

# Initialization

Welcome to the first assignment of "Improving Deep Neural Networks".

Training your neural network requires specifying an initial value of the weights. A well chosen initialization method will help learning.

If you completed the previous course of this specialization, you probably followed our instructions for weight initialization, and it has worked out so far. But how do you choose the initialization for a new neural network? In this notebook, you will see how different initializations lead to different results.

A well chosen initialization can:

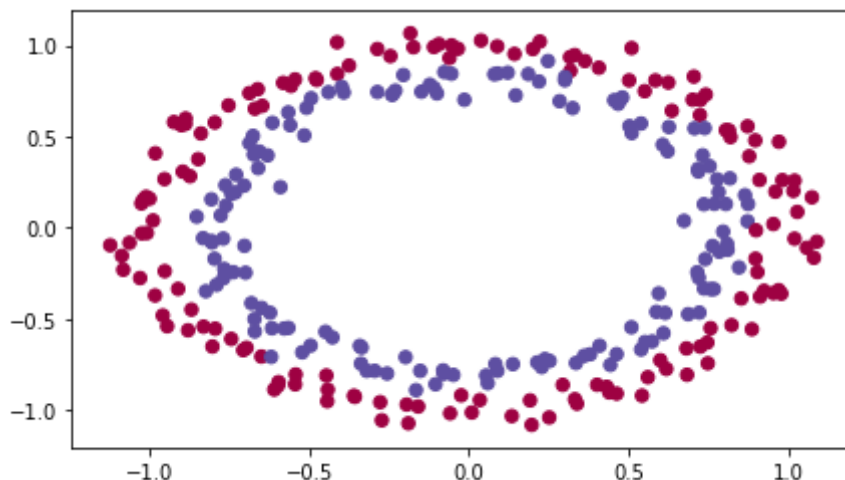
- Speed up the convergence of gradient descent
- Increase the odds of gradient descent converging to a lower training (and generalization) error

To get started, run the following cell to load the packages and the planar dataset you will try to classify.

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
import sklearn
import sklearn.datasets
from init_utils import sigmoid, relu, compute_loss, forward_propagation, backward_propagation
from init_utils import update_parameters, predict, load_dataset, plot_decision_boundary

%matplotlib inline
plt.rcParams['figure.figsize'] = (7.0, 4.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# load image dataset: blue/red dots in circles
train_X, train_Y, test_X, test_Y = load_dataset()
```



You would like a classifier to separate the blue dots from the red dots.

# 1 - Neural Network model

You will use a 3-layer neural network (already implemented for you). Here are the initialization methods you will experiment with:

- *Zeros initialization* -- setting `initialization = "zeros"` in the input argument.
- *Random initialization* -- setting `initialization = "random"` in the input argument. This initializes the weights to large random values.
- *He initialization* -- setting `initialization = "he"` in the input argument. This initializes the weights to random values scaled according to a paper by He et al., 2015.

**Instructions:** Please quickly read over the code below, and run it. In the next part you will implement the three initialization methods that this `model()` calls.

```

In [2]: def model(X, Y, learning_rate = 0.01, num_iterations = 15000, print_cost =
        """
        Implements a three-layer neural network: LINEAR->RELU->LINEAR->RELU->LI

Arguments:
X -- input data, of shape (2, number of examples)
Y -- true "label" vector (containing 0 for red dots; 1 for blue dots),
learning_rate -- learning rate for gradient descent
num_iterations -- number of iterations to run gradient descent
print_cost -- if True, print the cost every 1000 iterations
initialization -- flag to choose which initialization to use ("zeros", "

Returns:
parameters -- parameters learnt by the model
"""

    grads = {}
    costs = [] # to keep track of the loss
    m = X.shape[1] # number of examples
    layers_dims = [X.shape[0], 10, 5, 1]

    # Initialize parameters dictionary.
    if initialization == "zeros":
        parameters = initialize_parameters_zeros(layers_dims)
    elif initialization == "random":
        parameters = initialize_parameters_random(layers_dims)
    elif initialization == "he":
        parameters = initialize_parameters_he(layers_dims)

