

## Join GitHub today

[Dismiss](#)

GitHub is home to over 40 million developers working together to host and review code, manage projects, and build software together.

[Sign up](#)Branch: **master** ▼[Find file](#)[Copy path](#)

[deep-learning-specialization-coursera](#) / [02-Improving-Deep-Neural-Networks](#) / [week3](#) / [hyperparameter-tuning-and-programming-frameworks.ipynb](#)

**andersy005** add datasets

64a8031 on Oct 15, 2018

[1 contributor](#)[Raw](#)[Blame](#)[History](#)

455 lines (455 sloc) 12.7 KB

# Table of Contents

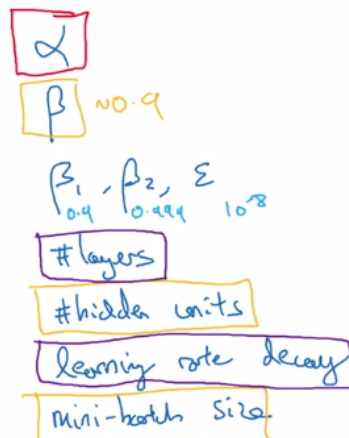
- 1. Hyperparameter tuning, Batch Normalization and Programming Frameworks
  - 1.1 Hyperparameter Tuning
    - 1.1.1 Tuning Process
    - 1.1.2 Using an appropriate scale to pick hyperparameters
    - 1.1.3 Hyperparameters tuning in practice: Pandas vs. Caviar
  - 1.2 Batch Normalization
    - 1.2.1 Normalizing activations in a network
    - 1.2.2 Fitting Batch Norm into a neural network
    - 1.2.3 Why does Batch Norm work?
    - 1.2.4 Batch Norm at test time
  - 1.3 Multi-class classification
    - 1.3.1 Softmax Regression
    - 1.3.2 Training a softmax classifier
  - 1.4 Introduction to programming frameworks
    - 1.4.1 Deep Learning Frameworks
    - 1.4.2 TensorFlow

