

Introduction to regression

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Predicting blood glucose levels

```
import pandas as pd  
  
diabetes_df = pd.read_csv("diabetes.csv")  
  
print(diabetes_df.head())
```

	pregnancies	glucose	triceps	insulin	bmi	age	diabetes
0	6	148	35	0	33.6	50	1
1	1	85	29	0	26.6	31	0
2	8	183	0	0	23.3	32	1
3	1	89	23	94	28.1	21	0
4	0	137	35	168	43.1	33	1

Creating feature and target arrays

```
X = diabetes_df.drop("glucose", axis=1).values  
y = diabetes_df["glucose"].values  
print(type(X), type(y))
```

```
<class 'numpy.ndarray'> <class 'numpy.ndarray'>
```

Making predictions from a single feature

```
X_bmi = X[:, 3]  
print(y.shape, X_bmi.shape)
```

```
(752,) (752,)
```

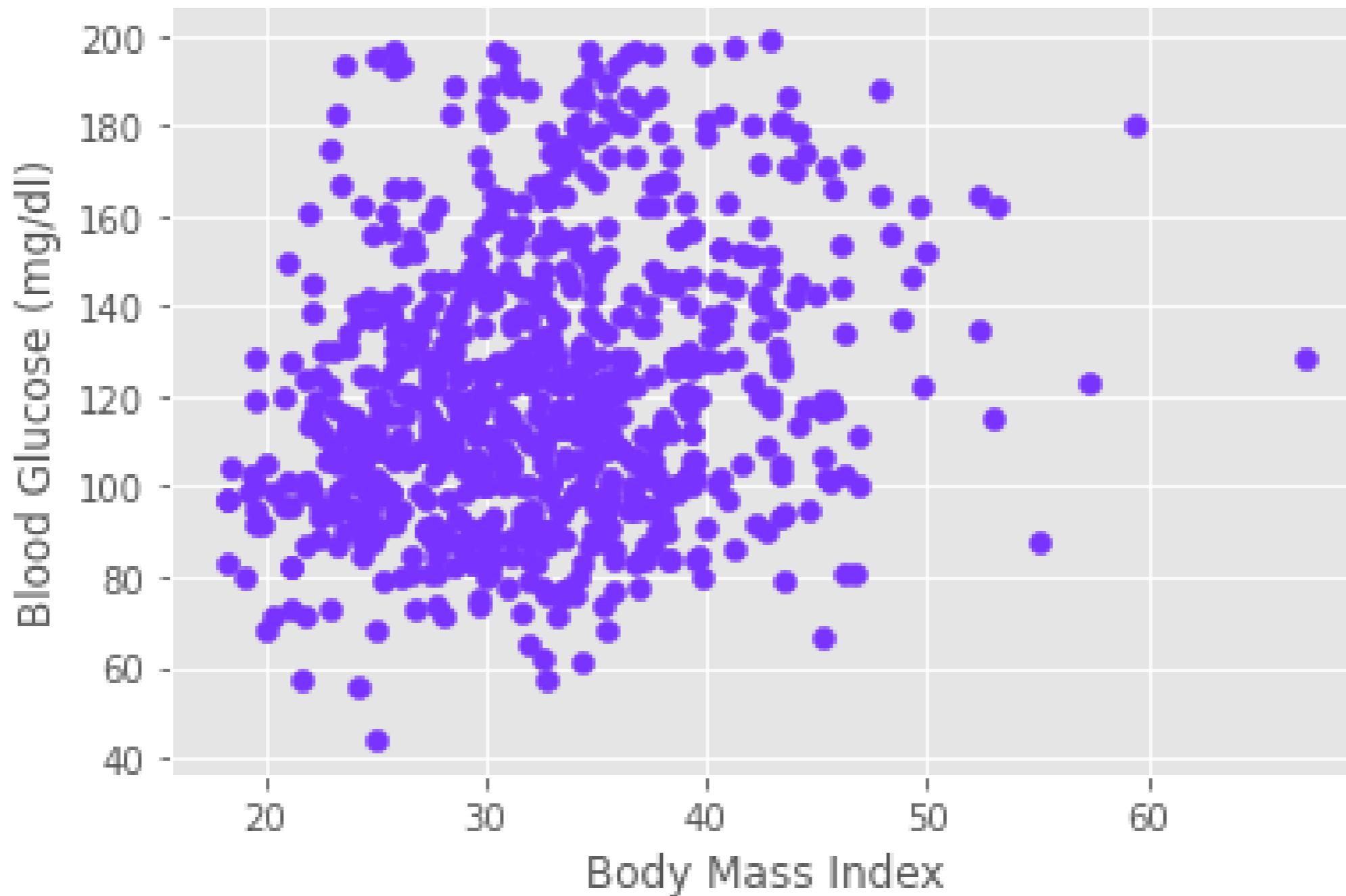
```
X_bmi = X_bmi.reshape(-1, 1)  
print(X_bmi.shape)
```

```
(752, 1)
```

Plotting glucose vs. body mass index

```
import matplotlib.pyplot as plt  
plt.scatter(X_bmi, y)  
plt.ylabel("Blood Glucose (mg/dL)")  
plt.xlabel("Body Mass Index")  
plt.show()
```

