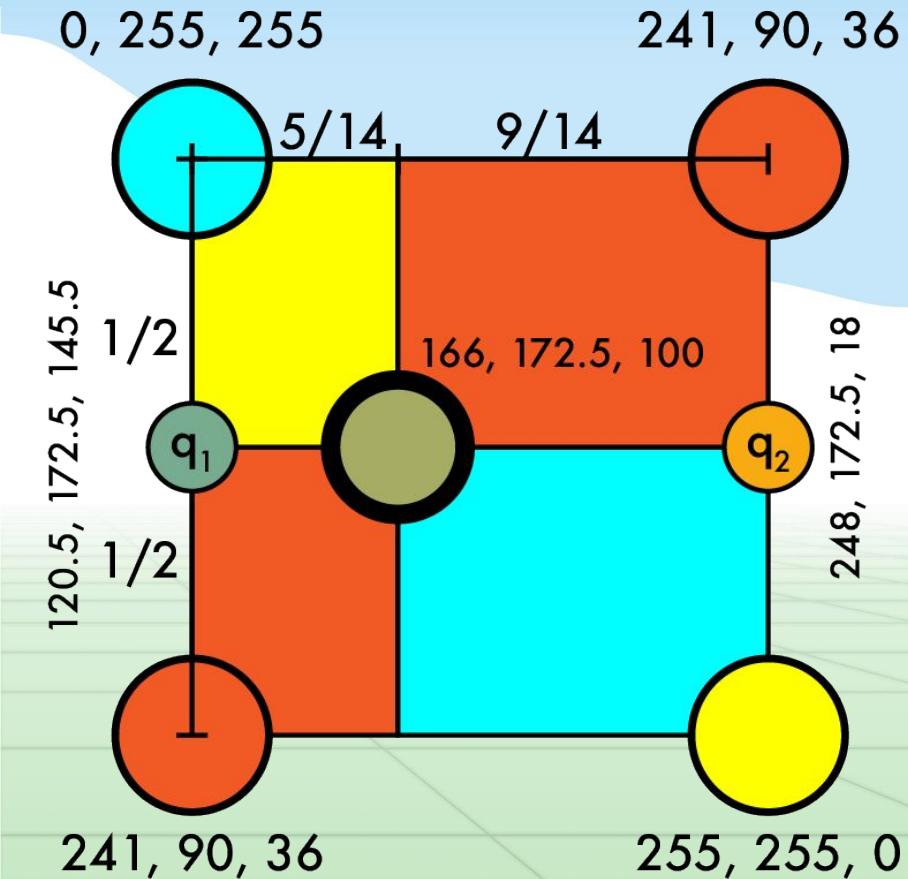
Resize 4x4 -> 7x7

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 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q_1 = (120.5, 172.5, 145.5)$
 - $q_2 = (248, 172.5, 18)$
 - $q = (166, 172.5, 100)$



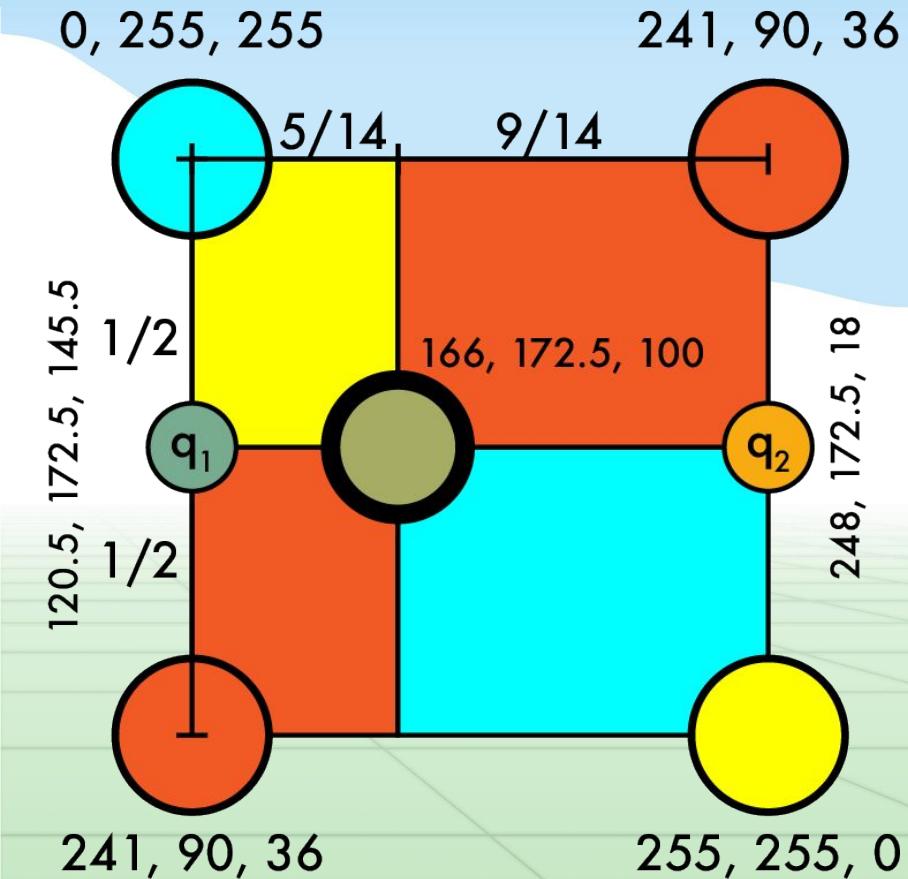
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- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$



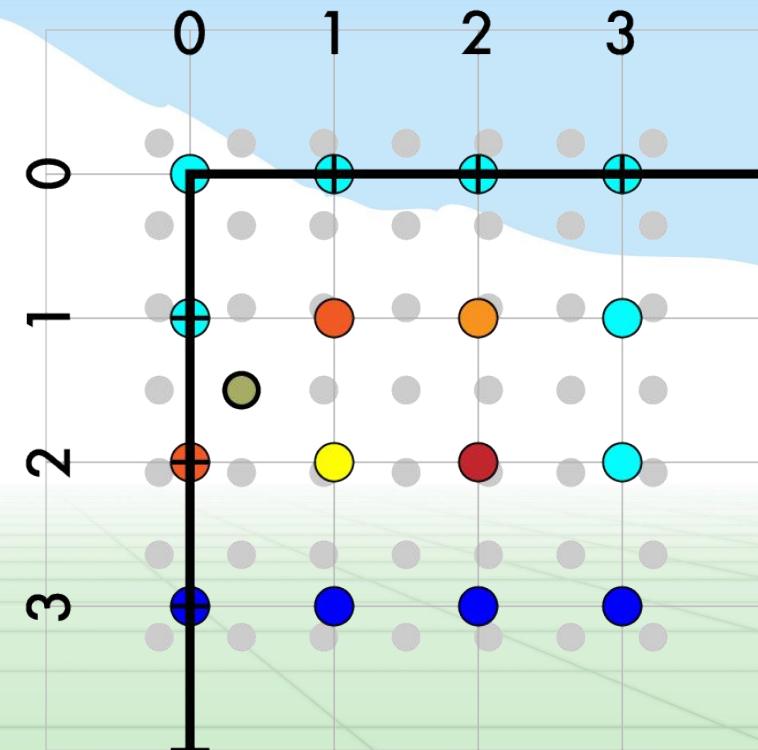
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$



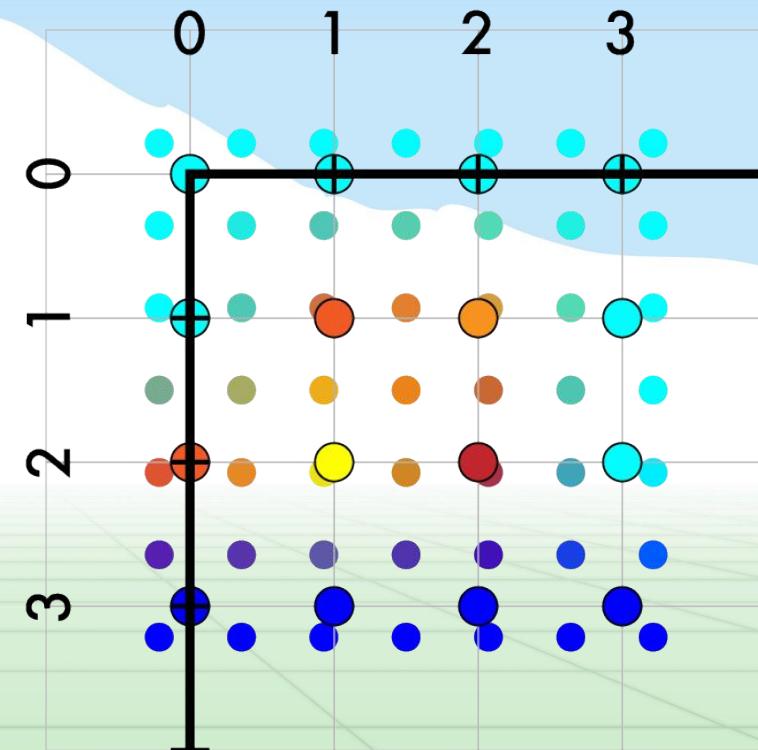
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$



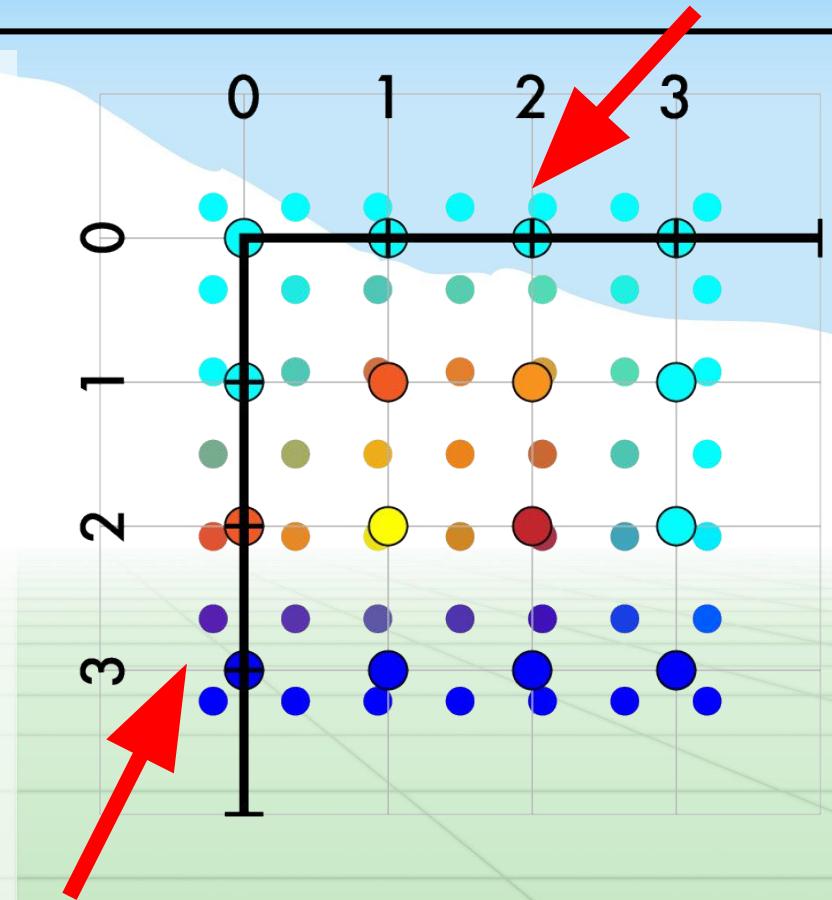
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$
- Fill in the rest



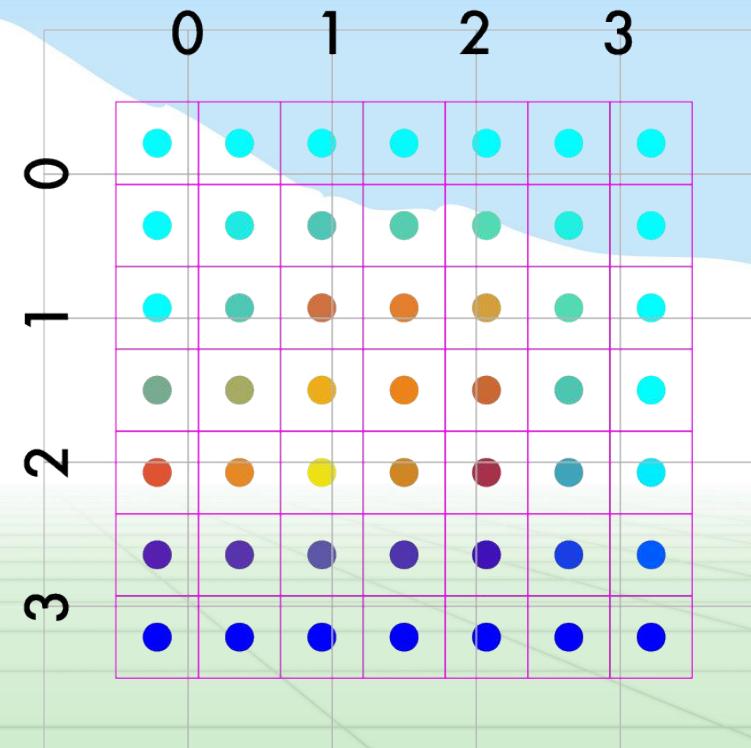
Resize 4x4 -> 7x7

- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
- Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$
- Fill in the rest
 - On outer edges use padding!



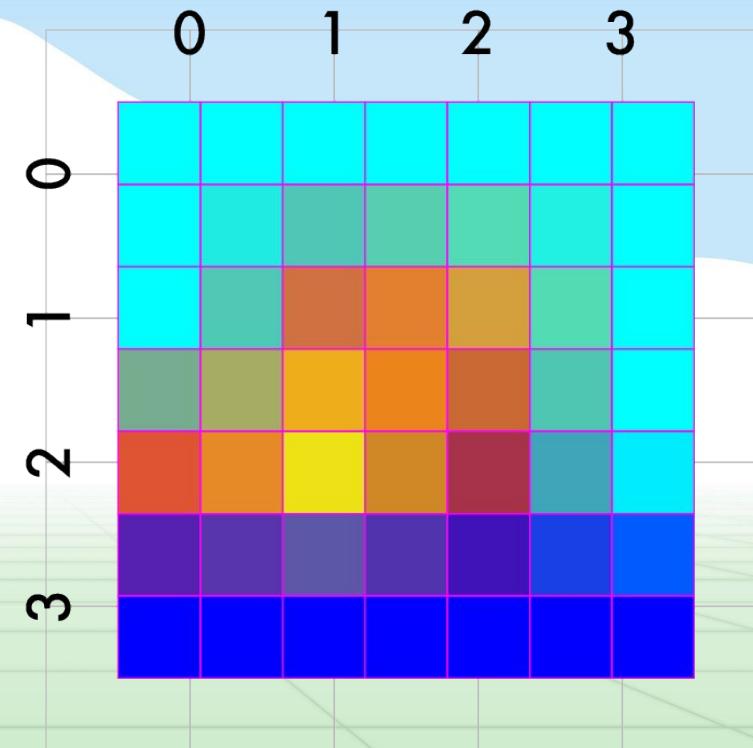
Resize 4x4 -> 7x7

- Create our new image
 - Match up coordinates
 - $4/7 X - 3/14 = Y$
 - Iterate over new pts
 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
 - $q = (166, 172.5, 100)$
 - Fill in the rest

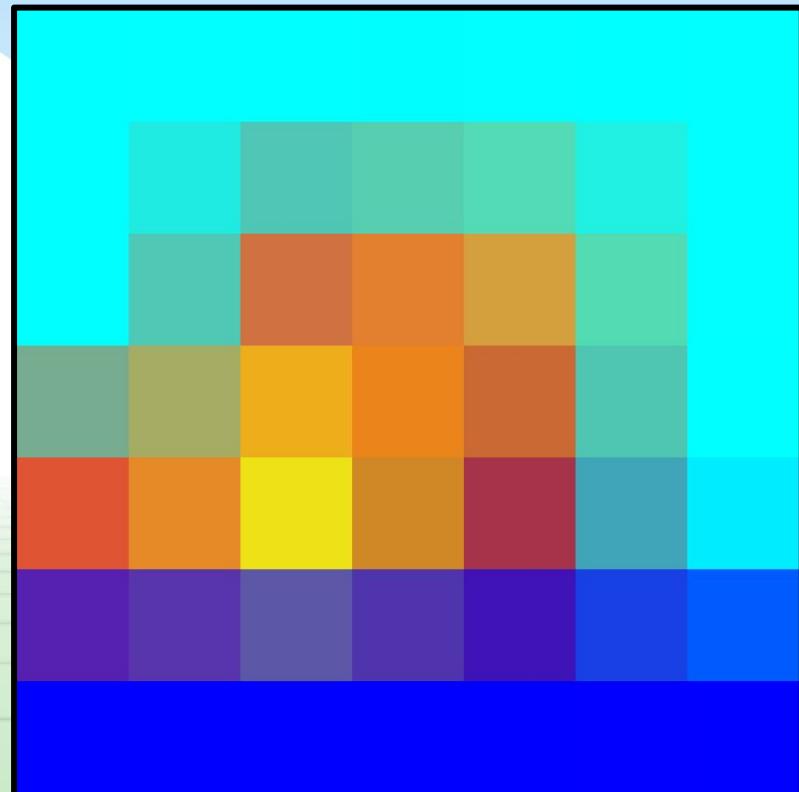
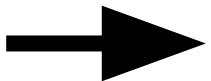
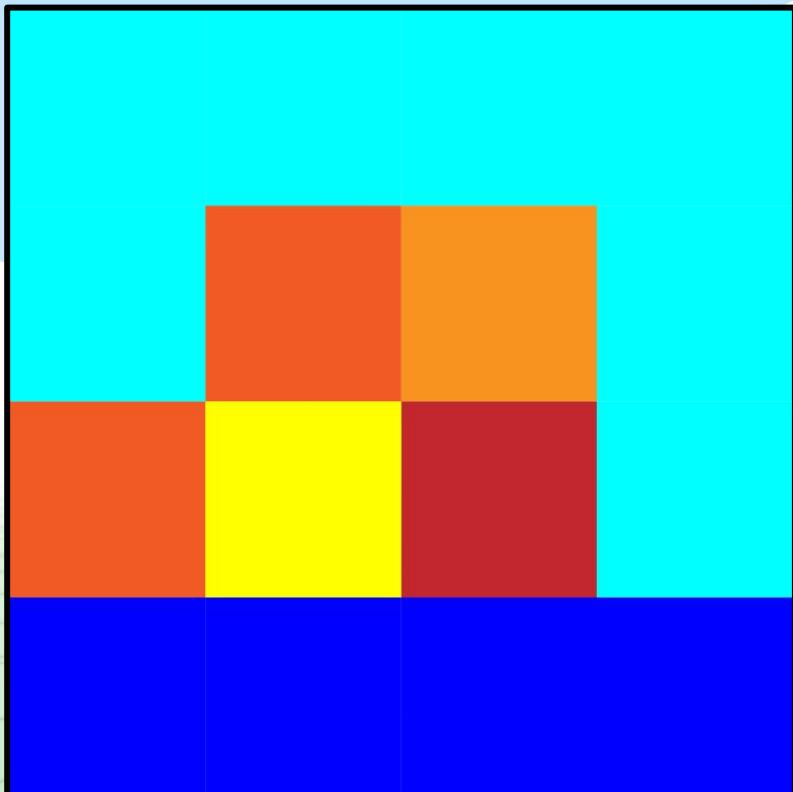


Resize 4x4 -> 7x7

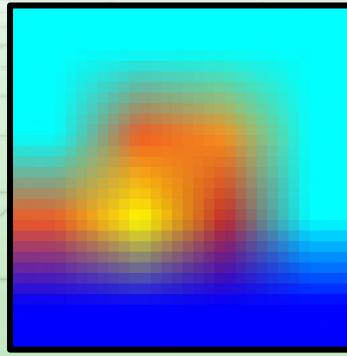
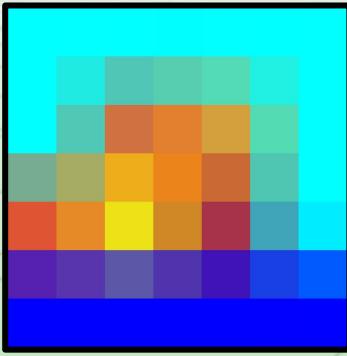
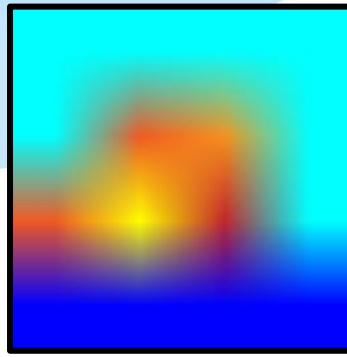
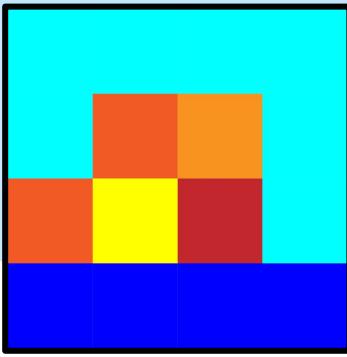
- Create our new image
- Match up coordinates
 - $4/7 X - 3/14 = Y$
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 - Map to old coords
 - $(1, 3) \rightarrow (5/14, 7/14)$
 - Interpolate old values
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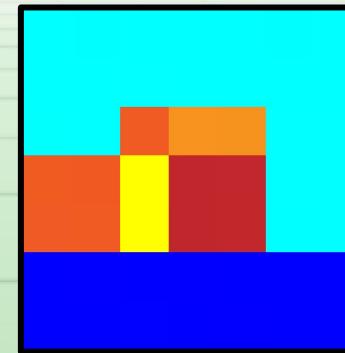
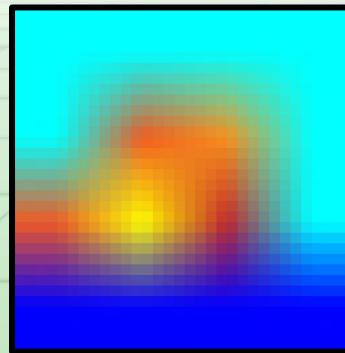
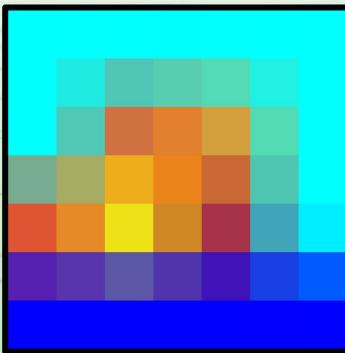
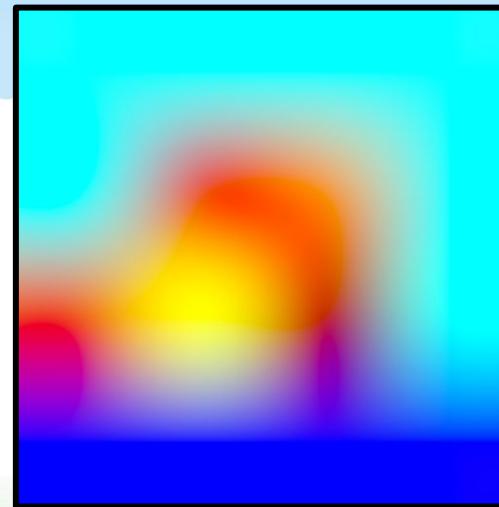
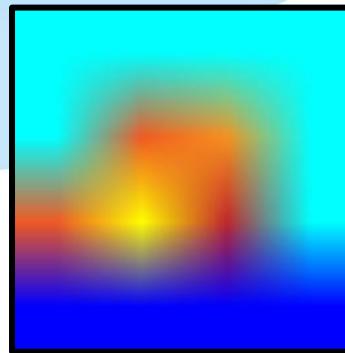
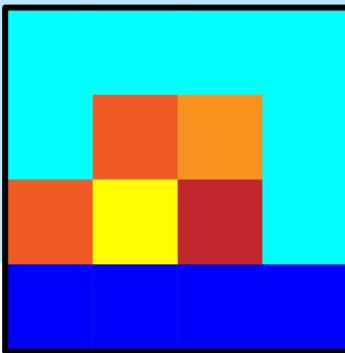
We did it!



Different scales



Different methods





Let's do something interesting
already!!

Want to make image smaller



448x448 -> 64x64



448x448 -> 64x64



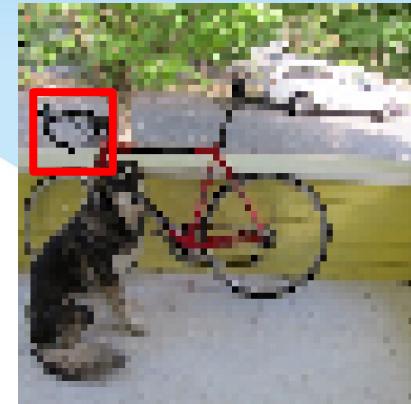
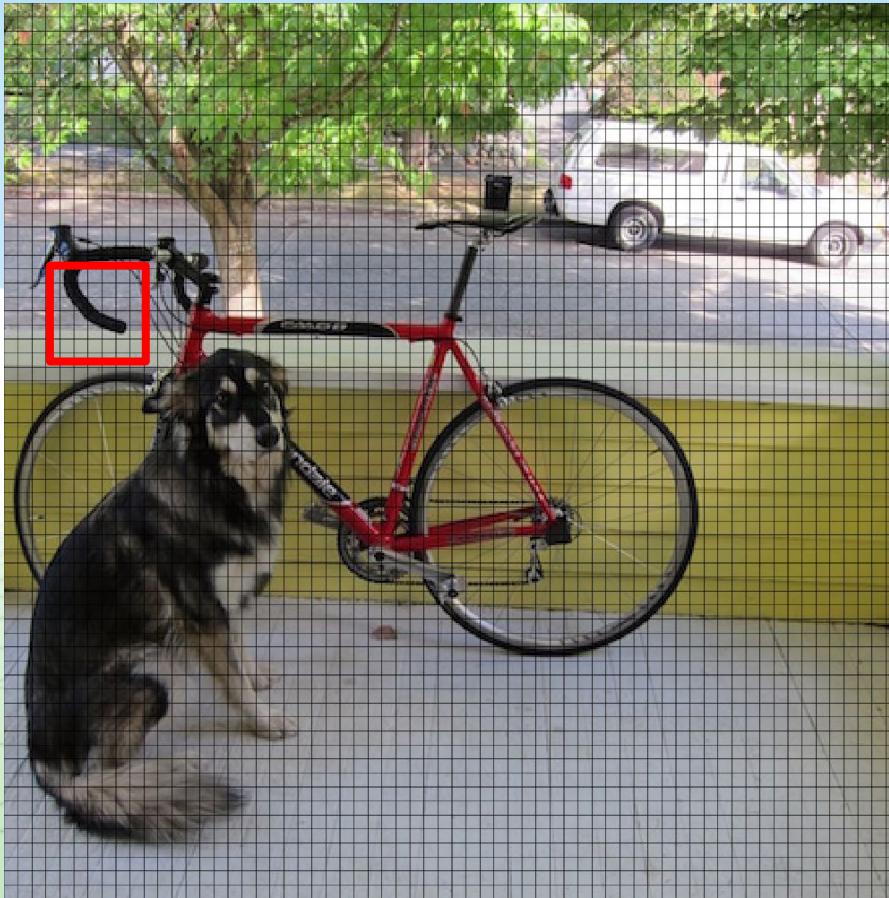
448x448 -> 64x64



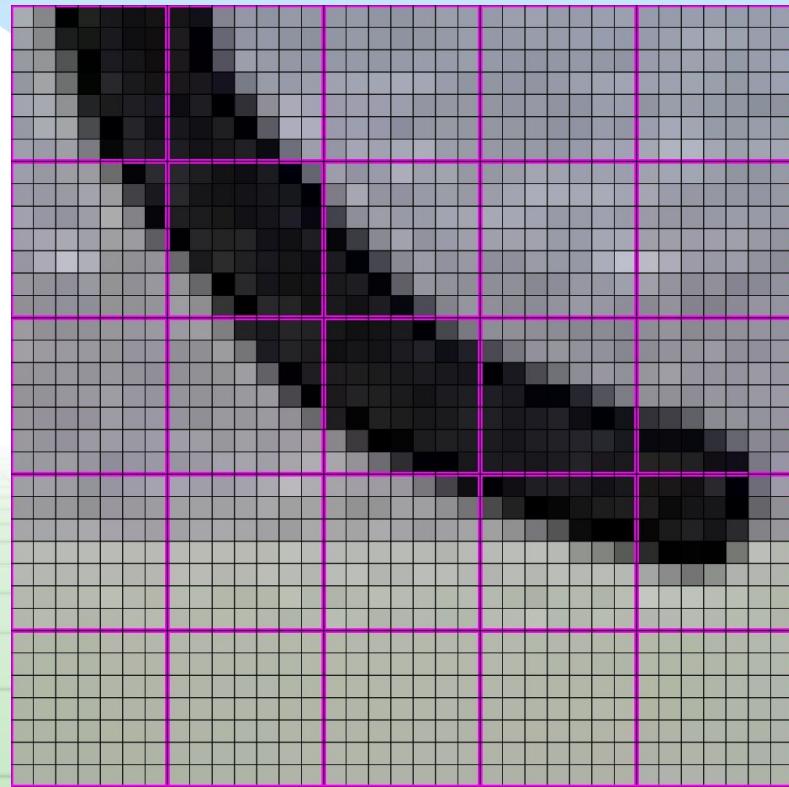
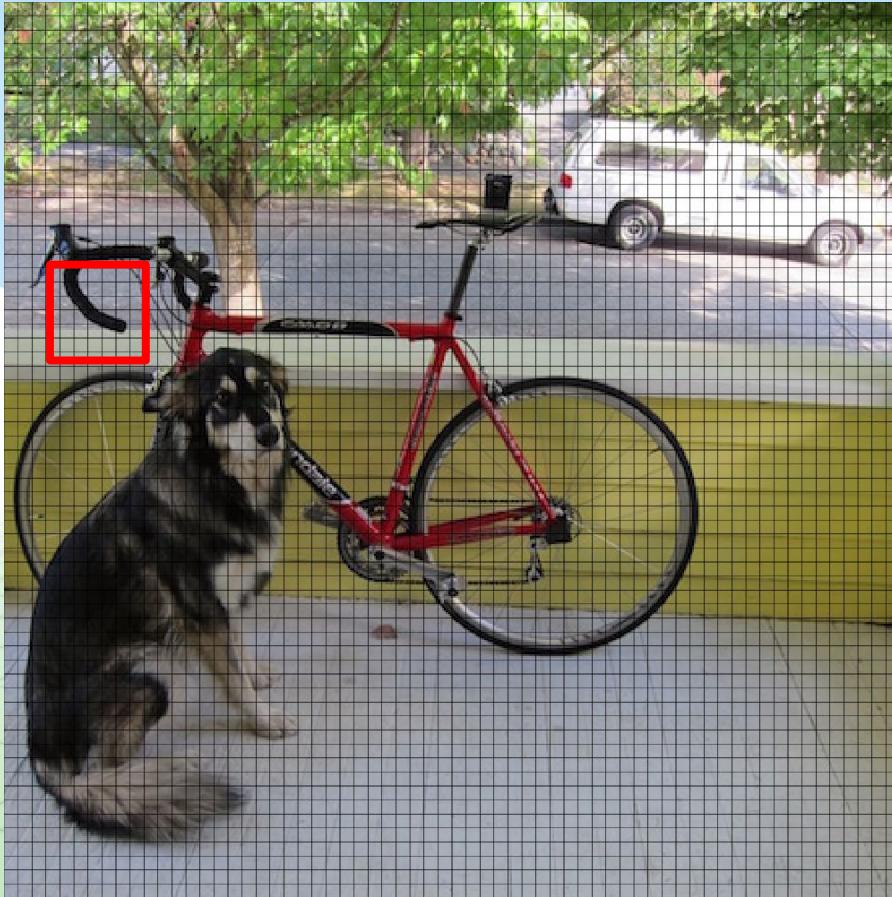
448x448 -> 64x64