    # Loop (gradient descent)

    for i in range(0, num_iterations):

        # Forward propagation: LINEAR -> RELU -> LINEAR -> RELU -> LINEAR -
        a3, cache = forward_propagation(X, parameters)

        # Loss
        cost = compute_loss(a3, Y)

        # Backward propagation.
        grads = backward_propagation(X, Y, cache)

        # Update parameters.
        parameters = update_parameters(parameters, grads, learning_rate)

        # Print the loss every 1000 iterations
        if print_cost and i % 1000 == 0:
            print("Cost after iteration {}: {}".format(i, cost))
            costs.append(cost)

        # plot the loss
        plt.plot(costs)
        plt.ylabel('cost')
        plt.xlabel('iterations (per hundreds)')
        plt.title("Learning rate =" + str(learning_rate))
        plt.show()

```

```
return parameters
```

## 2 - Zero initialization

There are two types of parameters to initialize in a neural network:

- the weight matrices ( $W^{[1]}, W^{[2]}, W^{[3]}, \dots, W^{[L-1]}, W^{[L]}$ )
- the bias vectors ( $b^{[1]}, b^{[2]}, b^{[3]}, \dots, b^{[L-1]}, b^{[L]}$ )

**Exercise:** Implement the following function to initialize all parameters to zeros. You'll see later that this does not work well since it fails to "break symmetry", but lets try it anyway and see what happens. Use `np.zeros(...)` with the correct shapes.

```
In [5]: # GRADED FUNCTION: initialize_parameters_zeros

def initialize_parameters_zeros(layers_dims):
    """
    Arguments:
    layer_dims -- python array (list) containing the size of each layer.

    Returns:
    parameters -- python dictionary containing your parameters "W1", "b1",
                  W1 -- weight matrix of shape (layers_dims[1], layers_dims[0])
                  b1 -- bias vector of shape (layers_dims[1], 1)
                  ...
                  WL -- weight matrix of shape (layers_dims[L], layers_dims[L-1])
                  bL -- bias vector of shape (layers_dims[L], 1)
    """

    parameters = {}
    L = len(layers_dims)           # number of layers in the network

    for l in range(1, L):
        ### START CODE HERE ### (~ 2 lines of code)
        parameters['W' + str(l)] = np.zeros( ( layers_dims[l], layers_dims[l-1] ) )
        parameters['b' + str(l)] = np.zeros( ( layers_dims[l], 1 ) )
        ### END CODE HERE ###
    return parameters
```

```
In [6]: parameters = initialize_parameters_zeros([3,2,1])
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
```

```
W1 = [[0. 0. 0.]
      [0. 0. 0.]]
b1 = [[0.]
      [0.]]
W2 = [[0. 0.]]
b2 = [[0.]]
```

**Expected Output:**

```

**W1**  [[ 0. 0. 0.] [ 0. 0. 0.]]

**b1**           [[ 0.] [ 0.]]

**W2**           [[ 0. 0.]]

**b2**           [[ 0.]]

```

Run the following code to train your model on 15,000 iterations using zeros initialization.

```

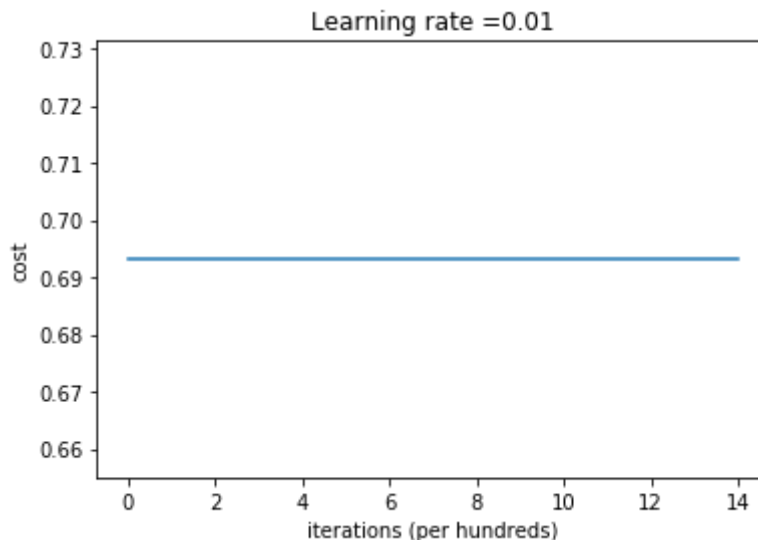
In [7]: parameters = model(train_X, train_Y, initialization = "zeros")
print ("On the train set:")
predictions_train = predict(train_X, train_Y, parameters)
print ("On the test set:")
predictions_test = predict(test_X, test_Y, parameters)

```