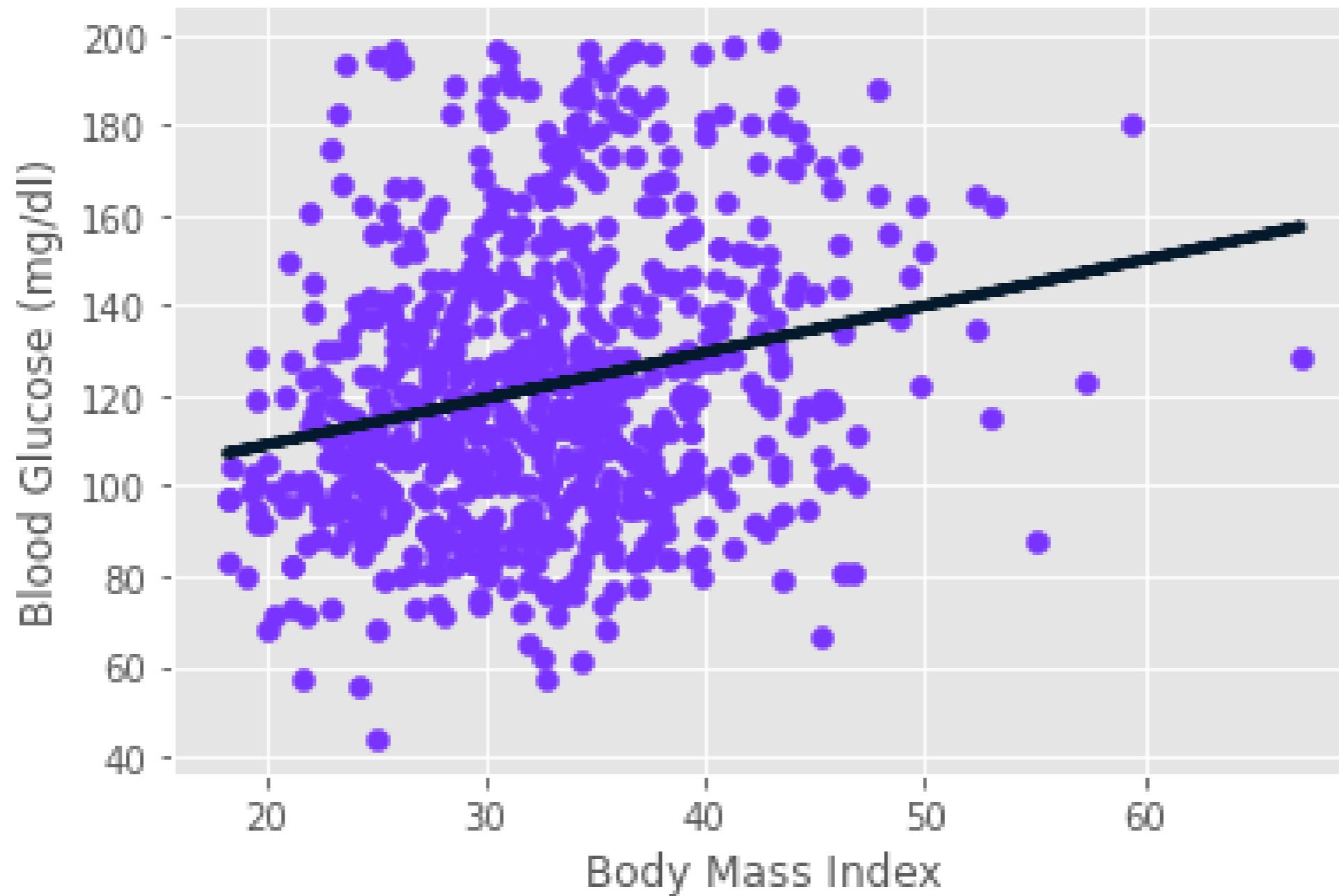
Plotting glucose vs. body mass index



Fitting a regression model

```
from sklearn.linear_model import LinearRegression  
reg = LinearRegression()  
reg.fit(X_bmi, y)  
predictions = reg.predict(X_bmi)  
plt.scatter(X_bmi, y)  
plt.plot(X_bmi, predictions)  
plt.ylabel("Blood Glucose (mg/dL)")  
plt.xlabel("Body Mass Index")  
plt.show()
```

Fitting a regression model



Let's practice!

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The basics of linear regression