## Hyperparameter tuning, Batch Normalization and Programming Frameworks

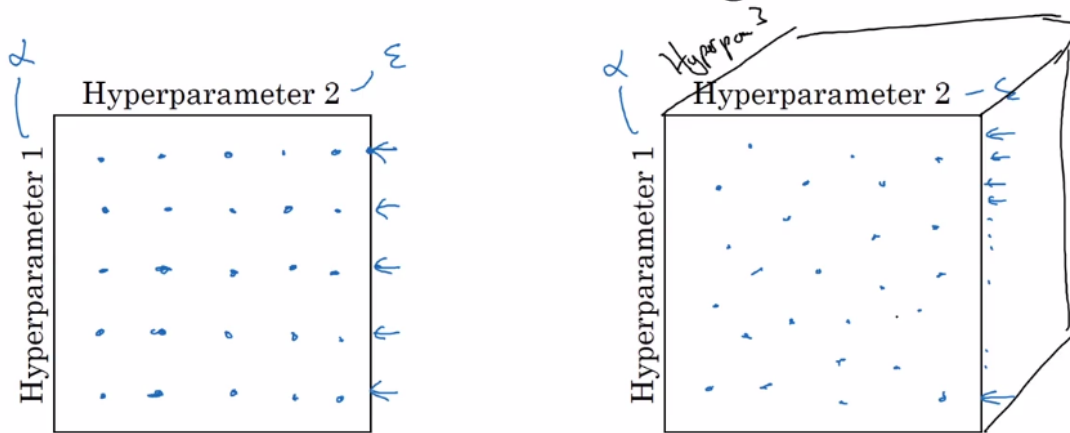
### Hyperparameter Tuning

#### Tuning Process

#### Hyperparameters

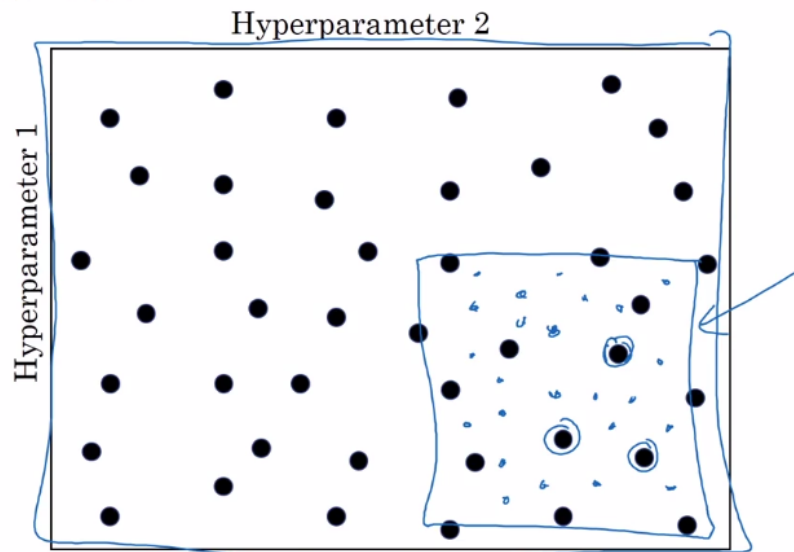


# Try random values: Don't use a grid



Andrew Ng

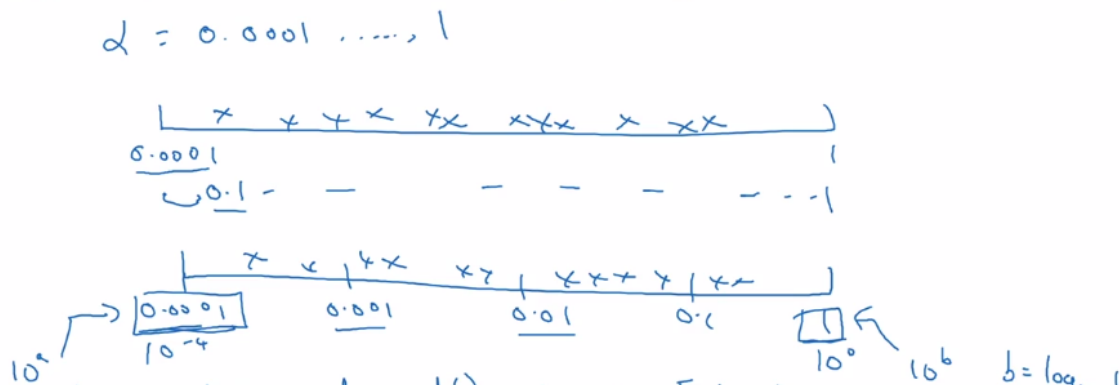
## Coarse to fine



Andrew Ng

## Using an appropriate scale to pick hyperparameters

### Appropriate scale for hyperparameters



$$a = \log_{10}(0.0001) \quad r = -4 * \text{np.random.randn}(1) \quad \leftarrow r \in [-4, 0] \quad \text{---} = 10^1$$

$$= -4 \quad \alpha = 10^r \quad \leftarrow 10^{-4} \dots 10^0$$

$$\underline{10^{-4} \dots 10^0} \quad \underline{r \in [a, b]} \quad \underline{\alpha = 10^r}$$

Andrew Ng

## Hyperparameters for exponentially weighted averages

$$\beta = 0.9 \dots 0.999$$

$$\downarrow \quad \quad \quad \downarrow$$

$$10 \quad \quad \quad 1000$$

$$1 - \beta = 0.1 \dots 0.001$$


---


$$\beta: 0.9000 \rightarrow 0.9005 \quad \sim 10$$

$$\beta: 0.999 \rightarrow 0.9995 \quad \sim 1000$$

$$\frac{1}{1 - \beta}$$

$$\beta = 0.9 \dots 0.999$$

$$\downarrow \quad \quad \quad \downarrow$$

$$0.1 \quad \quad \quad 0.001$$

$$10^{-1} \quad \quad \quad 10^{-3}$$

$$r \in [-3, -1]$$

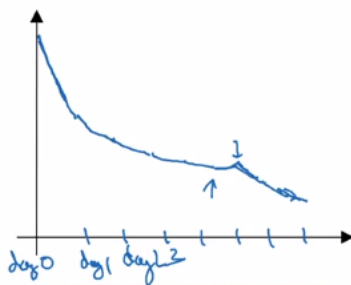
$$1 - \beta = 10^r$$

$$\beta = 1 - 10^r$$

Andrew Ng

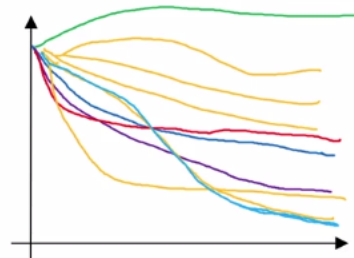
## Hyperparameters tuning in practice: Pandas vs. Caviar