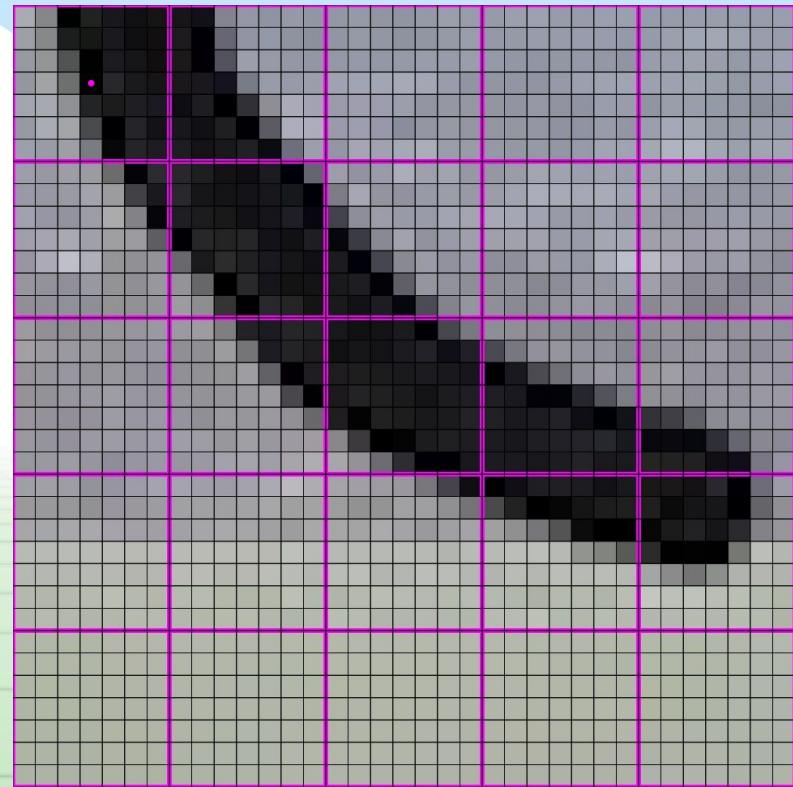
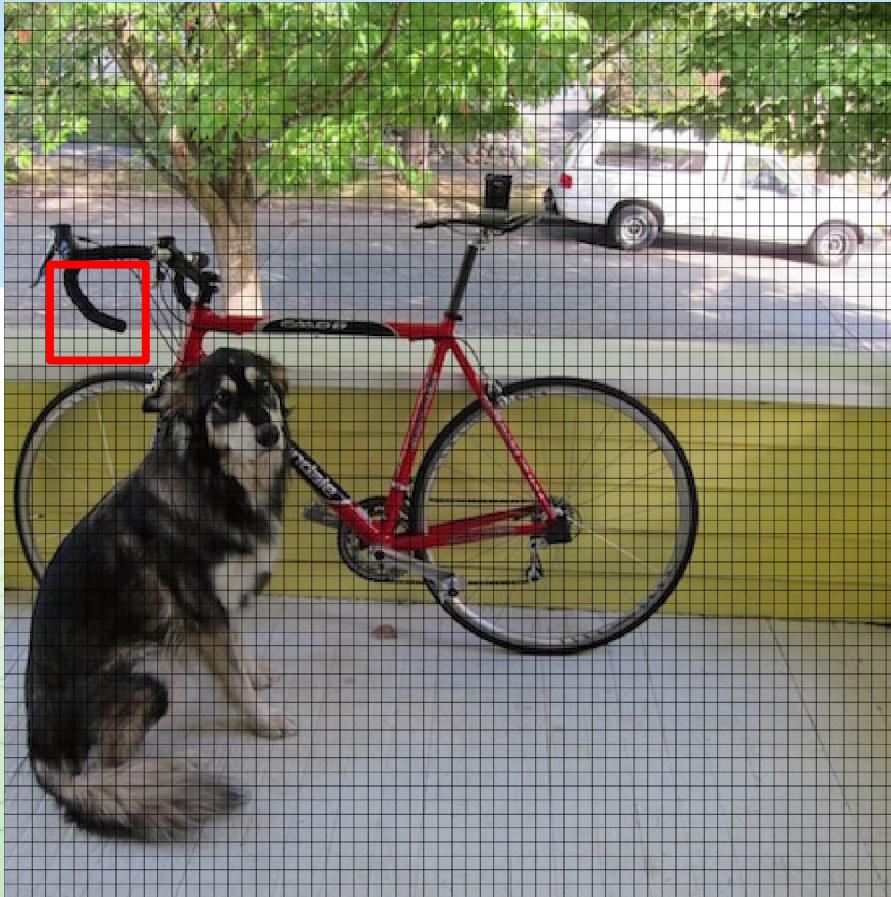
448x448 -> 64x64



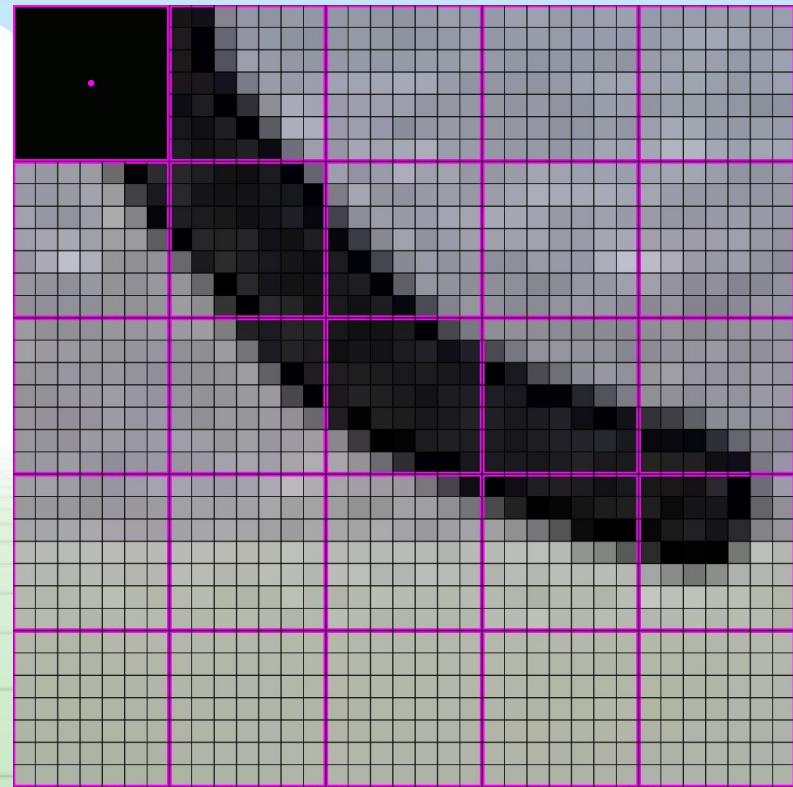
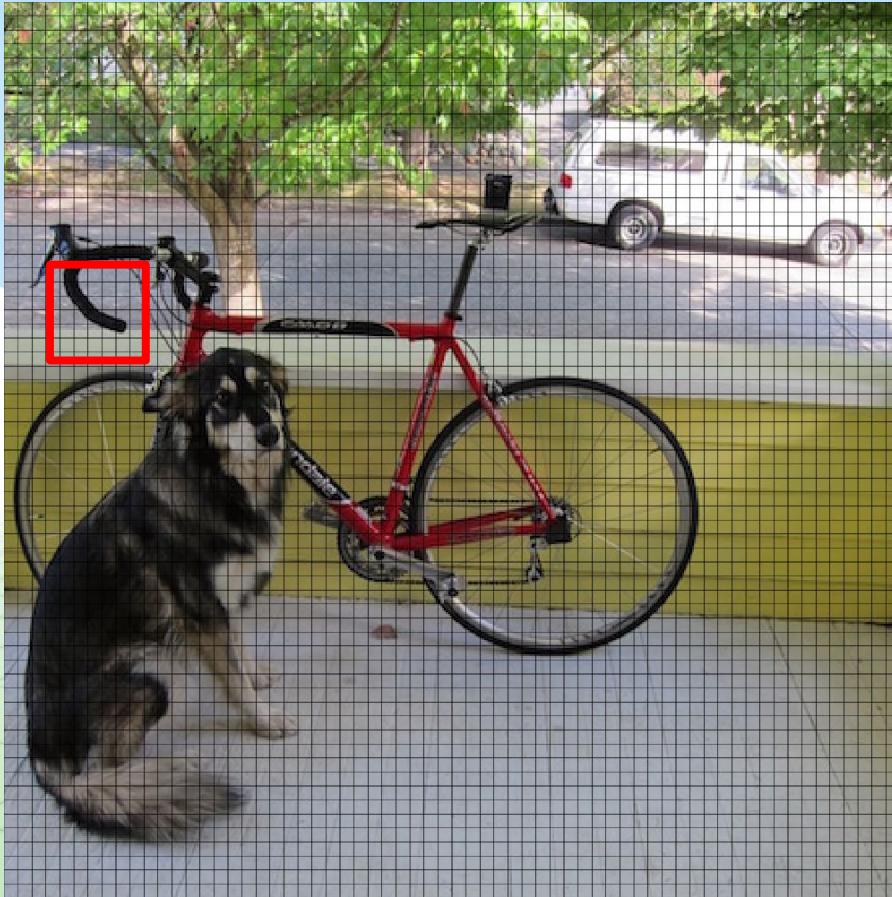
448x448 -> 64x64



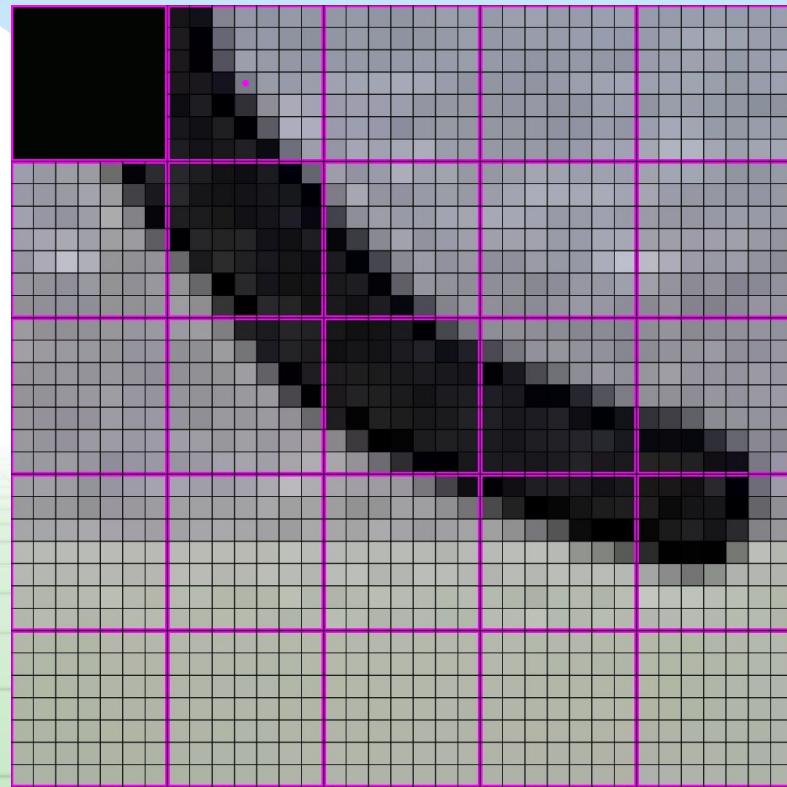
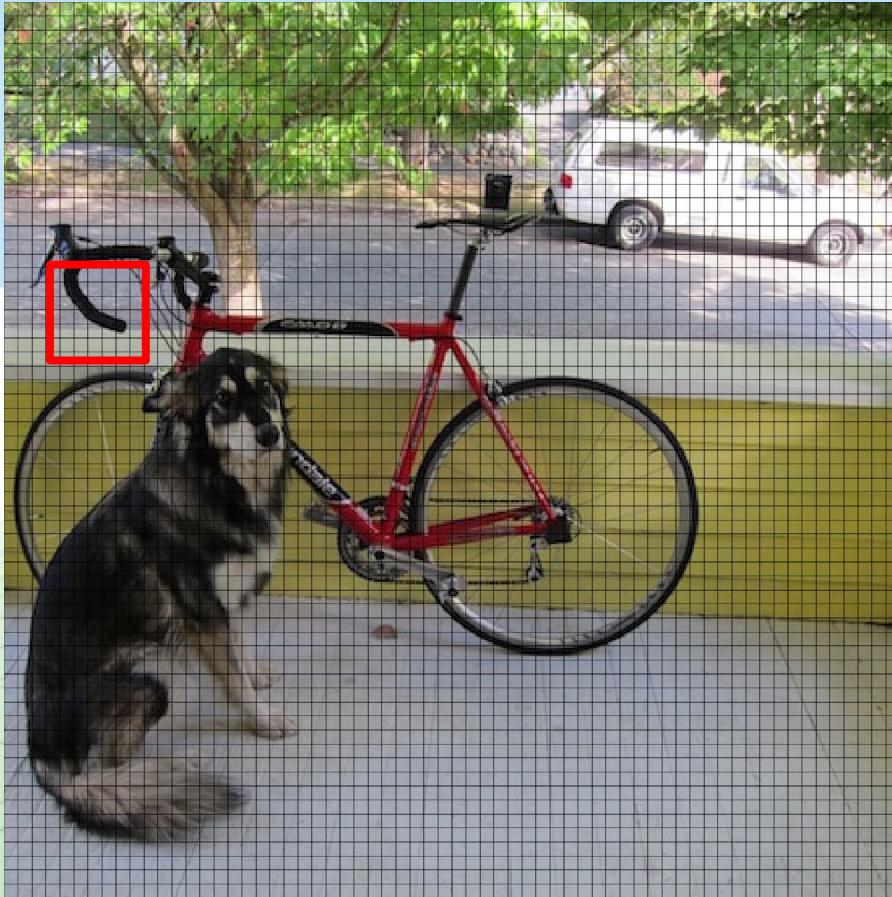
448x448 -> 64x64



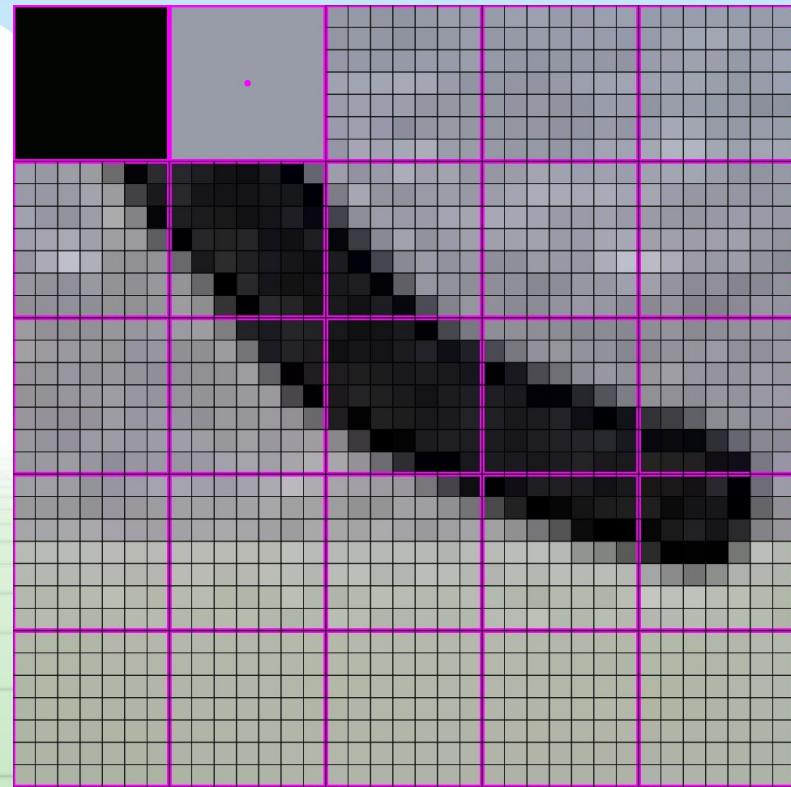
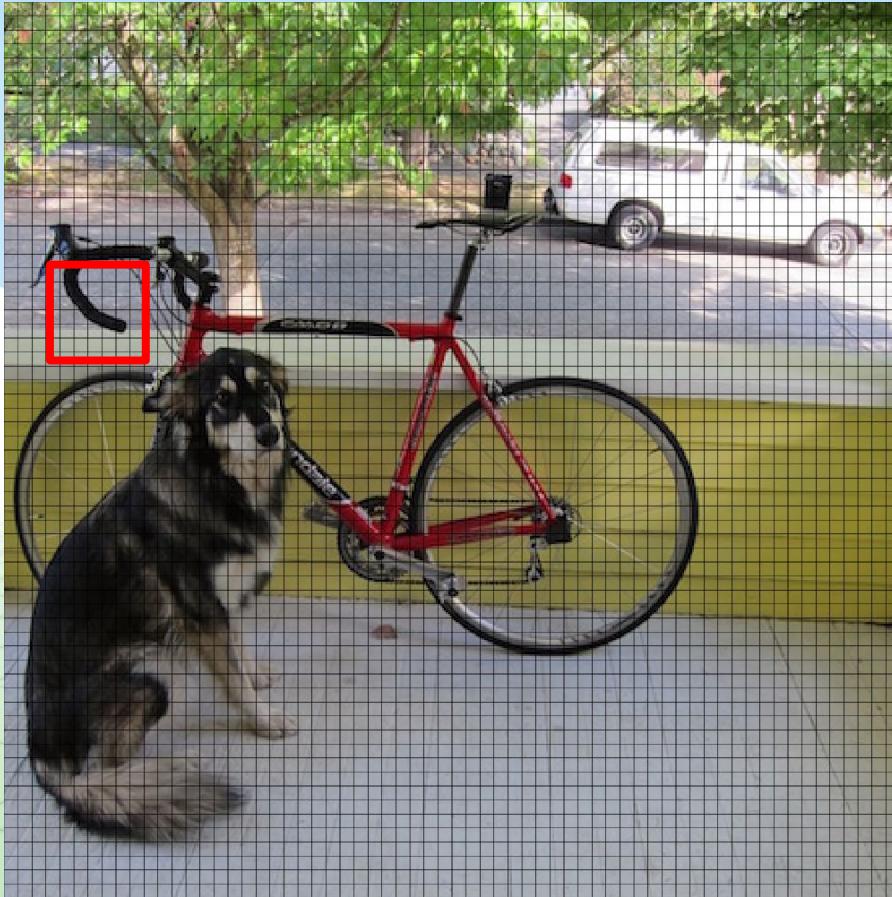
448x448 -> 64x64



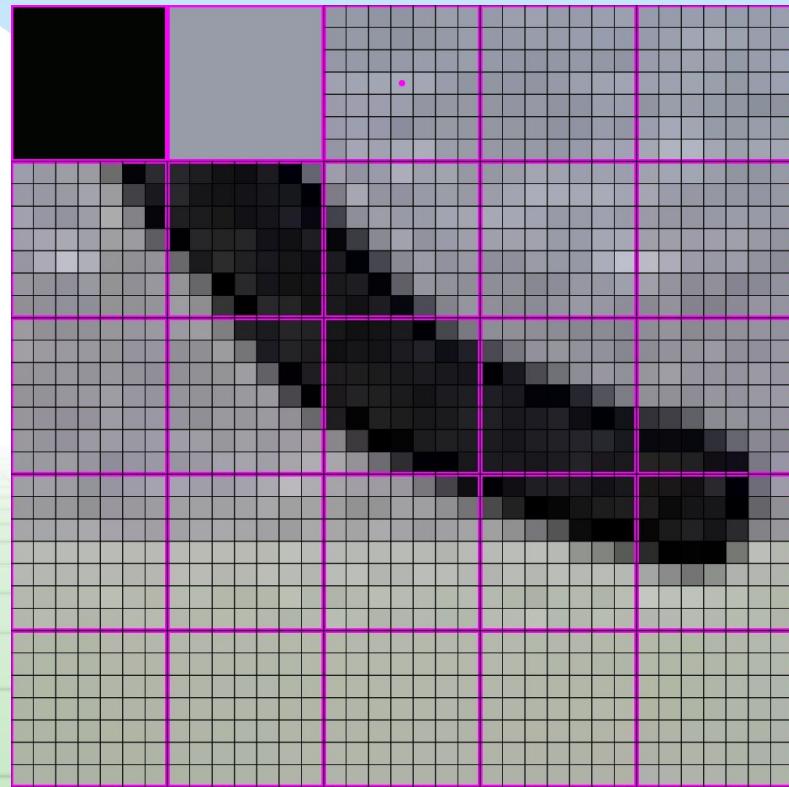
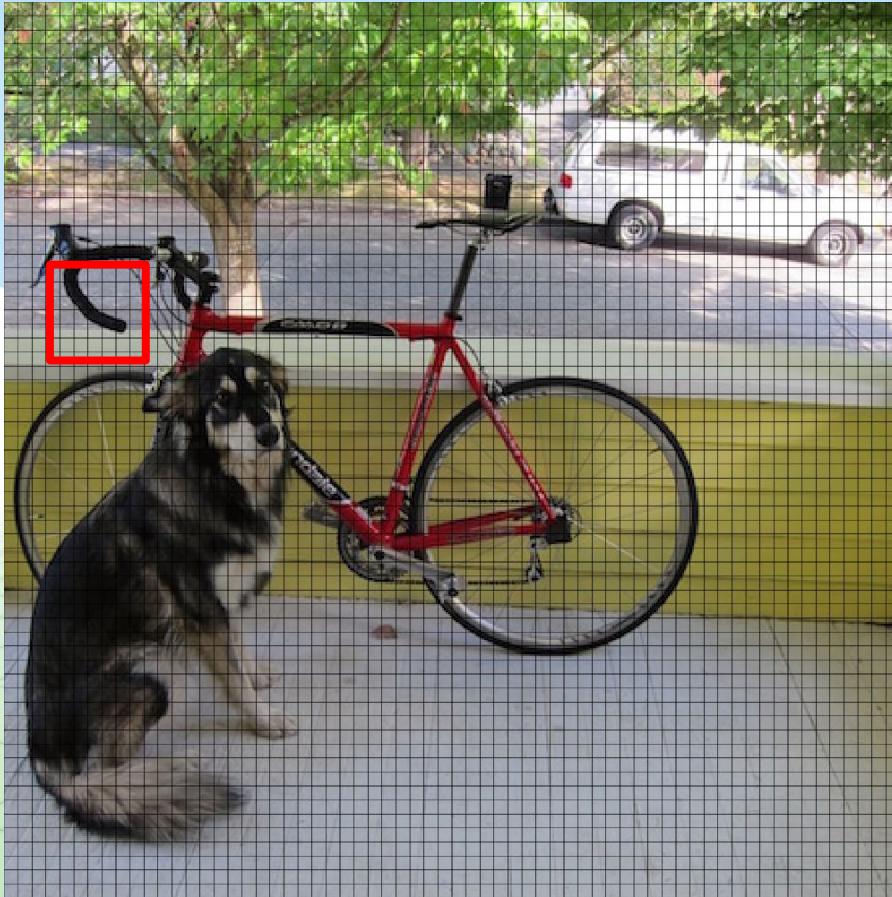
448x448 -> 64x64



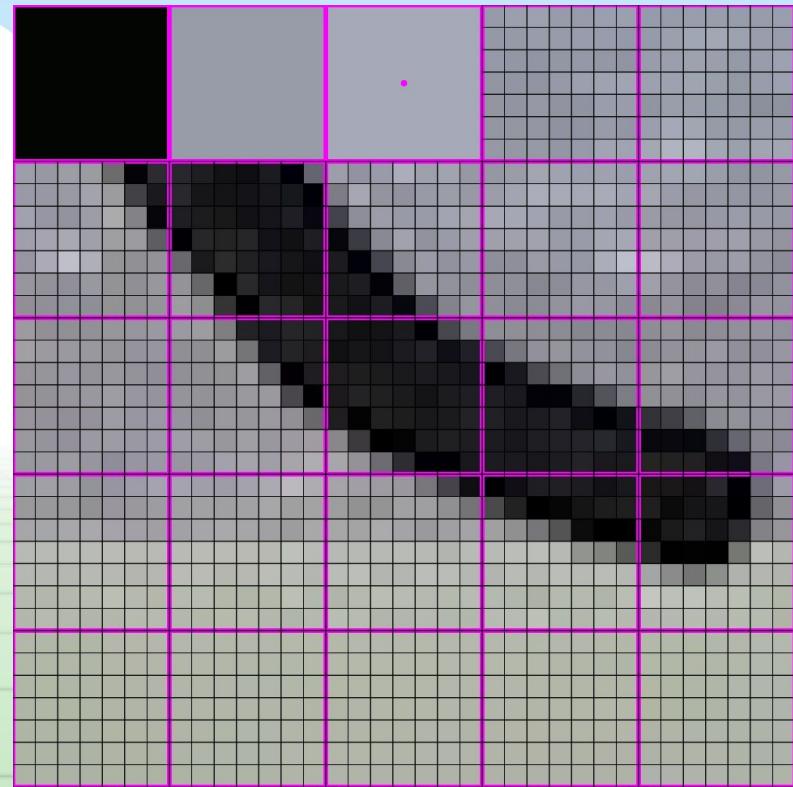
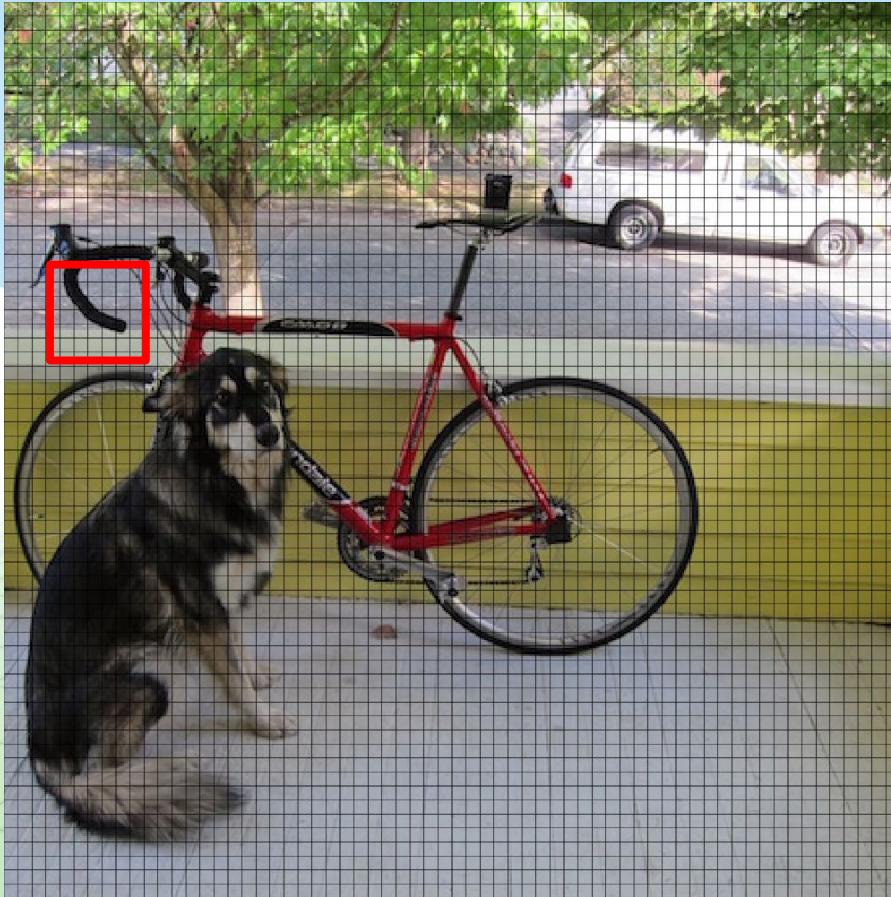
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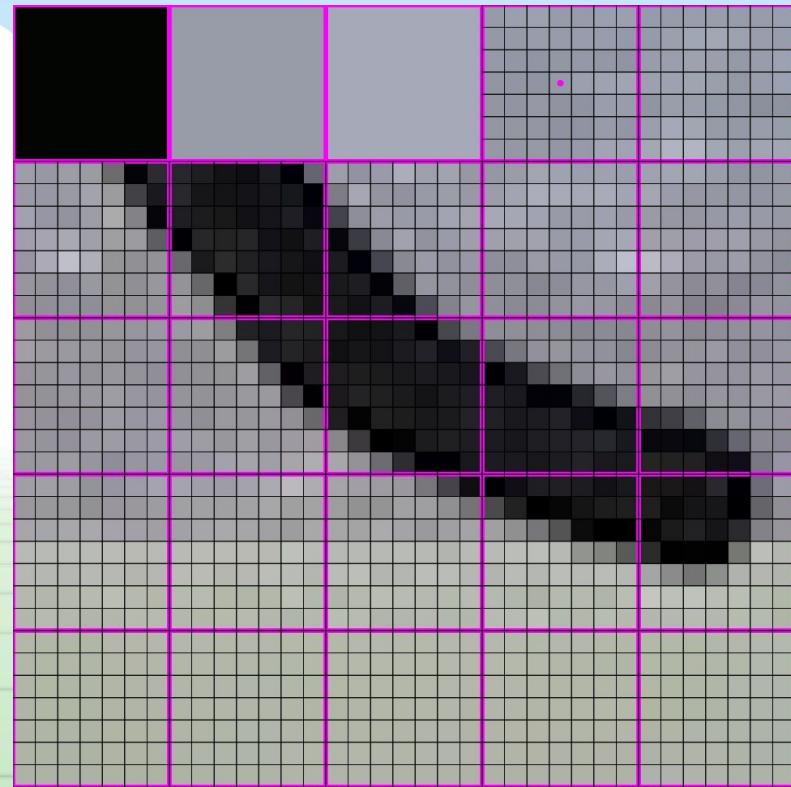
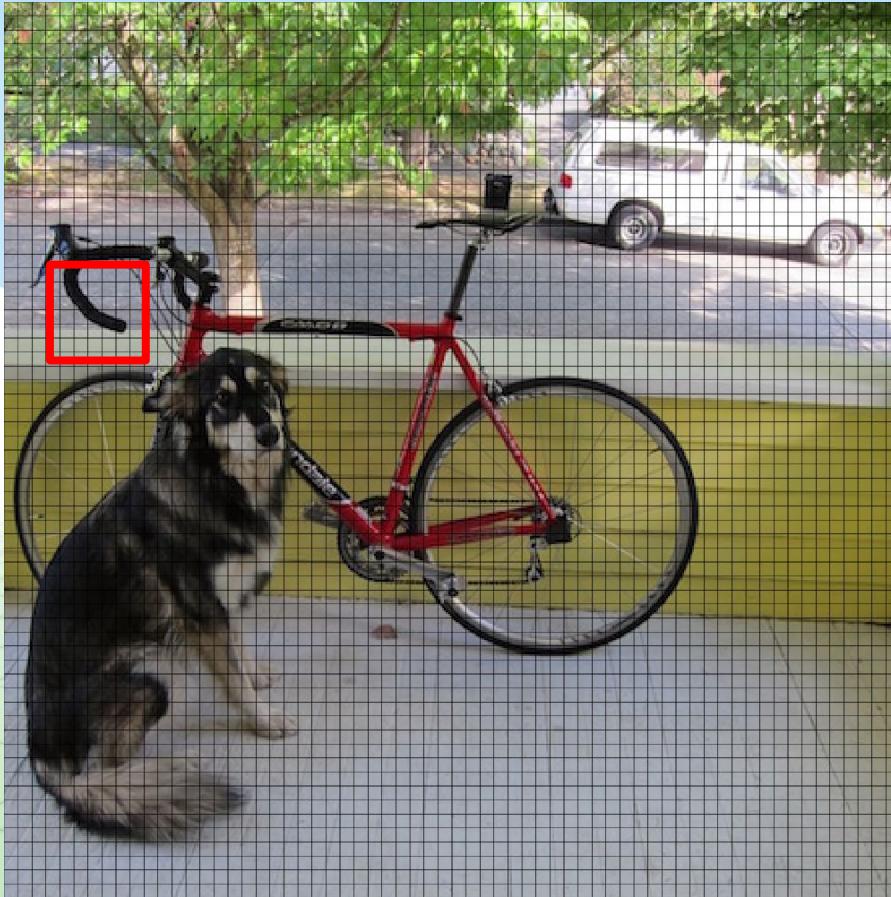
448x448 -> 64x64