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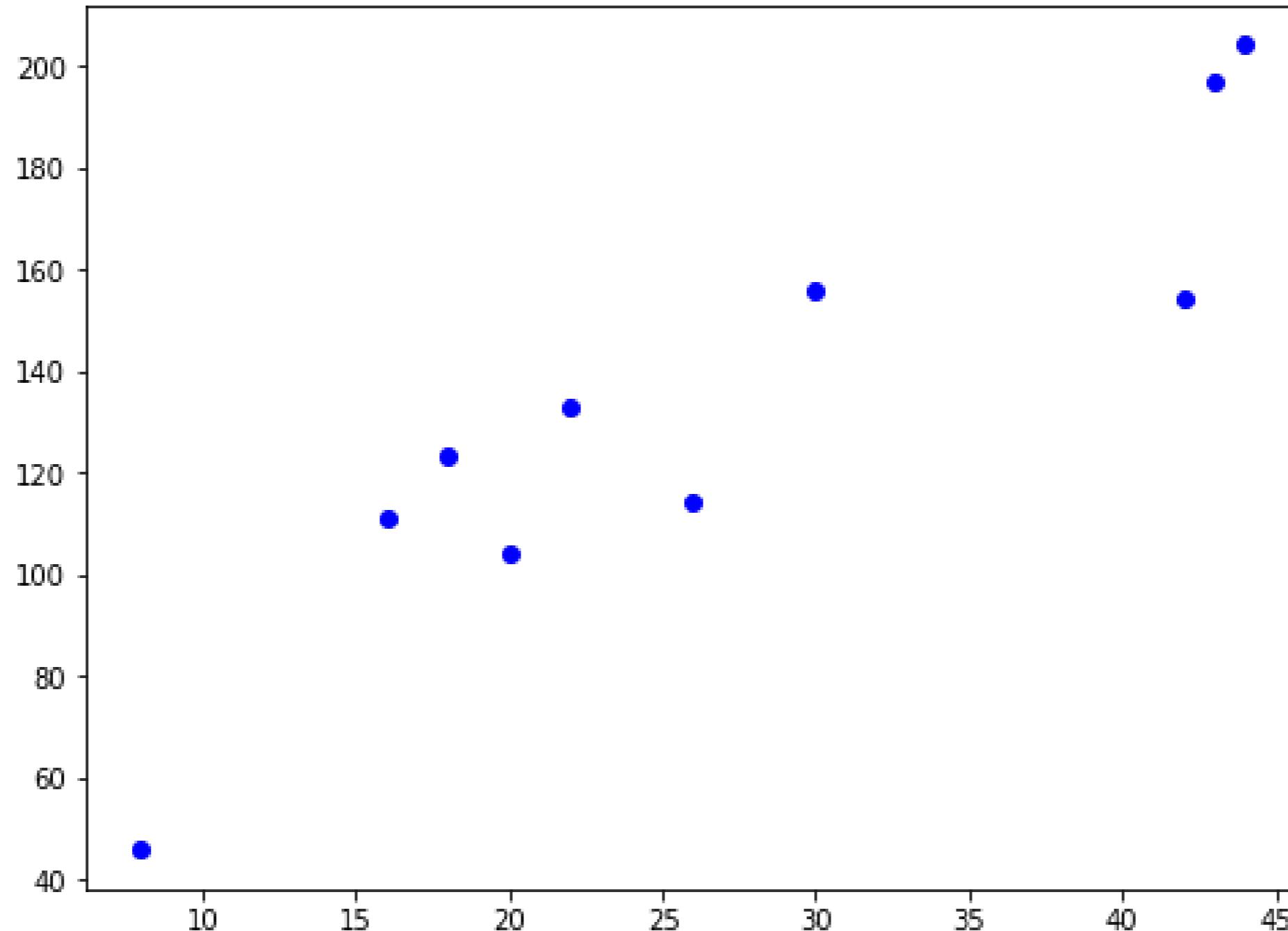
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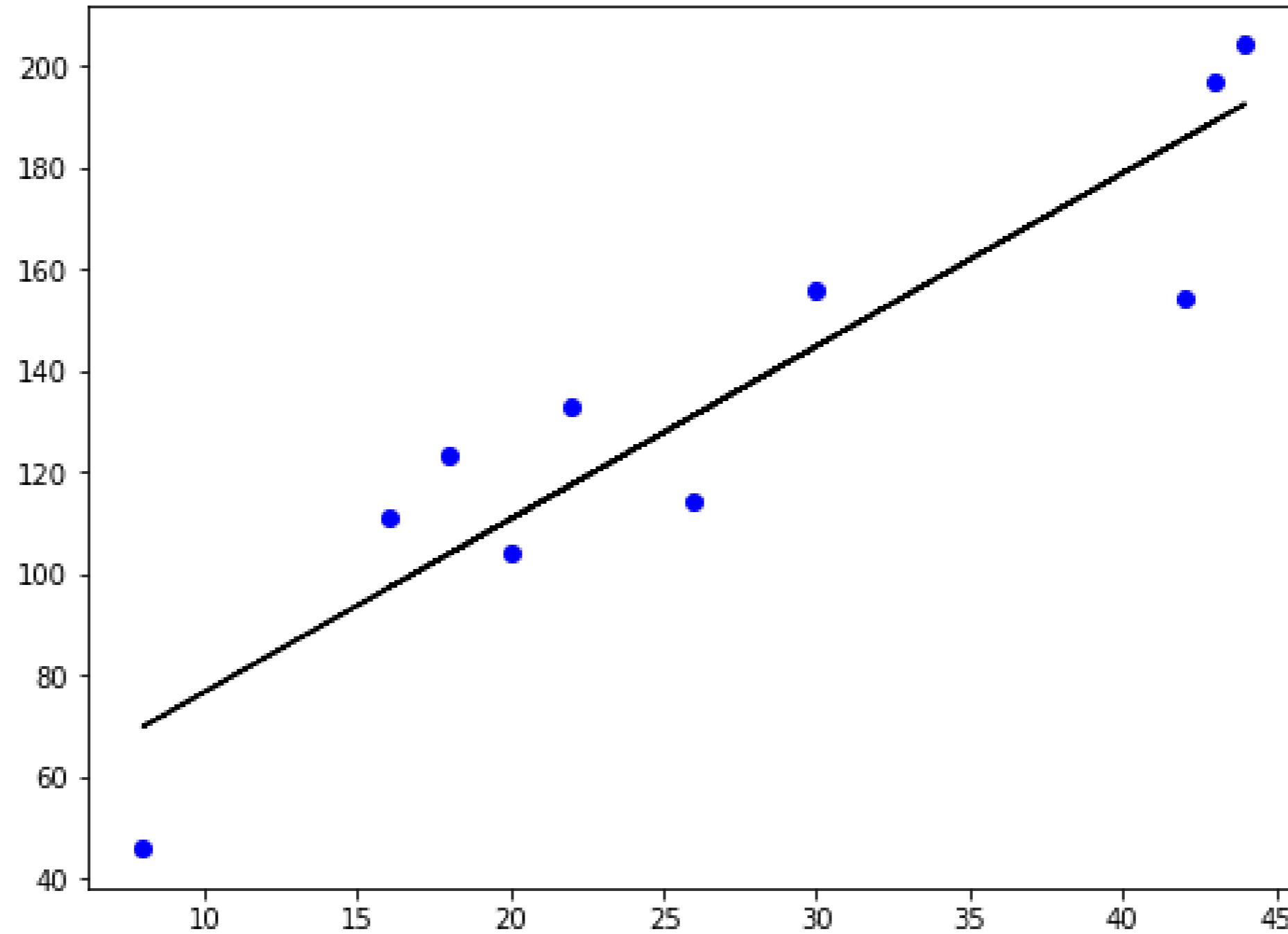
Regression mechanics

- $y = ax + b$
 - Simple linear regression uses one feature
 - y = target
 - x = single feature
 - a, b = parameters/coefficients of the model - slope, intercept
- How do we choose a and b ?
 - Define an error function for any given line
 - Choose the line that minimizes the error function
- Error function = loss function = cost function

