

# COE4DK4 – LAB 3

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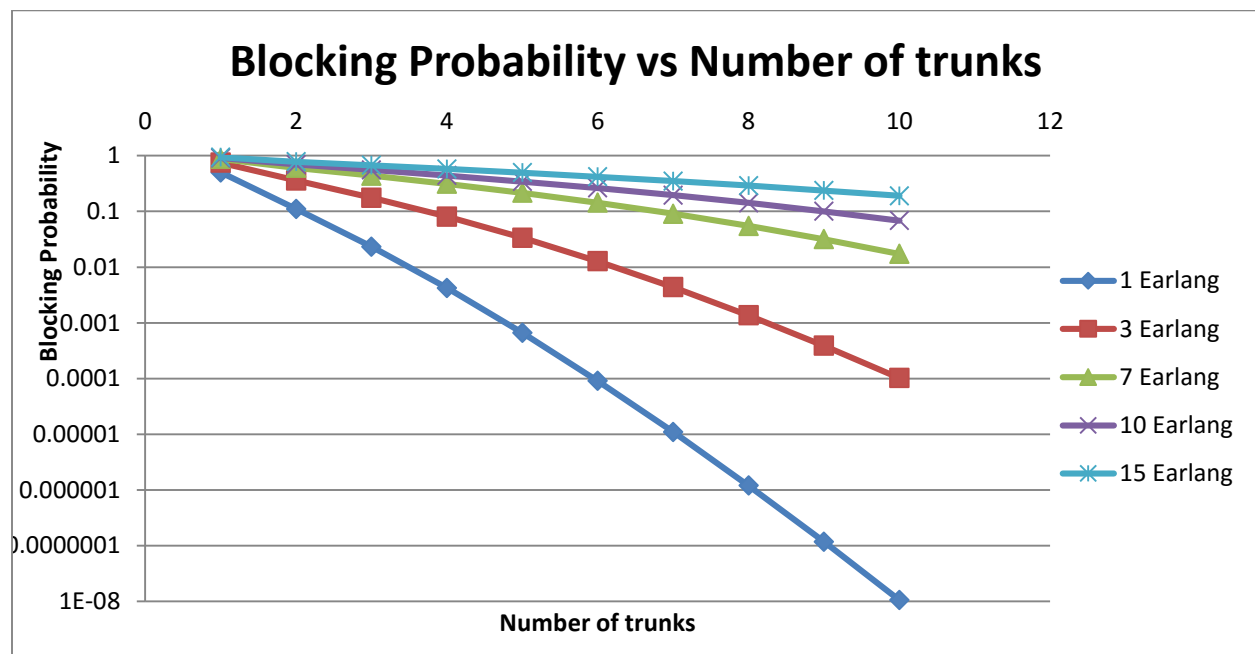
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## EXPERIMENT 2

During this experiment it was expected to code an Erlang B formula using to realize the tadeoffs between blocking probability, offered load and number of channels. In the table below it is shown that in order to keep 1% blocking probability performance, the required number of lines increases as the load increases. The relationship between the required number of lines and offered load is not a linear one but more of a logarithmic relationship. As it is seen, with an offered load of 1 erlang a total of 5 lines are required to maintain the 1% performance ratio. On the other hand when the offered load increases to 3 erlangs, a total of 8 lines are required. This result is caused because as the load on the system is increasing, so is the efficiency of the system to manage number of lines.

| Number of Lines | OFFERED LOAD (A) |            |            |            |            |
|-----------------|------------------|------------|------------|------------|------------|
|                 | 1                | 3          | 7          | 10         | 15         |
| 1               | 0.5              | 0.75       | 0.875      | 0.90909091 | 0.9375     |
| 2               | 0.111111111      | 0.36       | 0.60493827 | 0.69444444 | 0.77854671 |
| 3               | 0.023255814      | 0.17647059 | 0.43918054 | 0.55617353 | 0.67324955 |
| 4               | 0.004219409      | 0.08059701 | 0.31275238 | 0.44138418 | 0.58015608 |
| 5               | 0.000661813      | 0.03359602 | 0.21559321 | 0.34411562 | 0.49576458 |
| 6               | 9.07194E-05      | 0.01270588 | 0.14298215 | 0.26263815 | 0.4194902  |
| 7               | 1.10058E-05      | 0.0043596  | 0.09080987 | 0.19569441 | 0.35107428 |
| 8               | 1.19547E-06      | 0.00136121 | 0.0550136  | 0.14196879 | 0.29027739 |
| 9               | 1.17442E-07      | 0.00038853 | 0.03168491 | 0.10000363 | 0.23682716 |
| 10              | 1.0525E-08       | 0.0001019  | 0.01730502 | 0.06821351 | 0.19040392 |