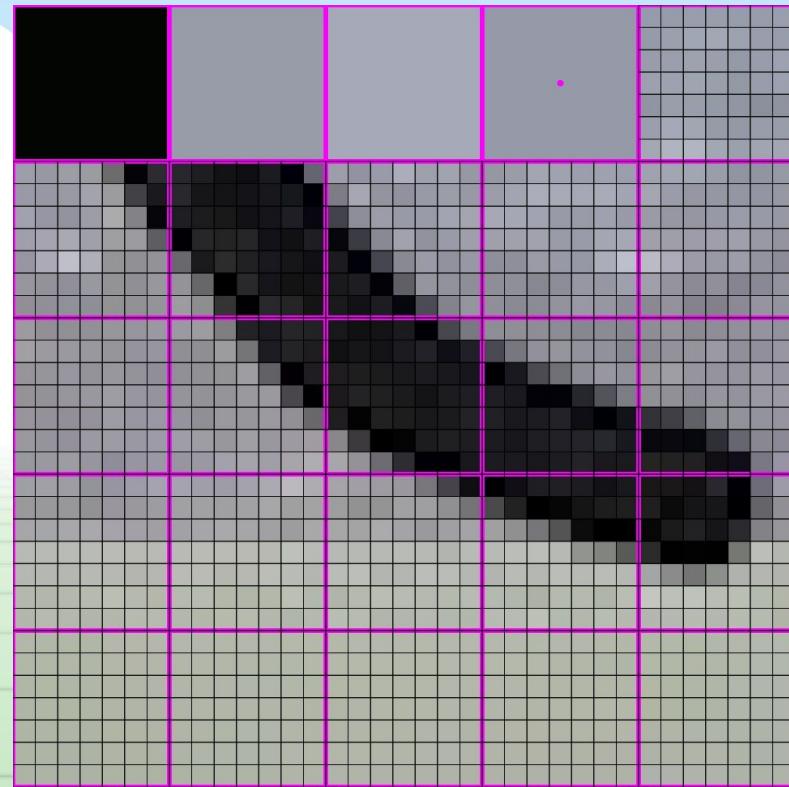
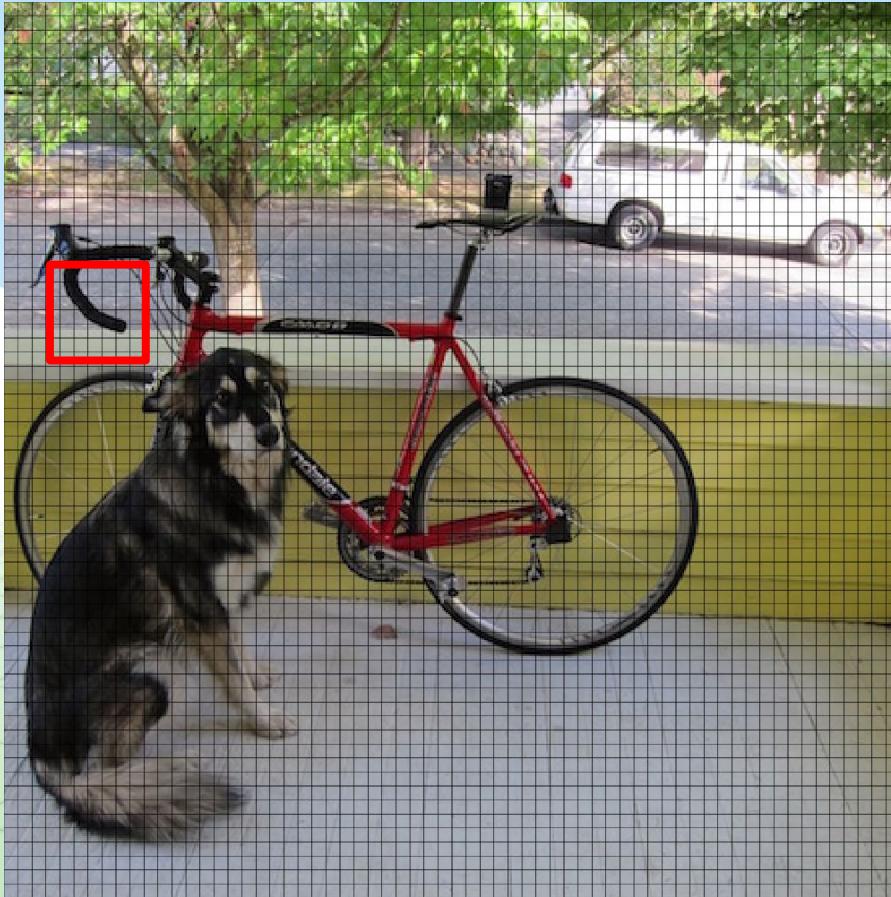
448x448 -> 64x64



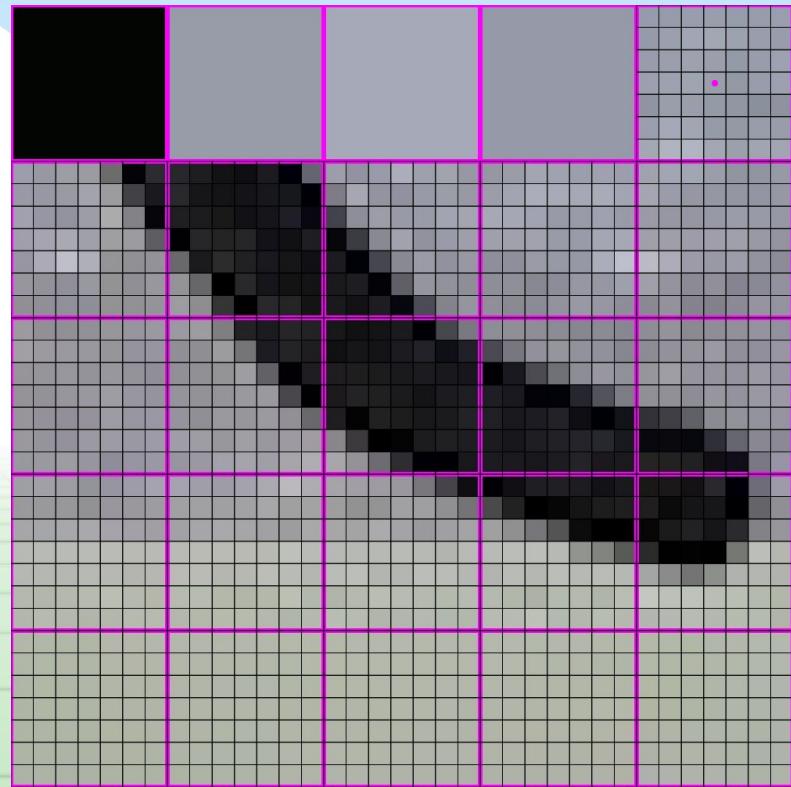
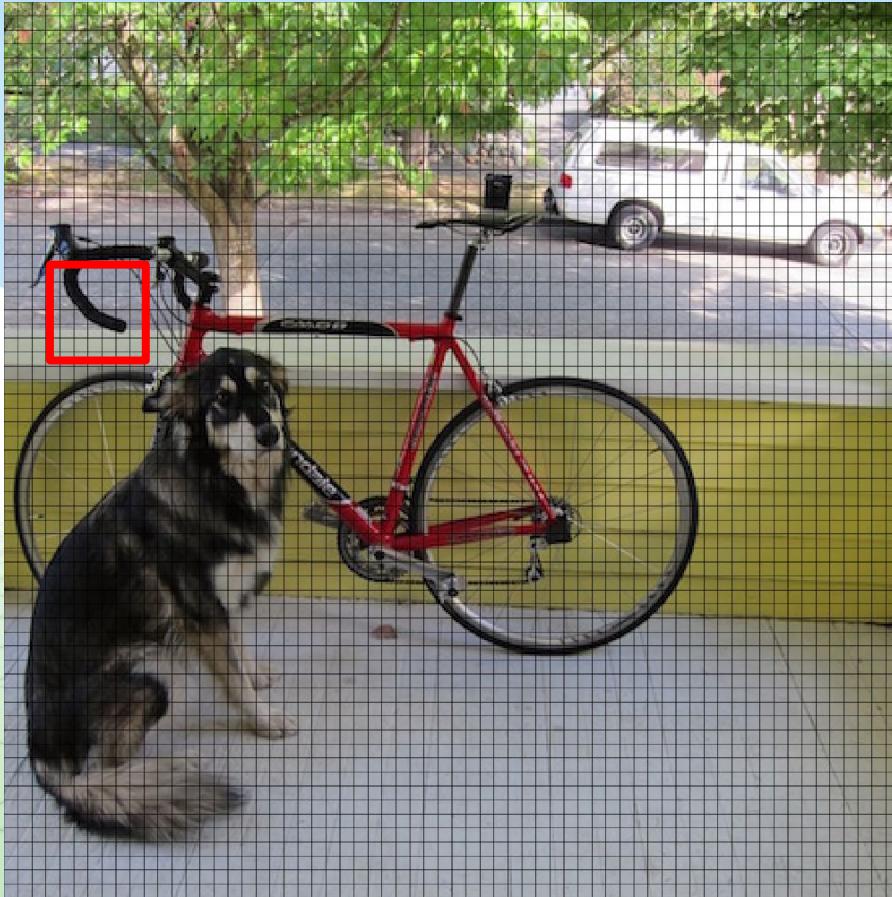
448x448 -> 64x64



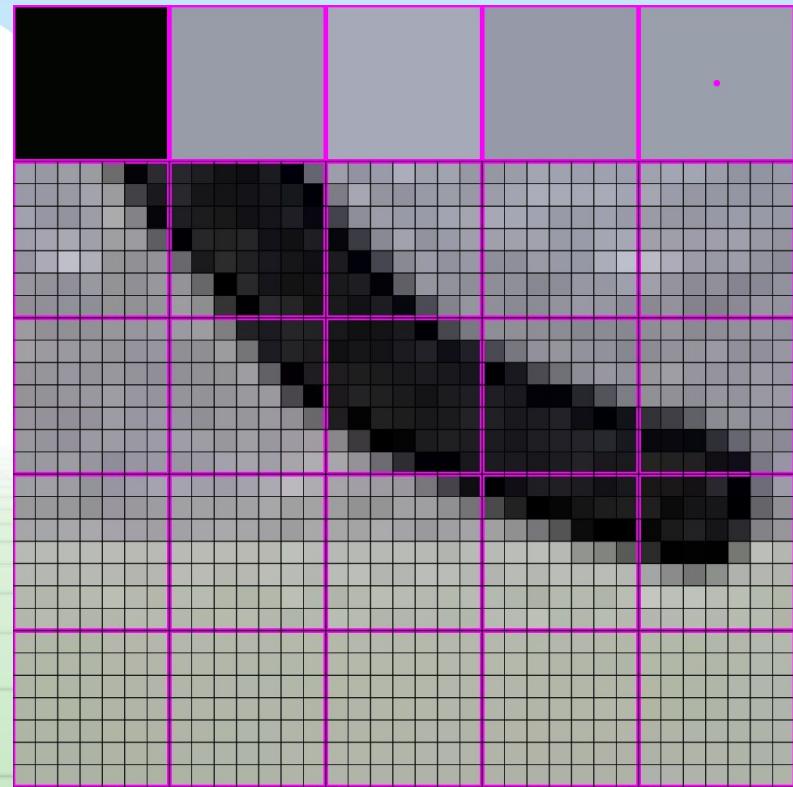
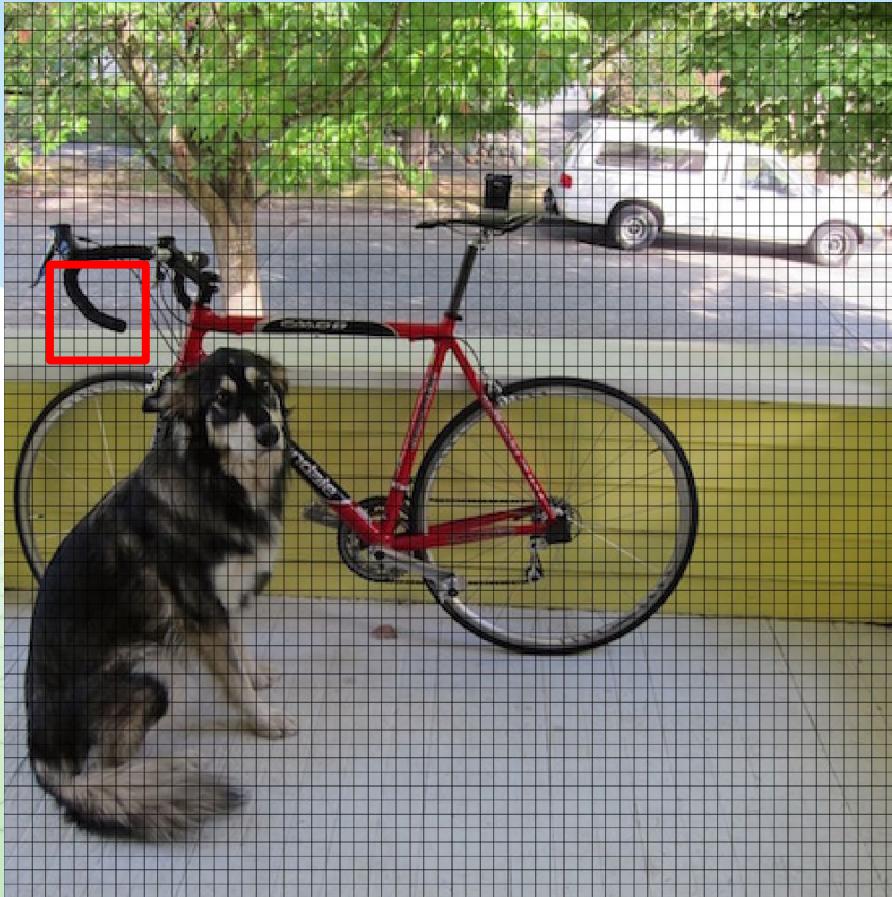
448x448 -> 64x64



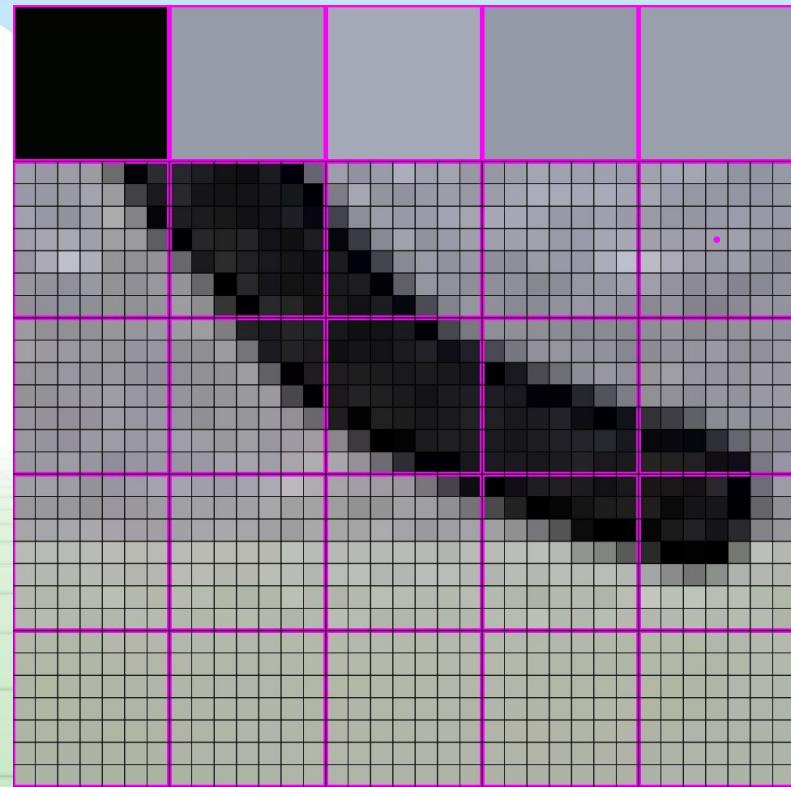
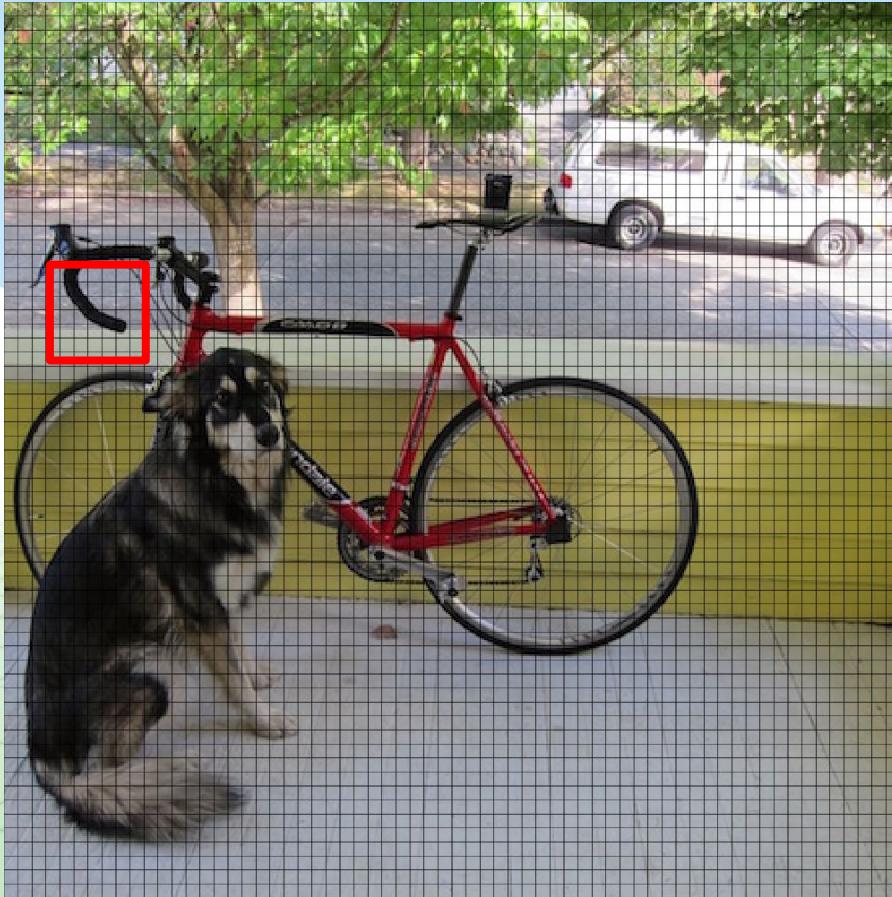
448x448 -> 64x64



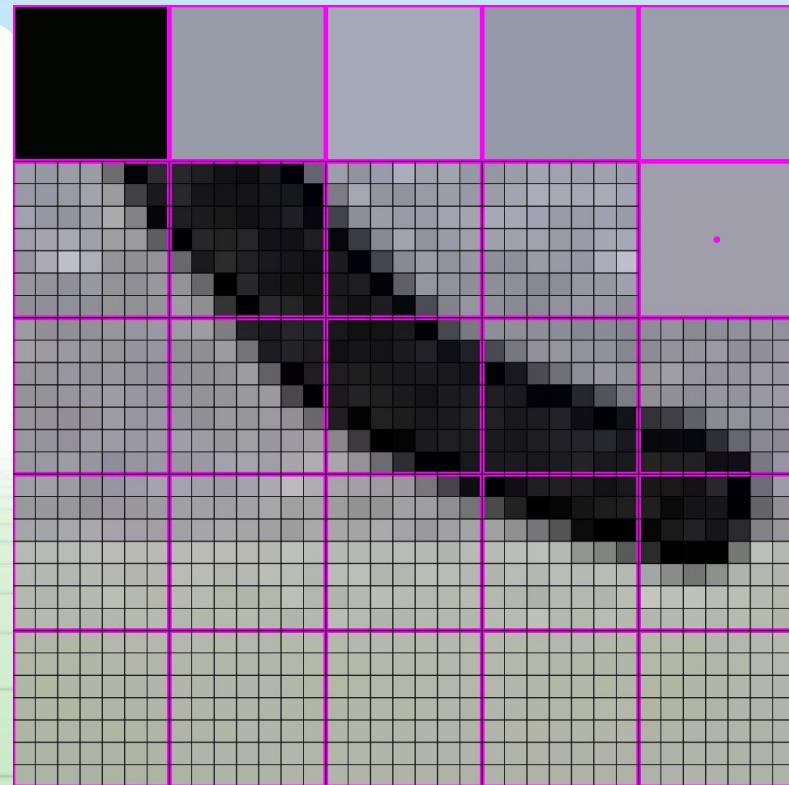
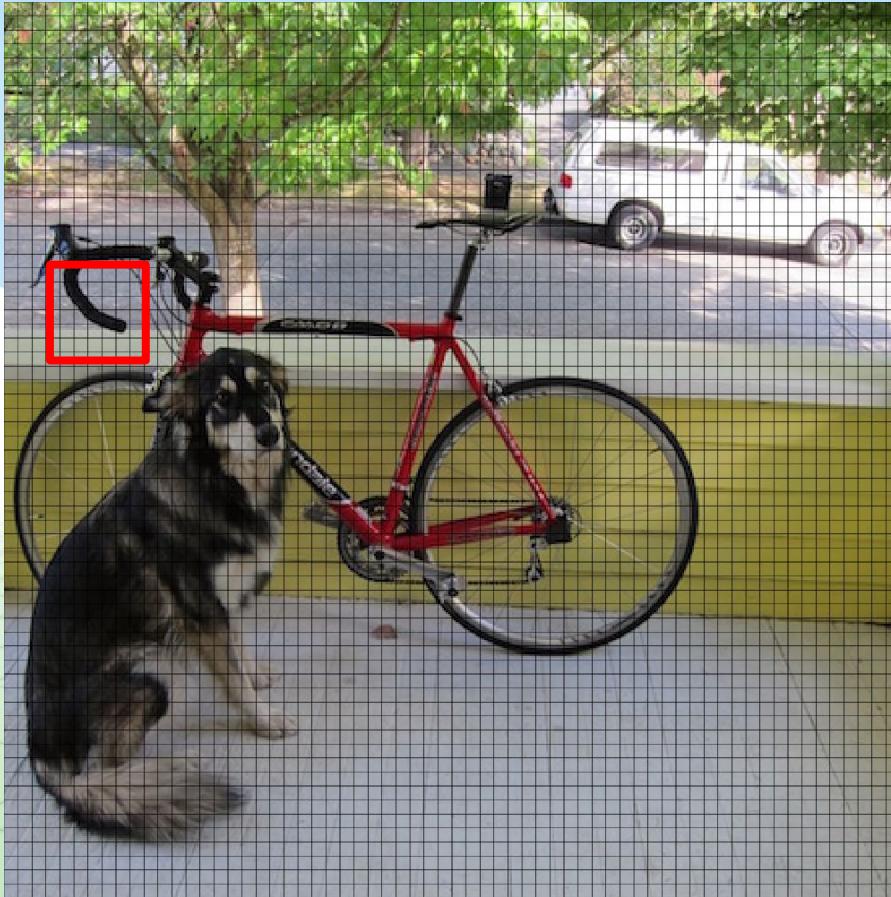
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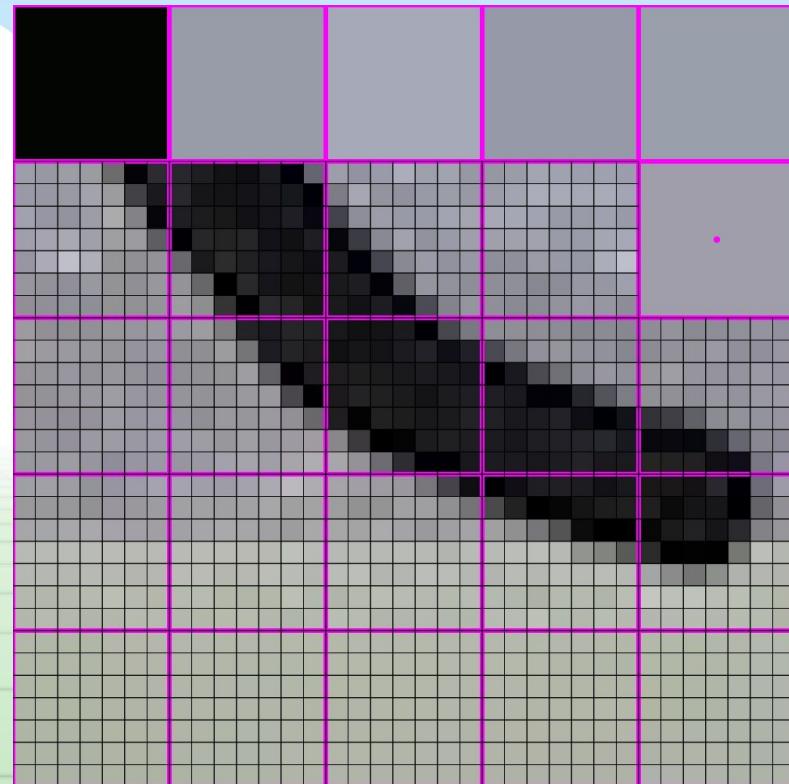
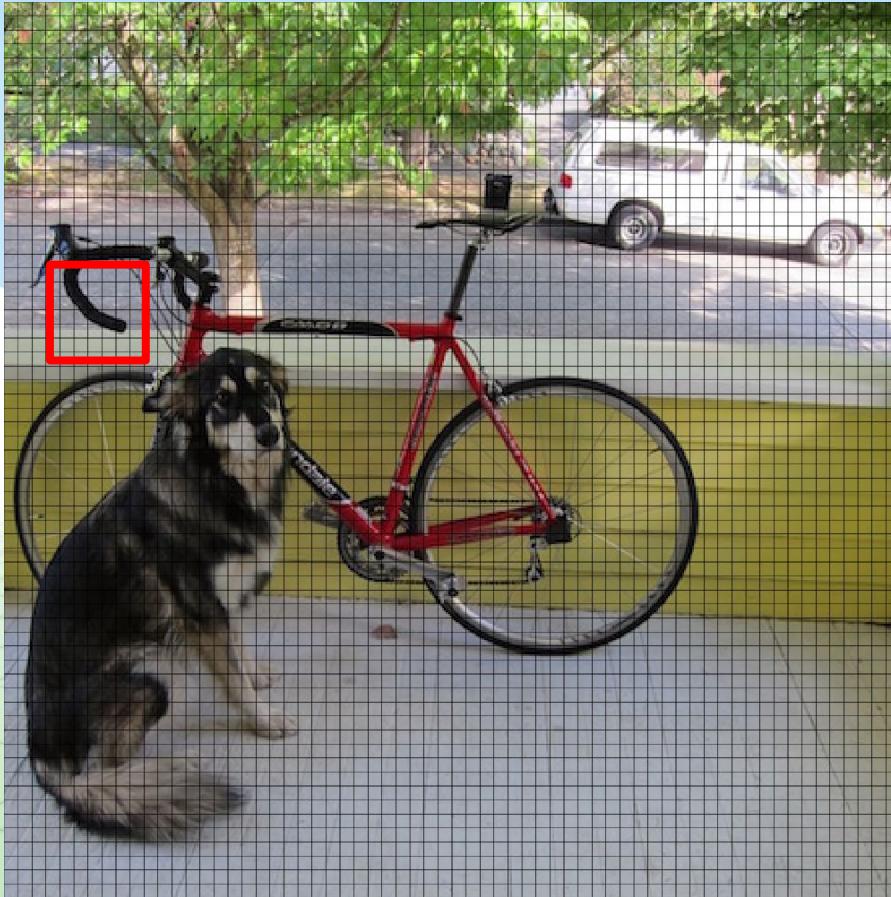
448x448 -> 64x64



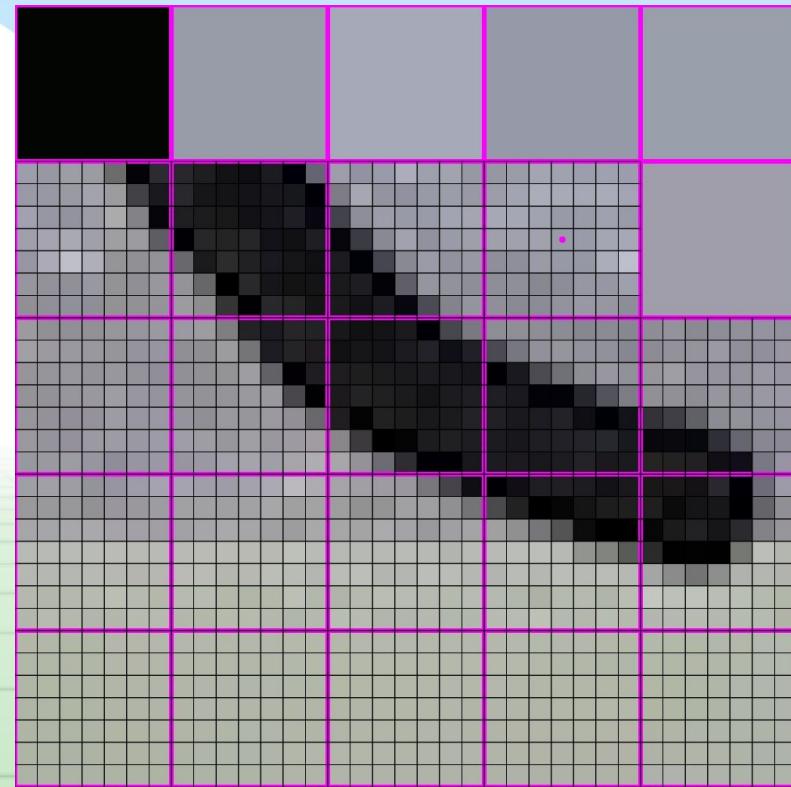
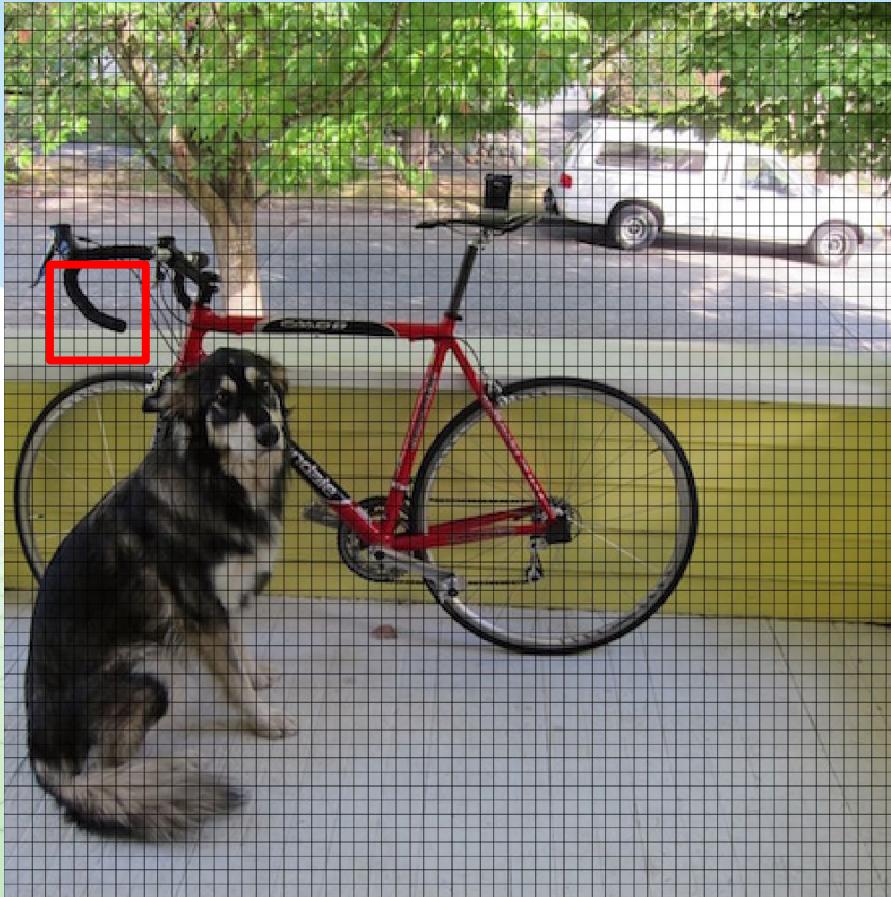
448x448 -> 64x64