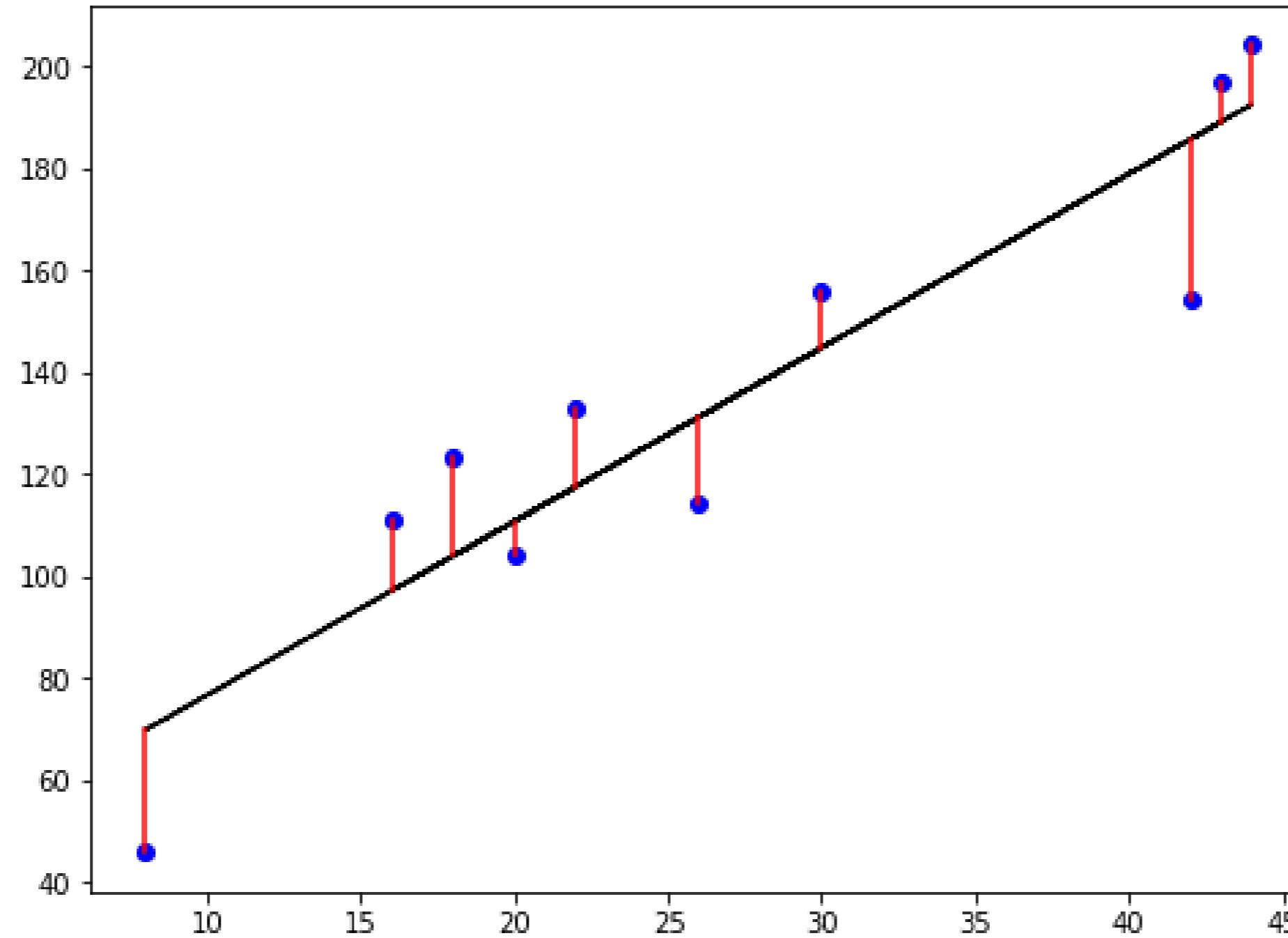
The loss function



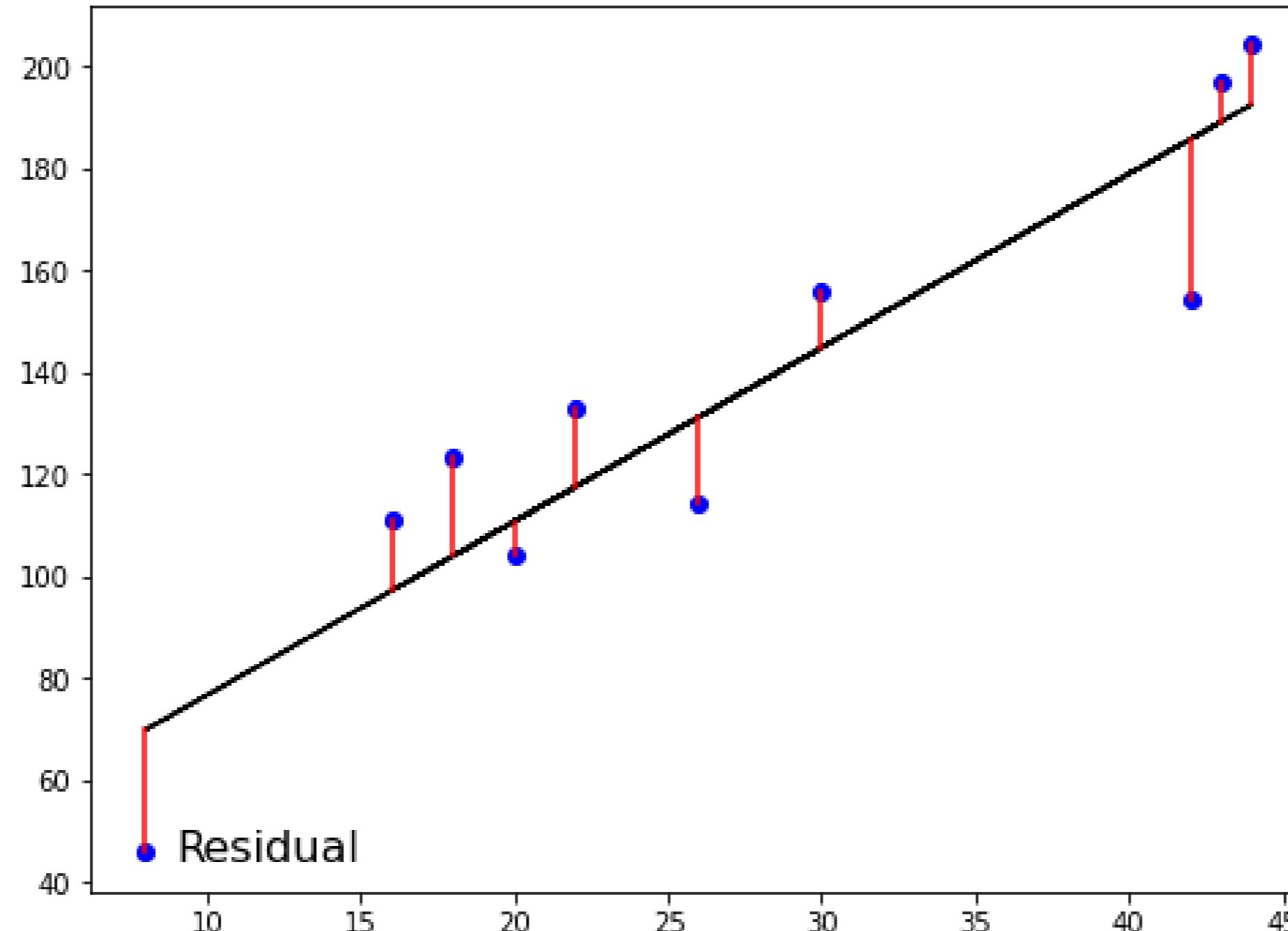
The loss function



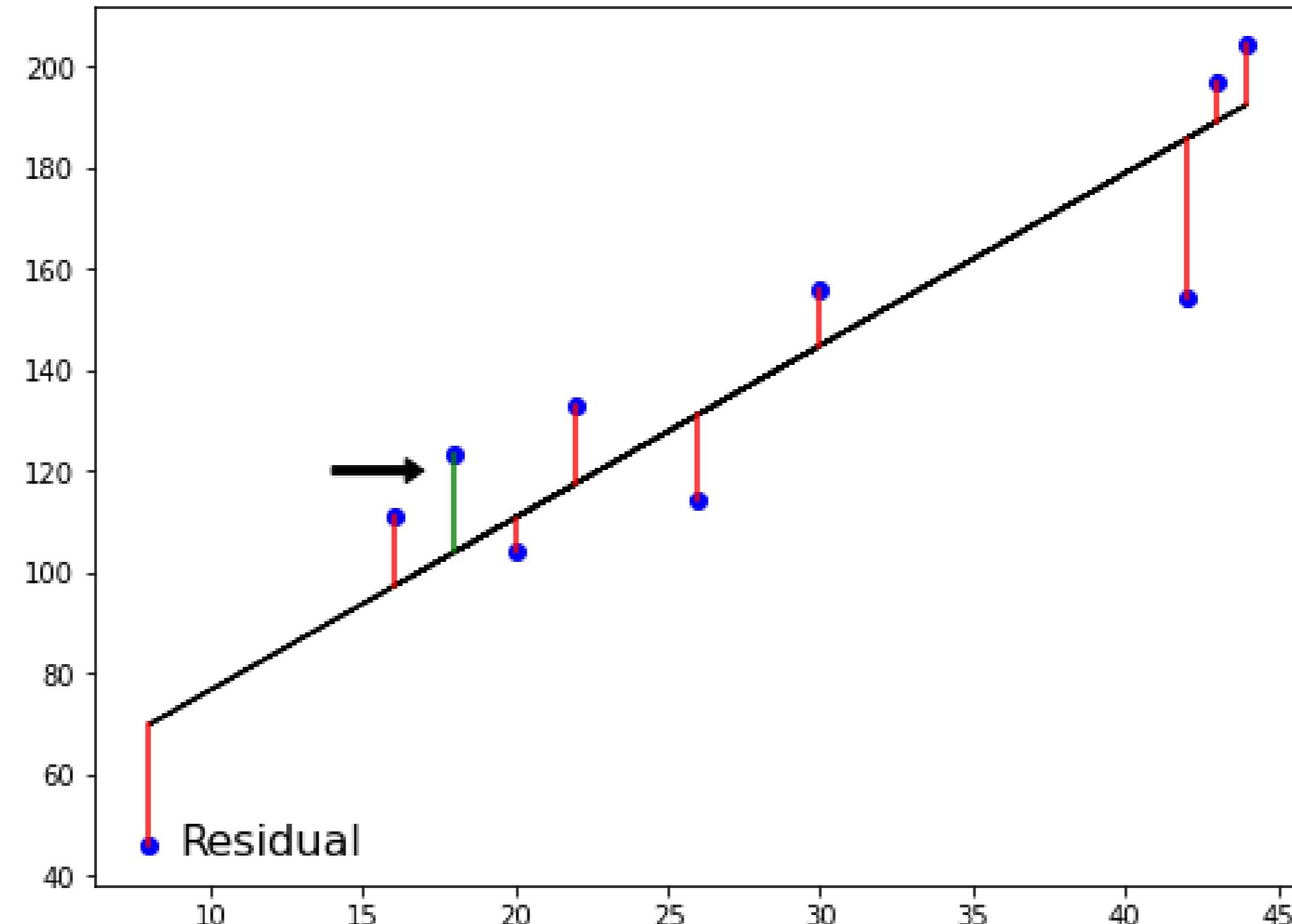
The loss function



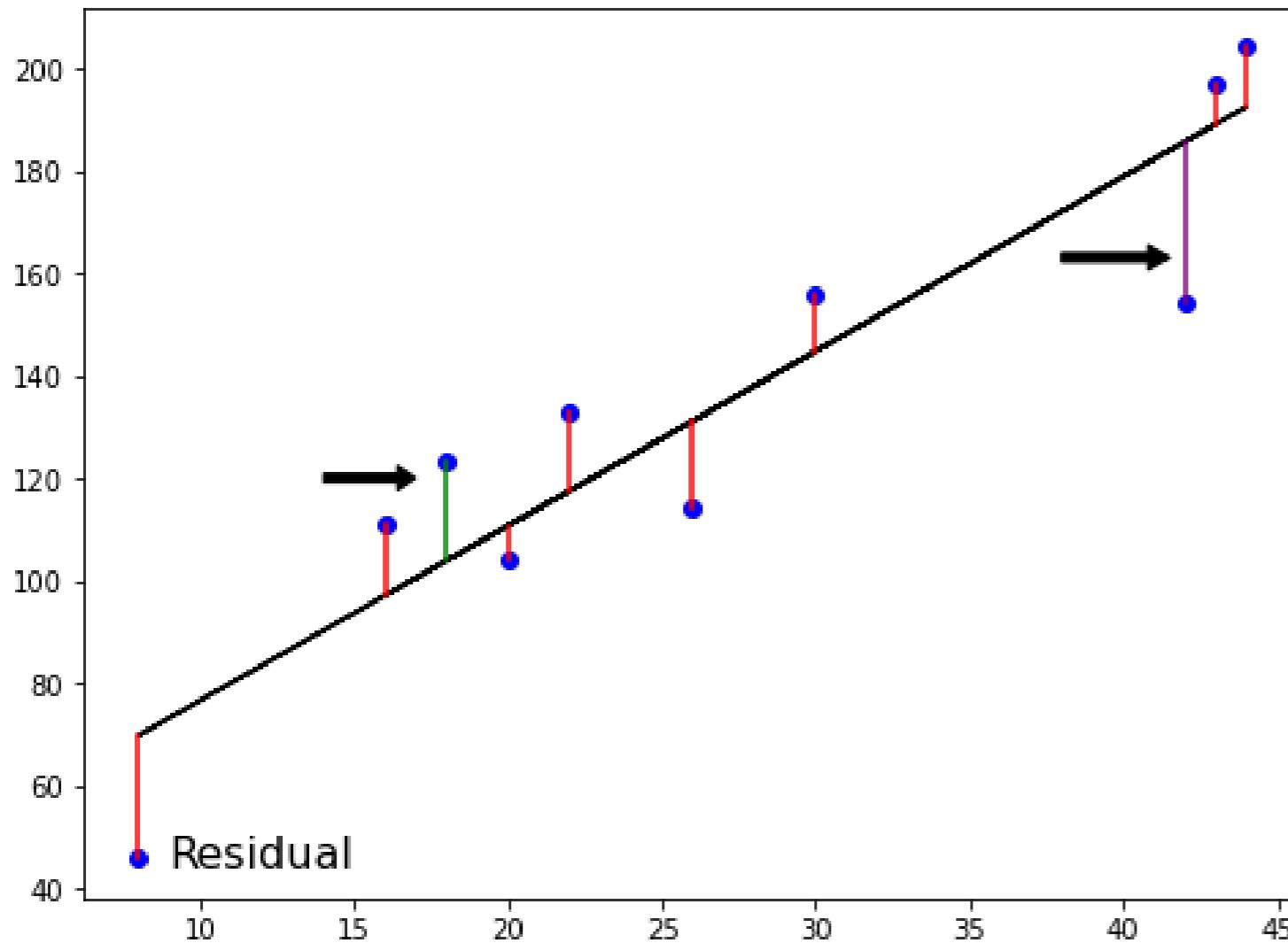
The loss function



The loss function



Ordinary Least Squares



$$RSS = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

Ordinary Least Squares (OLS): minimize RSS

Linear regression in higher dimensions

