syms d1 d2 d4 d5 l1 l3 l4 mu mu0 CC PR lc %syms NI(d2,l4,CC,PC) d3 = d4 + 3E-3; Acoil = 0.5 * l4 * (d2 - d3)

Acoil =

$$-\frac{l_4\left(d_4-d_2+\frac{3}{1000}\right)}{2}$$

var3 = double(subs(Acoil,[d2,d4,l4],[26E-3,8E-3,25E-3]))

var3 = 1.8750e-04

NI =

$$-\frac{\text{CC PR } l_4 \left(d_4 - d_2 + \frac{3}{1000}\right)}{2}$$

var2 = double(subs(NI,[CC,PR,d2,d4,14],[10E6,0.7,26E-3,8E-3,25E-3]))

var2 = 1.3125e+03

$$R_{vertial_in} = \frac{l_a - l_c}{\mu \cdot S_2} + \frac{l_c}{\mu_0 \cdot S_2}$$

$$12 = 14 + 6E - 3$$

12 =

$$l_4 + \frac{3}{500}$$

la =

$$\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}$$

$$1b = 0.5 * (0.5 * (d1 + d2) - d5)$$

1b =

$$\frac{d_1}{4} + \frac{d_2}{4} - \frac{d_5}{2}$$

$$S1 = 0.25 * (d1^2 - d2^2)$$

S1 =

$$\frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

$$S2 = 0.25 * pi * (d4^2 - d5^2)$$

S2 =

$$\frac{\pi \left(d_4^2 - d_5^2\right)}{4}$$

$$S3 = 0.5 * pi * 11 * lb$$

S3 =

$$\frac{\pi \ l_1 \ \left(\frac{d_1}{4} + \frac{d_2}{4} - \frac{d_5}{2}\right)}{2}$$

$$S4 = 0.5 * pi * 13 * 1b$$

S4 =

$$\frac{\pi \ l_3 \ \left(\frac{d_1}{4} + \frac{d_2}{4} - \frac{d_5}{2}\right)}{2}$$

$$Rvert_in = (la - lc) / (mu*S2) + lc/(mu0*S2)$$

Rvert_in =

$$\frac{4\left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 - lc + \frac{3}{500}\right)}{\mu \pi \left(d_4^2 - d_5^2\right)} + \frac{4 lc}{\mu_0 \pi \left(d_4^2 - d_5^2\right)}$$

$$R_{vertial_out} = \frac{l_a}{\mu \cdot S_1}$$

Rvert_out = la / (mu*S1)

Rvert_out =

$$\frac{\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}}{\mu \left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)}$$

$$R_{horizontal_top} = R_{horizontal_bottom} = \frac{l_b}{\mu \cdot S_3}$$

Rhor_top = 1b / (mu*S3)

Rhor top =

$$\frac{2}{l_1 \mu \pi}$$

Rhor_bot = 1b / (mu*S4)

Rhor_bot =

$$\frac{2}{l_3 \mu \pi}$$

Rtotal = Rvert_in + Rvert_out + Rhor_top + Rhor_bot

Rtotal =

$$\frac{\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}}{\mu \left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)} + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{4\left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 - lc + \frac{3}{500}\right)}{\mu \pi \sigma_1} + \frac{4 lc}{\mu_0 \pi \sigma_1}$$

where

$$\sigma_1 = d_4{}^2 - d_5{}^2$$

phi = NI / Rtotal

phi =

$$-\frac{\text{CC PR } l_4 \left(d_4 - d_2 + \frac{3}{1000}\right)}{2\left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}}{\mu\left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)} + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{4\left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 - \text{lc} + \frac{3}{500}\right)}{\mu \pi \sigma_1} + \frac{4 \text{lc}}{\mu_0 \pi \sigma_1}\right)}$$

where

$$\sigma_1 = d_4{}^2 - d_5{}^2$$

var4 = double(subs(phi,[CC,PR,d1,d2,d4,d5,l1,l3,l4,lc,mu,mu0],[10E6,0.7,30E-3,26E-3,8E-3,0E-3,6

var4 = 1.3808e-04

$$Fmag = 0.5 * phi^2 / (mu0 * S2)$$

Fmag =

$$\frac{\text{CC}^{2} \text{PR}^{2} l_{4}^{2} \left(d_{4}-d_{2}+\frac{3}{1000}\right)^{2}}{2 \mu_{0} \pi \sigma_{1} \left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}+\frac{3}{500}}{\mu \left(\frac{d_{1}^{2}}{4}-\frac{d_{2}^{2}}{4}\right)}+\frac{2}{l_{1} \mu \pi}+\frac{2}{l_{3} \mu \pi}+\frac{4 \left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}-\text{lc}+\frac{3}{500}\right)}{\mu \pi \sigma_{1}}+\frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}}\right)^{2}}$$

where

$$\sigma_1 = d_4^2 - d_5^2$$

ans = 150.9201

ans = 119.1669

phi_res = double(subs(phi,[CC,PR,d1,d2,d4,d5,l1,l3,l4,lc,mu,mu0],[10E6,0.7,30E-3,26E-3,8E-3,0E