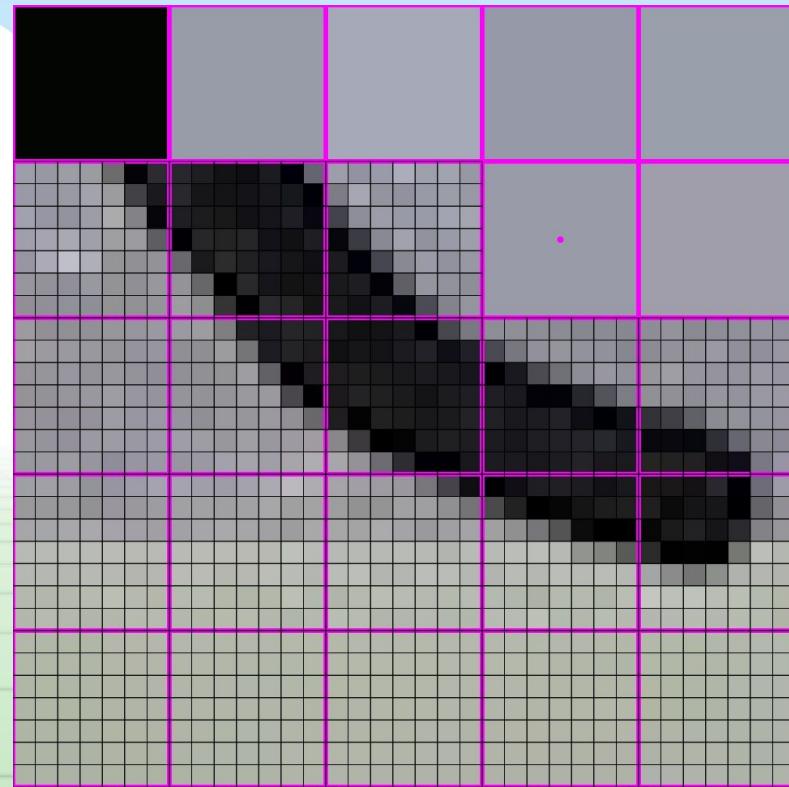
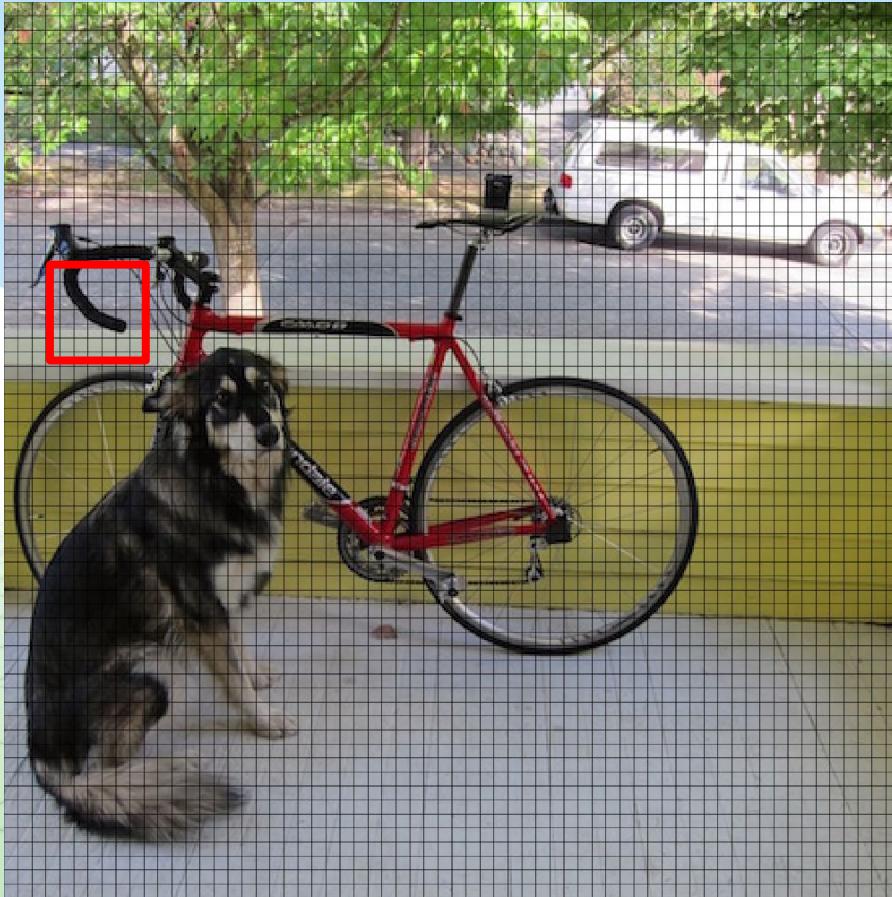
448x448 -> 64x64



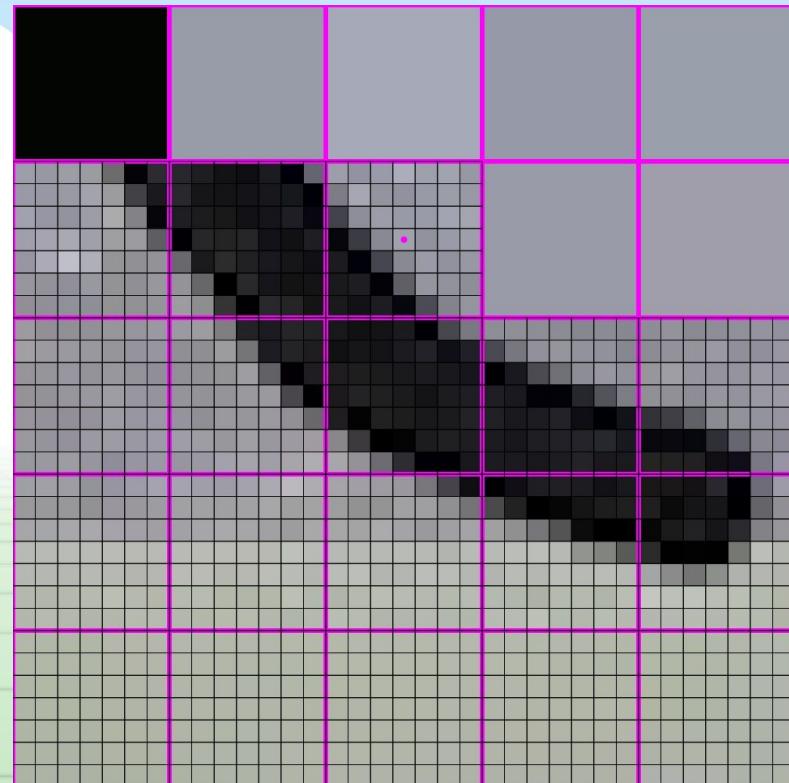
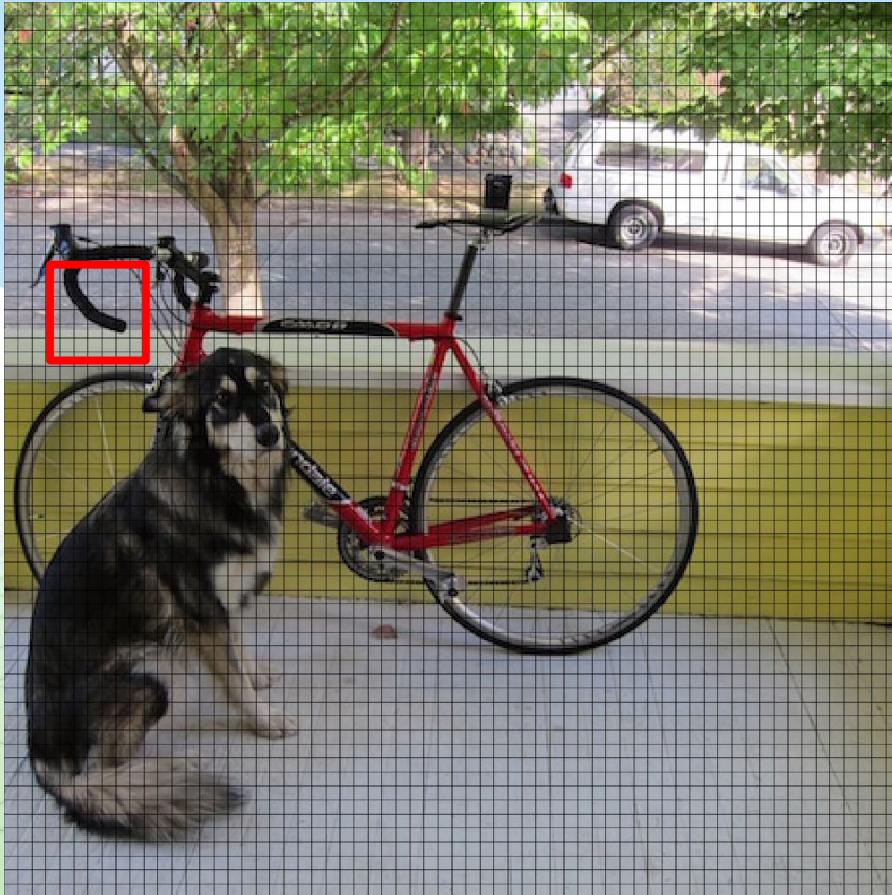
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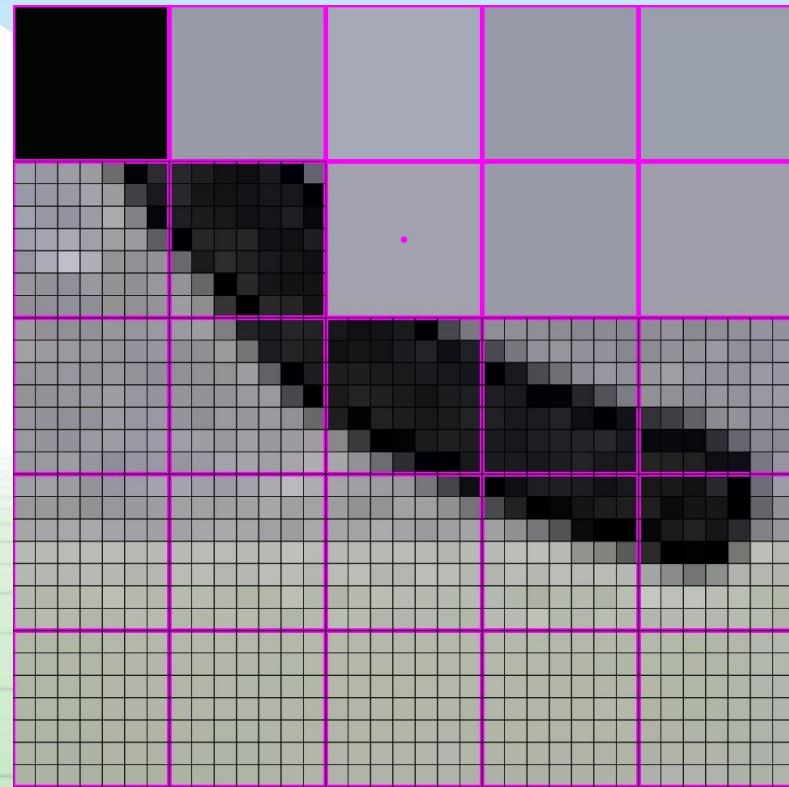
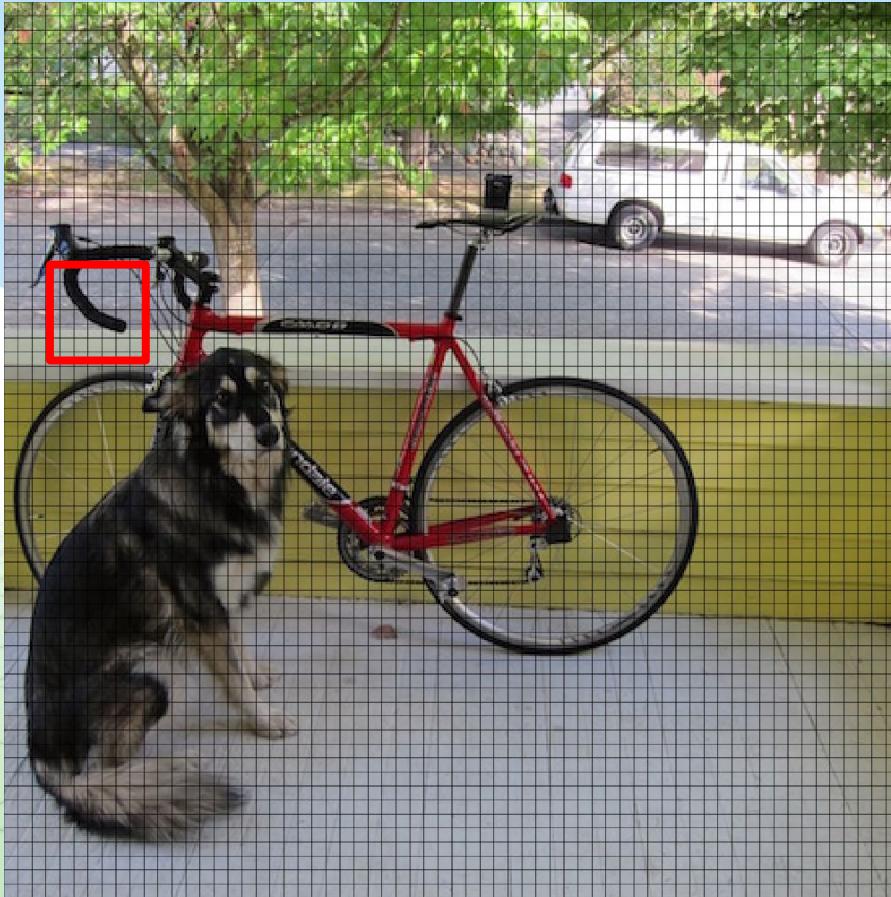
448x448 -> 64x64



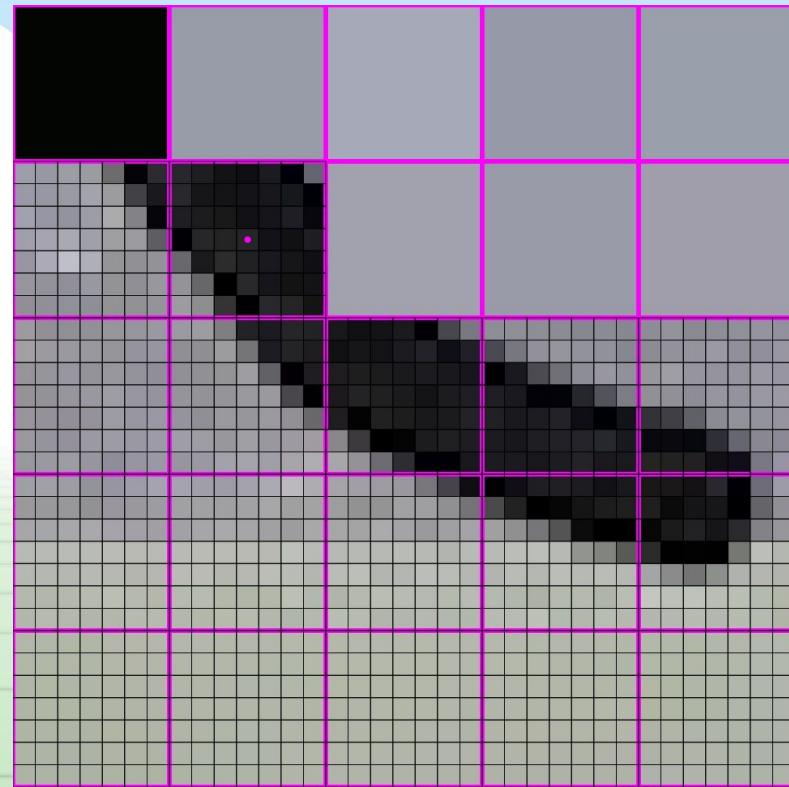
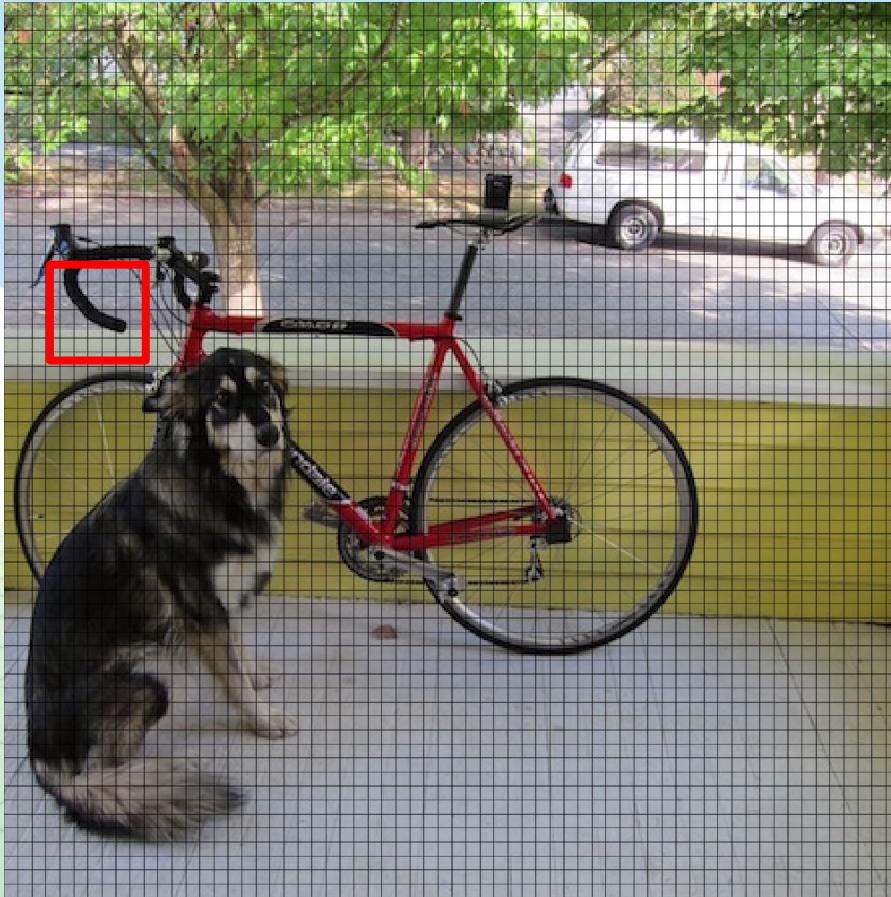
448x448 -> 64x64



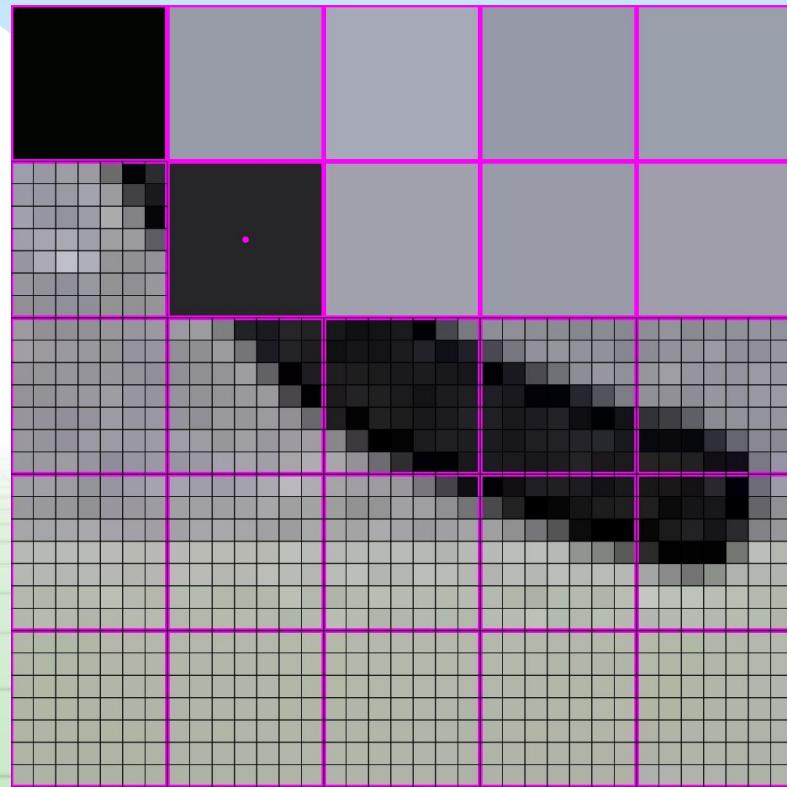
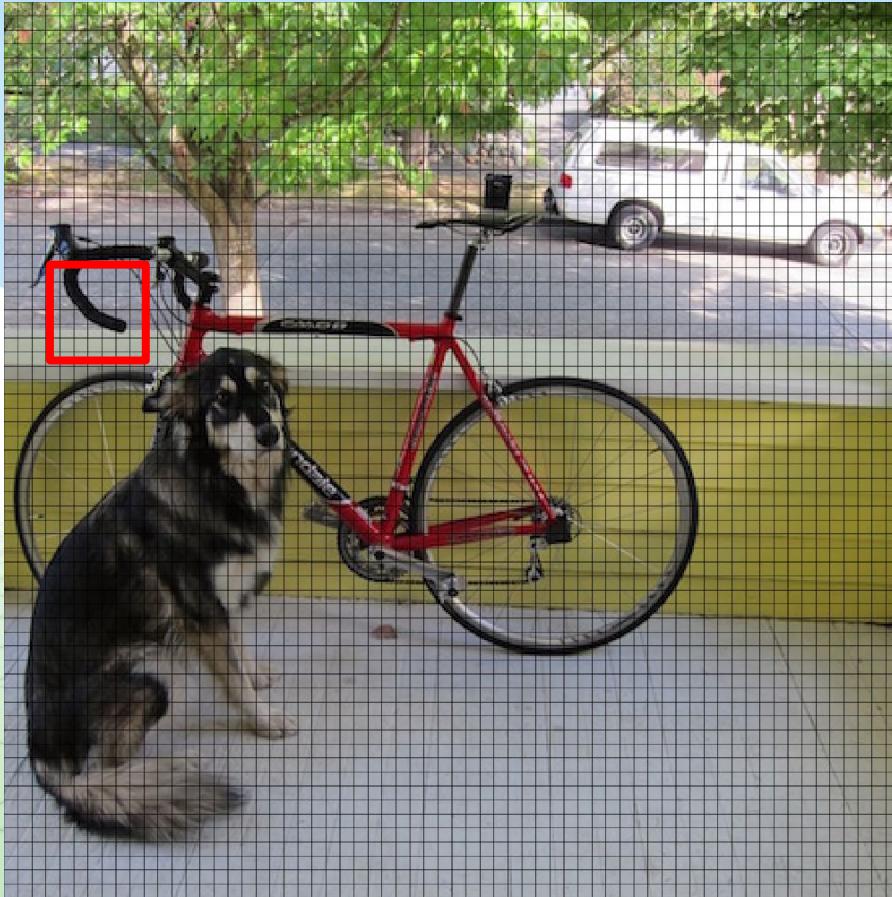
448x448 -> 64x64



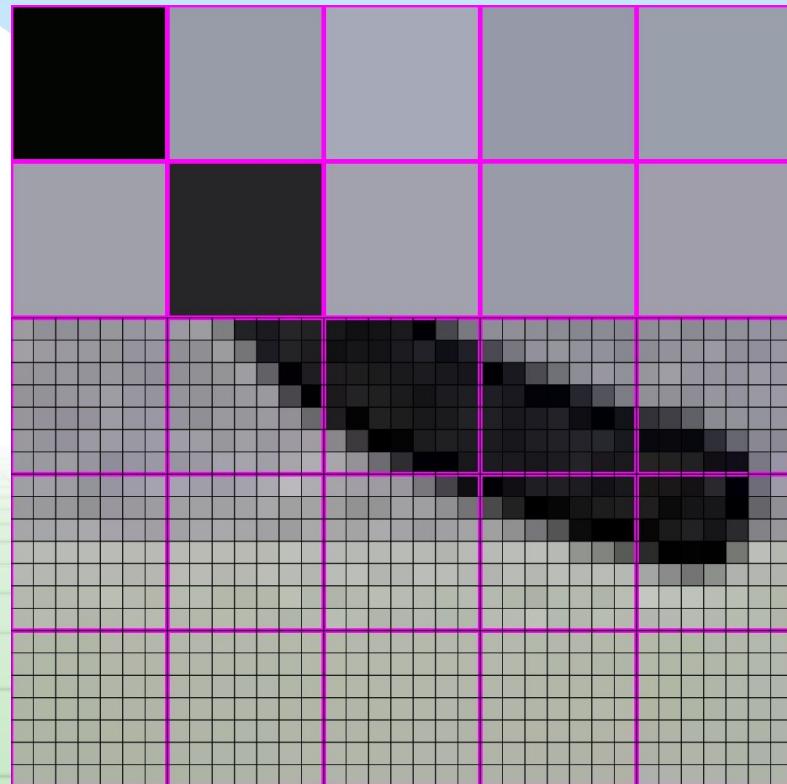
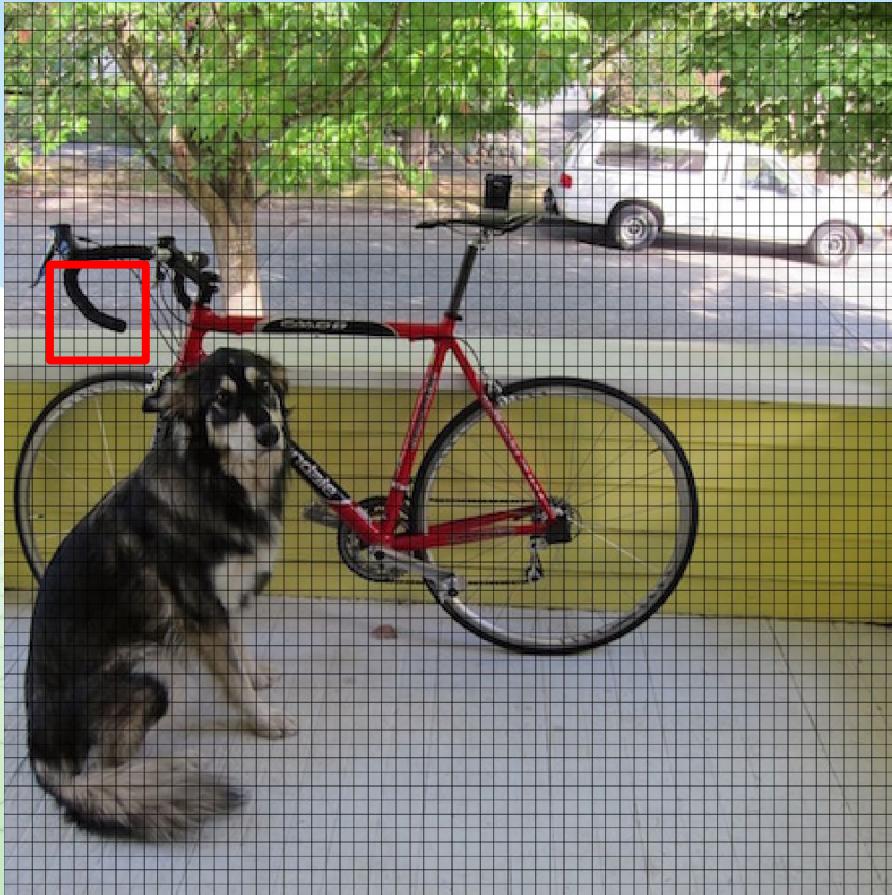
448x448 -> 64x64



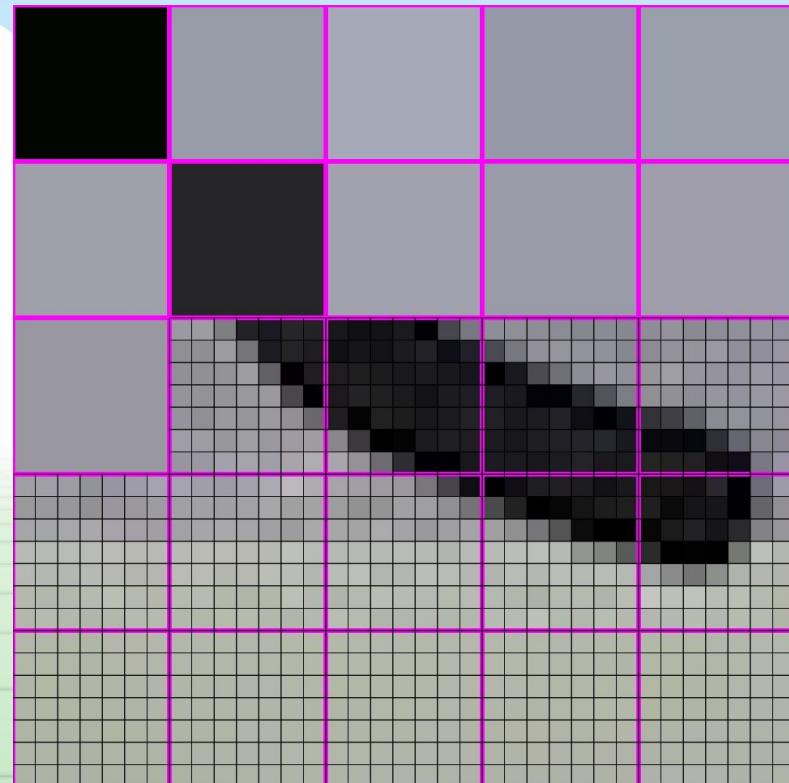
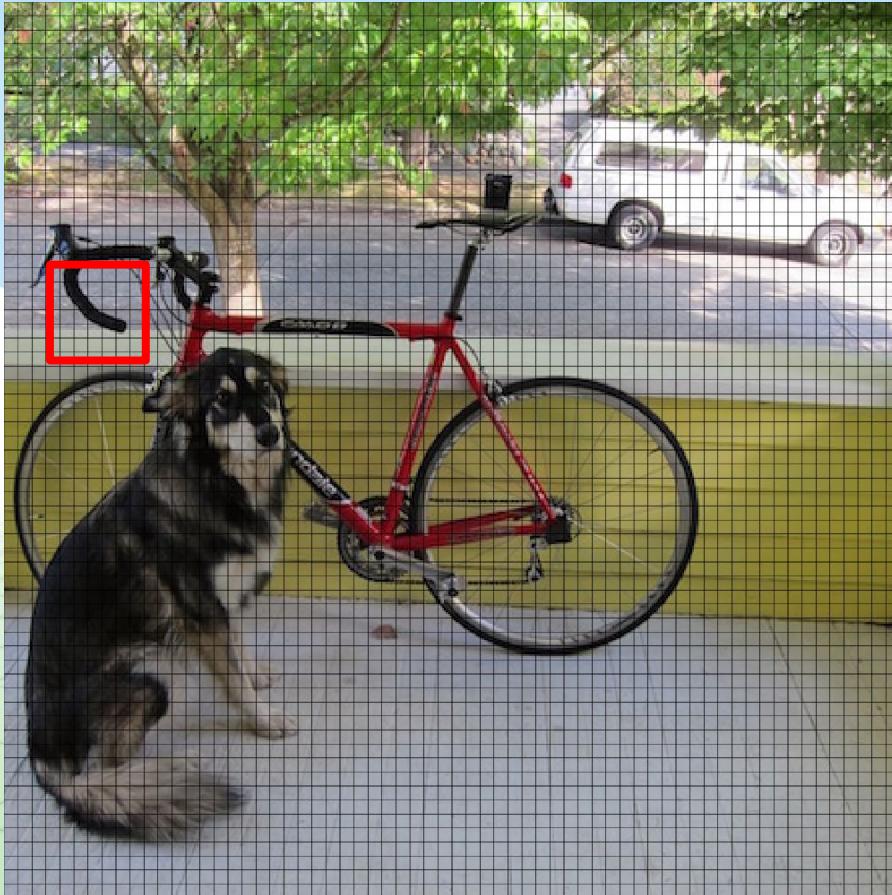
448x448 -> 64x64