```

Cost after iteration 0: 0.6931471805599453
Cost after iteration 1000: 0.6931471805599453
Cost after iteration 2000: 0.6931471805599453
Cost after iteration 3000: 0.6931471805599453
Cost after iteration 4000: 0.6931471805599453
Cost after iteration 5000: 0.6931471805599453
Cost after iteration 6000: 0.6931471805599453
Cost after iteration 7000: 0.6931471805599453
Cost after iteration 8000: 0.6931471805599453
Cost after iteration 9000: 0.6931471805599453
Cost after iteration 10000: 0.6931471805599455
Cost after iteration 11000: 0.6931471805599453
Cost after iteration 12000: 0.6931471805599453
Cost after iteration 13000: 0.6931471805599453
Cost after iteration 14000: 0.6931471805599453

```



```

On the train set:
Accuracy: 0.5
On the test set:
Accuracy: 0.5

```

The performance is really bad, and the cost does not really decrease, and the algorithm performs no better than random guessing. Why? Lets look at the details of the predictions and the decision



### 3 - Random initialization

To break symmetry, let's initialize the weights randomly. Following random initialization, each neuron can then proceed to learn a different function of its inputs. In this exercise, you will see what happens if the weights are initialized randomly, but to very large values.

**Exercise:** Implement the following function to initialize your weights to large random values (scaled by \*10) and your biases to zeros. Use `np.random.randn(...)*10` for weights and `np.zeros(...)` for biases. We are using a fixed `np.random.seed(...)` to make sure your "random" weights match ours, so don't worry if running several times your code gives you always the same initial values for the parameters.

```
In [13]: # GRADED FUNCTION: initialize_parameters_random

def initialize_parameters_random(layers_dims):
    """
    Arguments:
    layer_dims -- python array (list) containing the size of each layer.

    Returns:
    parameters -- python dictionary containing your parameters "W1", "b1",
        W1 -- weight matrix of shape (layers_dims[1], layers_dims[0])
        b1 -- bias vector of shape (layers_dims[1], 1)
        ...
        WL -- weight matrix of shape (layers_dims[L], layers_dims[L-1])
        bL -- bias vector of shape (layers_dims[L], 1)
    """

    np.random.seed(3)
    parameters = {}
    L = len(layers_dims)

    for l in range(1, L):
        ### START CODE HERE ### (~ 2 lines of code)
        parameters['W' + str(l)] = np.random.randn(layers_dims[l], layers_dims[l-1]) * 10
        parameters['b' + str(l)] = np.zeros((layers_dims[l], 1))
        ### END CODE HERE ###

    return parameters
```

```
In [14]: parameters = initialize_parameters_random([3, 2, 1])
print("W1 = " + str(parameters["W1"]))
print("b1 = " + str(parameters["b1"]))
print("W2 = " + str(parameters["W2"]))
print("b2 = " + str(parameters["b2"]))
```

```
W1 = [[ 17.88628473  4.36509851  0.96497468]
      [-18.63492703 -2.77388203 -3.54758979]]
b1 = [[0.]
      [0.]]
W2 = [[-0.82741481 -6.27000677]]
b2 = [[0.]
```

**Expected Output:**