To confirm our results from experiment 2, we used an online Erlang B calculator and the results are shown below in a chart.

Calculator: <http://www.erlang.com/calculator/erlb/>

### Erlang B Results Table

Here are the results (max 20) of the Erlang B Calculator. The unknown figures are shown in red.

| B.H.T. | Blocking | Lines |
|--------|----------|-------|
| 1.000  | 0.010    | 5     |
| 3.000  | 0.010    | 8     |
| 7.000  | 0.010    | 14    |
| 10.000 | 0.010    | 18    |
| 15.000 | 0.010    | 24    |

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Results displayed - 07/11/2015, 22:44:22

### MATLAB CODE:

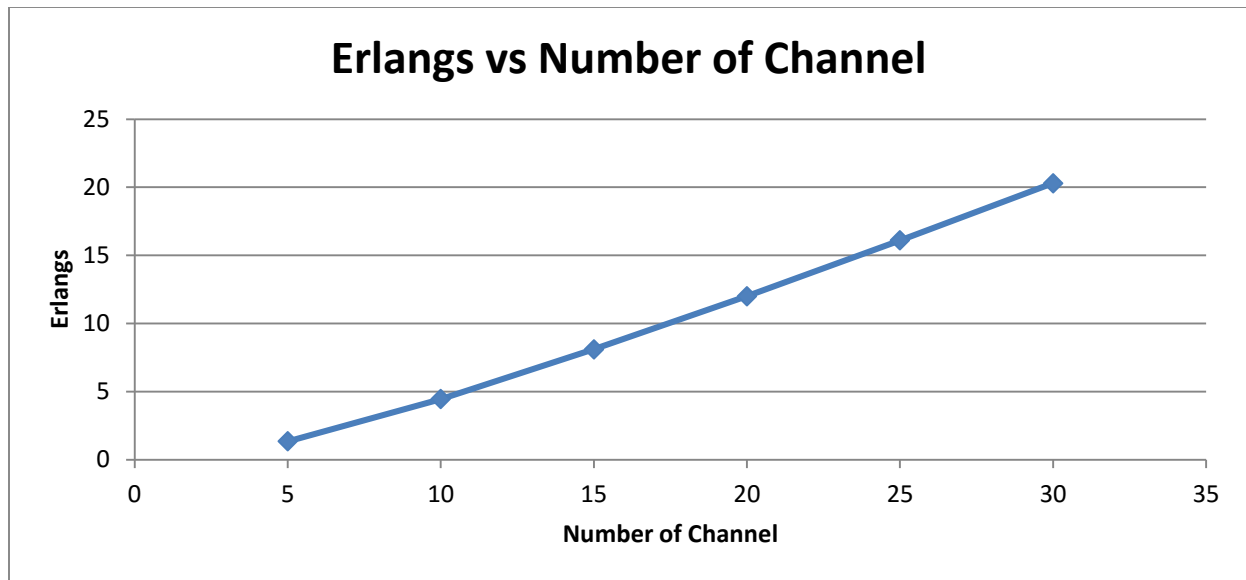
```
denom = 0;
for C = 1:20
    for k = 0:C
        denom = denom + ((9^k)/factorial(k));
    end
    Pb (C) = (9^C/factorial(C))/denom
end

xlswrite ('HelloWorld.xls', Pb)
```