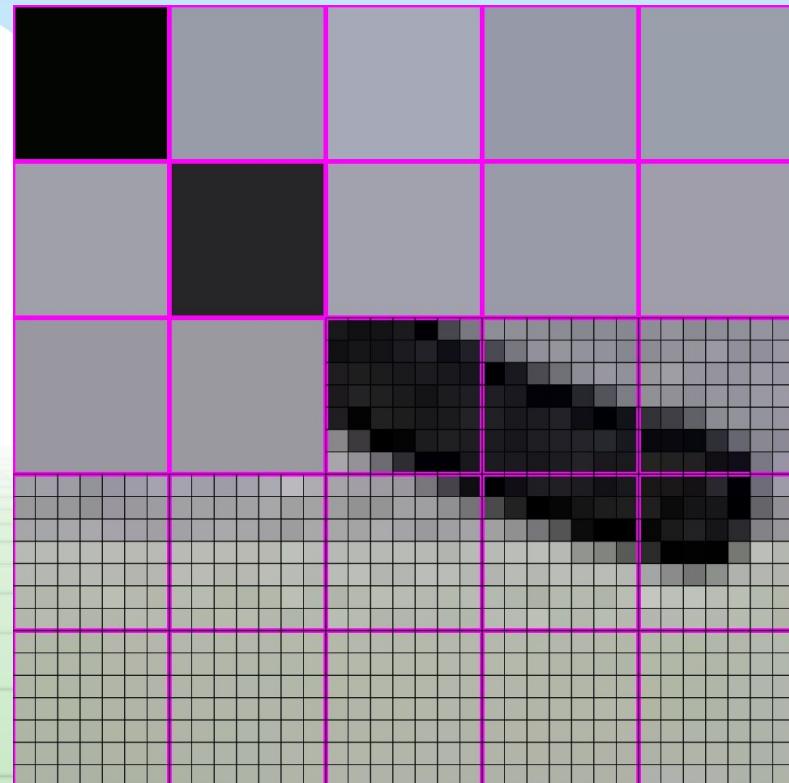
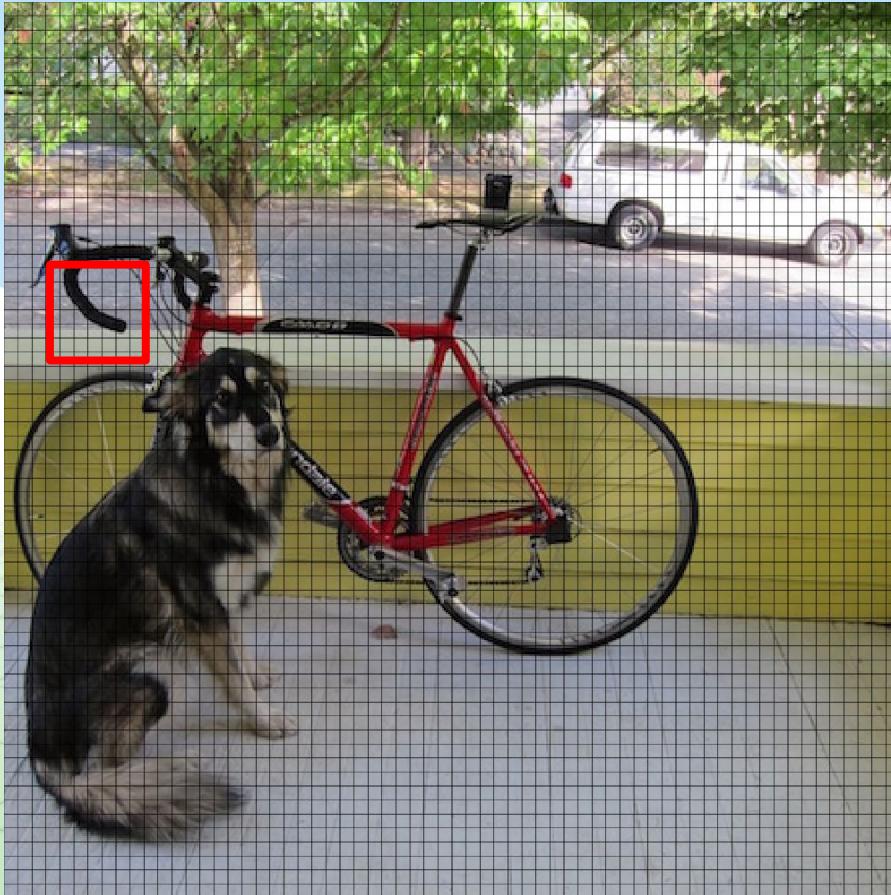
448x448 -> 64x64



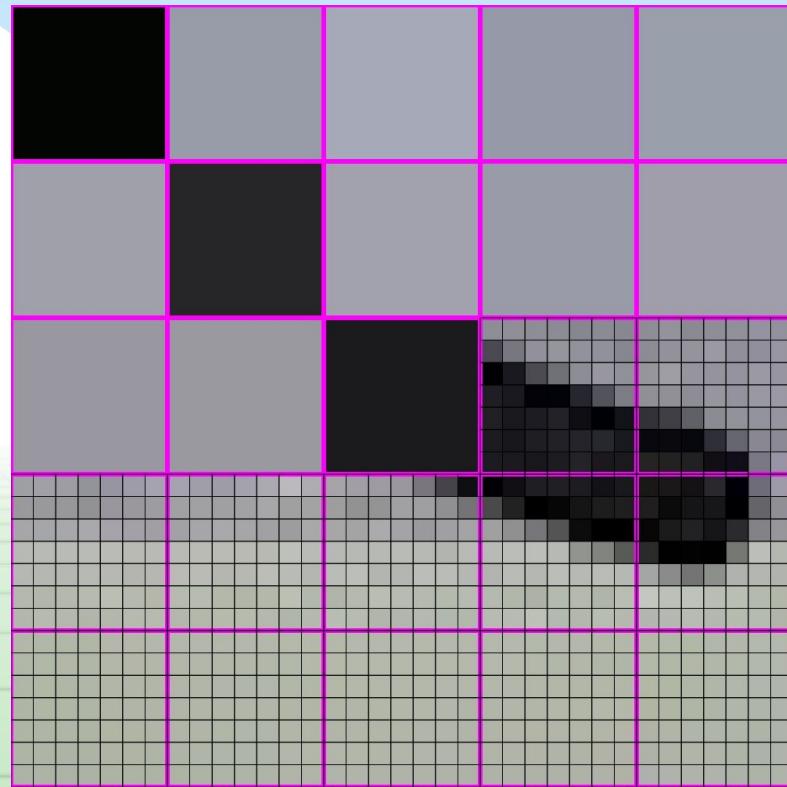
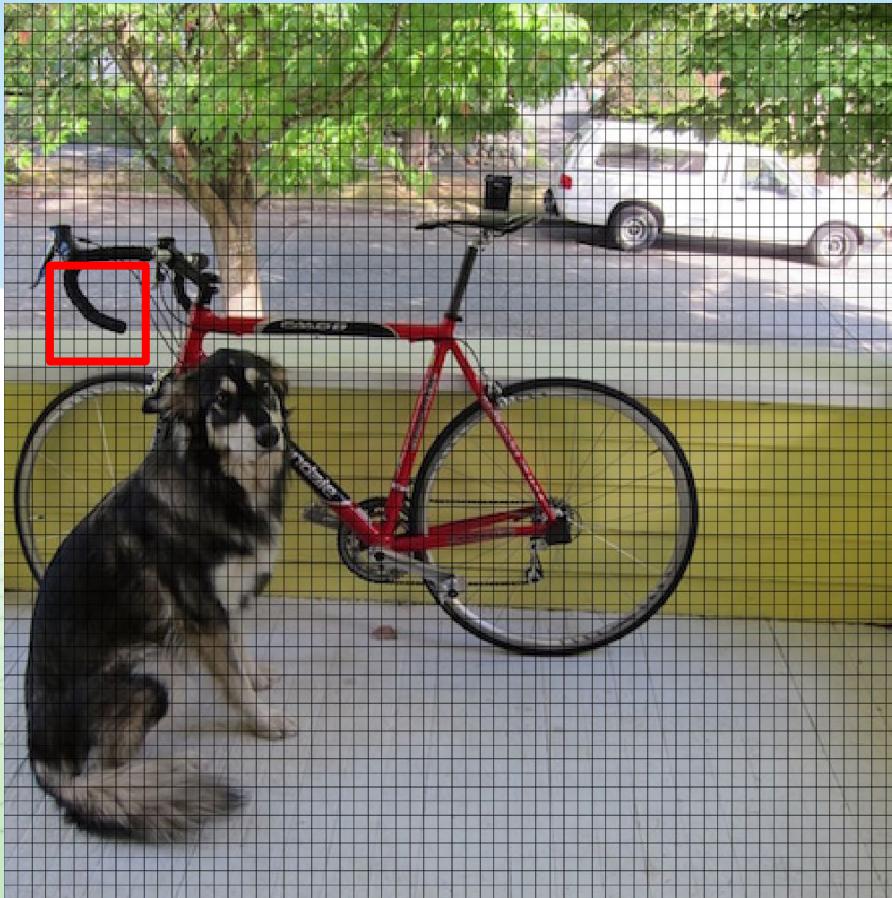
448x448 -> 64x64



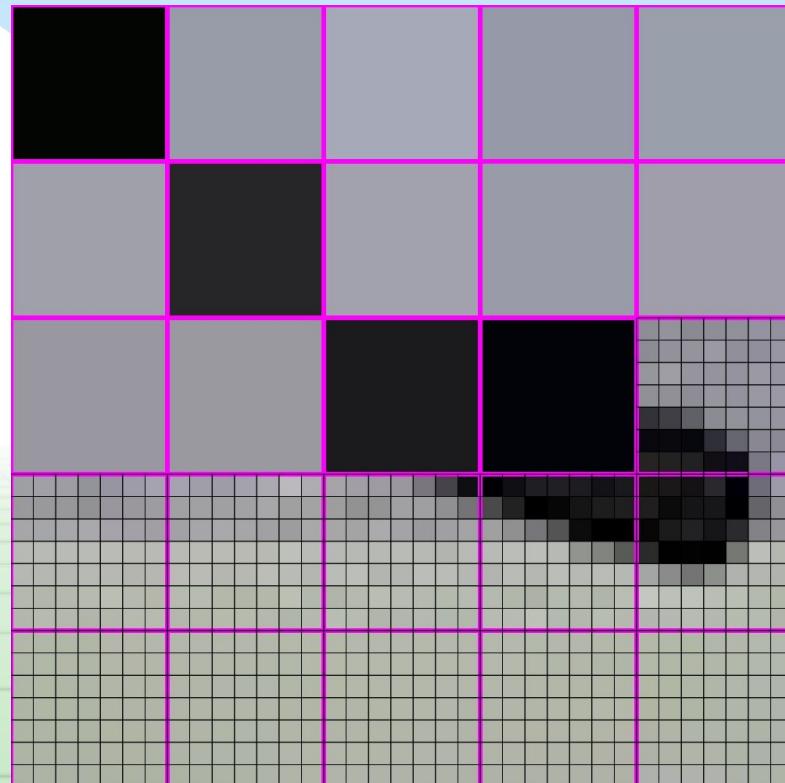
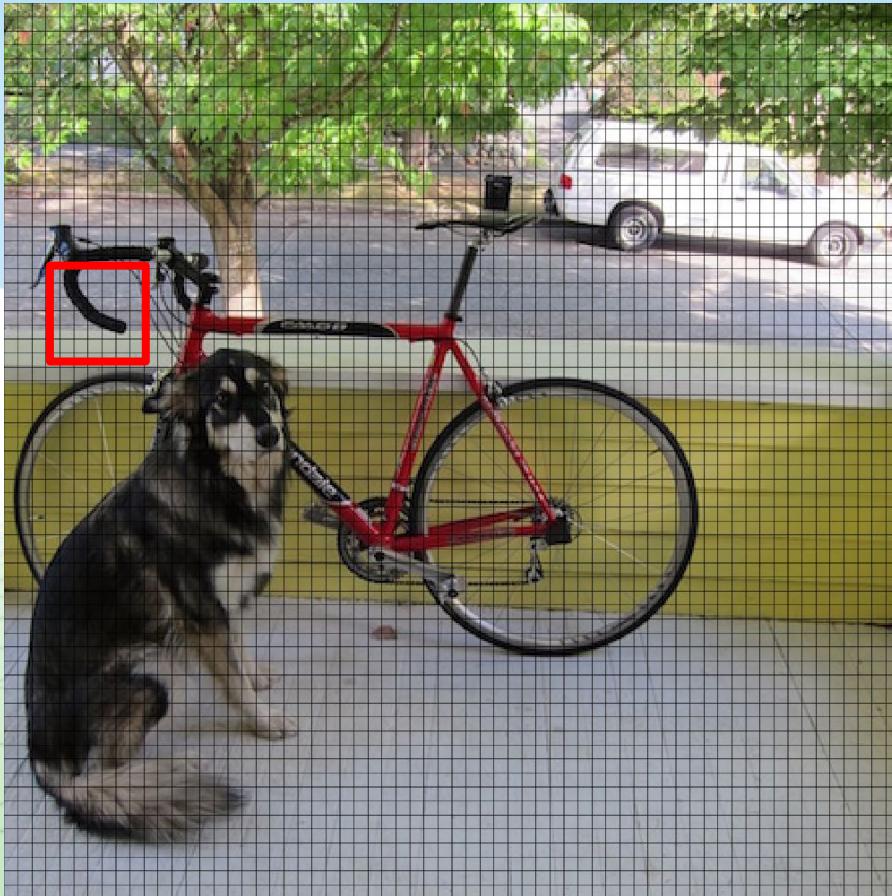
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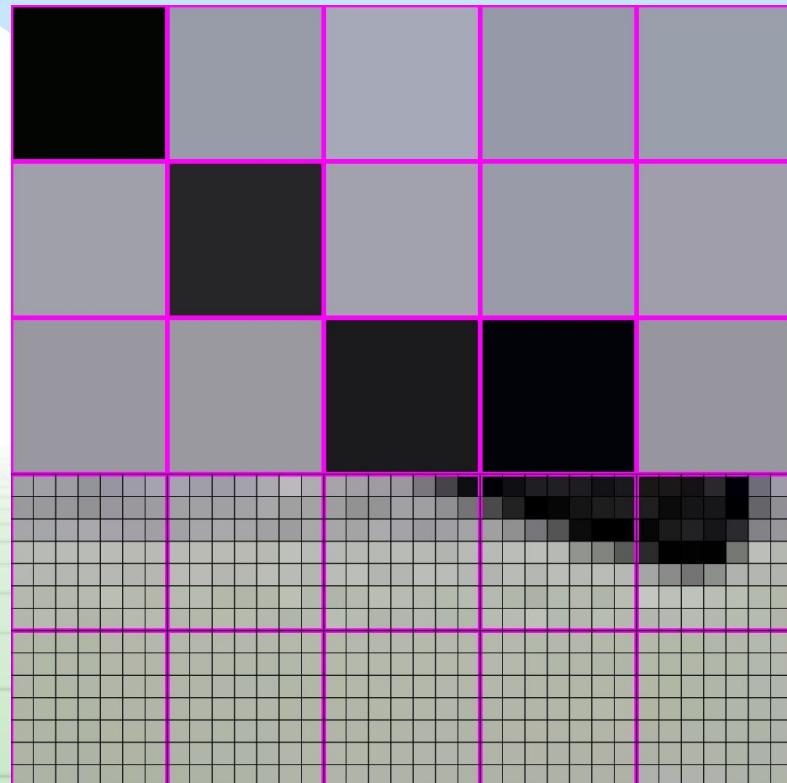
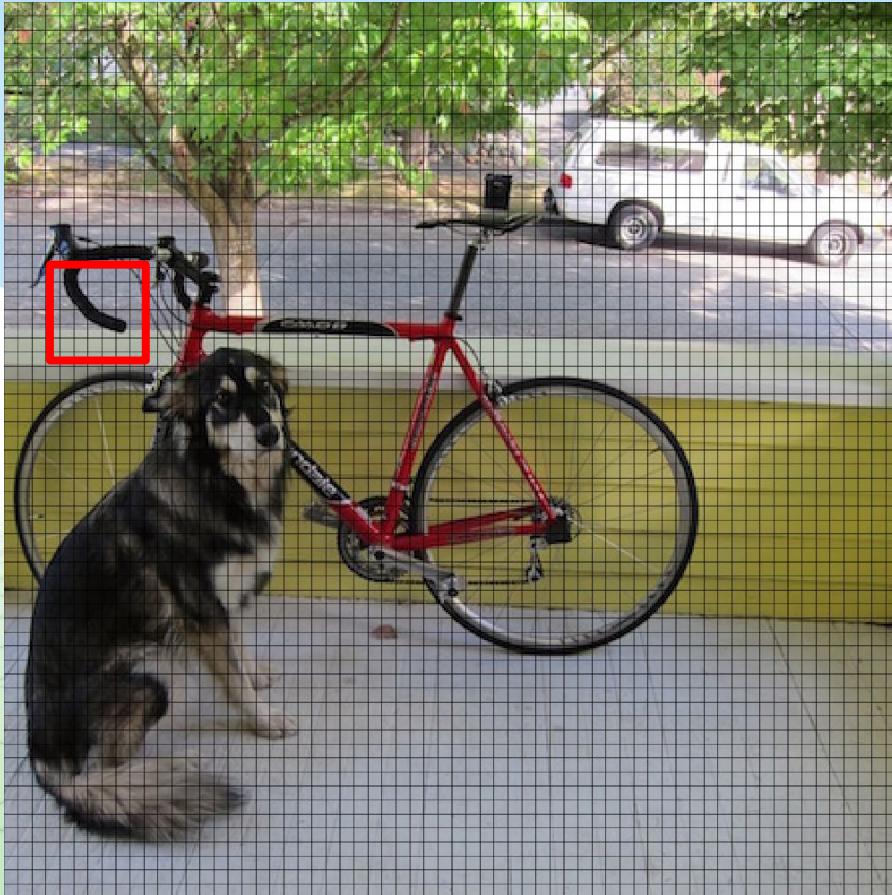
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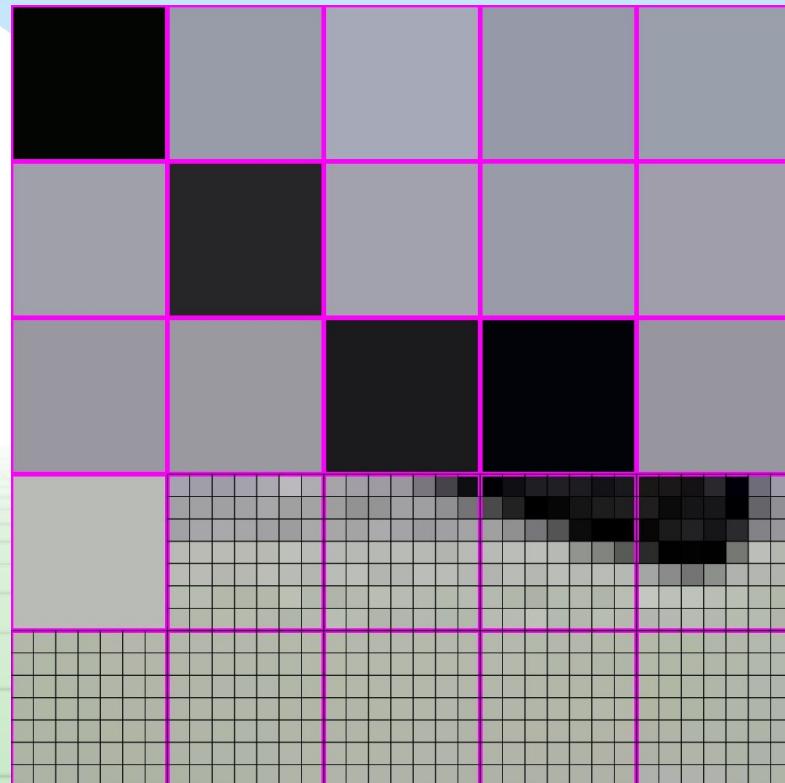
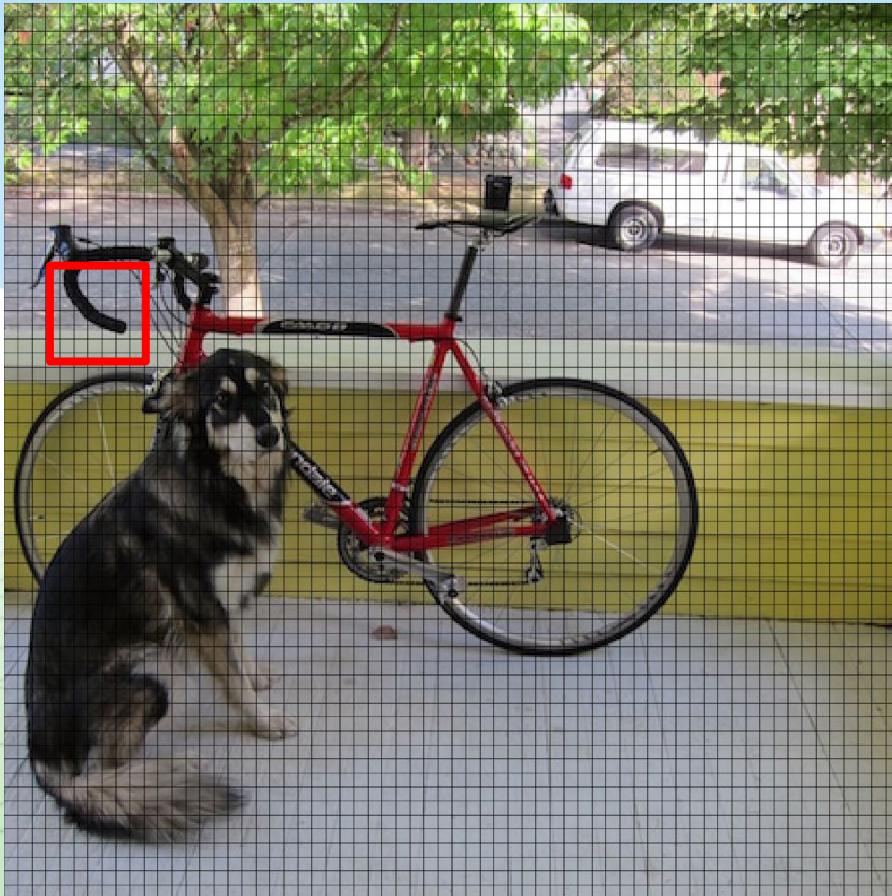
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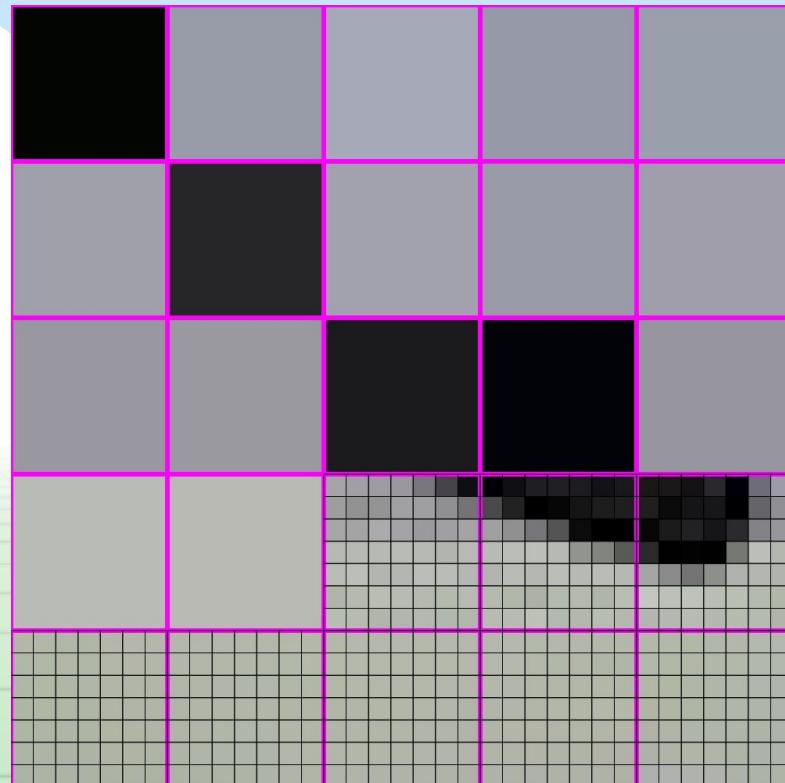
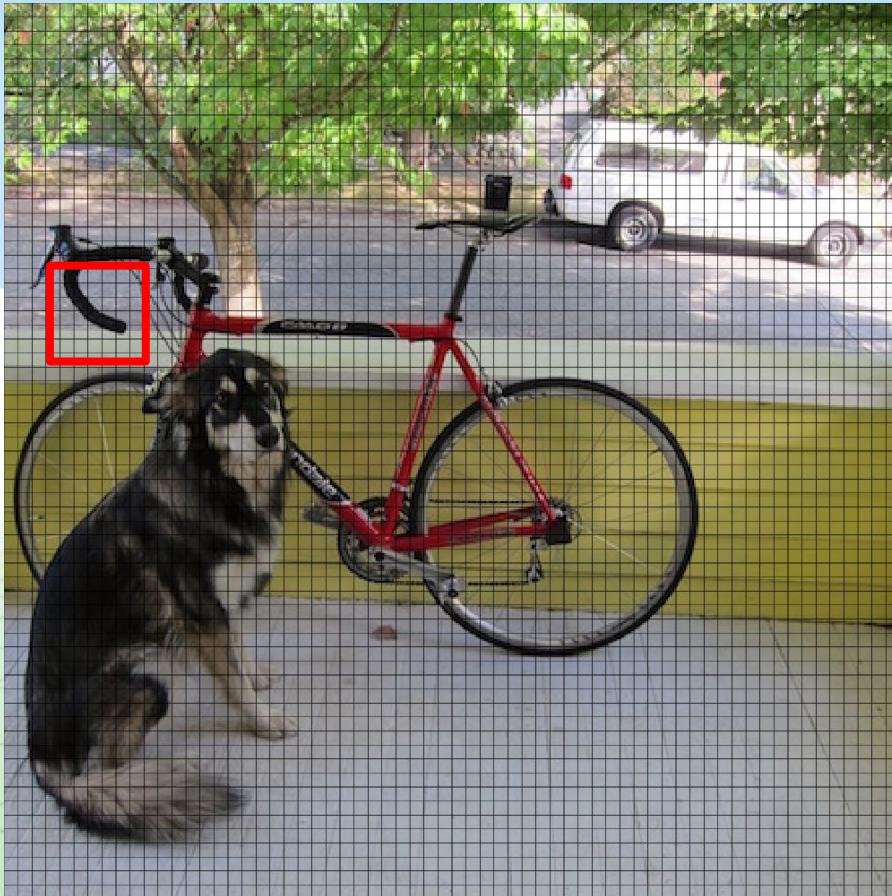
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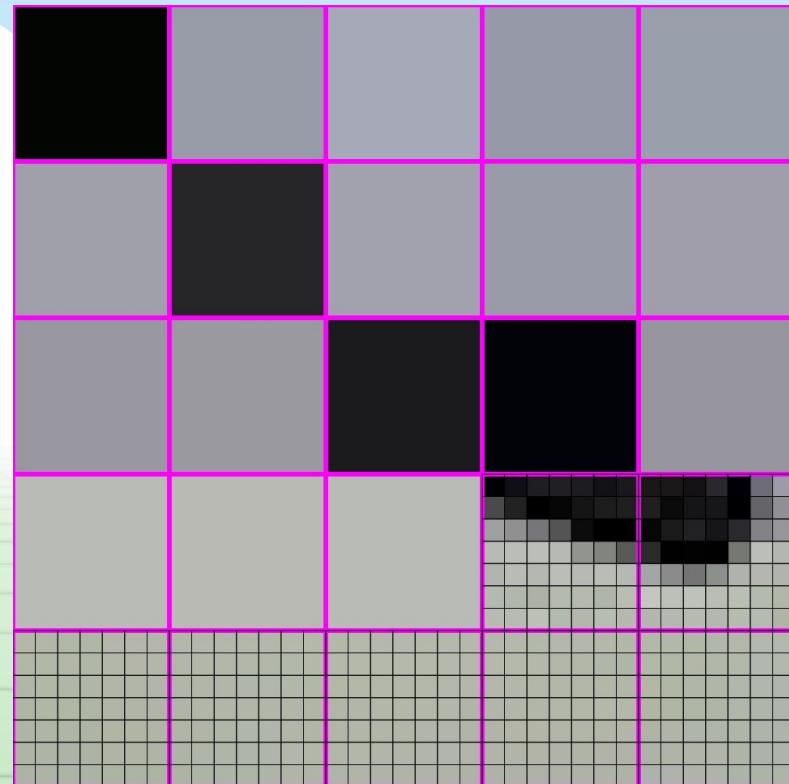
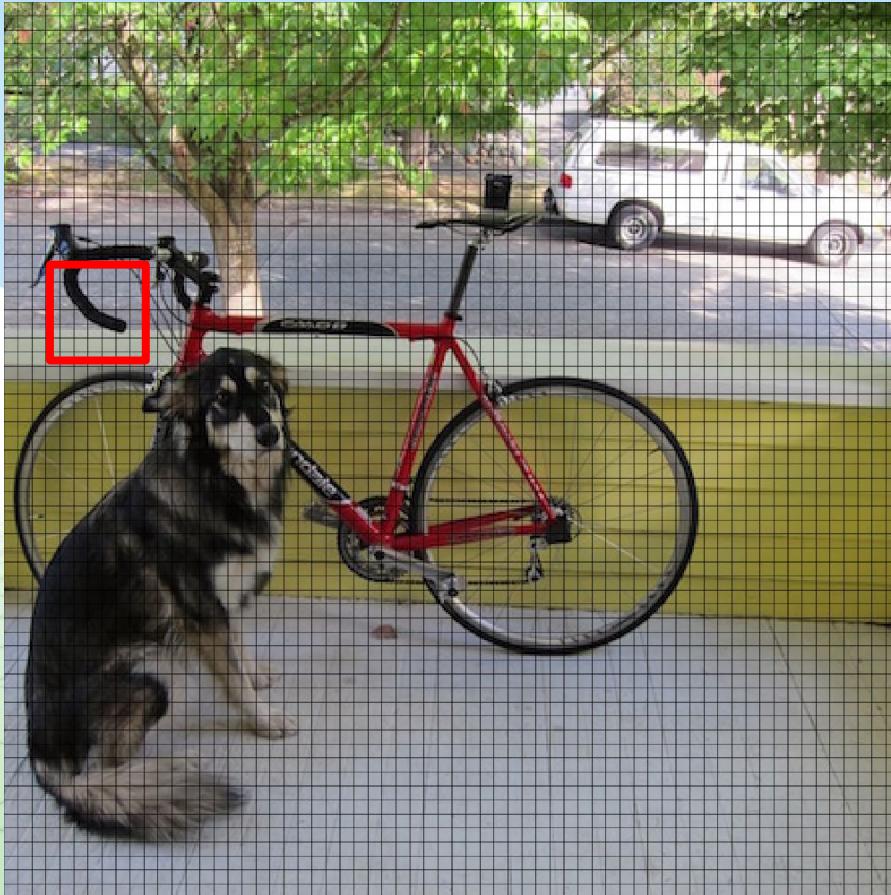
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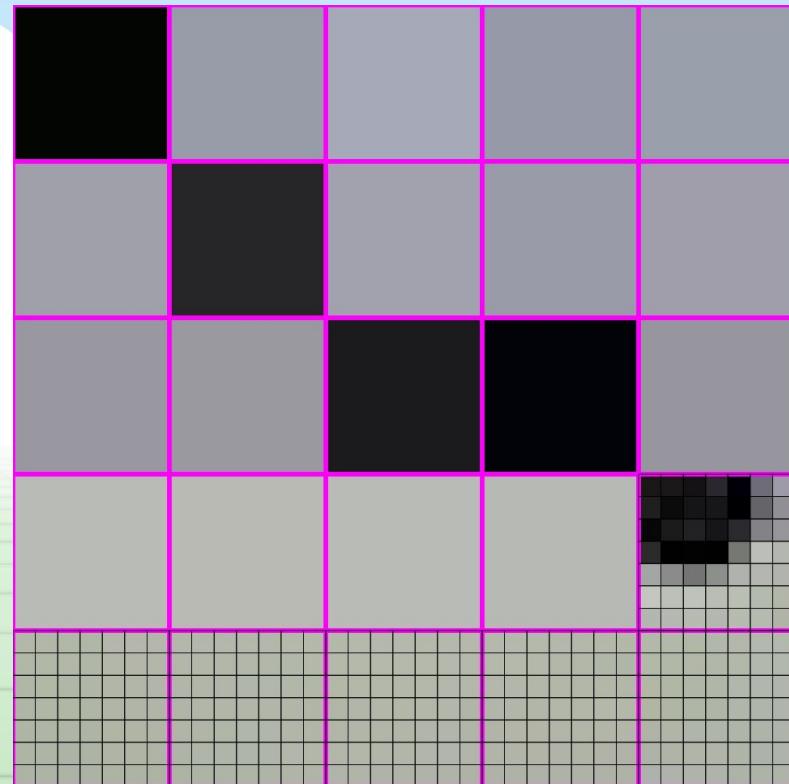
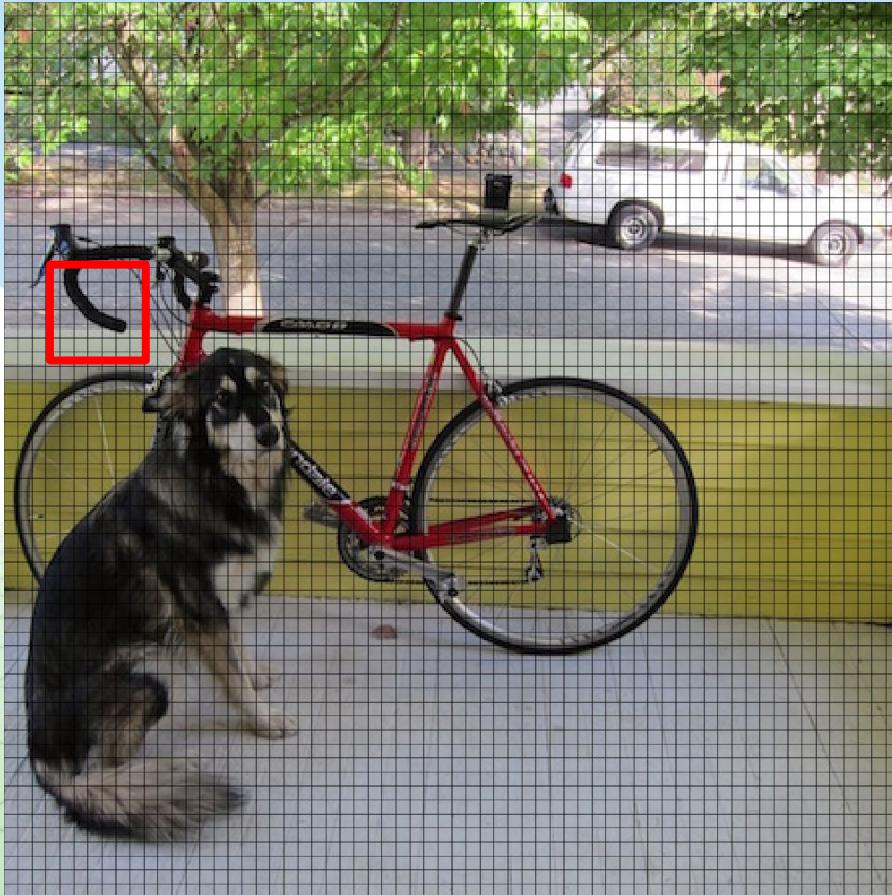
448x448 -> 64x64



