$A + (A \cdot B)$	Given
$(A\cdot 1)+(A\cdot B)$	A = (A . 1)
$A \cdot (1+B)$	A . (B . C) = (A . B) + (A . C)
$A \cdot (1)$	A + 1 = 1
A	A . 1 = A

$A + \overline{A}B$	Given		
$(A+\overline{AB})+\overline{A}B$	A = A + AB		
$A + (AB + \overline{A}B)$	A + (B + C) = (A + B) + C		
$A + (BA + B\overline{A})$	A . B = B . A		
$A+B(A+\overline{A})$	$A \cdot (B+C) = (A.B) + (A.C)$		
A + B(1)	A+ Ā = 1		
A + B	A .1 = A		

$\overline{A}BC + A\overline{B}C + AB\overline{C} + ABC$	Given	
$BC(\overline{A} + A) + A\overline{B}C + AB\overline{C}$	A.(B+C) = (A.B) + (A.C)	
$BC(1) + A\overline{B}C + AB\overline{C}$	A+Ā = 1	
$BC + A\overline{B}C + AB\overline{C}$	B.1 = B	
$B(C + A\overline{C}) + A\overline{B}C$	A.(B+C) = (A.B) + (A.C)	
$B(C+A)+A\overline{B}C$	A+Ā = 1	
$BC + AB + A\overline{B}C$	A.(B+C) = (A.B) + (A.C)	
$BC + A(B + \overline{B}C)$	A.(B+C) = (A.B) + (A.C)	
BC + A(B+C)	A+Ā = 1	
BC + AB + AC	A.(B+C) = (A.B) + (A.C)	
AB + BC + AC	ORGANISING	

	BC			
\overline{A}	0 0	0 1	1 1	1 0
0	1	1	0	1
1	1	1	0	1

Now give a simplified form for Y:

$$Y = B'C' + B'C + BC'$$