$$y = a_1x_1 + a_2x_2 + b$$

- To fit a linear regression model here:
 - Need to specify 3 variables: a_1 , a_2 , b
- In higher dimensions:
 - Known as multiple regression
 - Must specify coefficients for each feature and the variable b

$$y = a_1x_1 + a_2x_2 + a_3x_3 + \dots + a_nx_n + b$$

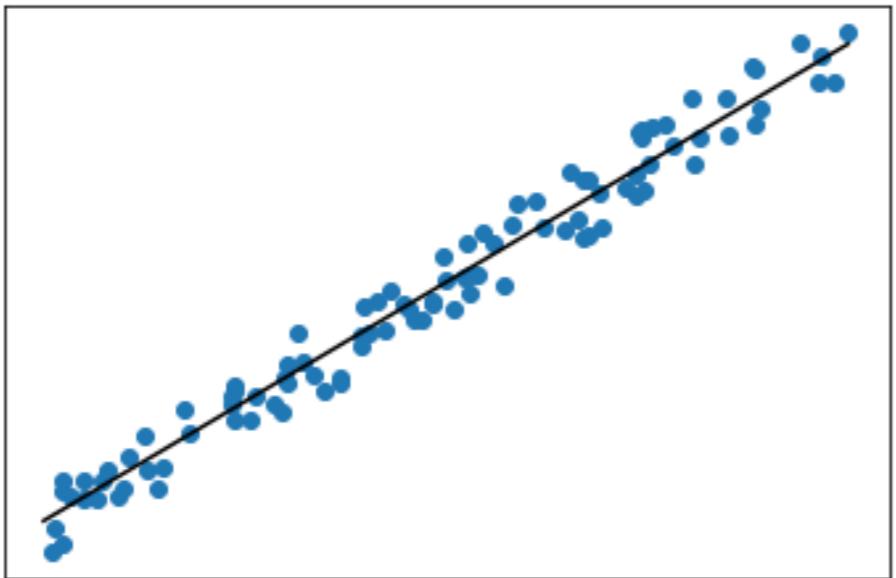
- scikit-learn works exactly the same way:
 - Pass two arrays: features and target

