

# report 9

Khaled Hasan

2024-05-19

## Data

```
GLOBALTEMPERATURE = read.csv(file = "C:\\Users/ss/Desktop/Time_series_Analysis/MyGlobalTemperetures.csv")
global_temp = ts(GLOBALTEMPERATURE[,1], start = c(1850, 1), frequency = 12)
northernhemisphere_temp = ts(GLOBALTEMPERATURE[,2], start = c(1850, 1), frequency = 12)
southernhemisphere_temp = ts(GLOBALTEMPERATURE[,3], start = c(1850, 1), frequency = 12)
LattitudinalTemps = read.csv(file = "C:\\Users/ss/Desktop/Time_series_Analysis/LatittudCuttedTemperetur.csv")
north = ts(LattitudinalTemps[, 2], start = c(1850, 1), frequency = 12)
tropical = ts(LattitudinalTemps[, 3], start = c(1850, 1), frequency = 12)
south = ts(LattitudinalTemps[, 4], , start = c(1850, 1), frequency = 12)
south_noPole = ts(LattitudinalTemps[, 5], start = c(1850, 1), frequency = 12)
```

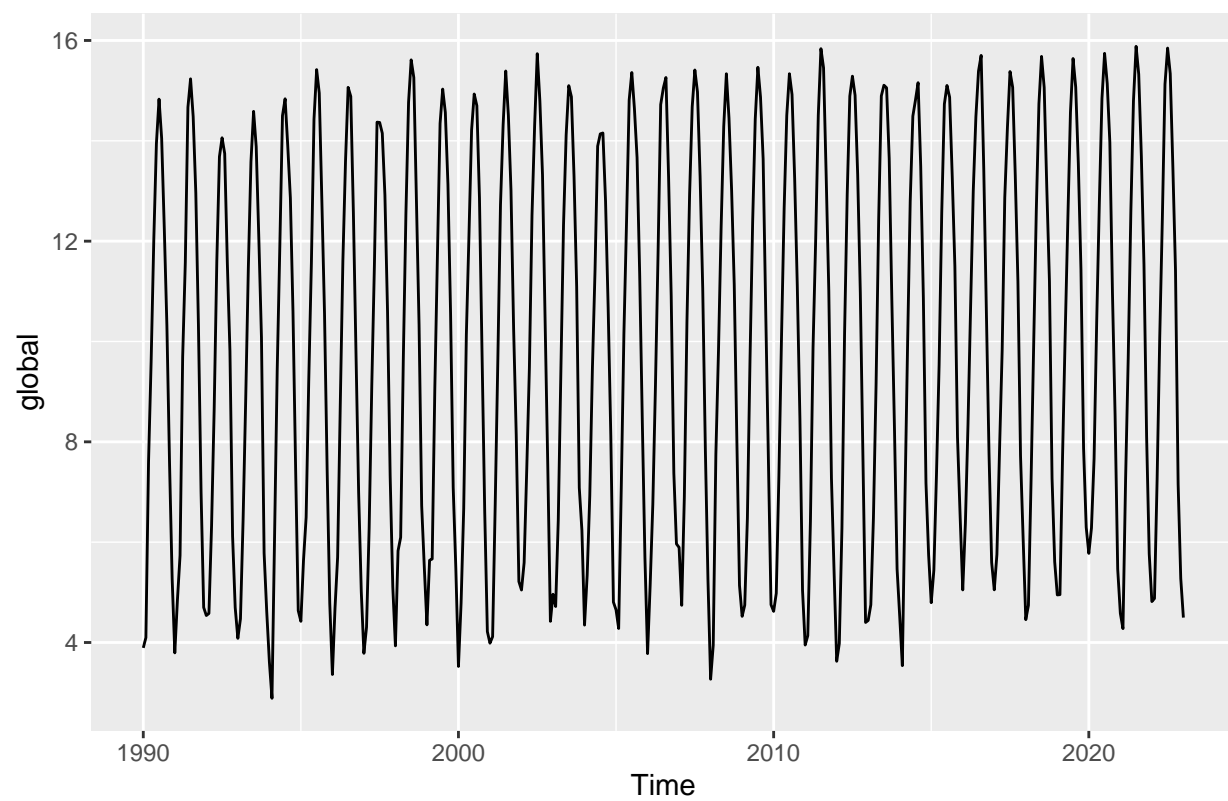
## plots

```
library(ggplot2)
library(gridExtra)
```