### Babysitting one model



Panda ←

### Training many models in parallel



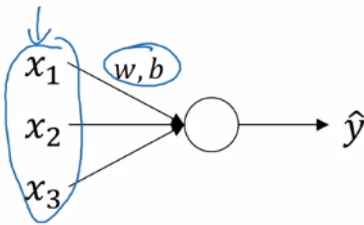
Caviar ←

Andrew Ng

## Batch Normalization

## Normalizing activations in a network

### Normalizing inputs to speed up learning



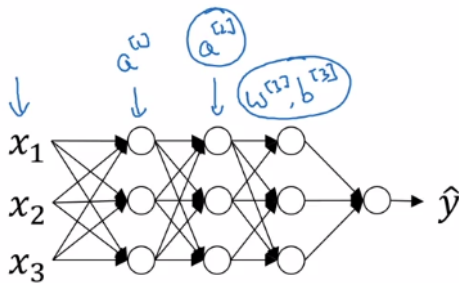
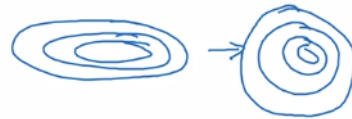
$$\mu = \frac{1}{m} \sum_i x^{(i)}$$

$$X = X - \mu$$

$$\sigma^2 = \frac{1}{m} \sum_i x^{(i)2}$$

$$X = X / \sigma^2$$

← element-wise



Can we normalize  $\frac{a^{[2]}}{w^{[12]}, b^{[12]}}$  so as to train faster?

Normalize  $z^{[2]}$

↑

Andrew Ng

### Implementing Batch Norm

Given some intermediate values in NN

$$\mu = \frac{1}{m} \sum_i z^{(i)}$$

$$\sigma^2 = \frac{1}{m} \sum_i (z^{(i)} - \mu)^2$$

$$z_{\text{norm}}^{(i)} = \frac{z^{(i)} - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

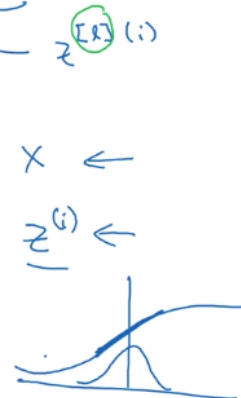
$$\hat{z}^{(i)} = \gamma z_{\text{norm}}^{(i)} + \beta$$

If  $\gamma = \sqrt{\sigma^2 + \epsilon}$

$\beta = \mu$

then  $\hat{z}^{(i)} = z^{(i)}$

learnable parameters of model.

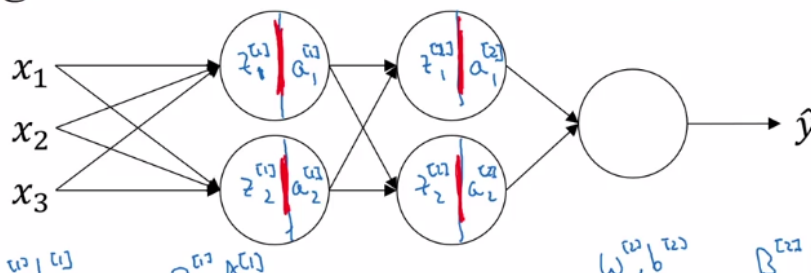


Use  $\gamma^{[12]}$  instead of  $\gamma^{[1]}$ .