```
-----  
**W1** [[ 17.88628473  4.36509851  0.96497468] [-18.63492703 -2.77388203 -3.54758979]]  
**b1** [[ 0.] [ 0.]]  
**W2** [[-0.82741481 -6.27000677]]  
**b2** [[ 0.]]
```

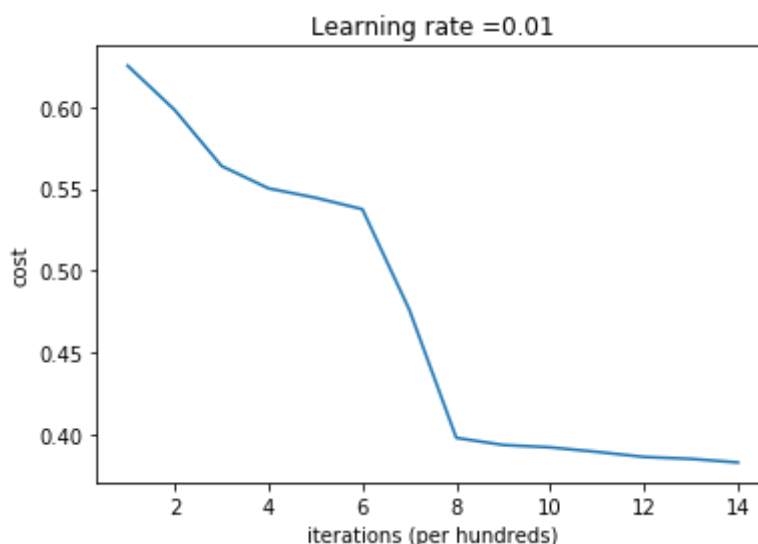
Run the following code to train your model on 15,000 iterations using random initialization.



```
In [15]: parameters = model(train_X, train_Y, initialization = "random")
print ("On the train set:")
predictions_train = predict(train_X, train_Y, parameters)
print ("On the test set:")
predictions_test = predict(test_X, test_Y, parameters)
```

```
/Users/gshyam/projects/work_projects/machine_learning/machinelearning44/D
eepLearning-2_improving_deepNN/assignments/week1/initialization/init_util
ls.py:145: RuntimeWarning: divide by zero encountered in log
  logprobs = np.multiply(-np.log(a3),Y) + np.multiply(-np.log(1 - a3), 1
- Y)
/Users/gshyam/projects/work_projects/machine_learning/machinelearning44/D
eepLearning-2_improving_deepNN/assignments/week1/initialization/init_util
ls.py:145: RuntimeWarning: invalid value encountered in multiply
  logprobs = np.multiply(-np.log(a3),Y) + np.multiply(-np.log(1 - a3), 1
- Y)
```

```
Cost after iteration 0: inf
Cost after iteration 1000: 0.6250884962121392
Cost after iteration 2000: 0.5981371467489438
Cost after iteration 3000: 0.5638539771863162
Cost after iteration 4000: 0.5501704762630747
Cost after iteration 5000: 0.5444592806792145
Cost after iteration 6000: 0.5374509252365552
Cost after iteration 7000: 0.4760640415643904
Cost after iteration 8000: 0.3978146724300182
Cost after iteration 9000: 0.3934785833165248
Cost after iteration 10000: 0.3920322287285902
Cost after iteration 11000: 0.38924754816043866
Cost after iteration 12000: 0.38615976417756703
Cost after iteration 13000: 0.38498687252939306
Cost after iteration 14000: 0.38278602219555746
```