Linear regression using all features

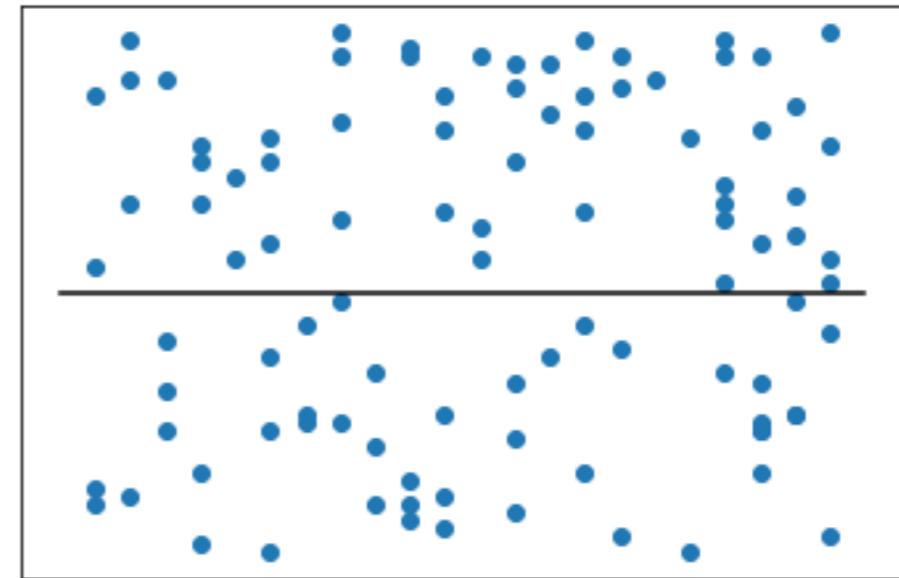
```
from sklearn.model_selection import train_test_split  
from sklearn.linear_model import LinearRegression  
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3,  
                                                random_state=42)  
reg_all = LinearRegression()  
reg_all.fit(X_train, y_train)  
y_pred = reg_all.predict(X_test)
```