Andrew Ng

### Fitting Batch Norm into a neural network

### Adding Batch Norm to a network



$$\begin{aligned}
 & X \xrightarrow{W^{[1]}, b^{[1]}} z^{[1]} \xrightarrow{\text{Batch Norm (BN)}} \tilde{z}^{[1]} \xrightarrow{W^{[2]}, b^{[2]}} a^{[2]} = g(z^{[2]}) \rightarrow z^{[2]} \xrightarrow{\text{BN}} \tilde{z}^{[2]} \rightarrow a^{[3]} \rightarrow \dots \\
 & \text{Parameters: } \{W^{[1]}, b^{[1]}, W^{[2]}, b^{[2]}, \dots, W^{[L]}, b^{[L]}\} \quad d\beta^{[L]} \quad \beta = \beta - \alpha d\beta^{[L]} \\
 & \quad \rightarrow \beta^{[1]}, \gamma^{[1]}, \beta^{[2]}, \gamma^{[2]}, \dots, \beta^{[L]}, \gamma^{[L]} \quad \text{tf.nn.batch-normalization} \leftarrow \\
 & \quad \rightarrow \beta
 \end{aligned}$$

Andrew Ng

## Working with mini-batches

$$\begin{aligned}
 & X^{[13]} \xrightarrow{W^{[1]}, b^{[1]}} z^{[1]} \xrightarrow{\text{BN}} \tilde{z}^{[1]} \xrightarrow{W^{[2]}, b^{[2]}} a^{[2]} \rightarrow z^{[2]} \rightarrow \dots \\
 & \boxed{X^{[23]}} \xrightarrow{W^{[1]}, b^{[1]}} z^{[1]} \xrightarrow{\text{BN}} \tilde{z}^{[1]} \rightarrow \dots \\
 & X^{[22]} \rightarrow \dots \\
 & \text{Parameters: } W^{[1]}, \cancel{b^{[1]}}, \beta^{[1]}, \gamma^{[1]}, \dots \\
 & \quad \quad \quad \uparrow \quad \quad \quad \uparrow \quad \quad \quad \uparrow \\
 & \quad \quad \quad (n^{[1]}, 1) \quad (n^{[2]}, 1) \quad (n^{[3]}, 1) \\
 & \quad \quad \quad \uparrow \quad \quad \quad \uparrow \quad \quad \quad \uparrow \\
 & \quad \quad \quad z^{[1]}_{(n^{[1]}, 1)} \quad z^{[2]}_{(n^{[2]}, 1)} \quad z^{[3]}_{(n^{[3]}, 1)} \\
 & \quad \quad \quad \rightarrow \tilde{z}^{[1]} = W^{[1]} a^{[0]} + \cancel{b^{[1]}} \quad \uparrow \\
 & \quad \quad \quad z^{[1]} = W^{[1]} a^{[0]} \\
 & \quad \quad \quad z^{[1]}_{\text{norm}} = \gamma^{[1]} z^{[1]} / \beta^{[1]} \quad \boxed{\beta^{[1]}} \leftarrow
 \end{aligned}$$

Andrew Ng

## Implementing gradient descent

for  $t = 1 \dots \text{num MiniBatches}$   
 Compute forward pass on  $X^{[t+1]}$ .

In each hidden layer, use BN to replace  $z^{[l]}$  with  $\tilde{z}^{[l]}$ .