### EXPERIMENT 3:

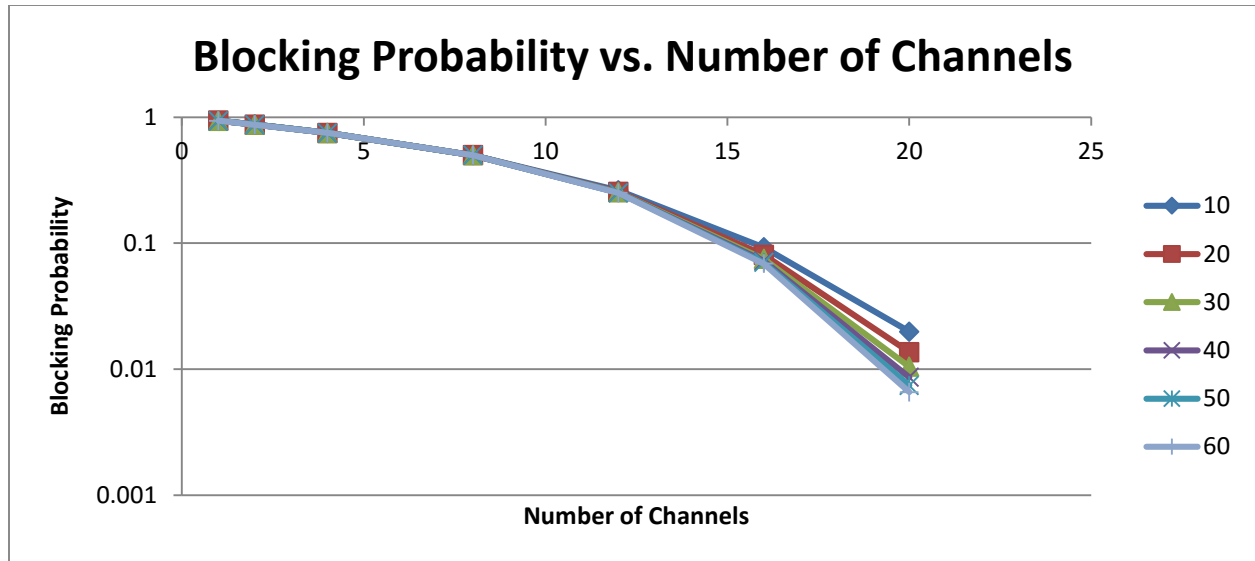
The chart below highlights the relationship between number of channels and the load it can handle. It is a direct relationship between the channels needed to handle a certain load while achieving the top performances.

| B.H.T. | Blocking | Lines |
|--------|----------|-------|
| 1.350  | 0.010    | 5     |
| 4.450  | 0.010    | 10    |
| 8.100  | 0.010    | 15    |
| 12.000 | 0.010    | 20    |
| 16.100 | 0.010    | 25    |
| 20.300 | 0.010    | 30    |