 $phi_res = 1.3808e-04$

 $S2_{res} = double(subs(S2,[d4,d5],[8E-3,0E-3]))$

 $S2_{res} = 5.0265e-05$

0.5*phi_res^2/(S2_res * 1.25663706212E-6)

ans = 150.9201

dMu

dFmag_dmu = diff(Fmag,mu)

dFmag_dmu =

$$\frac{\text{CC}^2 \text{PR}^2 l_4^2 \left(d_4 - d_2 + \frac{3}{1000}\right)^2 \left(\frac{\sigma_4}{\mu^2 \sigma_3} + \frac{2}{l_1 \mu^2 \pi} + \frac{2}{l_3 \mu^2 \pi} + \frac{\sigma_2}{\mu^2 \pi \sigma_1}\right)}{\mu_0 \pi \sigma_1 \left(\frac{\sigma_4}{\mu \sigma_3} + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{\sigma_2}{\mu \pi \sigma_1} + \frac{4 \text{lc}}{\mu_0 \pi \sigma_1}\right)^3}$$

where

$$\sigma_1 = d_4^2 - d_5^2$$

$$\sigma_2 = 4 \left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 - lc + \frac{3}{500} \right)$$

$$\sigma_3 = \frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

$$\sigma_4 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}$$

dLc

dFmag_dlc = diff(Fmag,lc)

dFmag_dlc =

$$\frac{\operatorname{CC}^{2}\operatorname{PR}^{2}l_{4}^{2}\left(\frac{4}{\mu\,\pi\,\sigma_{1}}-\frac{4}{\mu_{0}\,\pi\,\sigma_{1}}\right)\left(d_{4}-d_{2}+\frac{3}{1000}\right)^{2}}{\mu_{0}\,\pi\,\sigma_{1}\left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}+\frac{3}{500}}{\mu\,\left(\frac{d_{1}^{2}}{4}-\frac{d_{2}^{2}}{4}\right)}+\frac{2}{l_{1}\,\mu\,\pi}+\frac{2}{l_{3}\,\mu\,\pi}+\frac{4\left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}-\operatorname{lc}+\frac{3}{500}\right)}{\mu\,\pi\,\sigma_{1}}+\frac{4\operatorname{lc}}{\mu_{0}\,\pi\,\sigma_{1}}\right)^{2}}$$

$$\sigma_1 = d_4^2 - d_5^2$$

dd1

dFmag_dd1 =

$$\frac{\text{CC}^{2} \text{PR}^{2} d_{1} l_{4}^{2} \left(d_{4} - d_{2} + \frac{3}{1000}\right)^{2} \sigma_{3}}{2 \mu \mu_{0} \pi \sigma_{1} \sigma_{2}^{2} \left(\frac{\sigma_{3}}{\mu \sigma_{2}} + \frac{2}{l_{1} \mu \pi} + \frac{2}{l_{3} \mu \pi} + \frac{4 \left(\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} - \text{lc} + \frac{3}{500}\right)}{\mu \pi \sigma_{1}} + \frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}}\right)}$$

where

$$\sigma_1 = d_4^2 - d_5^2$$

$$\sigma_2 = \frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

$$\sigma_3 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}$$

dd2

 $dFmag_dd2 =$

$$\frac{3 \operatorname{CC}^{2} \operatorname{PR}^{2} l_{4}^{2} \sigma_{1} \left(\frac{\sigma_{5}}{\mu^{2} \sigma_{4}} + \frac{2}{l_{1} \mu^{2} \pi} + \frac{2}{l_{3} \mu^{2} \pi} + \frac{4 \sigma_{6}}{\mu^{2} \pi \sigma_{3}}\right)^{2}}{\mu_{0} \pi \sigma_{3} \sigma_{2}^{4}} - \frac{\operatorname{CC}^{2} \operatorname{PR}^{2} l_{4}^{2} \sigma_{1} \left(\frac{2 \sigma_{5}}{\mu^{3} \sigma_{4}} + \frac{4}{l_{1} \mu^{3} \pi} + \frac{4}{l_{3} \mu^{3} \pi} + \frac{8 \sigma_{6}}{\mu^{3} \pi \sigma_{4}}\right)^{2}}{\mu_{0} \pi \sigma_{3} \sigma_{2}^{3}}$$

$$\sigma_1 = \left(d_4 - d_2 + \frac{3}{1000}\right)^2$$

$$\sigma_2 = \frac{\sigma_5}{\mu \, \sigma_4} + \frac{2}{l_1 \, \mu \, \pi} + \frac{2}{l_3 \, \mu \, \pi} + \frac{4 \, \sigma_6}{\mu \, \pi \, \sigma_3} + \frac{4 \, \text{lc}}{\mu_0 \, \pi \, \sigma_3}$$

$$\sigma_3 = d_4^2 - d_5^2$$

$$\sigma_4 = \frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

$$\sigma_5 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}$$

$$\sigma_6 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 - lc + \frac{3}{500}$$

dd4

dFmag_dd4 = diff(Fmag,d4)