Use backprop to compute  $dW^{[l]}, d\beta^{[l]}, d\gamma^{[l]}$

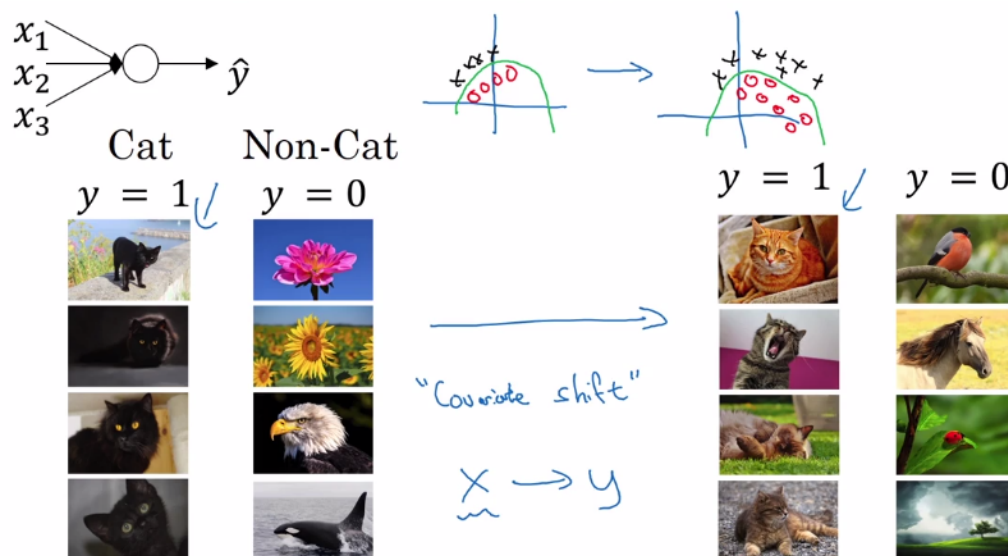
$$\begin{aligned}
 & \text{Update parameters } \left. \begin{aligned} W^{[l]} &:= W^{[l]} - \alpha dW^{[l]} \\ \beta^{[l]} &:= \beta^{[l]} - \alpha d\beta^{[l]} \\ \gamma^{[l]} &:= \dots \end{aligned} \right\} \leftarrow
 \end{aligned}$$

Works w/ momentum, RMSprop, Adam.

## Why does Batch Norm work?

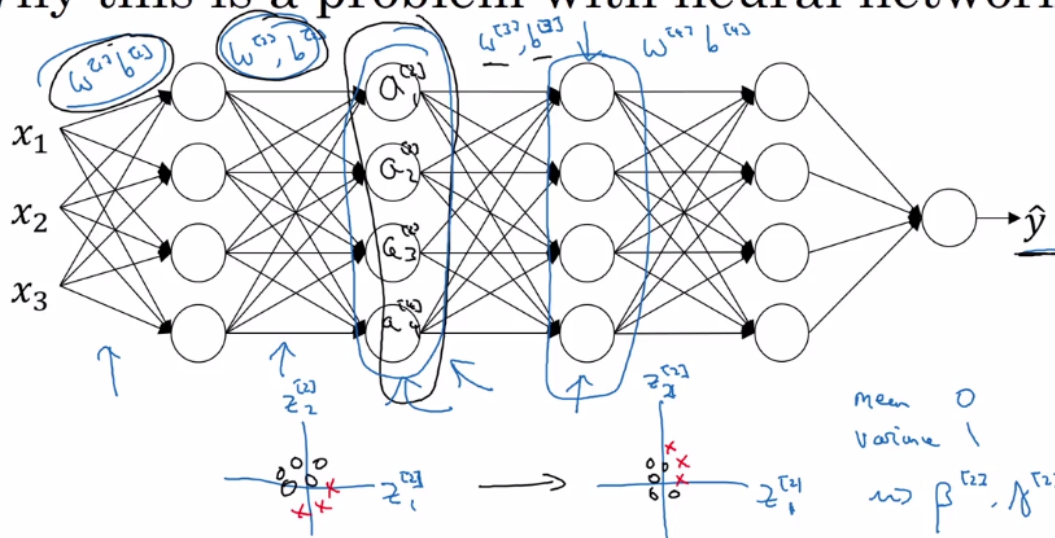
## Learning on shifting input distribution





Andrew Ng

## Why this is a problem with neural networks?



Andrew Ng

## Batch Norm as regularization

- Each mini-batch is scaled by the mean/variance computed on just that mini-batch.
- This adds some noise to the values  $z^{[l]}$  within that minibatch. So similar to dropout, it adds some noise to each hidden layer's activations.
- This has a slight regularization effect.