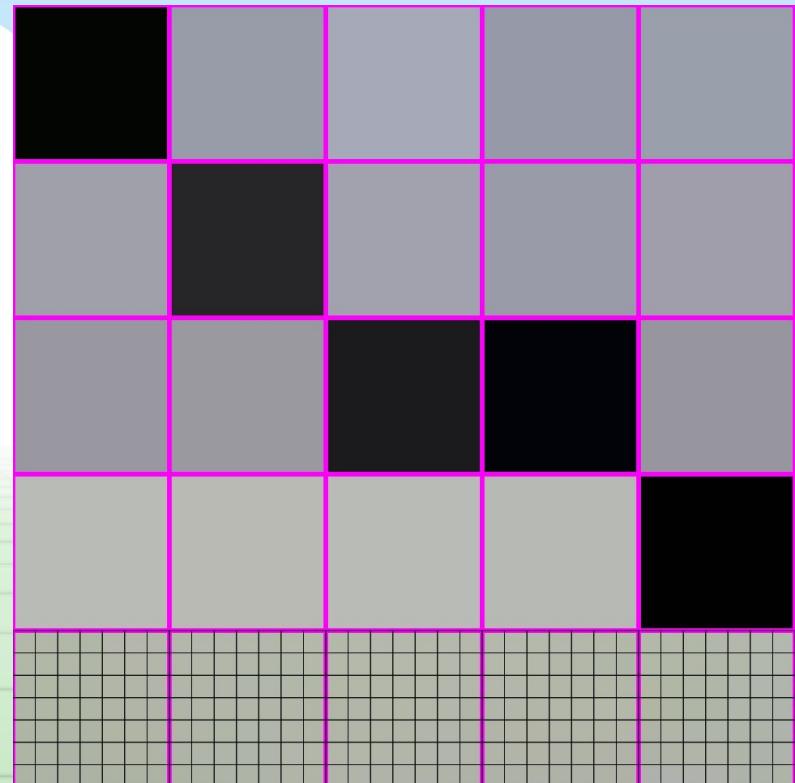
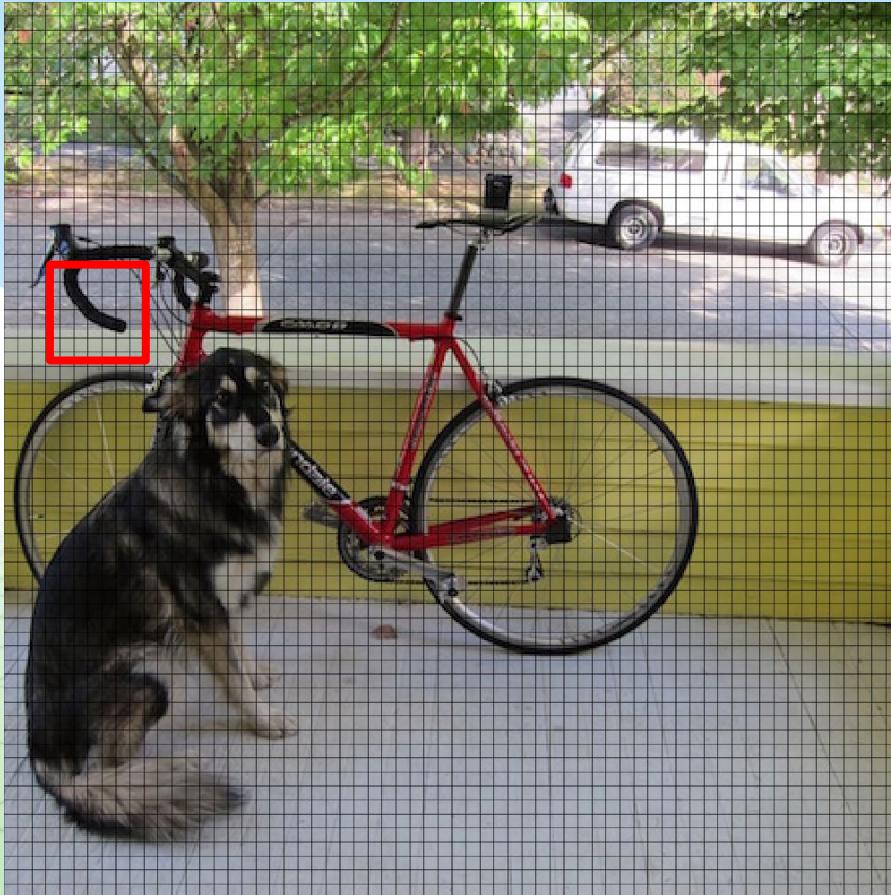
448x448 -> 64x64



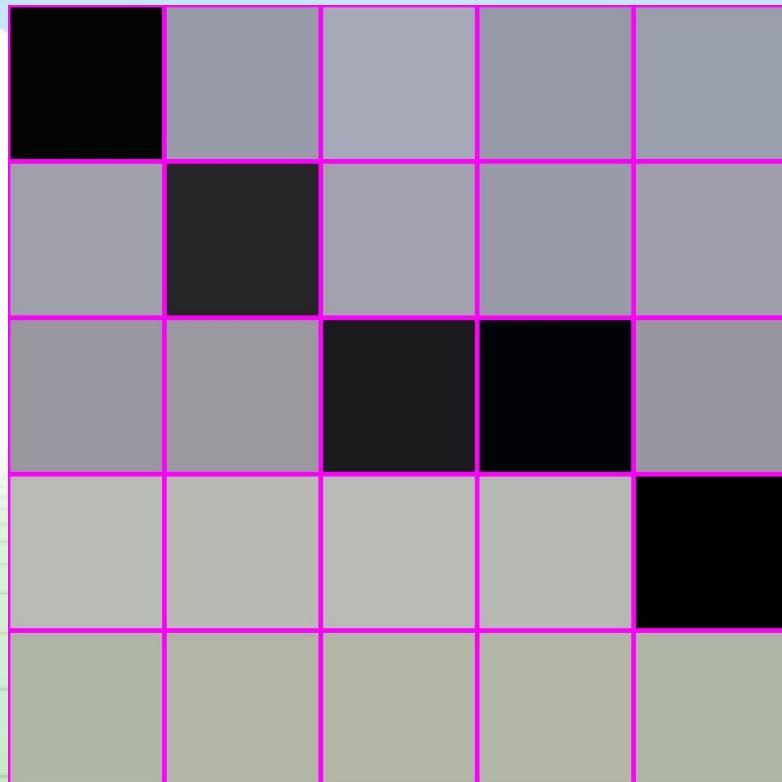
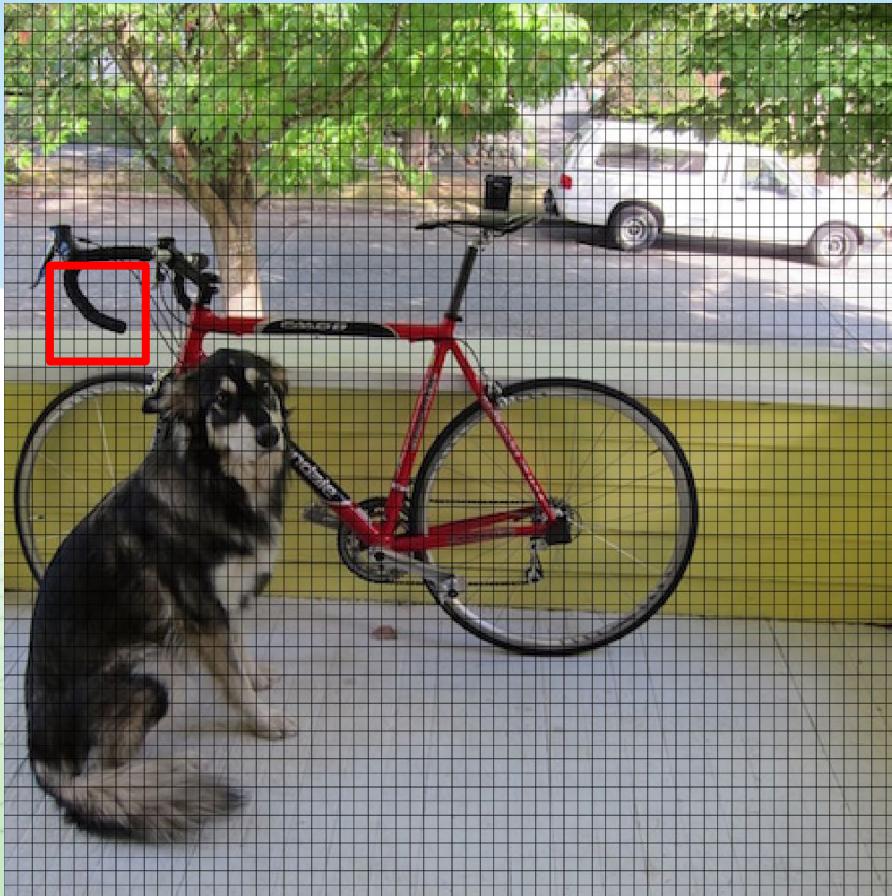
448x448 -> 64x64



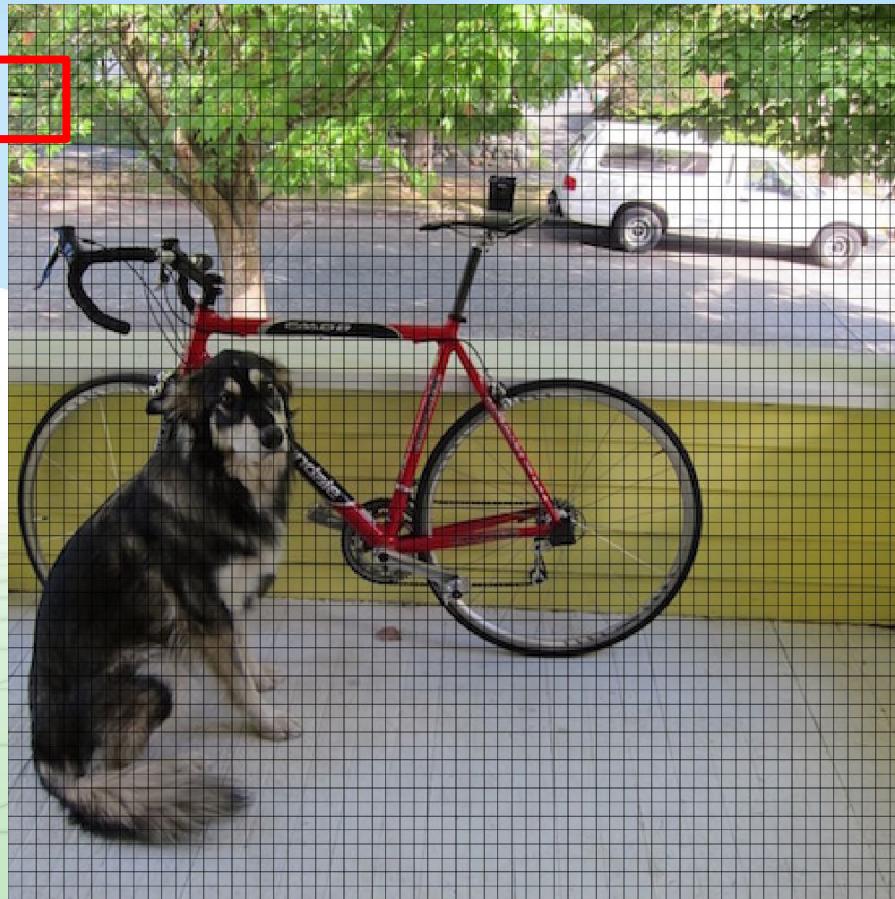
448x448 -> 64x64



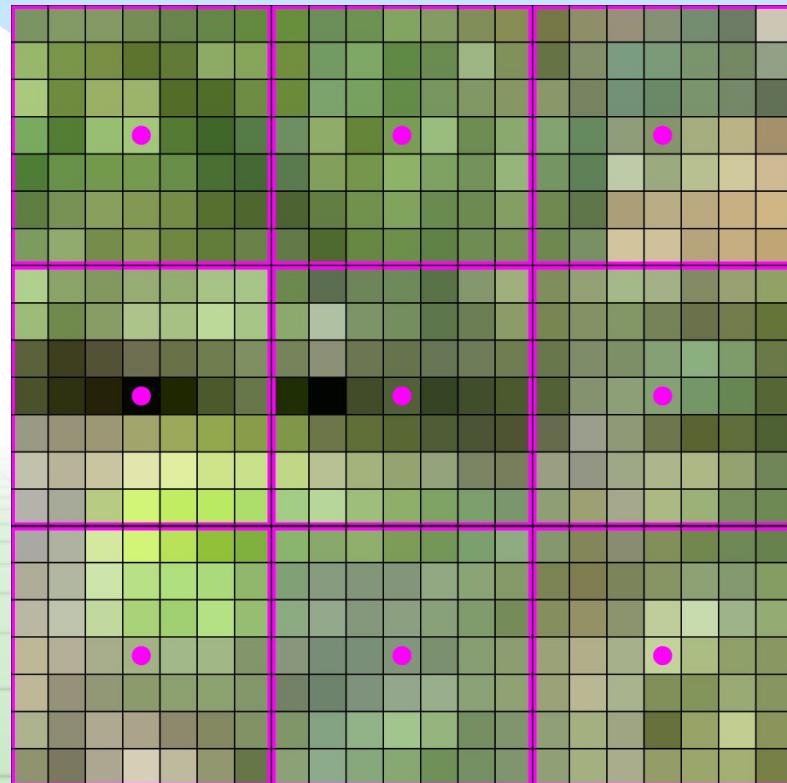
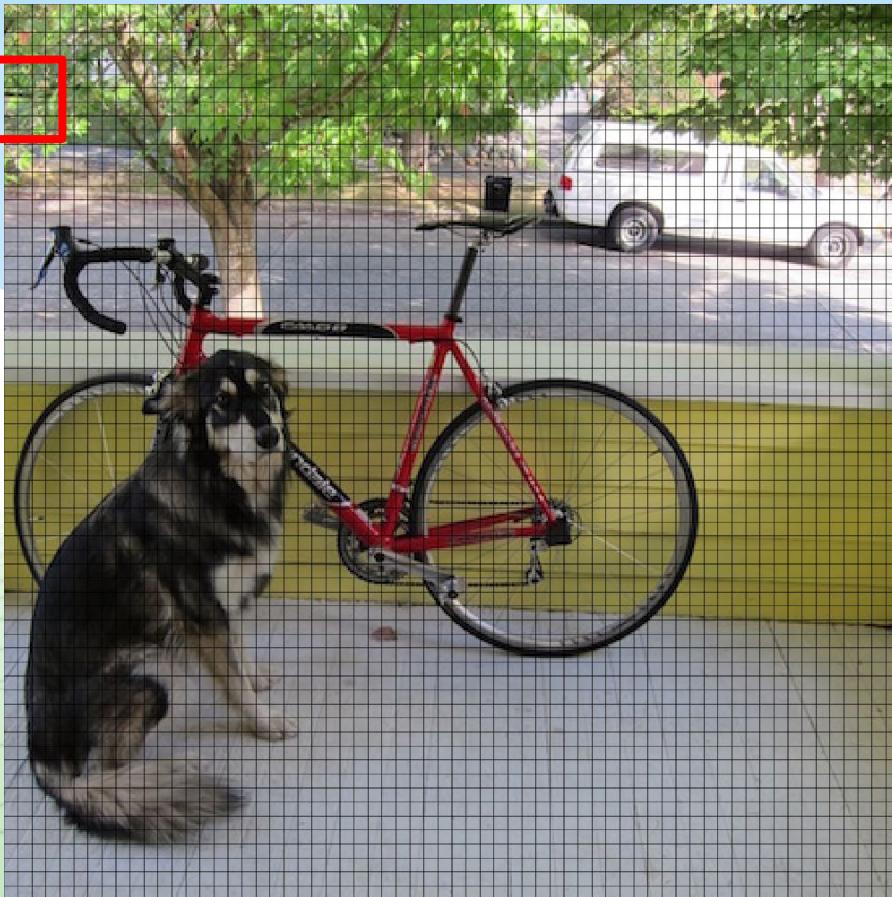
448x448 -> 64x64



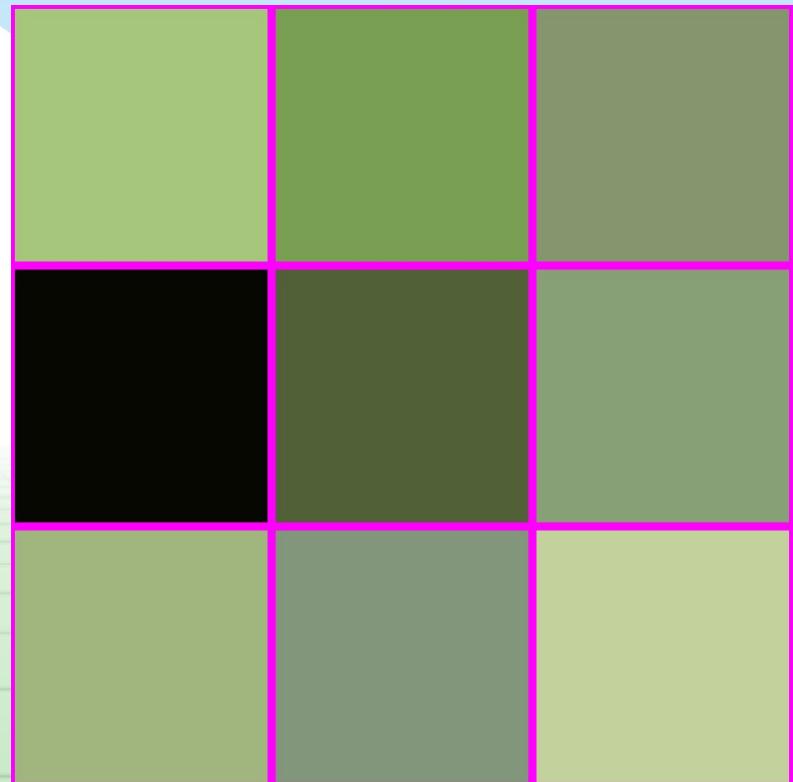
448x448 -> 64x64



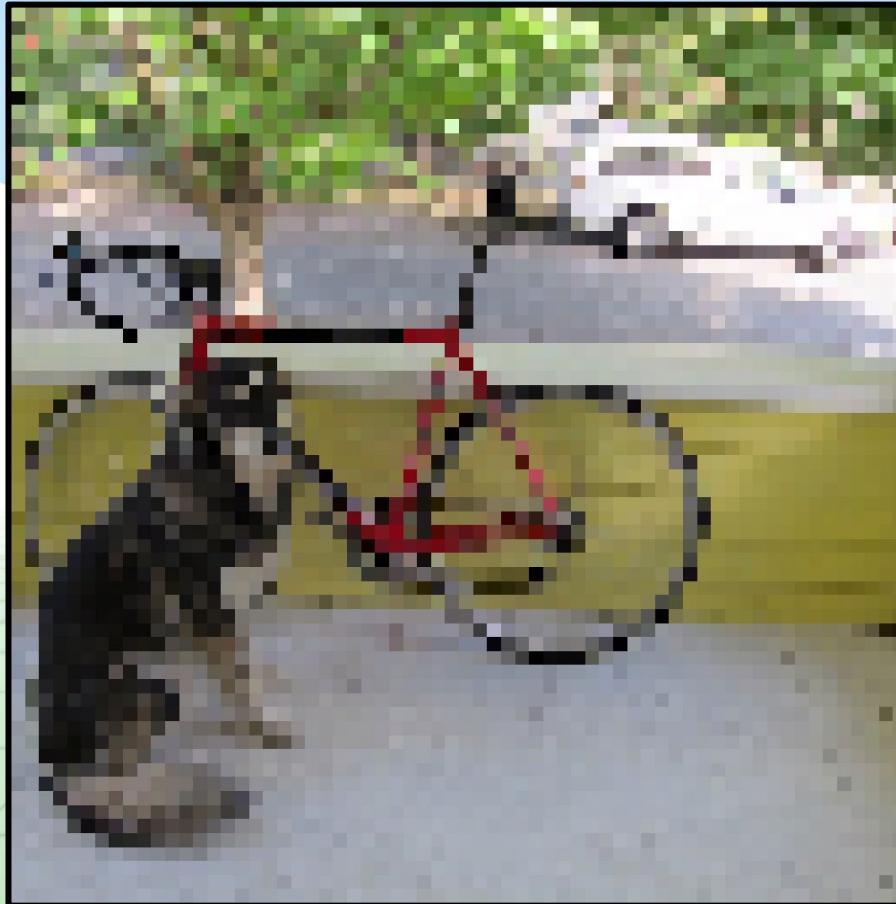
448x448 -> 64x64



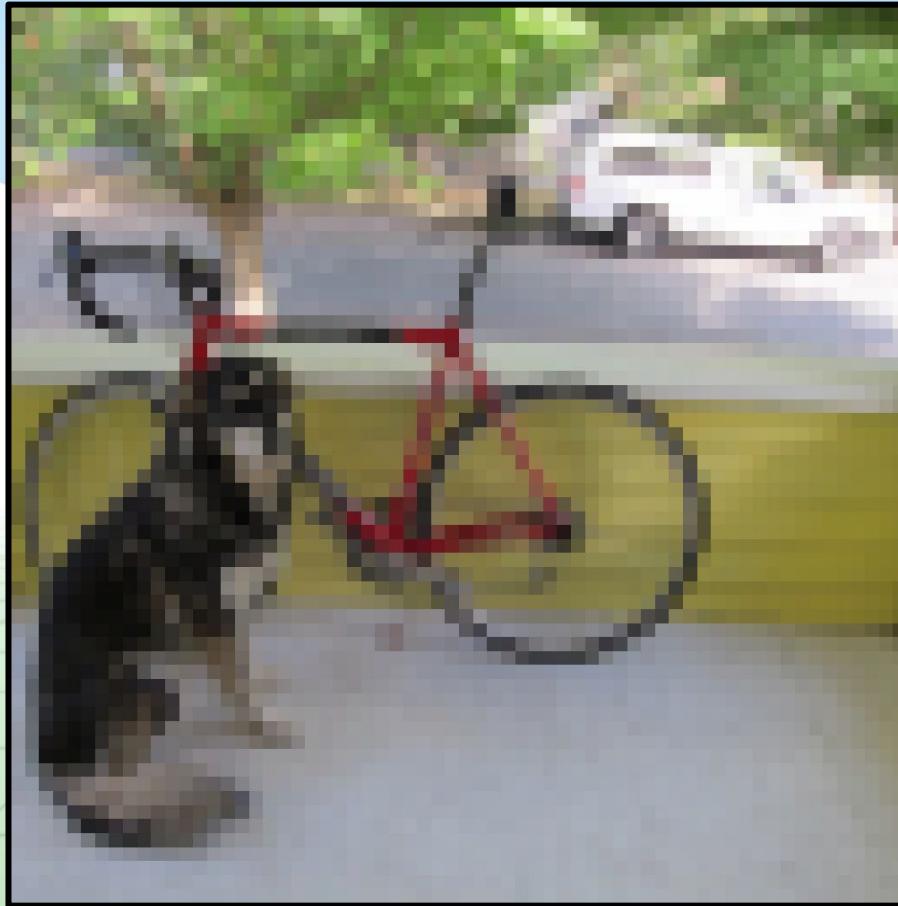
448x448 -> 64x64



IS THIS ALL THERE IS??



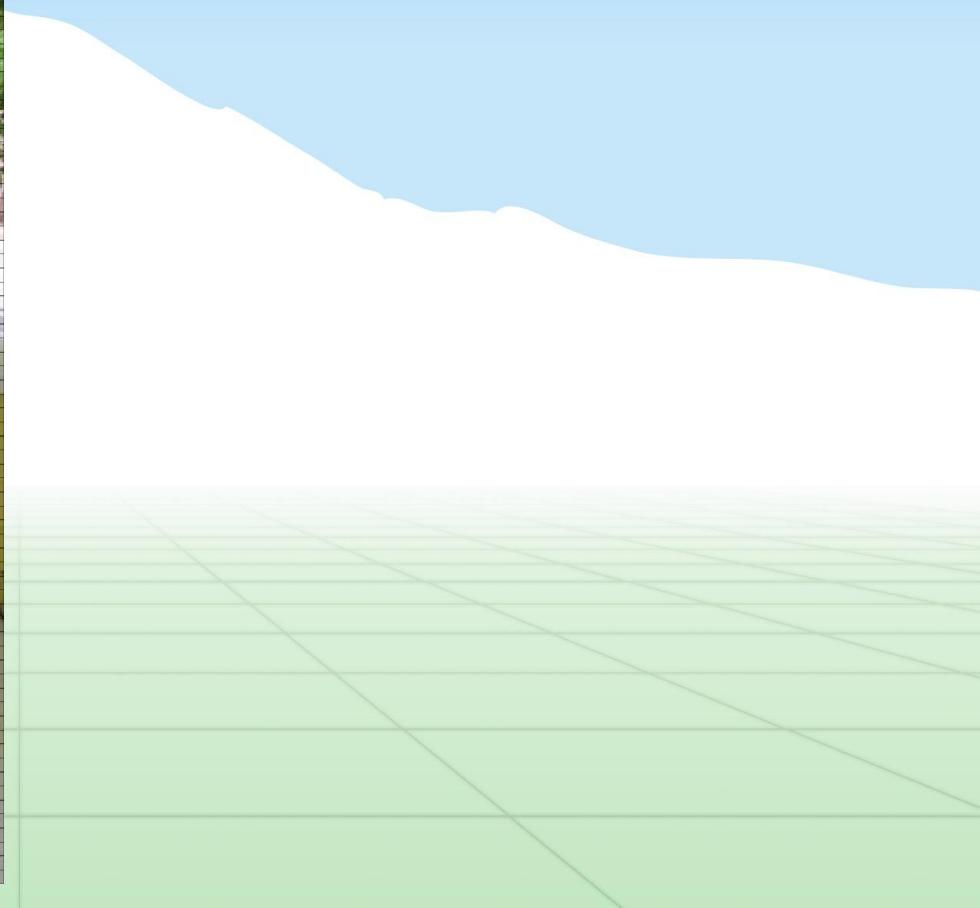
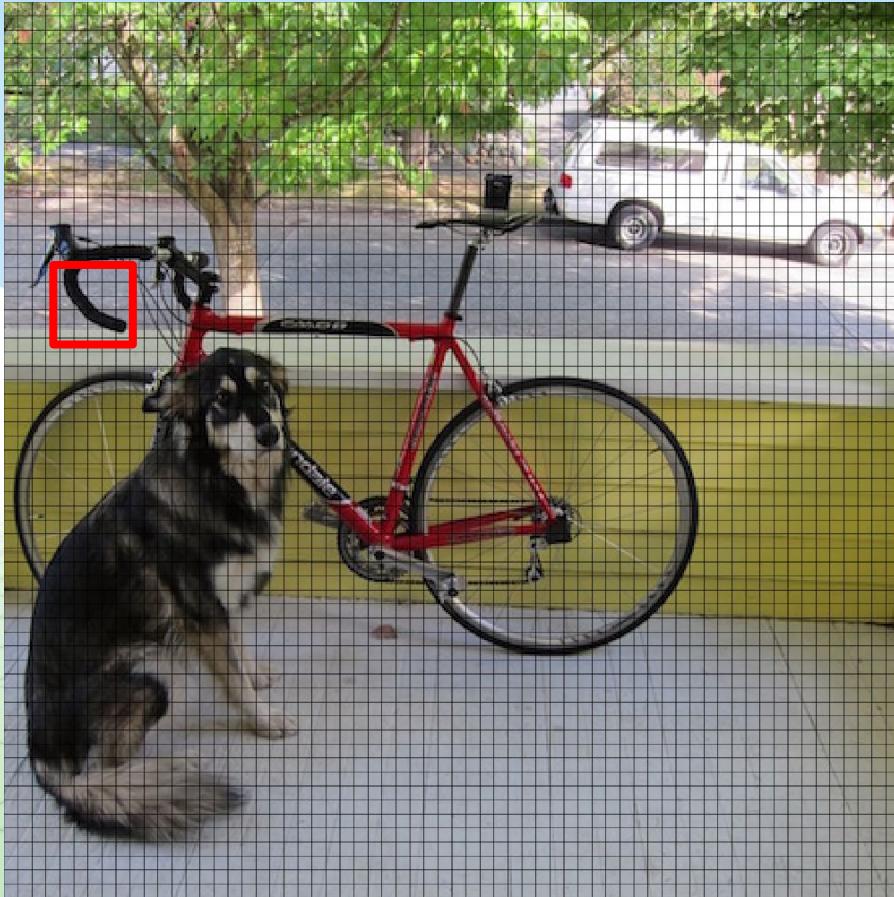
THERE IS A BETTER WAY!



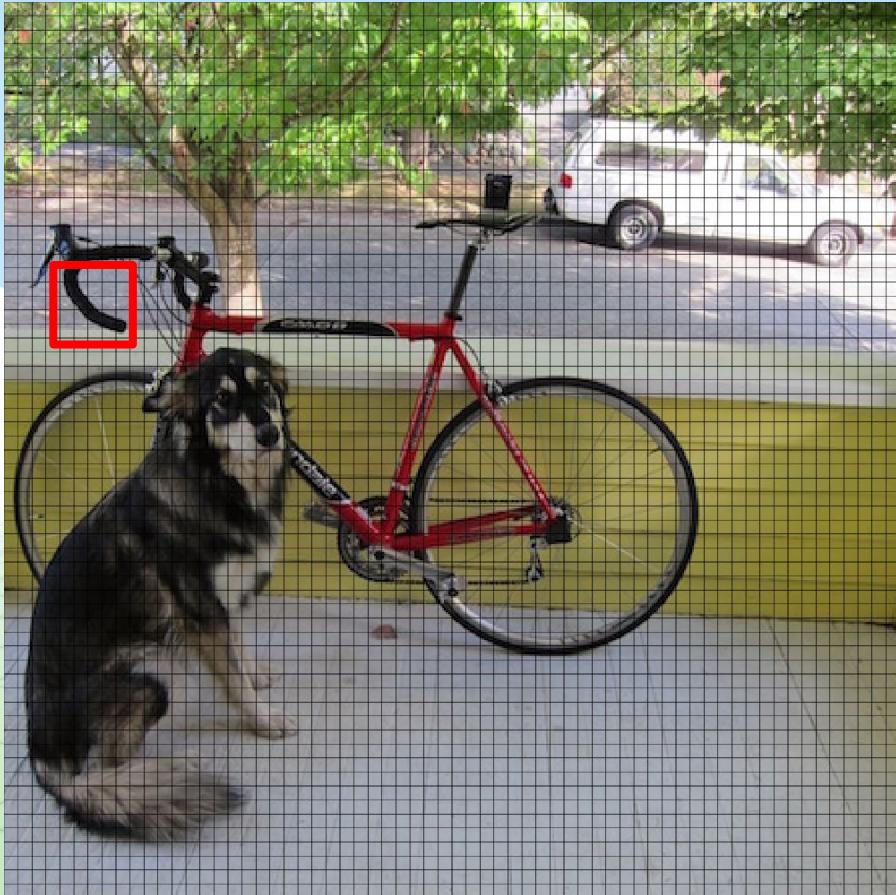
LOOK AT HOW MUCH BETTER



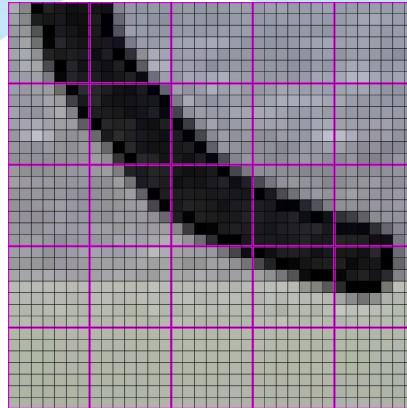
How do?