R-squared

- R^2 : quantifies the variance in target values explained by the features
 - Values range from 0 to 1
- High R^2 :



- Low R^2 :



R-squared in scikit-learn

```
reg_all.score(X_test, y_test)
```

```
0.356302876407827
```

Mean squared error and root mean squared error

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

- MSE is measured in target units, squared

$$RMSE = \sqrt{MSE}$$

- Measure $RMSE$ in the same units at the target variable

RMSE in scikit-learn

```
from sklearn.metrics import root_mean_squared_error  
  
root_mean_squared_error(y_test, y_pred)
```

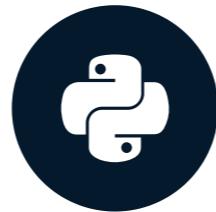
```
24.028109426907236
```

Let's practice!

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Cross-validation

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Cross-validation motivation

- Model performance is dependent on the way we split up the data
- Not representative of the model's ability to generalize to unseen data
- Solution: Cross-validation!

Cross-validation basics

Split 1

Fold 1

Fold 2

Fold 3

Fold 4

Fold 5

Cross-validation basics

Split 1

Fold 1

Fold 2

Fold 3

Fold 4

Fold 5

Test Data

Cross-validation basics

Split 1

Fold 1

Fold 2

Fold 3

Fold 4

Fold 5

Training Data Test Data

Cross-validation basics

Split 1

Fold 1

Fold 2

Fold 3

Fold 4

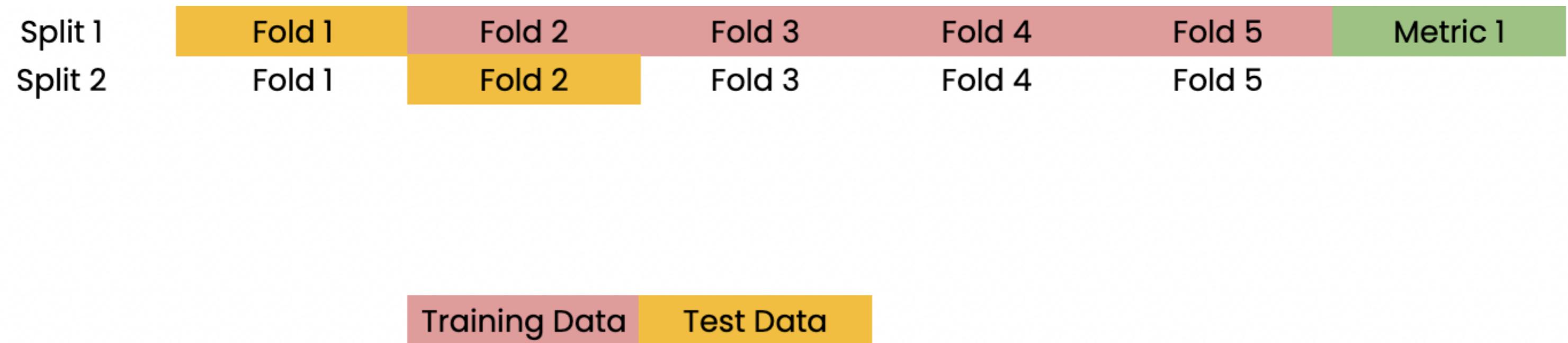
Fold 5

Metric 1

Training Data

Test Data

Cross-validation basics



Cross-validation basics

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
Split 2	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	
Training Data Test Data						

Cross-validation basics

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
Split 2	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 2

Training Data Test Data

Cross-validation basics

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
Split 2	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 2
Split 3	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 3

Training Data Test Data

Cross-validation basics

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
Split 2	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 2
Split 3	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 3
Split 4	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 4

Training Data Test Data

Cross-validation basics

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
Split 2	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 2
Split 3	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 3
Split 4	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 4
Split 5	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 5

Training Data Test Data

Cross-validation and model performance

- 5 folds = 5-fold CV
- 10 folds = 10-fold CV
- k folds = k -fold CV
- More folds = More computationally expensive

Cross-validation in scikit-learn

```
from sklearn.model_selection import cross_val_score, KFold  
kf = KFold(n_splits=6, shuffle=True, random_state=42)  
reg = LinearRegression()  
cv_results = cross_val_score(reg, X, y, cv=kf)
```

Evaluating cross-validation performance

```
print(cv_results)
```

```
[0.70262578, 0.7659624, 0.75188205, 0.76914482, 0.72551151, 0.73608277]
```

```
print(np.mean(cv_results), np.std(cv_results))
```

```
0.7418682216666667 0.023330243960652888
```

```
print(np.quantile(cv_results, [0.025, 0.975]))
```

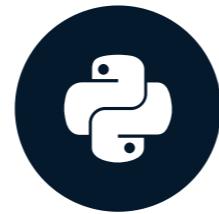
```
array([0.7054865, 0.76874702])
```

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Regularized regression

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Why regularize?