mini-batch: 64  $\rightarrow$  512

## Batch Norm at test time

### Batch Norm at test time

$$\mu = \frac{1}{m} \sum_i z^{(i)}$$

$$\sigma^2 = \frac{1}{m} \sum_i (z^{(i)} - \mu)^2$$

$$z_{\text{norm}}^{(i)} = \frac{z^{(i)} - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

$$\tilde{z}^{(i)} = \gamma z_{\text{norm}}^{(i)} + \beta$$

$\mu, \sigma^2$ : estimate using exponentially weighted average (across mini-batches).  
 $X^{[1]}, X^{[2]}, X^{[3]}, \dots$   
 $\mu^{[1]}, \mu^{[2]}, \mu^{[3]}, \dots \rightarrow \mu$   
 $\sigma^{[1]}, \sigma^{[2]}, \sigma^{[3]}, \dots \rightarrow \sigma^2$   
 $z_{\text{norm}} = \frac{z - \mu}{\sqrt{\sigma^2 + \epsilon}}$   
 $\tilde{z} = \gamma z_{\text{norm}} + \beta$

Andrew Ng

## Multi-class classification

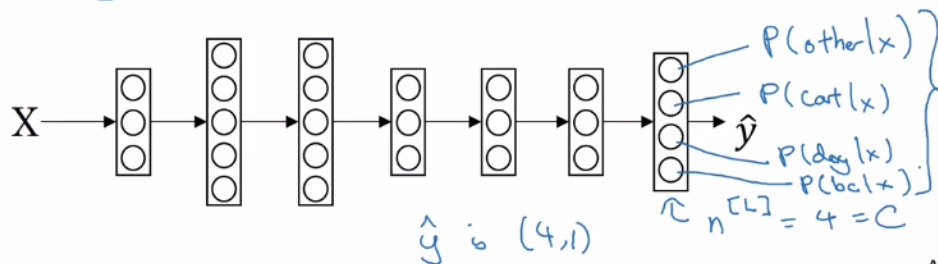
### Softmax Regression

Recognizing cats, dogs, and baby chicks, other



3 1 2 0 3 2 0 1

$C = \# \text{classes} = 4$  (0, ..., 3)



Andrew Ng

### Softmax layer

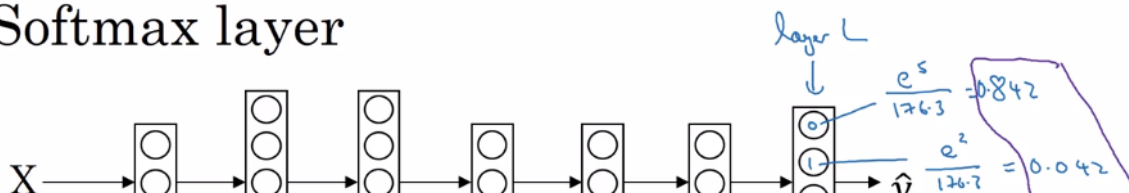




Diagram showing a neural network layer with 6 nodes. The first five nodes are inactive (0), and the sixth node is active (5). The handwritten notes show the calculation of the softmax output for the active node.

$$z^{[L]} = w^{[L]} a^{[L-1]} + b^{[L]} \quad (4,1)$$

$$z^{[L]} = \begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix}$$

Activation function:

$$t = e^{z^{[L]}} \quad (4,1)$$

$$a^{[L]} = \frac{e^{z^{[L]}}}{\sum_{j=1}^4 t_j}, \quad a_i = \frac{t_i}{\sum_{j=1}^4 t_j}$$

$$a^{[L]} = g^{[L]}(z^{[L]}) \quad (4,1)$$

$$t = \begin{bmatrix} e^5 \\ e^2 \\ e^{-1} \\ e^3 \end{bmatrix} = \begin{bmatrix} 148.4 \\ 7.4 \\ 0.4 \\ 20.1 \end{bmatrix}, \quad \sum_{j=1}^4 t_j = 176.3$$

$$a^{[L]} = \frac{t}{176.3}$$

Handwritten calculations for the active node (5):