#### EXPERIMENT 4

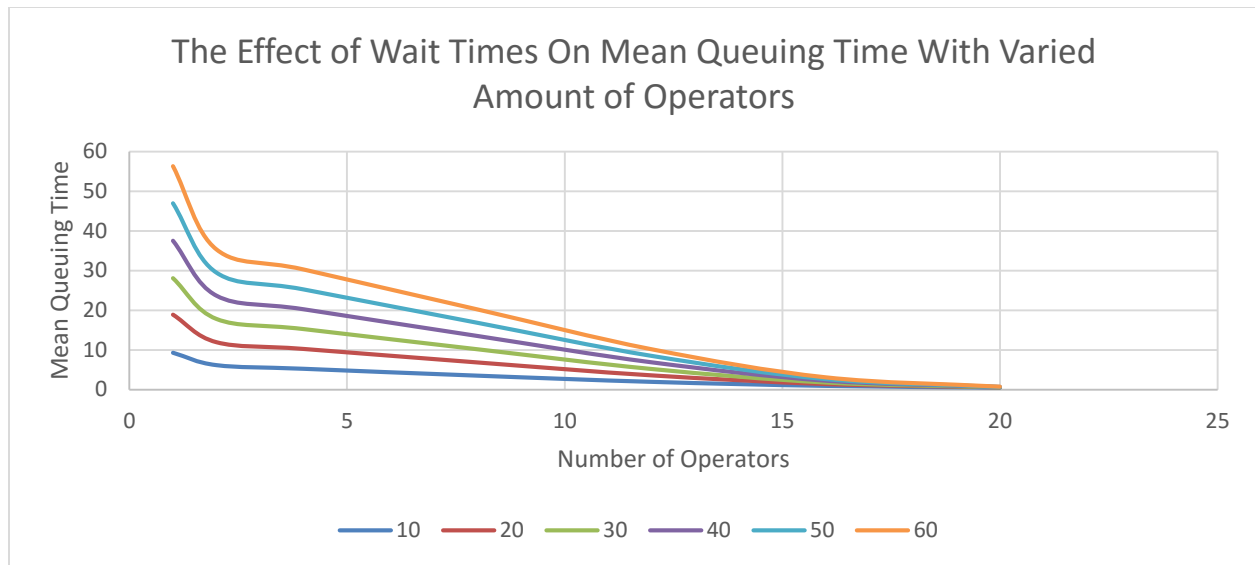
|    | Number of Channels |          |           |           |           |           |           |
|----|--------------------|----------|-----------|-----------|-----------|-----------|-----------|
|    | 1                  | 2        | 4         | 8         | 12        | 16        | 20        |
| 10 | 0.93811            | 0.87556  | 0.749975  | 0.499685  | 0.2626225 | 0.0927275 | 0.0198525 |
| 20 | 0.93857            | 0.874875 | 0.750075  | 0.50002   | 0.25601   | 0.0807825 | 0.0136625 |
| 30 | 0.93799            | 0.87234  | 0.7500675 | 0.50003   | 0.253205  | 0.075175  | 0.0104475 |
| 40 | 0.93781            | 0.87266  | 0.7500425 | 0.5000775 | 0.2520575 | 0.0723825 | 0.0086175 |
| 50 | 0.93765            | 0.872348 | 0.7499825 | 0.5000425 | 0.251275  | 0.0705175 | 0.00742   |
| 60 | 0.93756            | 0.87232  | 0.7499725 | 0.4999825 | 0.2502825 | 0.06883   | 0.006565  |



After modifying the simulation to act as a call center and graphing the results, some conclusions can be made about this system:

- A lower number of operators results in an increase in the chance of dropping a call due to huge wait times and vice versa.
- As the amount of operators decreases, small wait times have little impact on blocking probability and vice versa.

|    | Number of Operators |          |          |          |          |          |          |
|----|---------------------|----------|----------|----------|----------|----------|----------|
|    | 1                   | 2        | 4        | 8        | 12       | 16       | 20       |
| 10 | 9.32033             | 6.17123  | 5.248132 | 3.500072 | 1.928528 | 0.906407 | 0.461302 |
| 20 | 18.8981             | 11.94624 | 10.24807 | 6.835122 | 3.573943 | 1.38135  | 0.559497 |
| 30 | 28.03477            | 17.7845  | 15.24705 | 10.16594 | 5.212583 | 1.813472 | 0.609827 |
| 40 | 37.51453            | 23.66031 | 20.24435 | 13.49878 | 6.86205  | 2.239555 | 0.64346  |
| 50 | 46.92135            | 29.45831 | 25.24229 | 16.83158 | 8.503698 | 2.659643 | 0.674583 |
| 60 | 56.27163            | 35.28402 | 30.23905 | 20.16225 | 10.1223  | 3.052553 | 0.701198 |



Some more conclusions can be made about this system:

- A lower number of operators results in an increase in mean queuing time with the values of verging closer to the amount of wait time
- As the amount of operators increases, the mean queuing times verge closer to 0 around roughly 20 operators