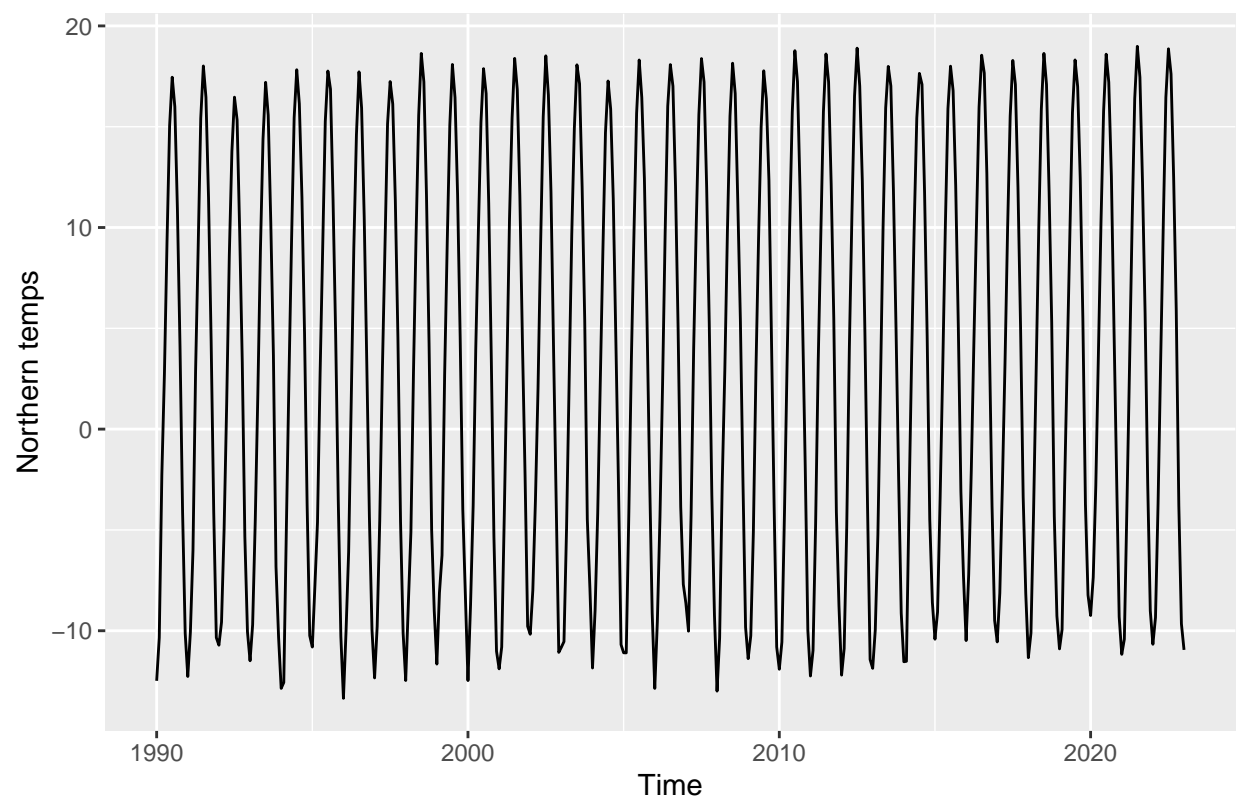
```
## Warning: package 'gridExtra' was built under R version 4.3.3
```

```
autoplot1 <- autoplot(window(global_temp, start = c(1990, 1), freq = 12), ylab = "global")
autoplot2 <- autoplot(window(north, start = c(1990, 1), freq = 12), ylab = "Northern temps")
autoplot3 <- autoplot(window(south, start = c(1990, 1), freq = 12), ylab = "southern temps")
autoplot4 <- autoplot(window(tropical, start = c(1990, 1), freq = 12), ylab = "tropical temps")
autoplot5 <- autoplot(window(south_noPole, start = c(1990, 1), freq = 12), ylab = "southern ex. Pole tem")

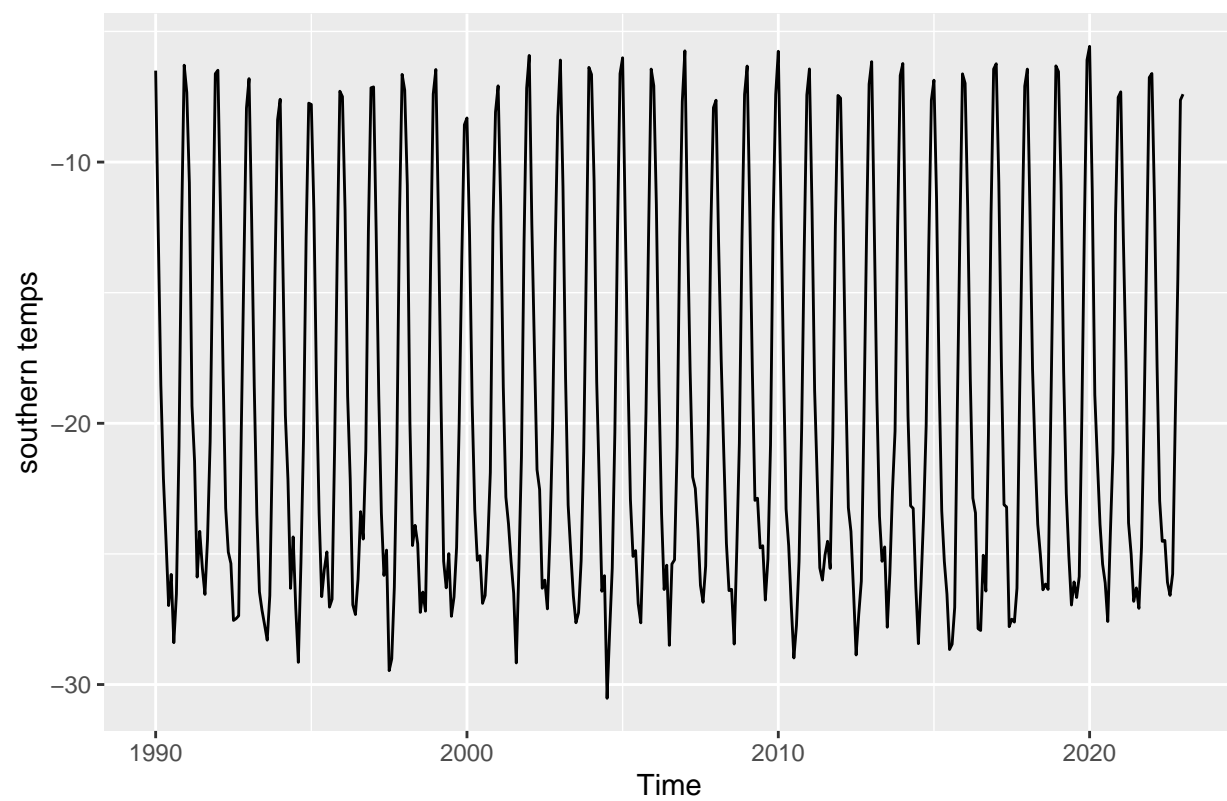
par(mfrow = c(1, 5))
plot(autoplot1)
```