```
On the train set:
Accuracy: 0.83
On the test set:
Accuracy: 0.86
```

If you see "inf" as the cost after the iteration 0, this is because of numerical roundoff; a more numerically sophisticated implementation would fix this. But this isn't worth worrying about for our

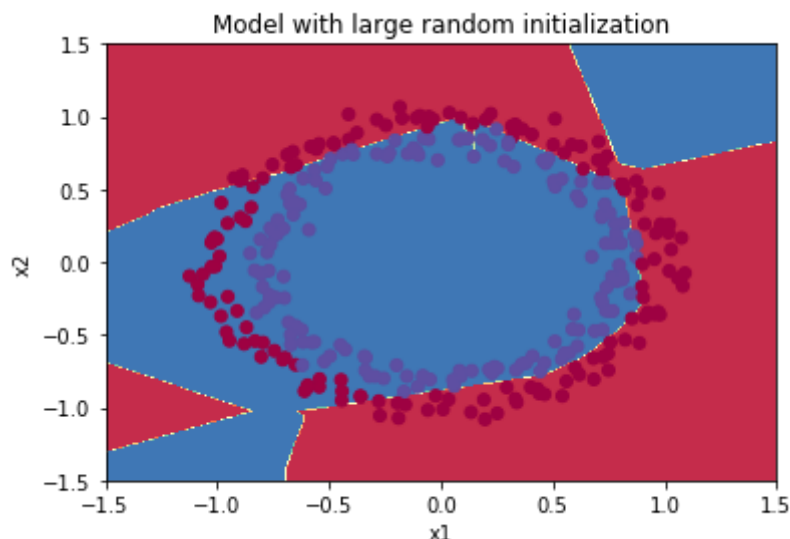
purposes.

Anyway, it looks like you have broken symmetry, and this gives better results. than before. The model is no longer outputting all 0s.

```
In [16]: print (predictions_train)
print (predictions_test)
```

```
[[1 0 1 1 0 0 1 1 1 1 1 0 1 0 0 1 0 1 1 0 0 0 1 0 1 1 1 1 1 1 0 1 1 0 0 1
 1 1 1 1 1 1 1 0 1 1 1 1 0 1 0 1 1 1 1 0 0 1 1 1 1 0 1 1 0 1 0 1 1 1 1 0
 0 0 0 0 1 0 1 0 1 1 1 0 0 1 1 1 1 1 1 0 0 1 1 1 0 1 1 0 1 0 1 1 0 1 1 0
 1 0 1 1 0 0 1 0 0 1 1 0 1 1 1 0 1 0 0 1 0 1 1 1 1 1 1 1 1 0 1 1 0 0 1 1 0
 0 0 1 0 1 0 1 0 1 1 1 0 0 1 1 1 1 0 1 1 0 1 0 1 1 0 1 1 0 1 1 1 1 0 1 1 1
 1 0 1 0 1 0 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 0 1 1 1 0 1 1 1 0 1 0 1 0 0 1
 0 1 1 0 1 1 0 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 1 1 0 1 1 1 0 0 0 1 1 0 1 1
 1 1 0 1 1 0 1 1 1 0 0 1 0 0 0 1 0 0 0 1 1 1 1 0 0 0 0 1 1 1 1 0 0 1 1 1
 1 1 1 1 0 0 0 1 1 1 1 0]]
[[1 1 1 1 0 1 0 1 1 0 1 1 1 0 0 0 0 1 0 1 0 0 1 0 1 0 1 1 1 1 1 0 0 0 0 1
 0 1 1 0 0 1 1 1 1 0 1 1 1 0 1 0 1 1 0 1 0 1 0 1 1 1 1 1 1 1 1 1 0 1 0
 1 1 1 1 1 0 1 0 0 1 0 0 0 1 1 0 1 1 0 0 0 1 1 0 1 1 0 0 0]]
```