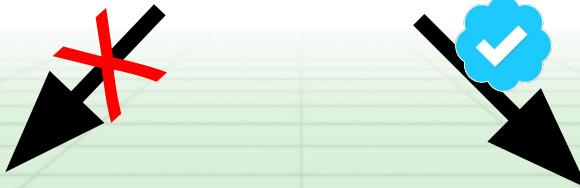
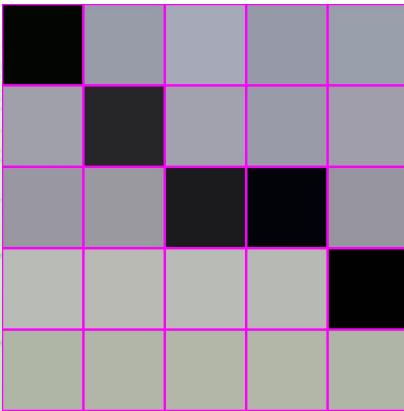
How do? Averaging!



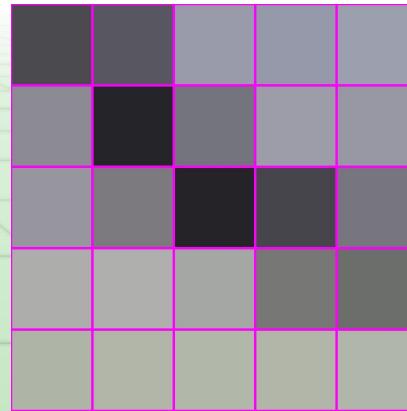
How do? Averaging!



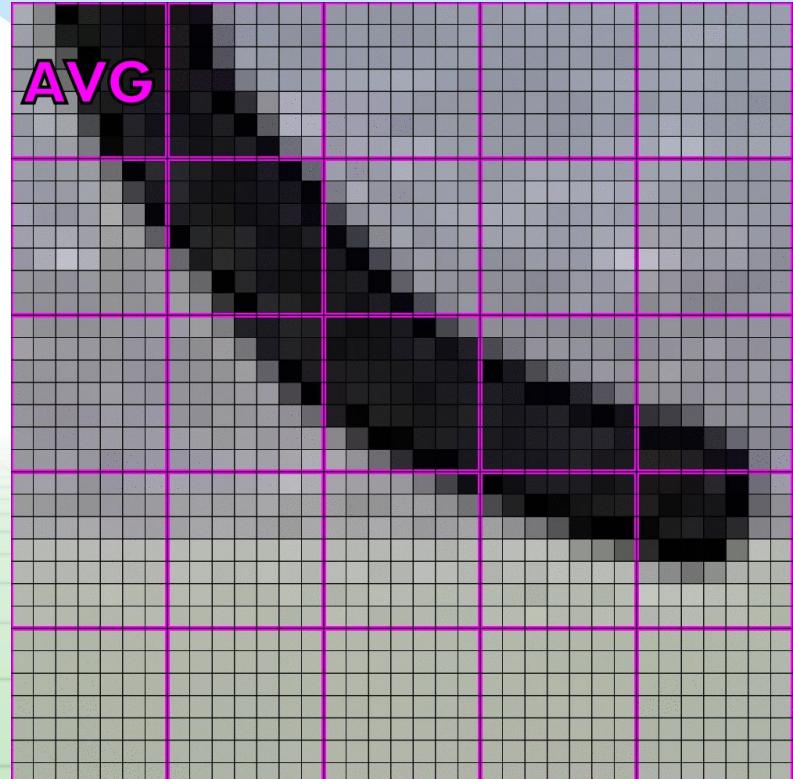
“interpolation”



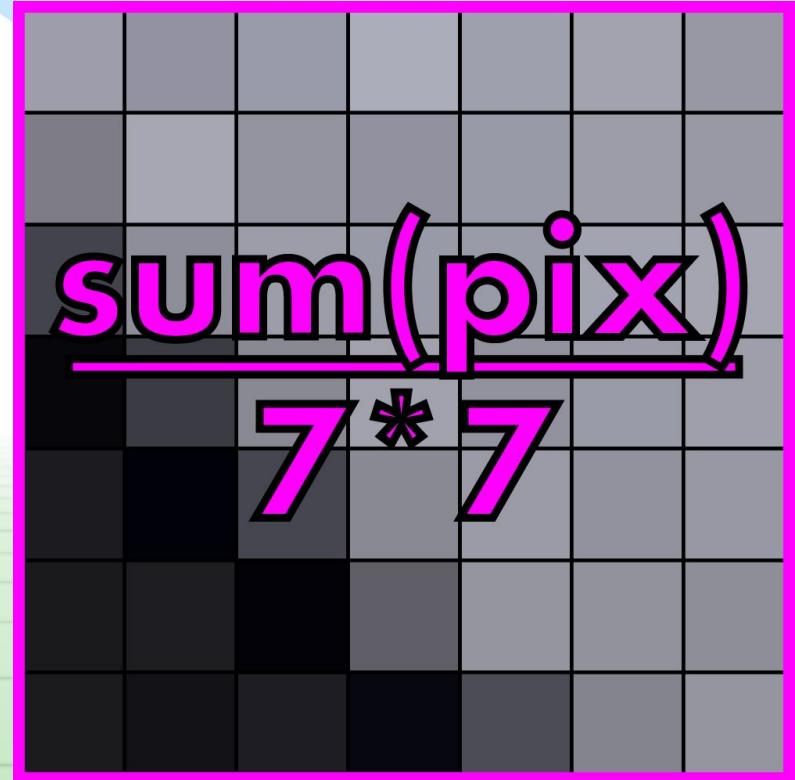
averaging



What is averaging?



What is averaging? A weighted sum



What is averaging? A weighted sum

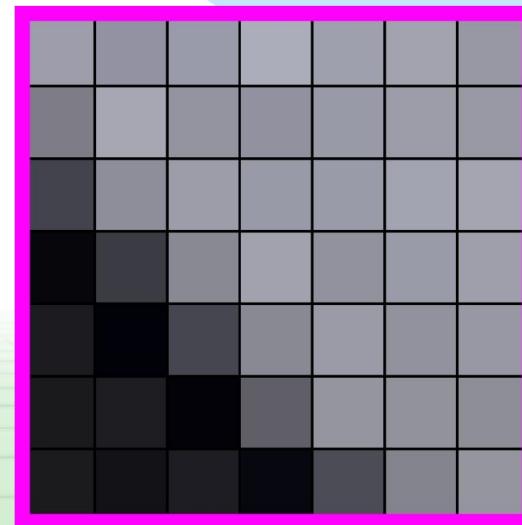
sum [$\frac{1}{49}$]

Call this operation “convolution”

Filter or kernel

$\frac{1}{49}$

$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							



Convolutions on larger images

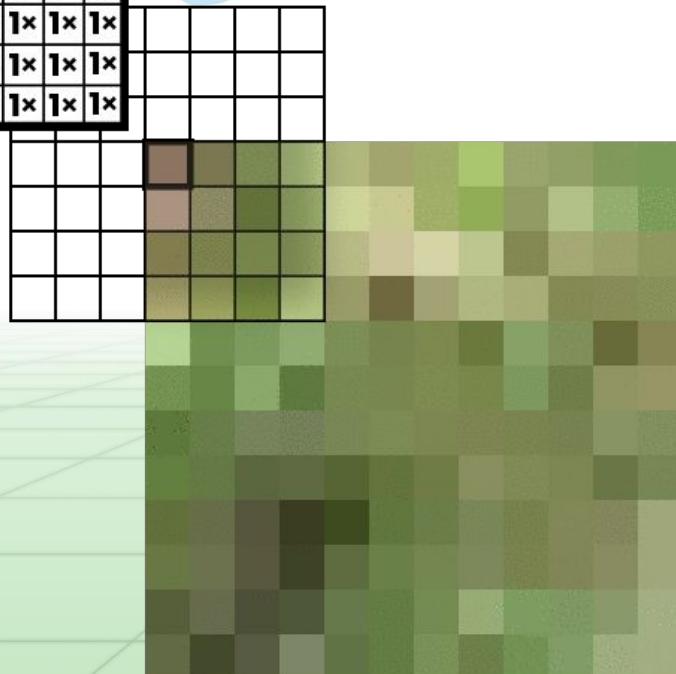
$\frac{1}{49}$

$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							
$1 \times$							



Kernel slides across image

1
49

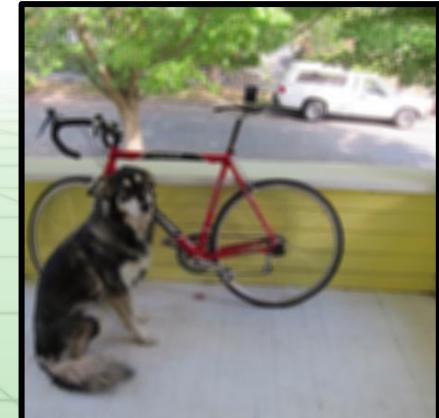
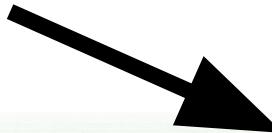


A 10x10 grid of squares. The first square in the top-left corner is filled with a light blue color. To the left of the grid, there is a vertical strip of green color.

Convolutions on larger images

$\frac{1}{49}$

1x							
1x							
1x							
1x							
1x							
1x							
1x							
1x							



This is called box filter

$\frac{1}{49}$

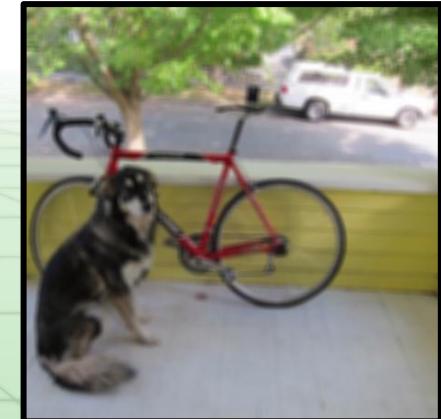
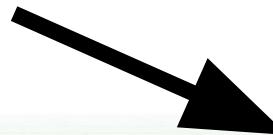
1x							
1x							
1x							
1x							
1x							
1x							
1x							
1x							



Box filters

$\frac{1}{N \times M}$

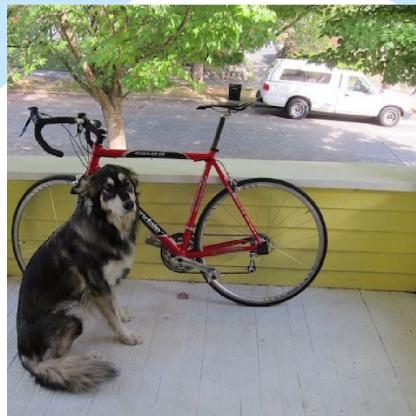
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
			...		M	
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x



Box filters smooth image

$\frac{1}{49}$

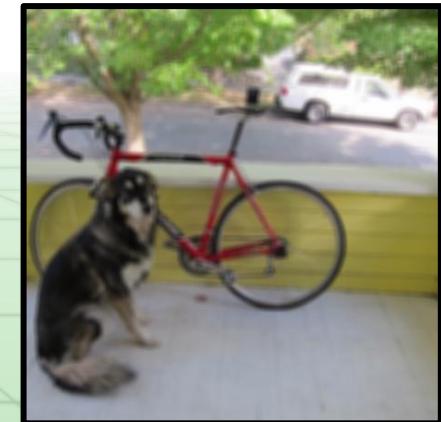
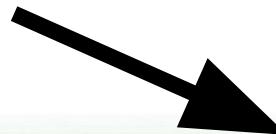
1x						
1x						
1x						
1x						
1x						
1x						
1x						



Box filters

$\frac{1}{N \times M}$

1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
			...		M	
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x



Box filters smooth image

$\frac{1}{49}$

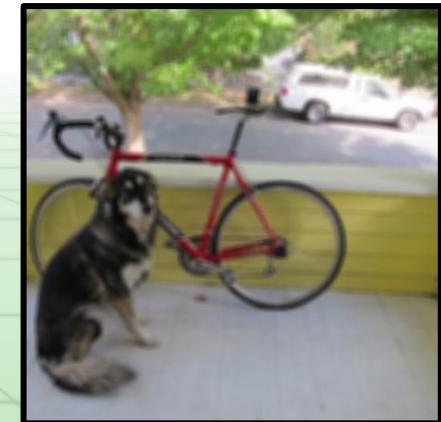
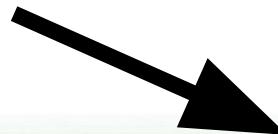
1x						
1x						
1x						
1x						
1x						
1x						
1x						



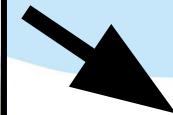
Box filters

$\frac{1}{N \times M}$

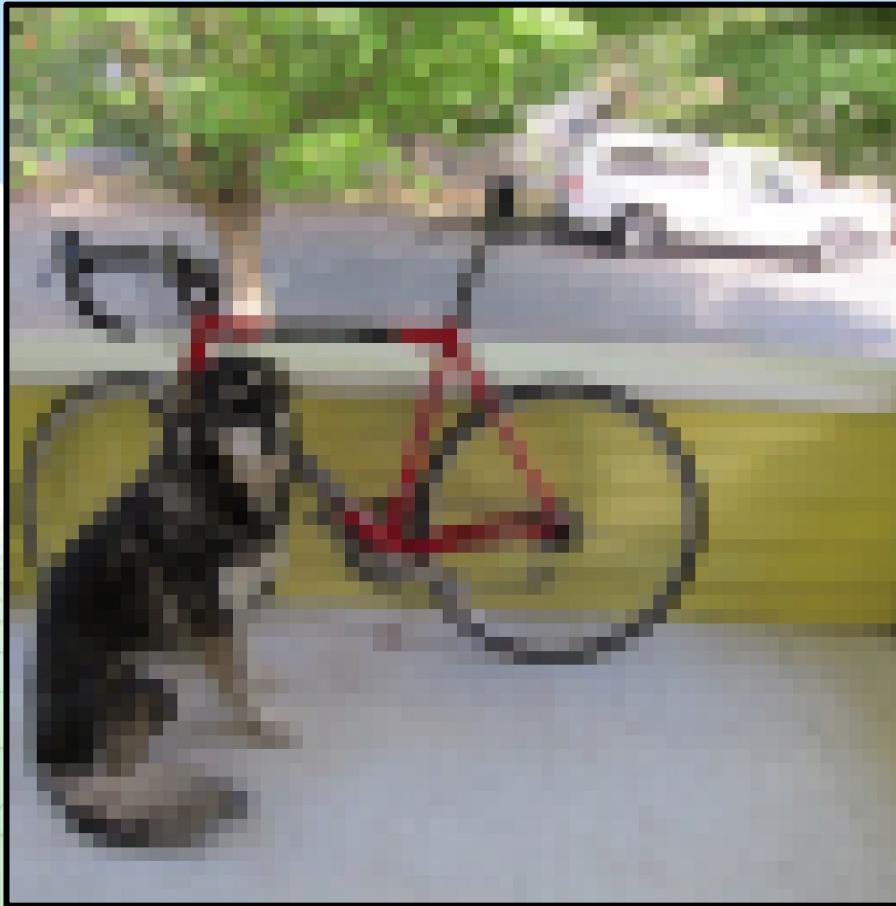
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x
			...		M	
1x	1x	1x	1x	1x		1x
1x	1x	1x	1x	1x		1x



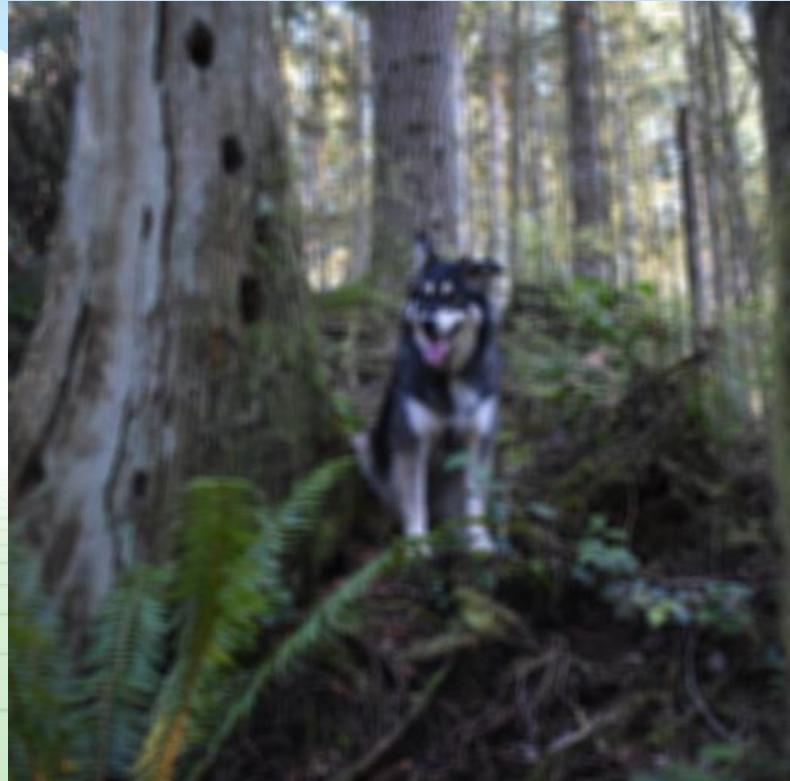
Now we resize our smoothed image



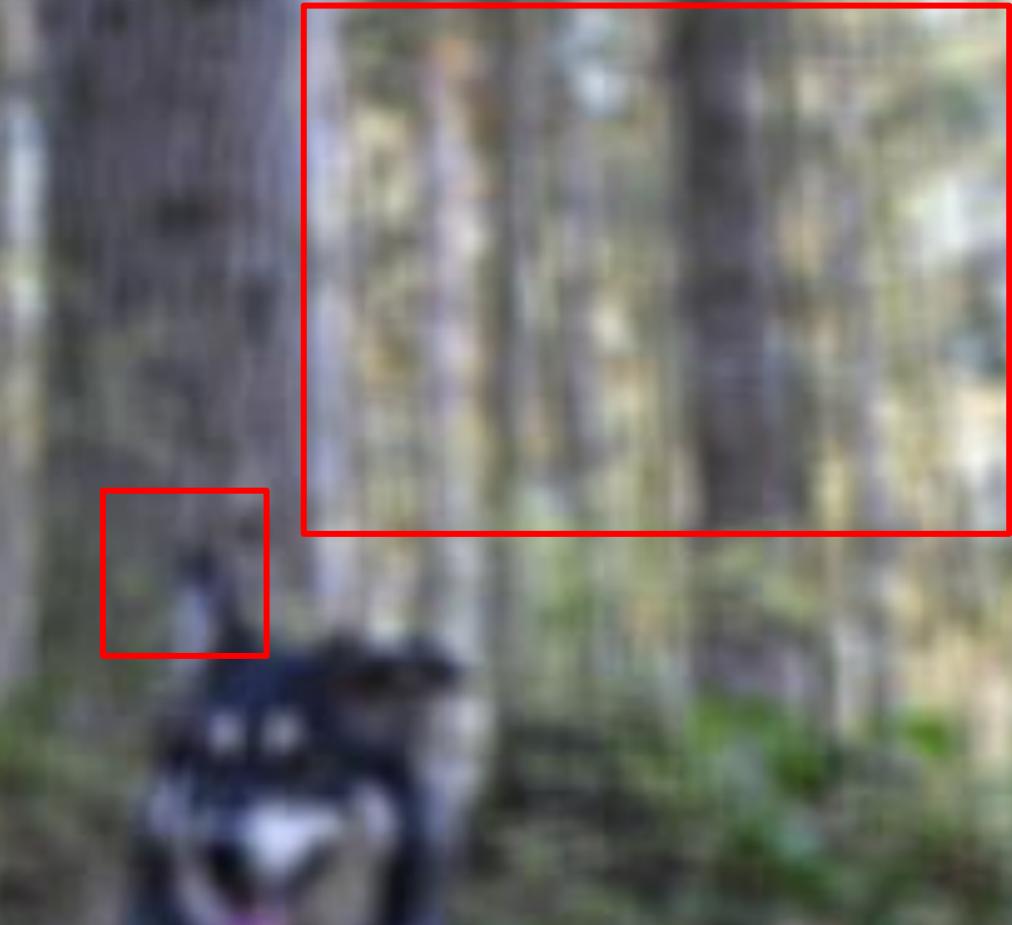
So much better!



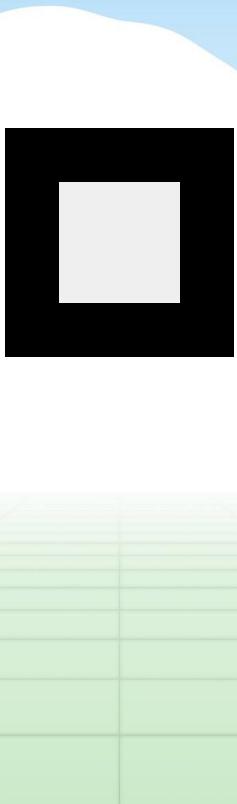
Box filters have artifacts



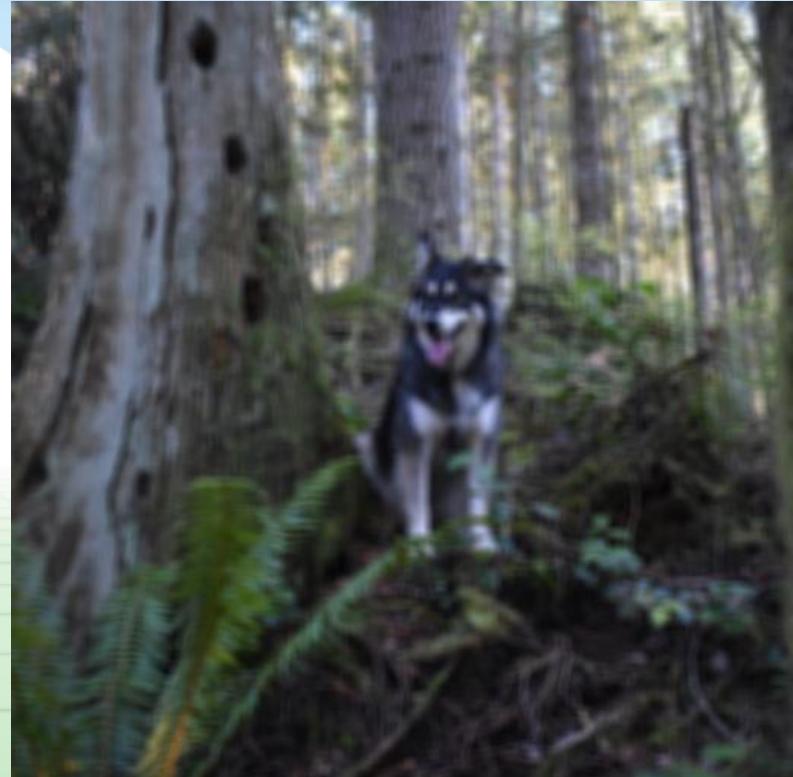
Box filters have artifacts



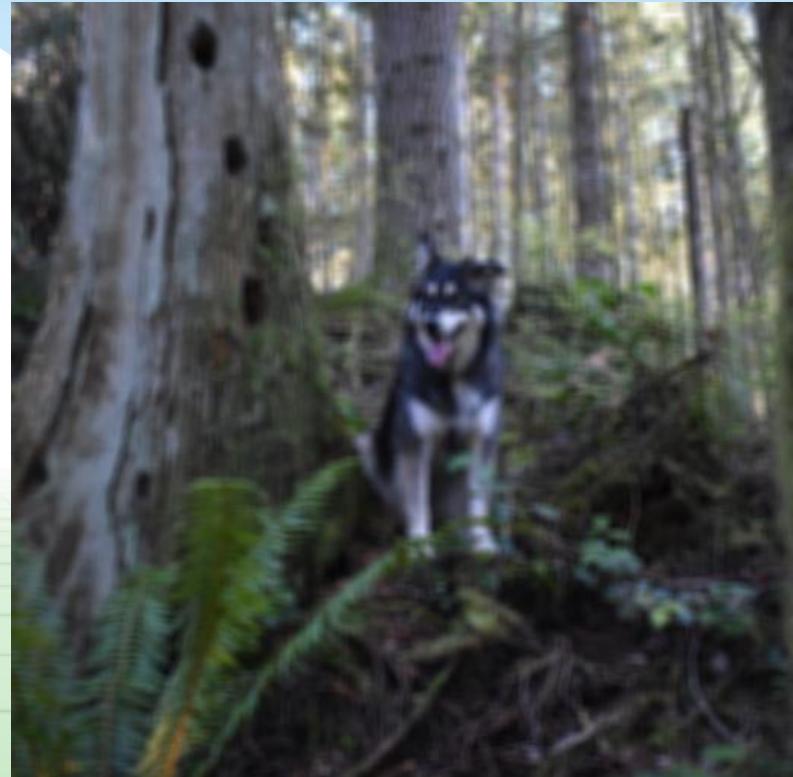
Box filters: vertical + horizontal streaking



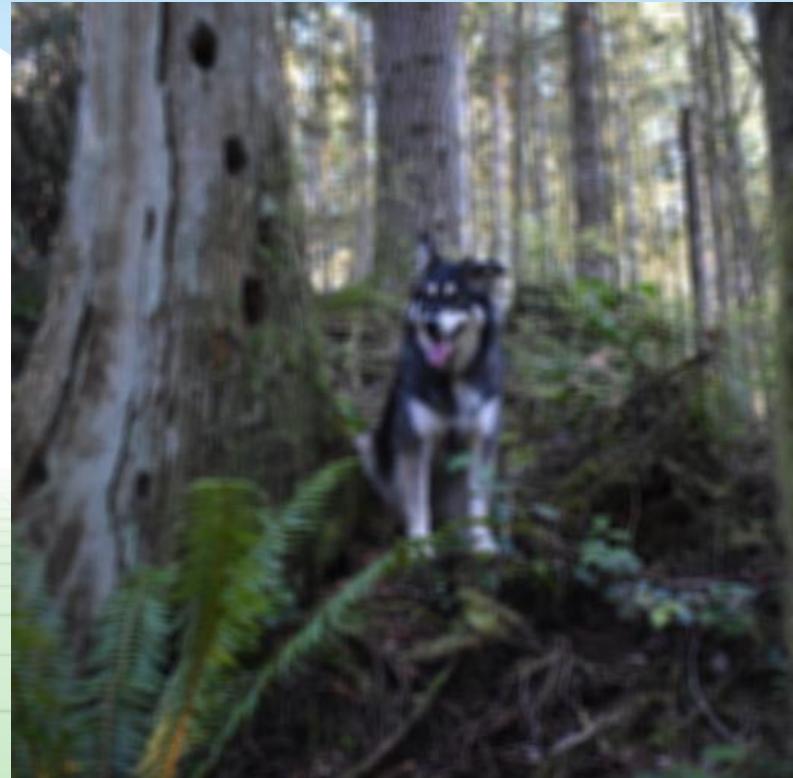
Box filters: vertical + horizontal streaking



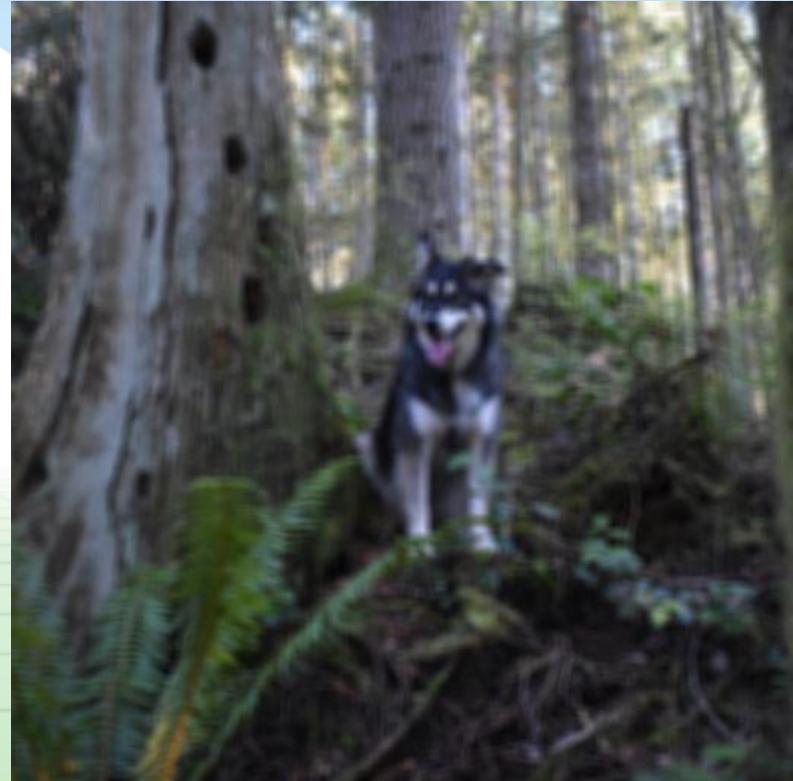
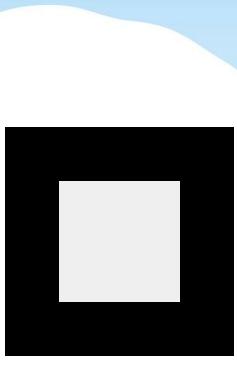
Box filters: vertical + horizontal streaking