$$\frac{e^{-1}}{176.3} = 0.002$$

$$\frac{e^3}{176.3} = 0.114$$

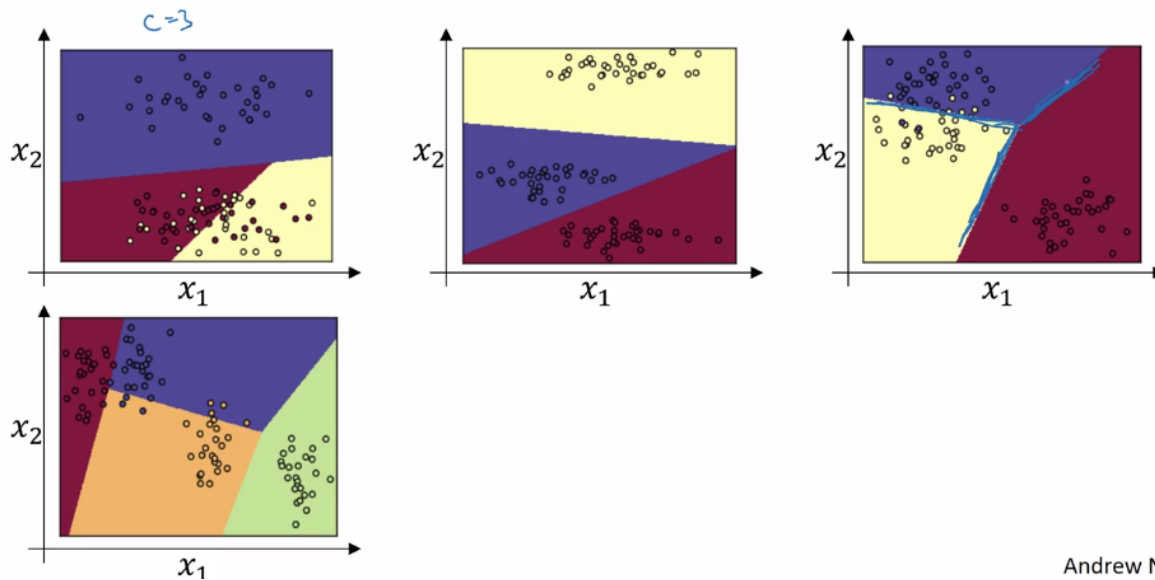
Andrew Ng

## Softmax examples

$$x_1, x_2 \rightarrow \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \rightarrow \hat{y}$$

$$z^{[L]} = w^{[L]} x + b^{[L]}$$

$$a^{[L]} = \hat{y} = g(z^{[L]})$$



Andrew Ng

## Training a softmax classifier

## Understanding softmax

Diagram showing the softmax function for a 4-class problem. The input vector  $z^{[L]}$  is  $\begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix}$ . The output vector  $a^{[L]}$  is  $\begin{bmatrix} 0.842 \\ 0.042 \\ 0.002 \\ 0.114 \end{bmatrix}$ .

$$z^{[L]} = \begin{bmatrix} 5 \\ 2 \\ -1 \\ 3 \end{bmatrix}, \quad t = \begin{bmatrix} e^5 \\ e^2 \\ e^{-1} \\ e^3 \end{bmatrix}$$

$$a^{[L]} = g^{[L]}(z^{[L]}) = \begin{bmatrix} e^5 / (e^5 + e^2 + e^{-1} + e^3) \\ e^2 / (e^5 + e^2 + e^{-1} + e^3) \\ e^{-1} / (e^5 + e^2 + e^{-1} + e^3) \\ e^3 / (e^5 + e^2 + e^{-1} + e^3) \end{bmatrix} = \begin{bmatrix} 0.842 \\ 0.042 \\ 0.002 \\ 0.114 \end{bmatrix}$$

Handwritten notes:

- "soft max"
- "hard max"
- $C=4$
- $g^{[L]}(\cdot)$

Softmax regression generalizes logistic regression to  $C$  classes.

If  $C=2$ , softmax reduces to logistic regress.  $a^{[L]} = \begin{bmatrix} 0.842 \\ 0.158 \end{bmatrix}$

## Loss function

$$y = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad \text{cat} \quad y_2 = 1 \quad y_1 = y_3 = y_4 = 0$$

$$\hat{y} = \begin{bmatrix} 0.3 \\ 0.2 \\ 0.1 \\ 0.4 \end{bmatrix} \quad C=4$$

$$\mathcal{L}(\hat{y}, y) = - \sum_{j=1}^C y_j \log \hat{y}_j$$

$$\mathcal{J}(w^{(1)}, b^{(1)}, \dots) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)})$$

$-y_2 \log \hat{y}_2 = -\log \hat{y}_2$       make  $\hat{y}_2$  big.