```
In [17]: plt.title("Model with large random initialization")
axes = plt.gca()
axes.set_xlim([-1.5,1.5])
axes.set_ylim([-1.5,1.5])
plot_decision_boundary(lambda x: predict_dec(parameters, x.T), train_X, tra
```



### Observations:

- The cost starts very high. This is because with large random-valued weights, the last activation (sigmoid) outputs results that are very close to 0 or 1 for some examples, and when it gets that example wrong it incurs a very high loss for that example. Indeed, when  $\log(a^{[3]}) = \log(0)$ , the loss goes to infinity.
- Poor initialization can lead to vanishing/exploding gradients, which also slows down the optimization algorithm.
- If you train this network longer you will see better results, but initializing with overly large random numbers slows down the optimization.

**\*\*In summary\*\***: - Initializing weights to very large random values does not work well. - Hopefully initializing with small random values does better. The important question is: how small should be these random values be? Lets find out in the next part!

## 4 - He initialization

Finally, try "He Initialization"; this is named for the first author of He et al., 2015. (If you have heard of "Xavier initialization", this is similar except Xavier initialization uses a scaling factor for the weights  $W^{[l]}$  of  $\sqrt{1./\text{layers\_dims}[l-1]}$  where He initialization would use  $\sqrt{2./\text{layers\_dims}[l-1]}$ .)

**Exercise**: Implement the following function to initialize your parameters with He initialization.

**Hint**: This function is similar to the previous `initialize_parameters_random(...)`. The only difference is that instead of multiplying `np.random.randn(...)` by 10, you will multiply it by  $\sqrt{\frac{2}{\text{dimension of the previous layer}}}$ , which is what He initialization recommends for layers with a ReLU activation.

```
In [20]: # GRADED FUNCTION: initialize_parameters_he

def initialize_parameters_he(layers_dims):
    """
    Arguments:
    layer_dims -- python array (list) containing the size of each layer.

    Returns:
    parameters -- python dictionary containing your parameters "W1", "b1",
        W1 -- weight matrix of shape (layers_dims[1], layers_dims[0])
        b1 -- bias vector of shape (layers_dims[1], 1)
        ...
        WL -- weight matrix of shape (layers_dims[L], layers_dims[L-1])
        bL -- bias vector of shape (layers_dims[L], 1)
    """

    np.random.seed(3)
    parameters = {}
    L = len(layers_dims) - 1 # integer representing the number of layers

    for l in range(1, L + 1):
        ### START CODE HERE ### (~ 2 lines of code)
        parameters['W' + str(l)] = np.random.randn(layers_dims[l], layers_dims[l-1])
        parameters['b' + str(l)] = np.zeros((layers_dims[l], 1))
        ### END CODE HERE ###

    return parameters
```

```
In [21]: parameters = initialize_parameters_he([2, 4, 1])
print("w1 = " + str(parameters["w1"]))
print("b1 = " + str(parameters["b1"]))
print("w2 = " + str(parameters["w2"]))
print("b2 = " + str(parameters["b2"]))

w1 = [[ 1.78862847  0.43650985]
      [ 0.09649747 -1.8634927 ]
      [-0.2773882  -0.35475898]
      [-0.08274148 -0.62700068]]
b1 = [[0.]
      [0.]
      [0.]
      [0.]]
w2 = [[-0.03098412 -0.33744411 -0.92904268  0.62552248]]
b2 = [[0.]]
```

**Expected Output:**

```
**w1**          [[ 1.78862847 0.43650985] [ 0.09649747 -1.8634927 ] [-0.2773882 -0.35475898] [-0.08274148
                                                         -0.62700068]]

**b1**                                                  [[ 0.] [ 0.] [ 0.] [ 0.]]

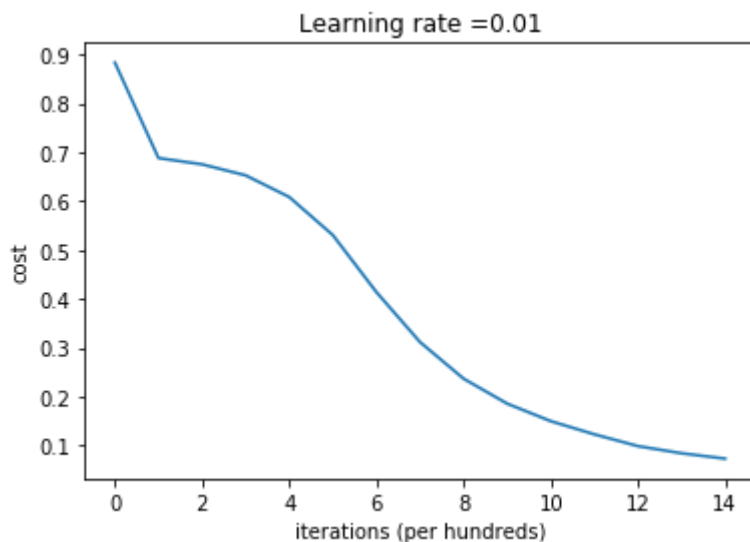
**w2**                                                  [[-0.03098412 -0.33744411 -0.92904268 0.62552248]]