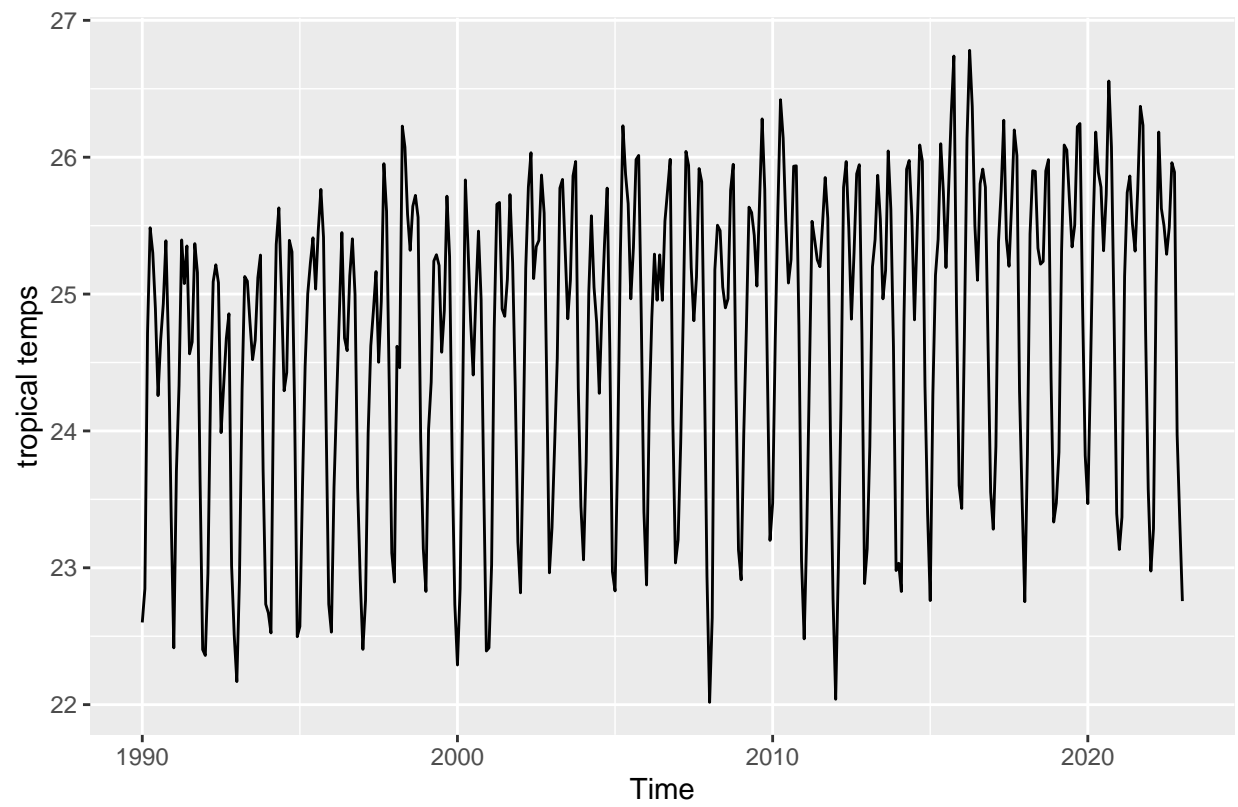
```
plot(autoplot2)
```



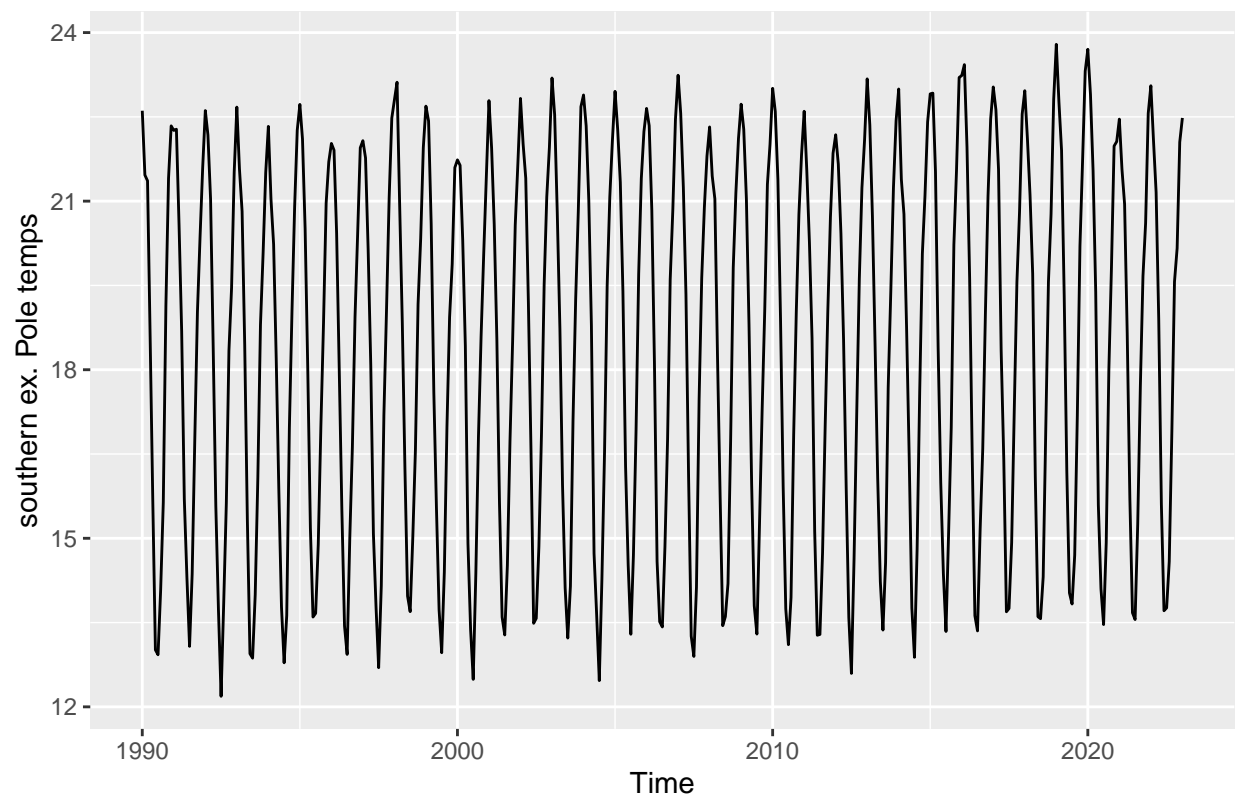
```
plot(autoplot3)
```



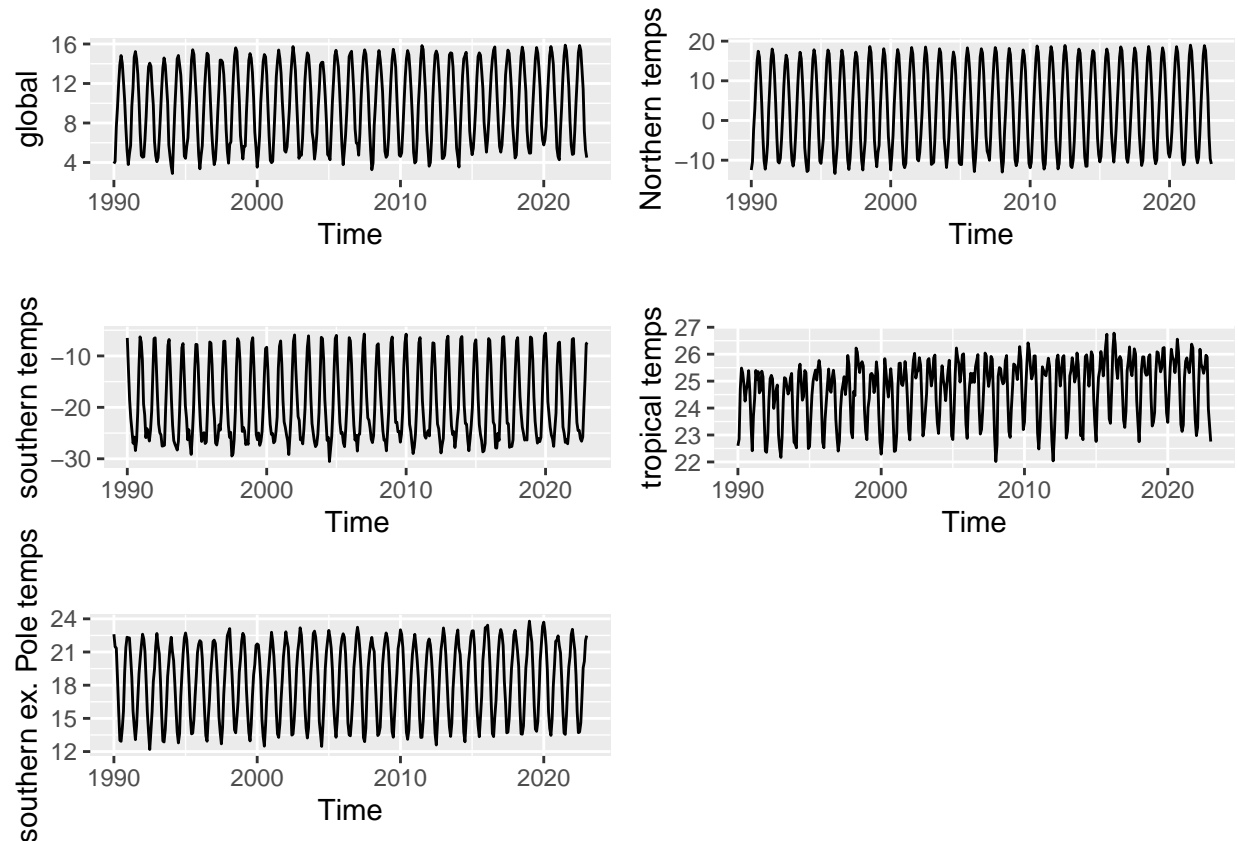
```
plot(autoplot4)
```



```
plot(autoplot5)
```



```
layout(matrix(c(1, 2, 3, 4, 5), nrow = 1))  
grid.arrange(autoplot1, autoplot2, autoplot3, autoplot4, autoplot5)
```



There are few interesting points about the above data. First, we notice that excluding north-pole did not seem to shift the time phase, but it significantly shifted the data upwards, we also notice that the tropical data seems to agree with the northern phase, suggesting that the region between latitudes  $-30^\circ$  and  $30^\circ$  has more mass in the northern hemisphere, but what is rather more interesting, is the seasonal patterns that defies the usual sinusoidal pattern, this behavior is to be studied.

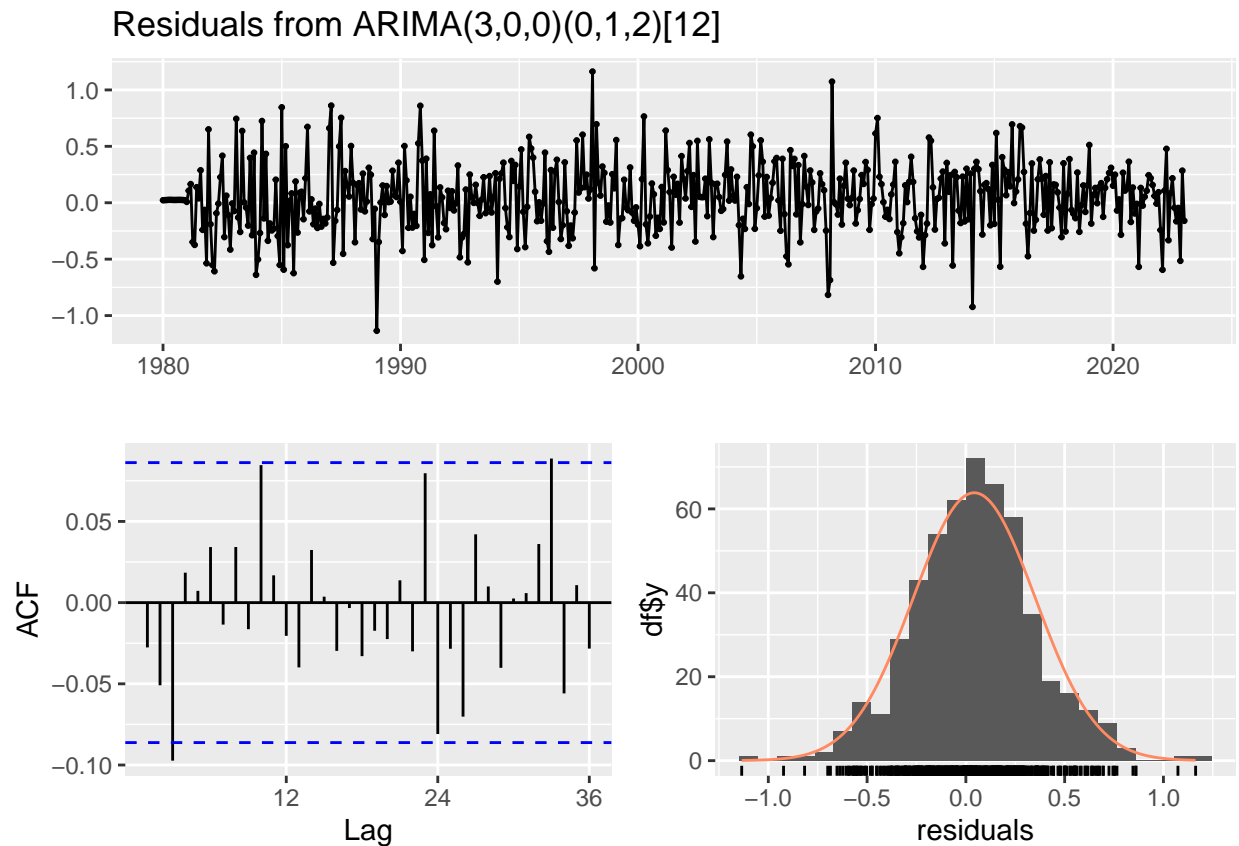
## Arima Fitting

```
tropical_autoArima_fit = auto.arima(window(tropical, start=c(1980, 1), freq=12), approximation = FALSE,
summary(tropical_autoArima_fit)
```

```
## Series: window(tropical, start = c(1980, 1), freq = 12)
## ARIMA(3,0,0)(0,1,2)[12]
##
## Coefficients:
##          ar1      ar2      ar3      sma1      sma2
##          0.4125  0.2153  0.0855 -0.9328  0.0507
## s.e.      0.0456  0.0478  0.0462   0.0498  0.0475
##
## sigma^2 = 0.1006: log likelihood = -143.67
## AIC=299.34   AICc=299.51   BIC=324.69
##
## Training set error measures:
```

```
##                      ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.04242536 0.3119142 0.2412032 0.1557792 0.9874523 0.6378395
##                      ACF1
## Training set -0.02759831
```

```
checkresiduals(tropical_autoArima_fit)
```



```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(3,0,0)(0,1,2)[12]
## Q* = 23.042, df = 19, p-value = 0.2355
##
## Model df: 5. Total lags used: 24
```