Code:

```
Call departure.c
void
end_call_on_channel_event(Simulation_Run_Ptr simulation_run, void * c_ptr)
{
    ...

    /*
     * See if there are calls waiting in the buffer. If so, take the next one
     immediately.
     */

    if ((channel = get_free_channel(simulation_run)) != NULL) {
        if (fifoqueue_size(sim_data->buffer) > 0) {
            for (q_count = 0; q_count < fifoqueue_size(sim_data->buffer);
q_count++) {
                next_call = (Call_Ptr)fifoqueue_get(sim_data->buffer);
                call_time = simulation_run_get_time(simulation_run) -
this_call->arrive_time;

                sim_data->queue_wait_time += call_time;
                if (call_time >= MAX_WAIT_TIME) {
                    sim_data->blocked_call_count++;
                    TRACE(sprintf("Call Blocked"));
                }
                else {
                    next_call->arrive_time =
simulation_run_get_time(simulation_run);
                    next_call->call_duration = get_call_duration();
```

```

server_put(channel, (void*)next_call);
next_call->channel = channel;

schedule_end_call_on_channel_event(simulation_run,
simulation_run_get_time(simulation_run) + get_call_duration(), (void *)channel);
TRACE(printf("Waiting Call Completed"));
break;
    }
}
}
}

```

### Call\_arrival.c

```

void
call_arrival_event(Simulation_Run_Ptr simulation_run, void * ptr)
{
...
if((free_channel = get_free_channel(simulation_run)) != NULL) {
...
} else {
    new_call = (Call_Ptr)xmalloc(sizeof(Call));
    new_call->arrive_time = now;
    fifoqueue_put(sim_data->buffer, (void*)new_call);
    sim_data->calls_in_queue++;
    TRACE(printf("Call placed in Queue"));
}
}

```

### main.h

```

typedef struct _call_
{
    double arrive_time;
    double call_duration;
    Channel_Ptr channel;
    Call_Status status;
} Call, * Call_Ptr;

typedef struct _simulation_run_data_
{
    double queue_wait_time;
} Simulation_Run_Data, * Simulation_Run_Data_Ptr;

```

### Simpameters.h

```
#define MAX_WAIT_TIME 5
```

### Output.c

```

void output_results(Simulation_Run_Ptr this_simulation_run)
{
    double xmtted_fraction;
    double avgQTime;
    ...
    avgQTime = (sim_data->queue_wait_time) / (fifoqueue_size(sim_data->buffer));
    ...
    printf("Average Wait Time of the Queue = %.5f\n", avgQTime);
}

```

### Main.c

```
int main(void)
```

```

{
...
while ((random_seed = RANDOM_SEEDS[j++]) != 0) {
...
    data.calls_in_queue = 0;
    data.queue_wait_time = 0.0;
...
    data.buffer = fifoqueue_new();
...
}
...
}

```

## **EXPERIMENT 5**

We selected our system parameters to be  $A = 7*7$  or 49 with our  $N = 63$ , that gives us  $W(t) = 98.16\%$  success rate and  $1.84\%$  failure rate and if we compare to our results, we get  $W(t)$  as  $(98.2 + 98.12 + 98.09 + 98.15 + 98.12)/5 = 98.136\%$ .

Code changes:

### **Call departure.c**

```

void
end_call_on_channel_event(Simulation_Run_Ptr simulation_run, void * c_ptr)
{
...

    /*
     * See if there are calls waiting in the buffer. If so, take the next one
     immediately.
     */

    if ((channel = get_free_channel(simulation_run)) != NULL) {
        if (fifoqueue_size(sim_data->buffer) > 0) {
            for (q_count = 0; q_count < fifoqueue_size(sim_data->buffer);
q_count++) {
                next_call = (Call_Ptr)fifoqueue_get(sim_data->buffer);
                call_time = simulation_run_get_time(simulation_run) -
this_call->arrive_time;

                sim_data->queue_wait_time += call_time;
                if (call_time >= MAX_WAIT_TIME) {
                }
                else {
                    next_call->arrive_time =
simulation_run_get_time(simulation_run);
                    next_call->call_duration = get_call_duration();
                    server_put(channel, (void*)next_call);
                    next_call->channel = channel;

                    schedule_end_call_on_channel_event(simulation_run,
simulation_run_get_time(simulation_run) + get_call_duration(), (void *)channel);
                    TRACE(sprintf("Waiting Call Completed"));
                    break;
                }
            }
        }
    }
}

```