- Recall: Linear regression minimizes a loss function
- It chooses a coefficient, a , for each feature variable, plus b
- Large coefficients can lead to overfitting
- Regularization: Penalize large coefficients

Ridge regression

- Loss function = OLS loss function +

$$\alpha * \sum_{i=1}^n a_i^2$$

- Ridge penalizes large positive or negative coefficients
- α : parameter we need to choose
- Picking α is similar to picking k in KNN
- Hyperparameter: variable used to optimize model parameters
- α controls model complexity
 - $\alpha = 0$ = OLS (Can lead to overfitting)
 - Very high α : Can lead to underfitting

Ridge regression in scikit-learn

```
from sklearn.linear_model import Ridge
scores = []
for alpha in [0.1, 1.0, 10.0, 100.0, 1000.0]:
    ridge = Ridge(alpha=alpha)
    ridge.fit(X_train, y_train)
    y_pred = ridge.predict(X_test)
    scores.append(ridge.score(X_test, y_test))
print(scores)
```

```
[0.2828466623222221, 0.28320633574804777, 0.2853000732200006,
0.26423984812668133, 0.19292424694100963]
```

Lasso regression

- Loss function = OLS loss function +

$$\alpha * \sum_{i=1}^n |a_i|$$

Lasso regression in scikit-learn

```
from sklearn.linear_model import Lasso
scores = []
for alpha in [0.01, 1.0, 10.0, 20.0, 50.0]:
    lasso = Lasso(alpha=alpha)
    lasso.fit(X_train, y_train)
    lasso_pred = lasso.predict(X_test)
    scores.append(lasso.score(X_test, y_test))
print(scores)
```

```
[0.99991649071123, 0.99961700284223, 0.93882227671069, 0.74855318676232, -0.05741034640016]
```

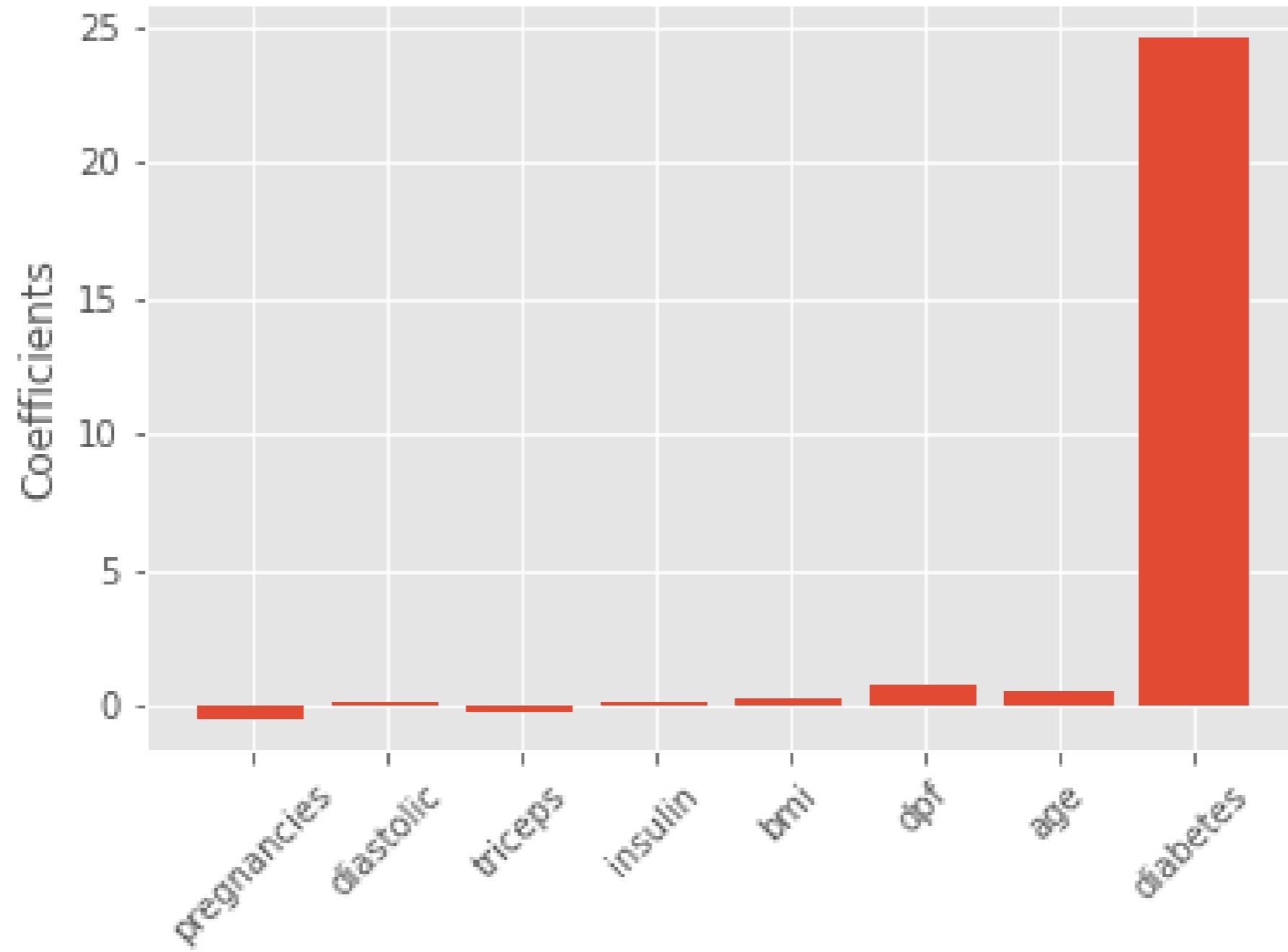
Lasso regression for feature selection

- Lasso can select important features of a dataset
- Shrinks the coefficients of less important features to zero
- Features not shrunk to zero are selected by lasso

Lasso for feature selection in scikit-learn

```
from sklearn.linear_model import Lasso  
X = diabetes_df.drop("glucose", axis=1).values  
y = diabetes_df["glucose"].values  
names = diabetes_df.drop("glucose", axis=1).columns  
lasso = Lasso(alpha=0.1)  
lasso_coef = lasso.fit(X, y).coef_  
plt.bar(names, lasso_coef)  
plt.xticks(rotation=45)  
plt.show()
```

Lasso for feature selection in scikit-learn



Let's practice!

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