doing the same with different latitudinal cuts:

```
global_autoArima_fit = auto.arima(window(global_temp, start=c(1980, 1), freq=12), approximation = FALSE, season
north_autoArima_fit = auto.arima(window(north, start=c(1980, 1), freq=12), approximation = FALSE, season
south_autoArima_fit = auto.arima(window(south, start=c(1980, 1), freq=12), approximation = FALSE, season
south_np_autoArima_fit = auto.arima(window(south_noPole, start=c(1980, 1), freq=12), approximation = FALSE, season
```

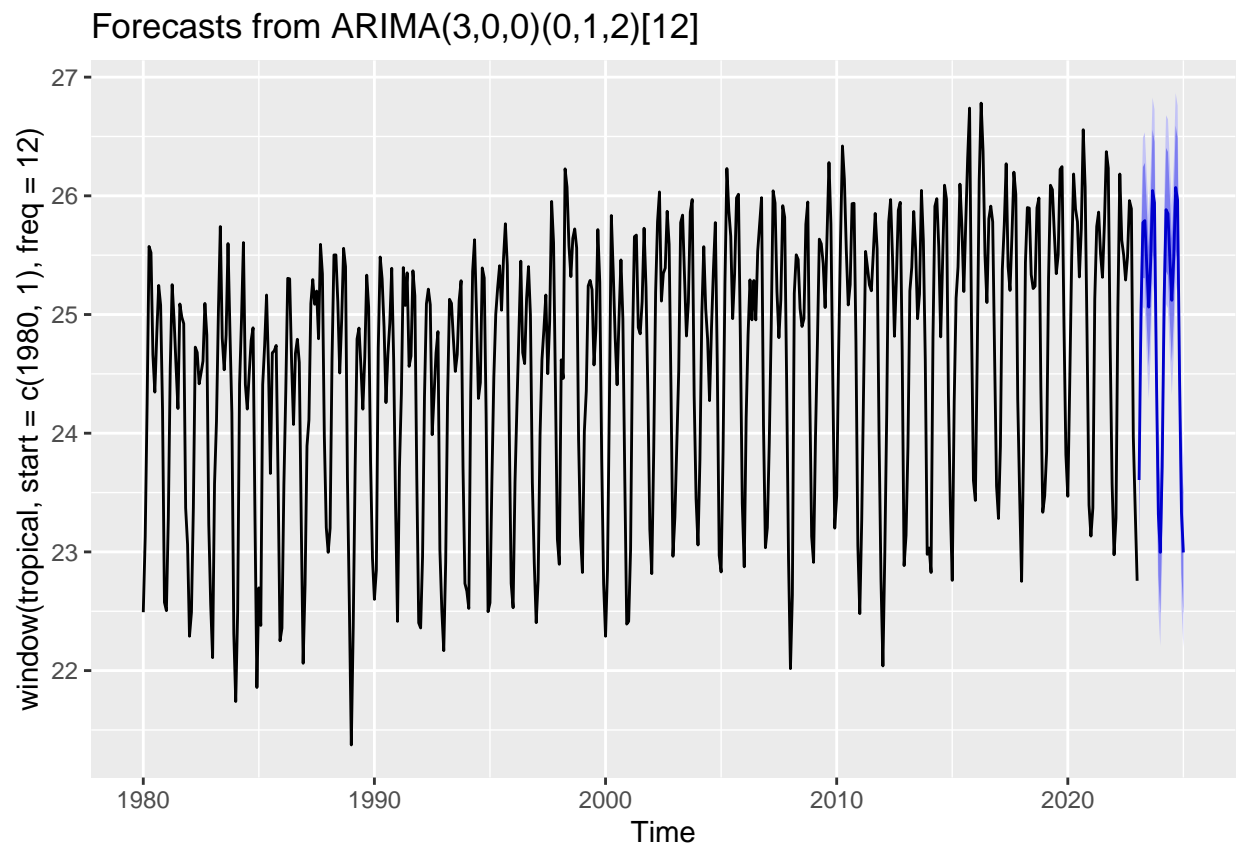


```
northernhemisphereArimaFit = auto.arima(window(northernhemisphere_temp, start=c(1980, 1), freq=12), app
southernhemisphereArimaFit = auto.arima(window(southernhemisphere_temp, start=c(1980, 1), freq=12), app
```

```
{
  print(global_autoArima_fit$arima)
  print(north_autoArima_fit$arima)
  print(south_autoArima_fit$arima)
  print(south_np_autoArima_fit$arima)
  print(northernhemisphereArimaFit$arima)
  print(southernhemisphereArimaFit$arima)
}
```

```
## [1] 1 1 1 1 12 0 1
## [1] 2 0 1 1 12 0 1
## [1] 1 0 2 0 12 0 1
## [1] 3 0 0 1 12 0 1
## [1] 1 1 0 2 12 0 1
## [1] 2 0 0 1 12 0 1
```

```
tropical_autoArima_fit %>% forecast(h = 24) %>% autoplot()
```



```
{
  print(global_autoArima_fit$aicc)
}
```

```

print(north_autoArima_fit$aicc)
print(tropical_autoArima_fit$aicc)
print(south_autoArima_fit$aicc)
print(south_np_autoArima_fit$aicc)
print(northernhemisphereArimaFit$aicc)
print(southernhemisphereArimaFit$aicc)
}