**b2**                                                  [[ 0.]]
```

Run the following code to train your model on 15,000 iterations using He initialization.

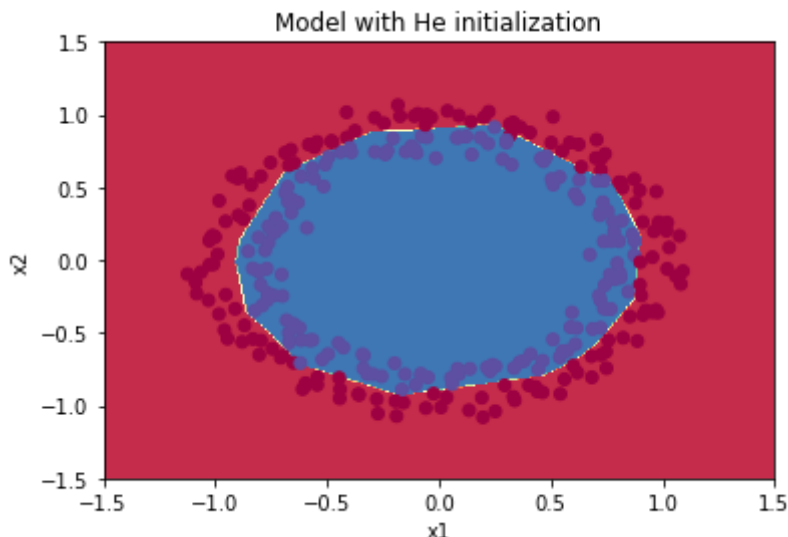
```
In [22]: parameters = model(train_X, train_Y, initialization = "he")
print ("On the train set:")
predictions_train = predict(train_X, train_Y, parameters)
print ("On the test set:")
predictions_test = predict(test_X, test_Y, parameters)
```

```
Cost after iteration 0: 0.8830537463419761
Cost after iteration 1000: 0.6879825919728063
Cost after iteration 2000: 0.6751286264523371
Cost after iteration 3000: 0.6526117768893807
Cost after iteration 4000: 0.6082958970572938
Cost after iteration 5000: 0.5304944491717495
Cost after iteration 6000: 0.4138645817071795
Cost after iteration 7000: 0.31178034648444414
Cost after iteration 8000: 0.2369621533032257
Cost after iteration 9000: 0.18597287209206845
Cost after iteration 10000: 0.1501555628037181
Cost after iteration 11000: 0.12325079292273548
Cost after iteration 12000: 0.09917746546525937
Cost after iteration 13000: 0.08457055954024273
Cost after iteration 14000: 0.07357895962677366
```



```
On the train set:
Accuracy: 0.9933333333333333
On the test set:
Accuracy: 0.96
```

```
In [23]: plt.title("Model with He initialization")
axes = plt.gca()
axes.set_xlim([-1.5,1.5])
axes.set_ylim([-1.5,1.5])
plot_decision_boundary(lambda x: predict_dec(parameters, x.T), train_X, tra
```



### Observations:

- The model with He initialization separates the blue and the red dots very well in a small number of iterations.

## 5 - Conclusions

You have seen three different types of initializations. For the same number of iterations and same hyperparameters the comparison is:

**Model**	**Train accuracy**	**Problem/Comment**
3-layer NN with zeros initialization	50%	fails to break symmetry
3-layer NN with large random initialization	83%	too large weights
3-layer NN with He initialization	99%	recommended method

**\*\*What you should remember from this notebook\*\*:** - Different initializations lead to different results  
 - Random initialization is used to break symmetry and make sure different hidden units can learn

different things - Don't initialize to values that are too large - He initialization works well for networks with ReLU activations.