---

$Y = [y^{(1)} \ y^{(2)} \ \dots \ y^{(m)}]$        $\hat{Y} = [\hat{y}^{(1)} \ \dots \ \hat{y}^{(m)}]$

$= \begin{bmatrix} 0 & 0 & 1 & 0 & \dots \\ 1 & 0 & 0 & 0 & \dots \\ 0 & 1 & 0 & 0 & \dots \\ 0 & 0 & 0 & 0 & \dots \end{bmatrix}$        $= \begin{bmatrix} 0.3 & & & & \\ 0.2 & & & & \\ 0.1 & & & & \\ 0.4 & & & & \end{bmatrix}$

$(4, m)$        $(4, m)$

Andrew Ng

## Loss function

$$y = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \quad \text{cat} \quad y_2 = 1 \quad y_1 = y_3 = y_4 = 0$$

$$\hat{y} = \begin{bmatrix} 0.3 \\ 0.2 \\ 0.1 \\ 0.4 \end{bmatrix} \quad C=4$$

$$\mathcal{L}(\hat{y}, y) = - \sum_{j=1}^C y_j \log \hat{y}_j$$

$$\mathcal{J}(w^{(1)}, b^{(1)}, \dots) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)})$$

$-y_2 \log \hat{y}_2 = -\log \hat{y}_2$       make  $\hat{y}_2$  big.

---

$Y = [y^{(1)} \ y^{(2)} \ \dots \ y^{(m)}]$        $\hat{Y} = [\hat{y}^{(1)} \ \dots \ \hat{y}^{(m)}]$

$= \begin{bmatrix} 0 & 0 & 1 & 0 & \dots \\ 1 & 0 & 0 & 0 & \dots \\ 0 & 1 & 0 & 0 & \dots \\ 0 & 0 & 0 & 0 & \dots \end{bmatrix}$        $= \begin{bmatrix} 0.3 & & & & \\ 0.2 & & & & \\ 0.1 & & & & \\ 0.4 & & & & \end{bmatrix}$

$(4, m)$        $(4, m)$

Andrew Ng

## Introduction to programming frameworks

### Deep Learning Frameworks

## Deep learning frameworks

- Caffe/Caffe2
- CNTK
- DL4J

Choosing deep learning frameworks

- Ease of programming (development and deployment)

- Keras
  - Lasagne
  - mxnet
  - PaddlePaddle
  - TensorFlow
  - Theano
  - Torch
- Running speed
  - - Truly open (open source with good governance)

Andrew

## TensorFlow

```
In [1]: import tensorflow as tf
import numpy as np
```

```
In [2]: w = tf.Variable(0, dtype=tf.float32)
cost = tf.add(tf.add(w**2, tf.multiply(-10., w)), 25)
```

```
In [3]: train = tf.train.GradientDescentOptimizer(0.01).minimize(cost)
```

```
In [4]: init = tf.global_variables_initializer()
```

```
In [5]: session = tf.Session()
```

```
In [6]: %time session.run(init)
```

```
CPU times: user 6.07 ms, sys: 2.41 ms, total: 8.48 ms
Wall time: 5.82 ms
```

```
In [7]: print(session.run(w))
```

```
0.0
```

```
In [8]: %time session.run(train)
```

```
CPU times: user 16.1 ms, sys: 2.34 ms, total: 18.4 ms
Wall time: 15.9 ms
```

```
In [9]: %time print(session.run(w))
```

```
0.099999994
CPU times: user 815 µs, sys: 243 µs, total: 1.06 ms
Wall time: 807 µs
```

```
In [10]: %load_ext version_information
%version_information tensorflow, numpy
```

```
Out[10]:
```

Software	Version
Pvthon	3.6.6 64bit [GCC 4.2.1 Compatible Apple LLVM 6.1.0 (clang-

Python	602.0.53]
IPython	7.0.1
OS	Darwin 17.7.0 x86_64 i386 64bit
tensorflow	1.10.0
numpy	1.15.1
Sun Oct 14 21:48:53 2018 MDT	