```

```

## [1] 698.1978
## [1] 1158.212
## [1] 299.5073
## [1] 1560.526
## [1] 524.4886
## [1] 835.0459
## [1] 830.8596

```

```

Arima_fittng <- function(timeseries, startingPoint = start(timeseries), endingPoint = end(timeseries)){
  cutted_data = window(timeseries, start = startingPoint, end = endingPoint, freq = 12)
  t = seq_along(cutted_data)
  regressors = cbind(sin(pi/6*t), cos(pi/6*t), t)
  arima_fit = auto.arima(cutted_data, xreg = regressors, approximation = FALSE, stepwise = FALSE, season
  return(arima_fit)
}

```

```

global_fitting_Arimareg = Arima_fittng(global_temp, startingPoint = c(1980, 1))

```

```

north_reg = Arima_fittng(north, startingPoint = c(1980, 1))

```

```

tropical_reg = Arima_fittng(tropical, startingPoint = c(1980, 1))

```

```

south_reg = Arima_fittng(south, startingPoint = c(1980, 1))

```

```

south_np_reg = Arima_fittng(south_noPole, startingPoint = c(1980, 1))

```

```

summary(north_reg)

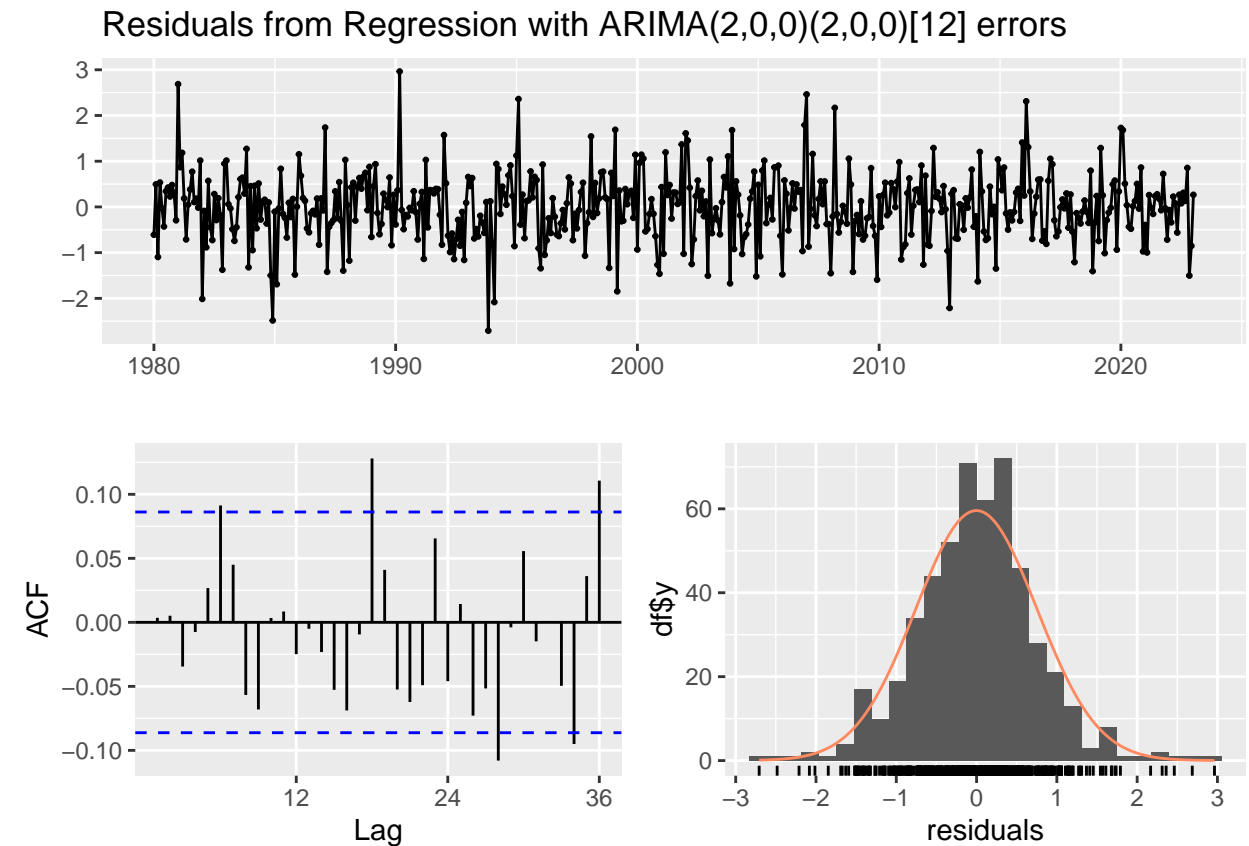
```

```

## Series: cutted_data
## Regression with ARIMA(2,0,0)(2,0,0)[12] errors
##
## Coefficients:
##          ar1      ar2      sar1      sar2  intercept              t
##          0.2510  0.1117  0.0788  0.2104         2.3072 -8.0905 -12.4163  0.0034
## s.e.    0.0438  0.0451  0.0431  0.0447         0.1407  0.0855  0.0854  0.0005
##
## sigma^2 = 0.5779:  log likelihood = -588.48
## AIC=1194.95   AICc=1195.31   BIC=1233.19
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.0023746 0.7543063 0.571757 -0.4562573 9.325695 0.7164933
##              ACF1
## Training set 0.003511724

```

```
checkresiduals(north_reg)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from Regression with ARIMA(2,0,0)(2,0,0)[12] errors
## Q* = 33.454, df = 20, p-value = 0.03007
##
## Model df: 4.    Total lags used: 24
```