Box filters: vertical + horizontal streaking

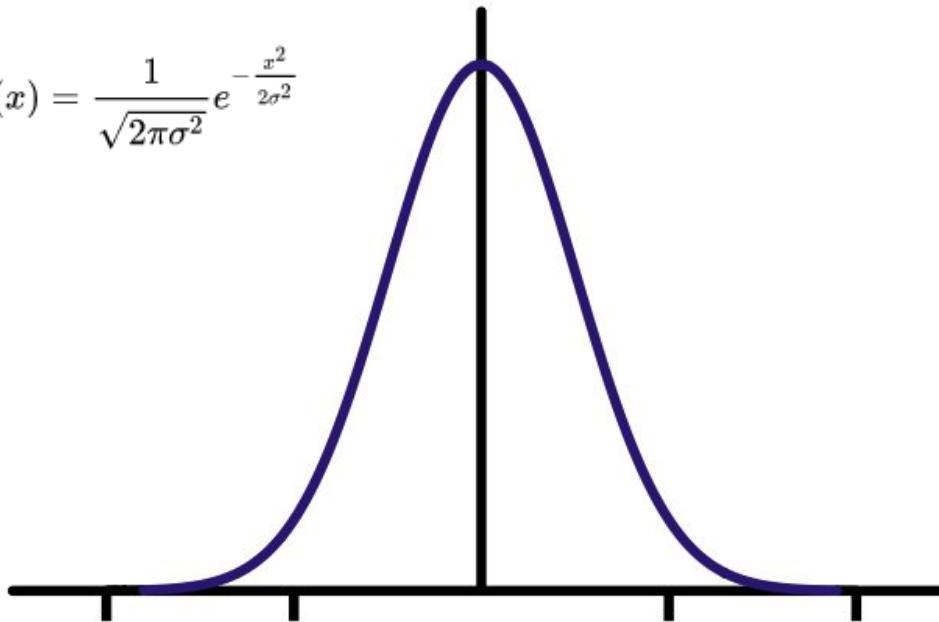


We want a smoothly weighted kernel



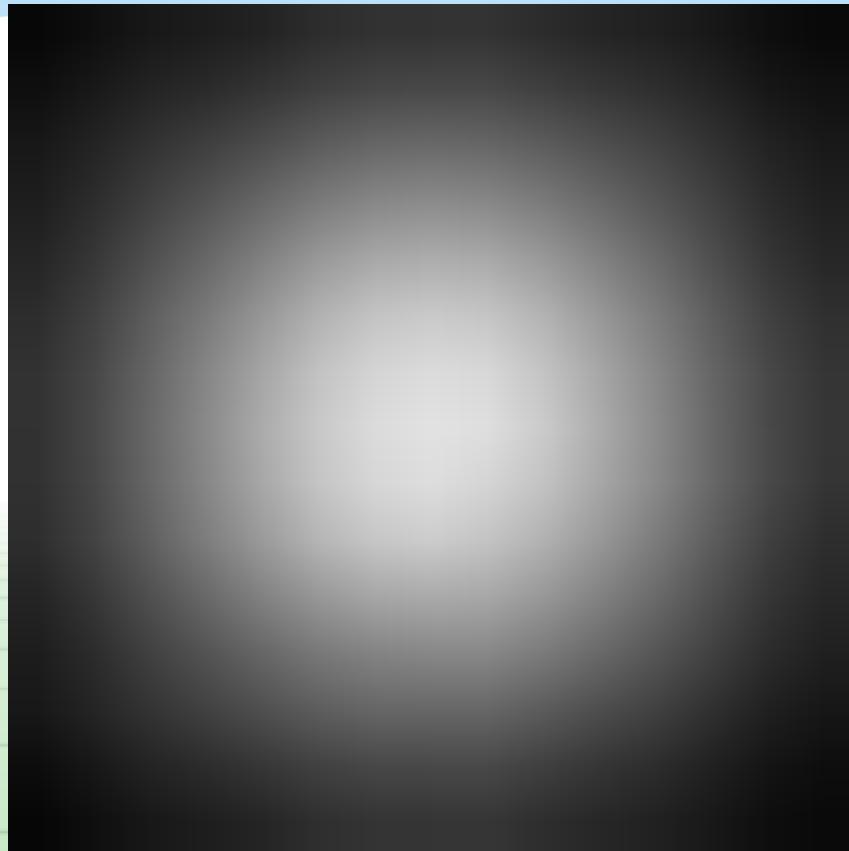
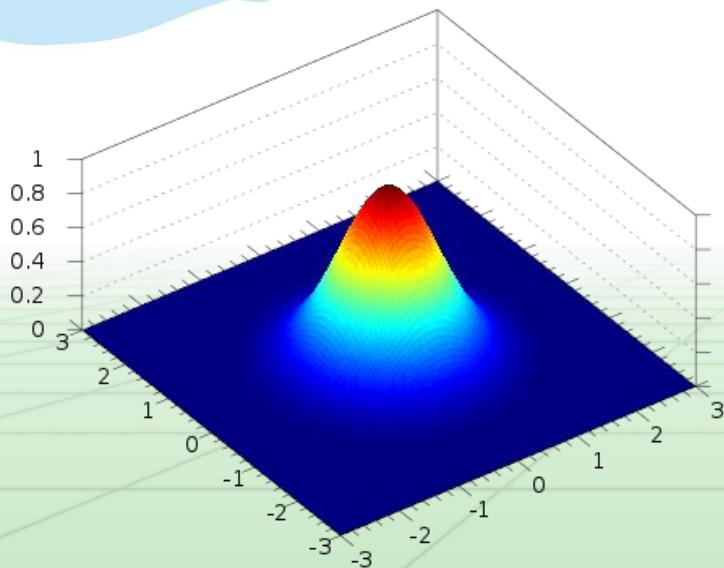
Gaussians

$$G(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{x^2}{2\sigma^2}}$$

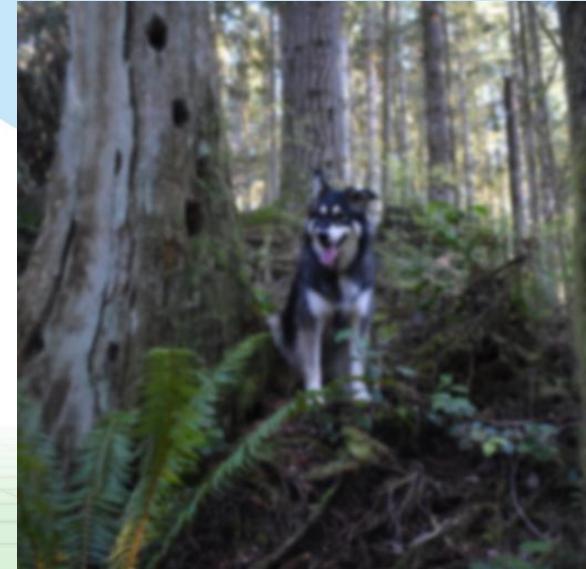


2d Gaussian

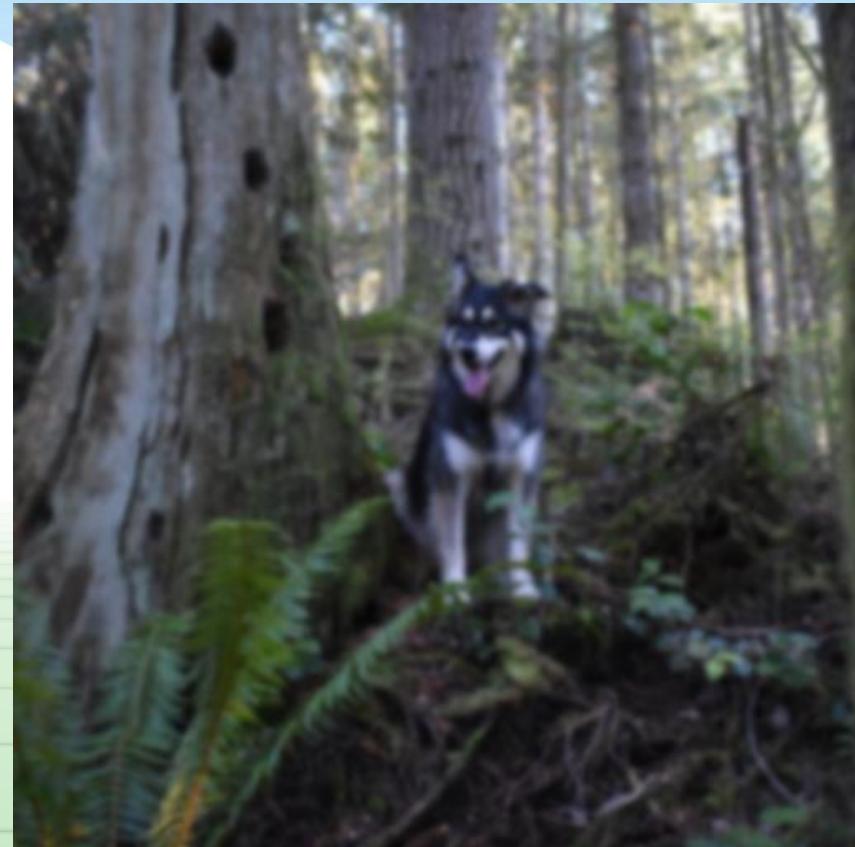
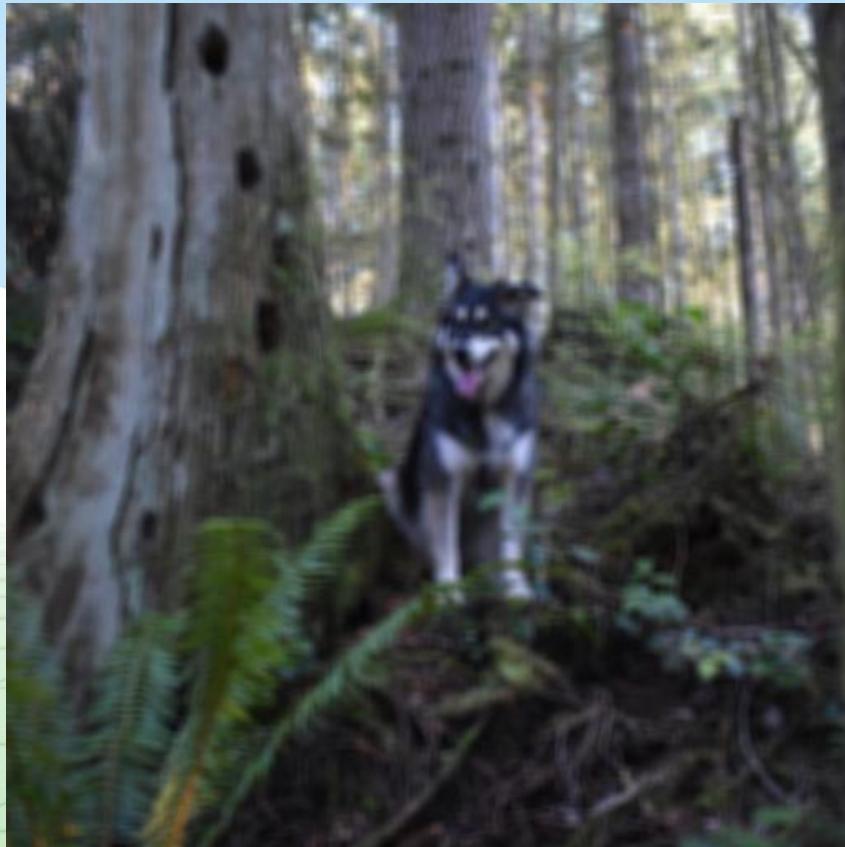
$$g(x, y) = \frac{1}{2\pi\sigma^2} \cdot e^{-\frac{x^2+y^2}{2\sigma^2}}$$



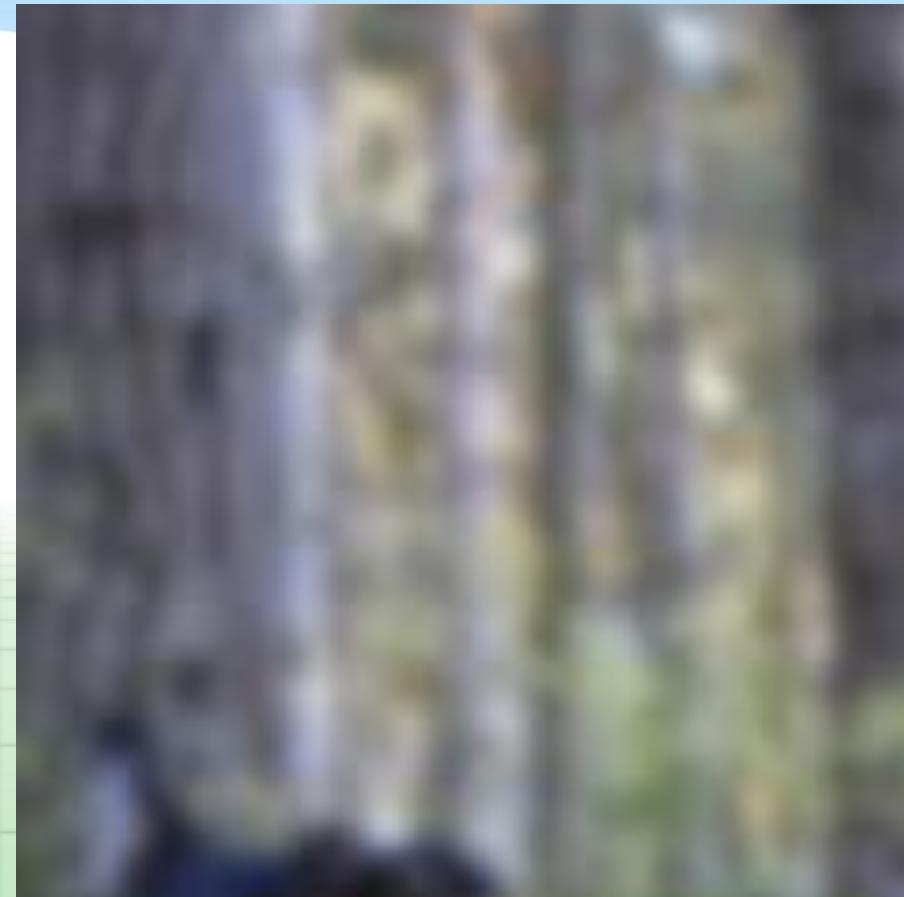
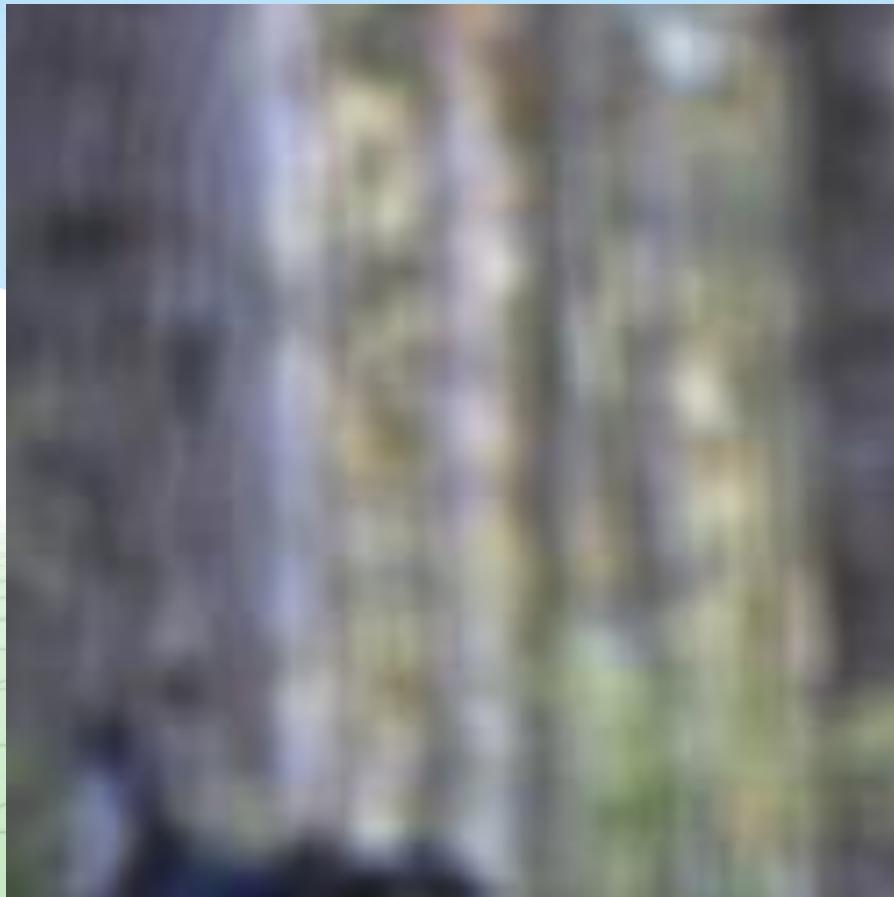
Better smoothing with Gaussians

 $*$  $=$ 

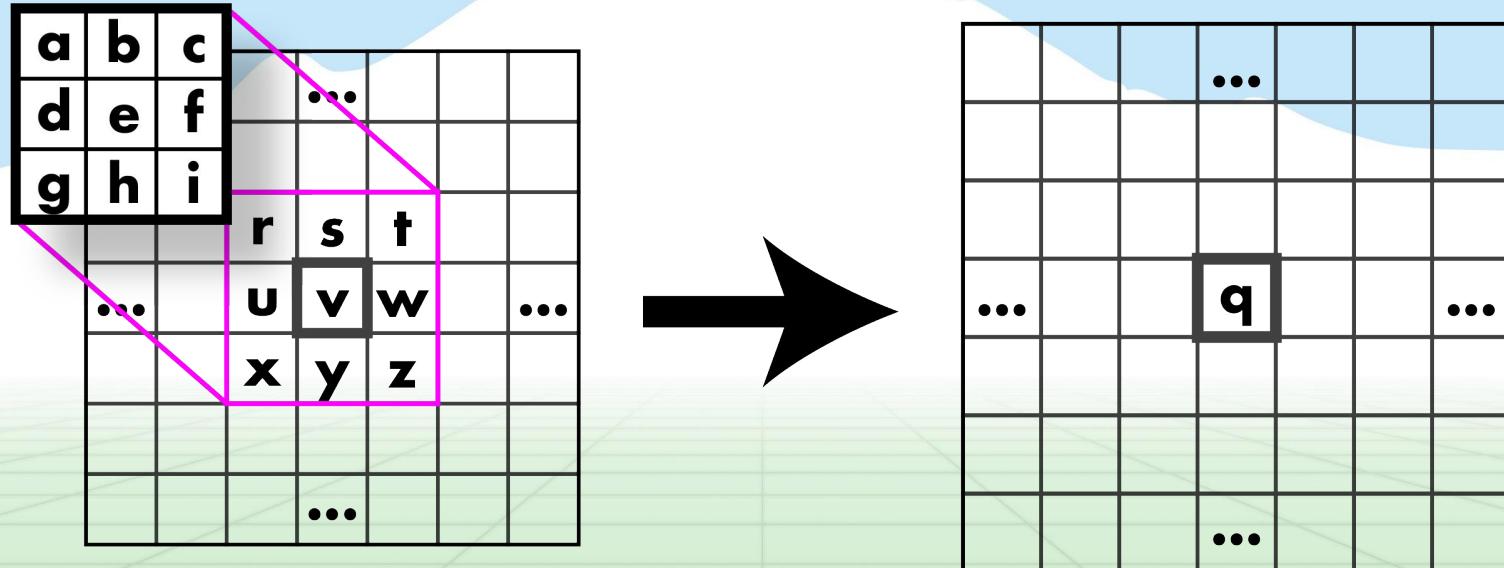
Better smoothing with Gaussians



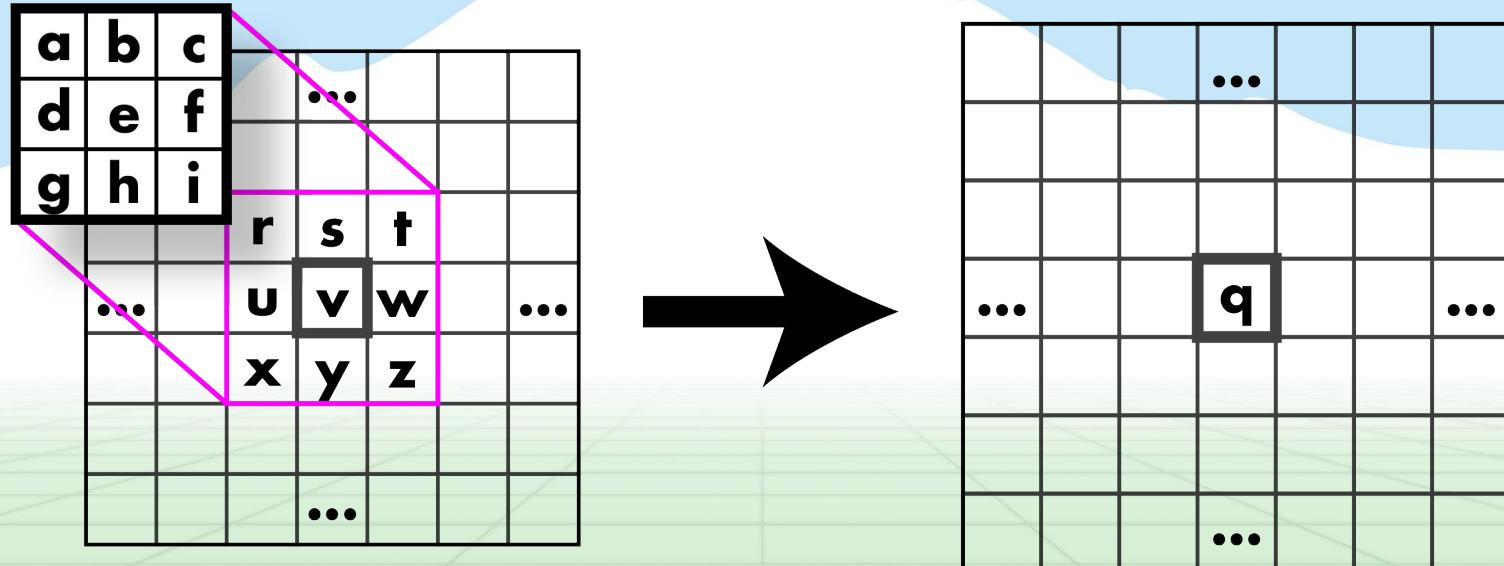
Better smoothing with Gaussians



Wow, so what was that convolution thing??



Wow, so what was that convolution thing??

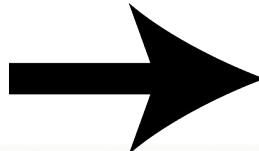


$$q = a \times r + b \times s + c \times t + d \times u + e \times v + f \times w + g \times x + h \times y + i \times z$$

Calculate it, go!

2	-1	-1
-1	2	-1
-1	-1	2

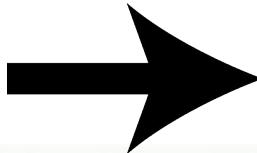
			...			
			45	51	57	
			46	46	67	...
			26	19	64	...



			...			
			q			
			...			
			...			

Calculate it, go!

-1	-1	-1						
-1	8	-1						
-1	-1	-1						
			...					
			16	105	153			
			15	104	113			...
			18	111	136			
			...					



			...					
			q					
			...					
			...					

Guess that kernel!

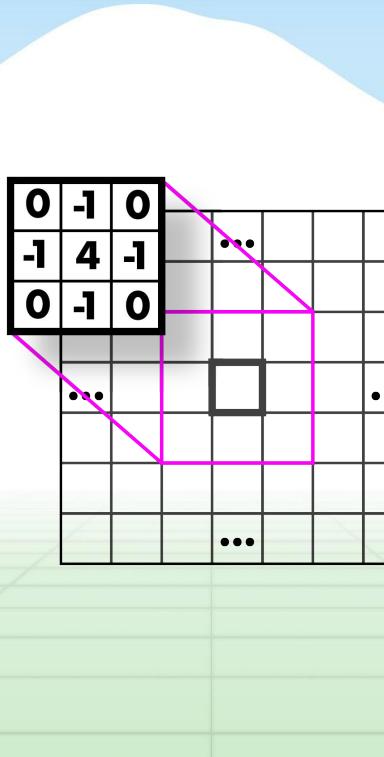


0	-1	0
-1	4	-1
0	-1	0

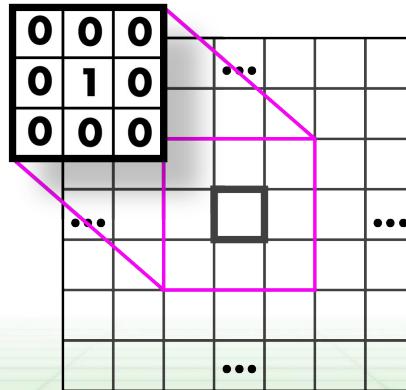
A 3x3 matrix with values 0, -1, and 4. A pink line starts from the top-left cell (0) and follows a path through the grid, ending at the center cell (4). Ellipses indicate the matrix continues beyond the visible 3x3 area.

...
...
...
...
...
...

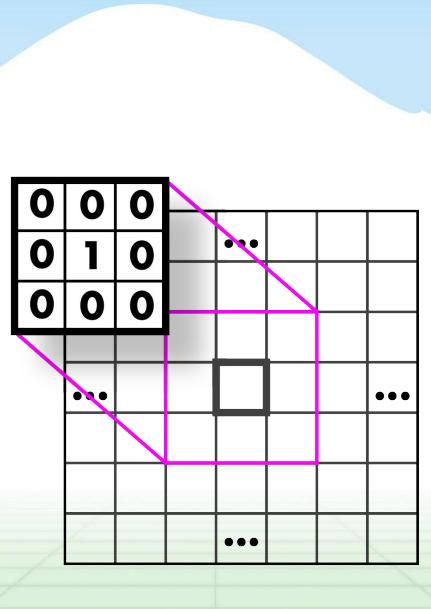
Highpass Kernel: finds edges



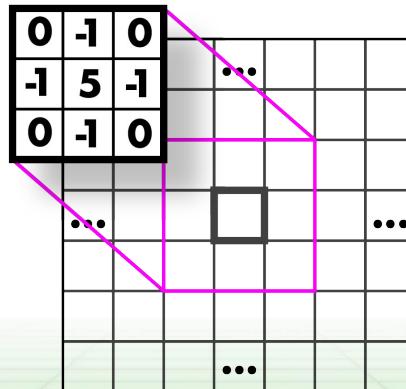
Guess that kernel!



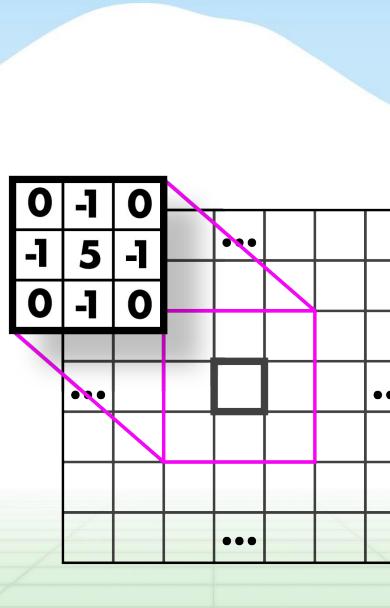
Identity Kernel: Does nothing!



Guess that kernel!

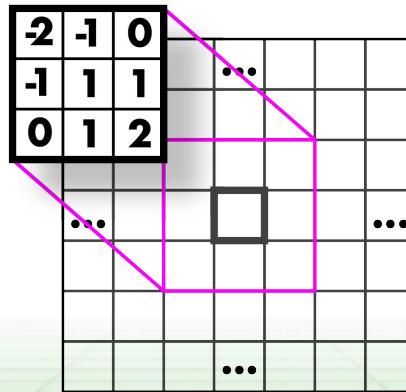


Sharpen Kernel: sharpens!

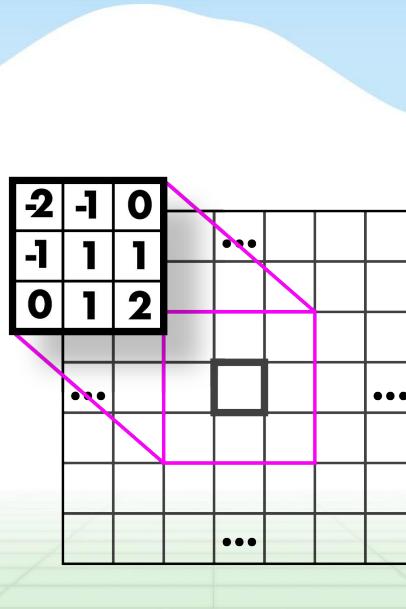


Note: sharpen = highpass + identity!

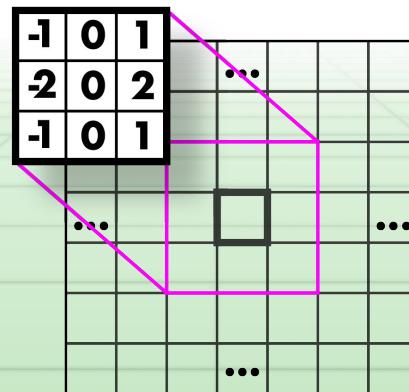
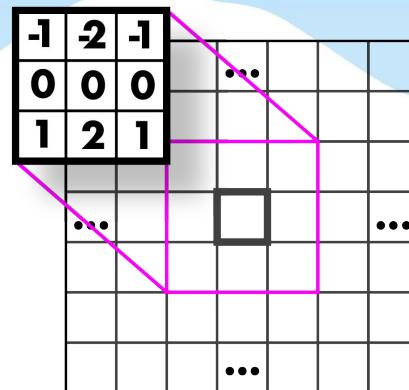
Guess that kernel!



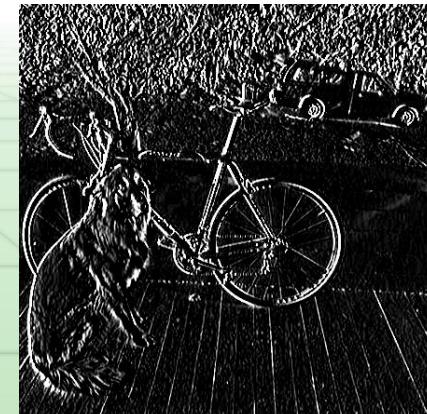
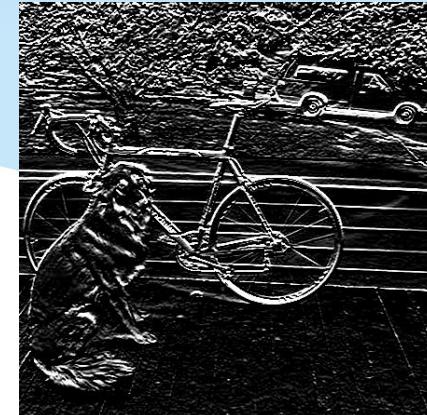
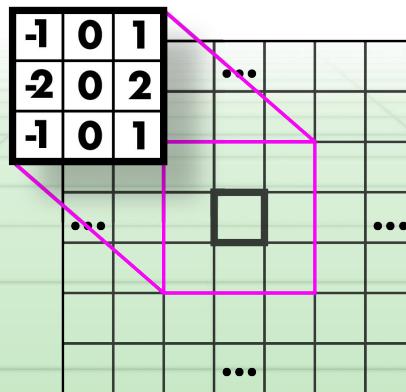
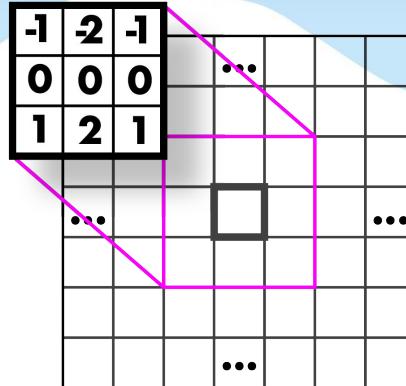
Emboss Kernel: stylin'



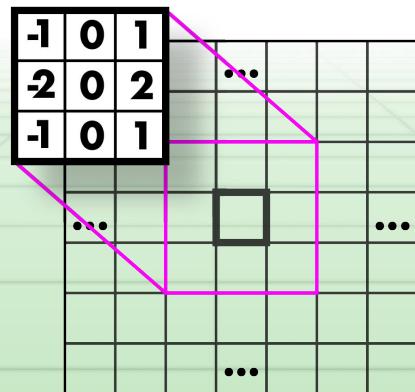
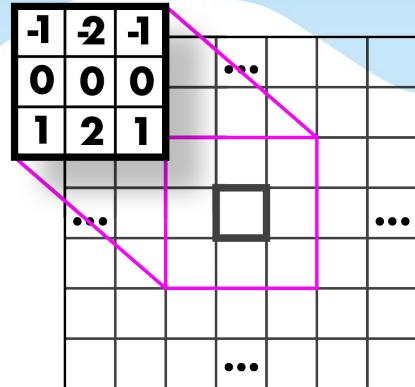
Guess those kernels!



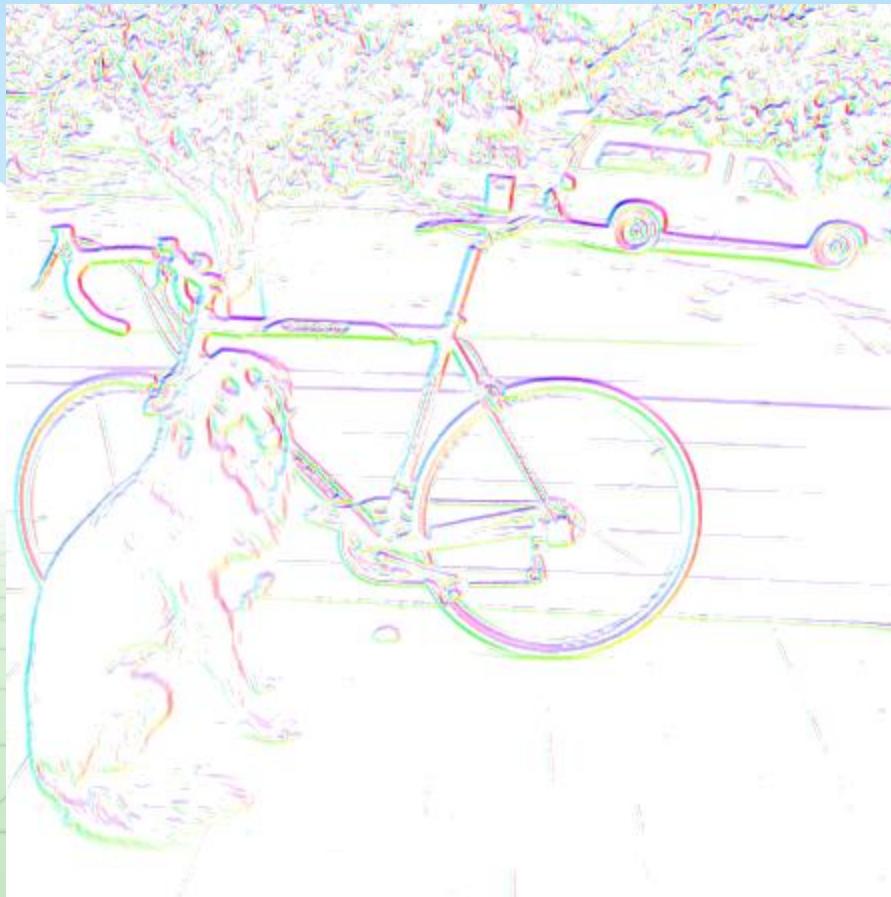
Sobel Kernels: edges and...



Sobel Kernels: edges and gradient!



Sobel Kernels: edges and gradient!



And so much more!!