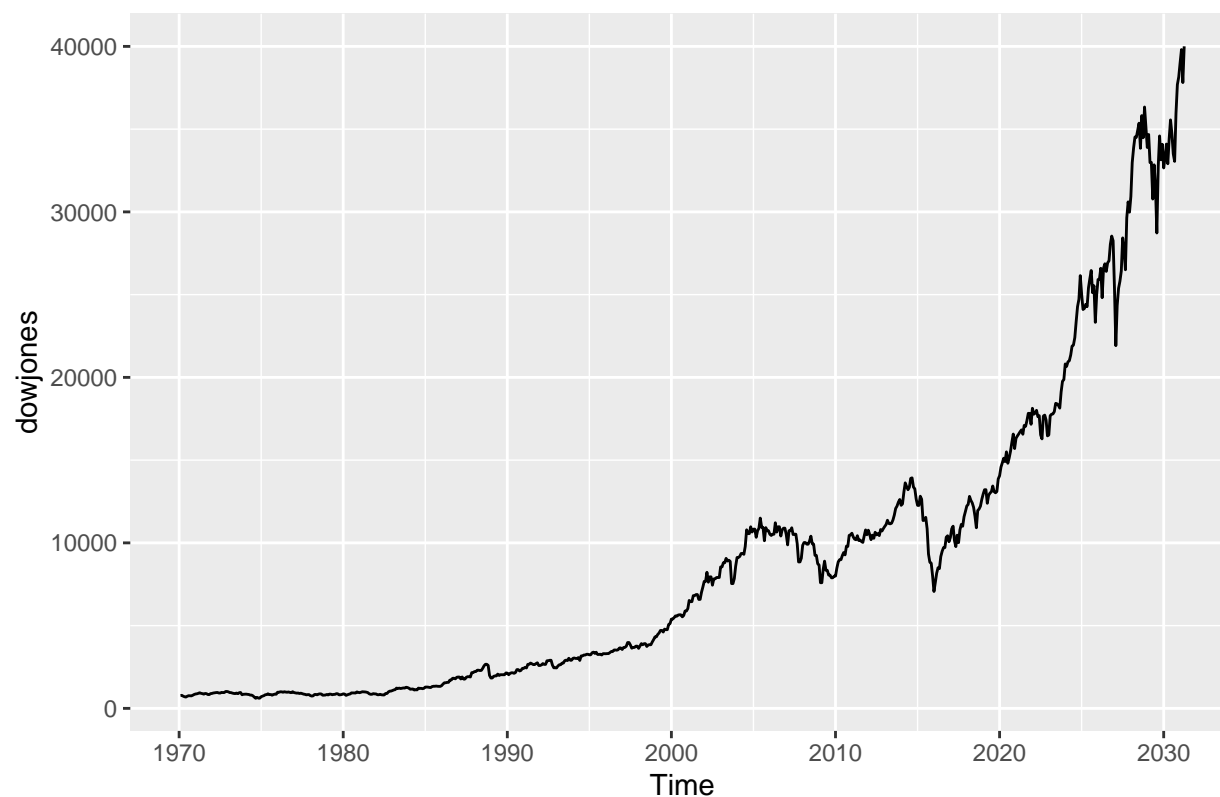
Notice that the regression models here did not fit the data as well as the global case, despite using periodic fits to handle seasonality.

**Trying finer frequencies:**

**Dow Jones data:**

src: <https://www.investing.com/indices/us-30-historical-data>

```
DOWJONES = read.csv(file= "C:\\Users/ss/Desktop/Time_series_Analysis/Dow Jones Industrial Average Histor
dowjones = ts(DOWJONES[, 2], start=c(1970, 2), frequency = 12)
autoplot(dowjones)
```



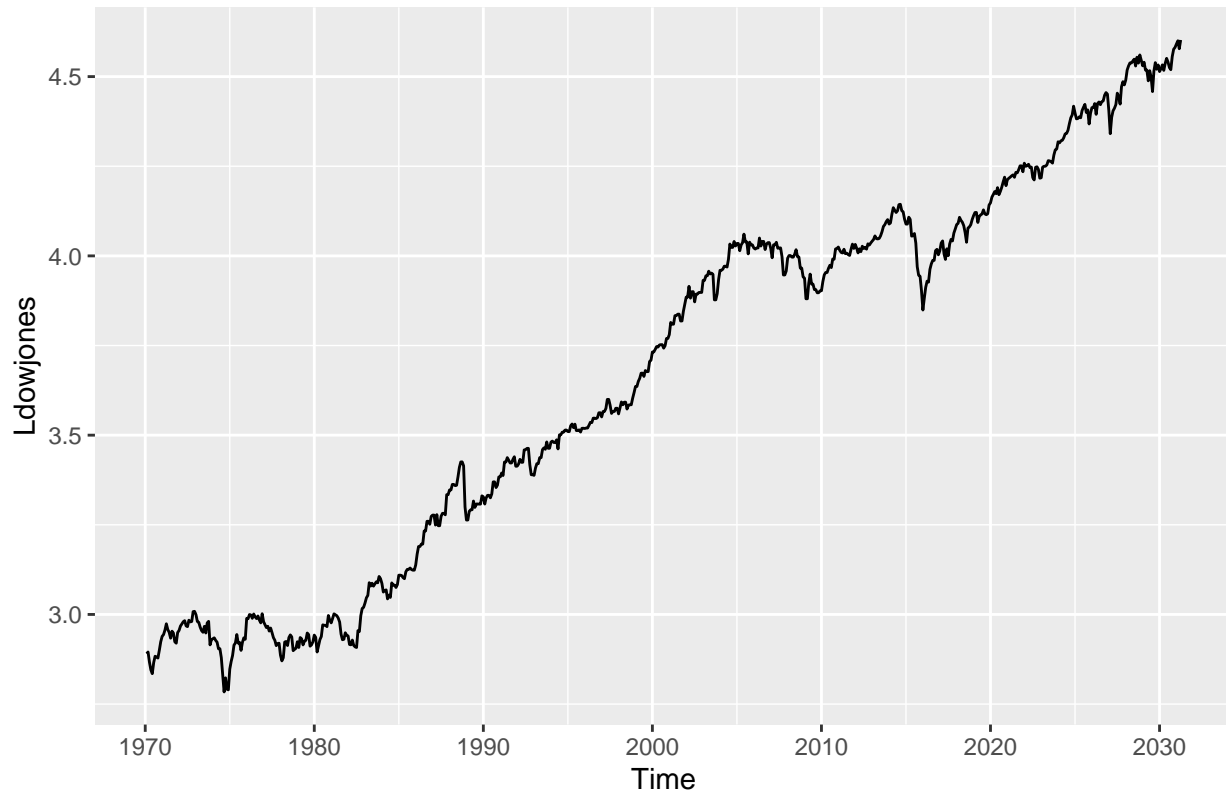
Now I will fit it to autoArima

```
dowjones_autoArima_fit = auto.arima(dowjones, approximation = FALSE, seasonal = TRUE, stepwise = FALSE,
summary(dowjones_autoArima_fit)
```

```
## Series: dowjones
## ARIMA(1,2,3)
##
## Coefficients:
##      ar1      ma1      ma2      ma3
##      -0.6725 -0.4261 -0.7751  0.2175
## s.e.    0.0988  0.0999  0.0878  0.0379
##
## sigma^2 = 293999: log likelihood = -5654.95
## AIC=11319.89  AICc=11319.97  BIC=11342.88
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 25.3025 539.9988 278.2725 0.1578803 3.068817 0.2765872
##              ACF1
## Training set -0.002058391
```

try logarithmic transformation:

```
Ldowjones = log10(dowjones)
autoplot(Ldowjones)
```

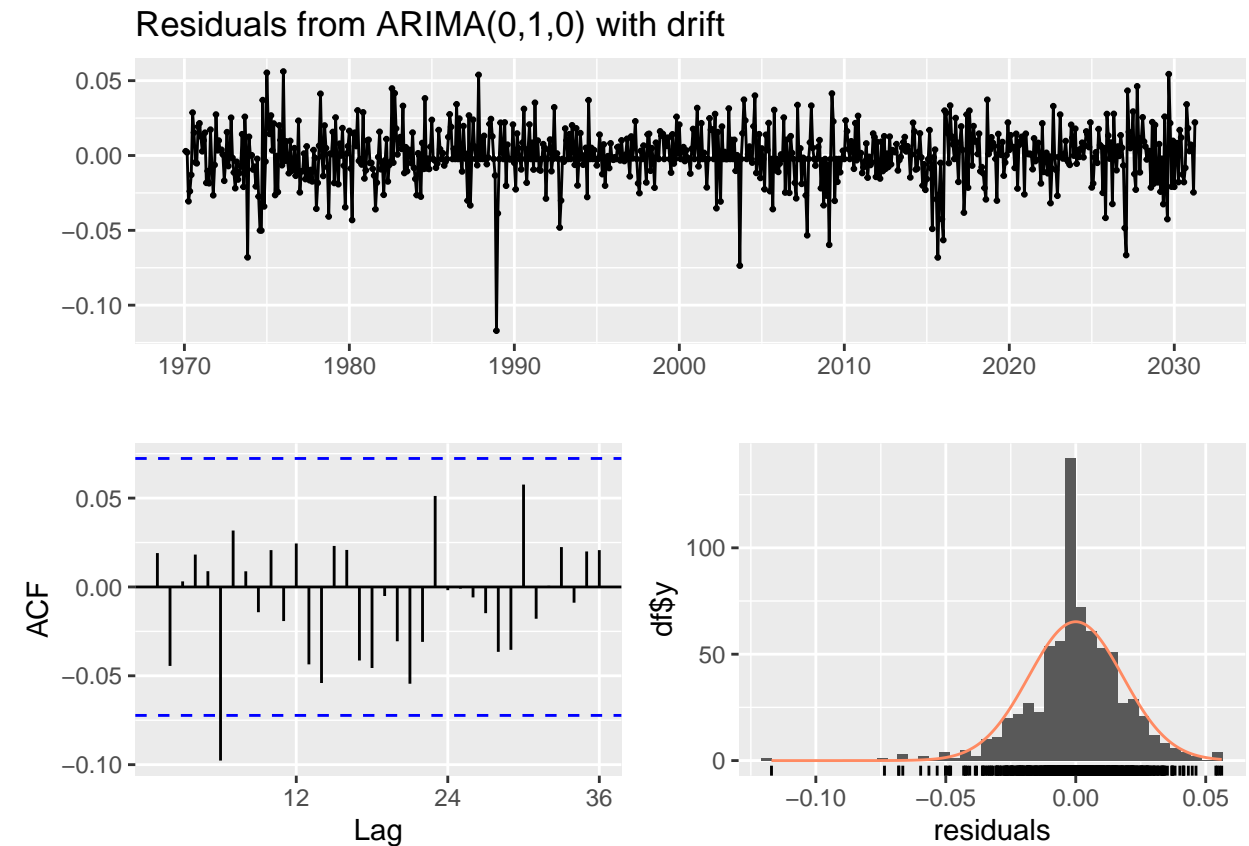


```
Ldowjones_autoArima_fit = auto.arima(Ldowjones, approximation = FALSE, seasonal = TRUE, stepwise = FALSE)

summary(Ldowjones_autoArima_fit)
```

```
## Series: Ldowjones
## ARIMA(0,1,0) with drift
##
## Coefficients:
##      drift
##      0.0023
## s.e.  0.0007
##
## sigma^2 = 0.0003281:  log likelihood = 1903.19
## AIC=-3802.38   AICc=-3802.36   BIC=-3793.18
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 3.92982e-06 0.0180881 0.01292583 -0.002732865 0.3610894 0.2404342
##              ACF1
## Training set 0.01905663
```

```
checkresiduals(Ldowjones_autoArima_fit)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from ARIMA(0,1,0) with drift
## Q* = 24.05, df = 24, p-value = 0.4588
##
## Model df: 0.   Total lags used: 24
```

```
summary(auto.arima(Ldowjones, approximation = FALSE, seasonal = TRUE, stepwise = FALSE, allowdrift = FALSE))
```

```
## Series: Ldowjones
## ARIMA(0,1,0)
##
## sigma^2 = 0.0003331:  log likelihood = 1897.15
## AIC=-3792.3   AICc=-3792.29   BIC=-3787.7
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.002332309 0.01823755 0.01293023 0.06206203 0.3603578 0.2405161
##              ACF1
## Training set 0.01903661
```