 $dFmag_dd4 =$

$$\frac{\text{CC}^2 \, \text{PR}^2 \, l_4{}^2 \, \left(2 \, d_4 - 2 \, d_2 + \frac{3}{500}\right)}{2 \, \mu_0 \, \pi \, \sigma_3 \, \sigma_2{}^2} - \frac{\text{CC}^2 \, \text{PR}^2 \, d_4 \, l_4{}^2 \, \sigma_1}{\mu_0 \, \pi \, \sigma_3{}^2 \, \sigma_2{}^2} + \frac{\text{CC}^2 \, \text{PR}^2 \, l_4{}^2 \, \left(\frac{8 \, d_4 \, \sigma_4}{\mu \, \pi \, \sigma_3{}^2} + \frac{8 \, d_4 \, \text{lc}}{\mu_0 \, \pi \, \sigma_3{}^2}\right) \, \sigma_1}{\mu_0 \, \pi \, \sigma_3 \, \sigma_2{}^3}$$

$$\sigma_1 = \left(d_4 - d_2 + \frac{3}{1000}\right)^2$$

$$\sigma_2 = \frac{\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}}{\mu \left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)} + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{4 \sigma_4}{\mu \pi \sigma_3} + \frac{4 \text{lc}}{\mu_0 \pi \sigma_3}$$

$$\sigma_3 = d_4^2 - d_5^2$$

$$\sigma_4 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 - 1c + \frac{3}{500}$$

dd5

dFmag_dd5 = diff(Fmag,d5)

 $dFmag_dd5 =$

$$\frac{\text{CC}^2 \, \text{PR}^2 \, d_5 \, {l_4}^2 \, \sigma_1}{\mu_0 \, \pi \, {\sigma_3}^2 \, {\sigma_2}^2} - \frac{\text{CC}^2 \, \text{PR}^2 \, {l_4}^2 \, \left(\frac{8 \, d_5 \, \sigma_4}{\mu \, \pi \, {\sigma_3}^2} + \frac{8 \, d_5 \, \text{lc}}{\mu_0 \, \pi \, {\sigma_3}^2}\right) \sigma_1}{\mu_0 \, \pi \, \sigma_3 \, {\sigma_2}^3}$$

where

$$\sigma_1 = \left(d_4 - d_2 + \frac{3}{1000}\right)^2$$

$$\sigma_2 = \frac{\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}}{\mu \left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)} + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{4 \sigma_4}{\mu \pi \sigma_3} + \frac{4 lc}{\mu_0 \pi \sigma_3}$$

$$\sigma_3 = d_4^2 - d_5^2$$

$$\sigma_4 = \frac{l_1}{2} + \frac{l_3}{2} + l_4 - lc + \frac{3}{500}$$

dl1

dFmag_dl1 = diff(Fmag,l1)

dFmag_dl1 =

$$\frac{\text{CC}^{2} \text{PR}^{2} l_{4}^{2} \left(d_{4} - d_{2} + \frac{3}{1000} \right)^{2} \left(\frac{1}{2 \mu \sigma_{2}} + \frac{2}{\mu \pi \sigma_{1}} - \frac{2}{l_{1}^{2} \mu \pi} \right) }{\mu \sigma_{1} \sigma_{1} \left(\frac{l_{1}^{2} + l_{3}^{2} + l_{4} + \frac{3}{500}}{\mu \sigma_{2}} + \frac{2}{l_{1} \mu \pi} + \frac{2}{l_{3} \mu \pi} + \frac{4 \left(\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} - \text{lc} + \frac{3}{500} \right)}{\mu \pi \sigma_{1}} + \frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}} \right) }$$

where

$$\sigma_1 = d_4{}^2 - d_5{}^2$$

$$\sigma_2 = \frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

dl3

dFmag_dl3 = diff(Fmag,l3)

dFmag_dl3 =

$$\frac{\text{CC}^{2} \text{PR}^{2} l_{4}^{2} \left(d_{4} - d_{2} + \frac{3}{1000}\right)^{2} \left(\frac{1}{2 \mu \sigma_{2}} + \frac{2}{\mu \pi \sigma_{1}} - \frac{2}{l_{3}^{2} \mu \pi}\right)}{\mu \sigma_{2} \left(\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} + \frac{3}{500} + \frac{2}{l_{1} \mu \pi} + \frac{2}{l_{3} \mu \pi} + \frac{4}{2} \left(\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} - \text{lc} + \frac{3}{500}\right) + \frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}}\right)^{3}} + \frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}}$$

where

$$\sigma_1 = d_4{}^2 - d_5{}^2$$

$$\sigma_2 = \frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}$$

dl4

dFmag_dl4 = diff(Fmag,l4)

 $dFmag_dl4 =$

$$\frac{\text{CC}^2 \text{PR}^2 l_4 \left(d_4 - d_2 + \frac{3}{1000}\right)^2}{\mu_0 \pi \sigma_2 \sigma_1^2} - \frac{\text{CC}^2 \text{PR}^2 l_4^2 \left(\frac{1}{\mu \left(\frac{d_1^2}{4} - \frac{d_2^2}{4}\right)} + \frac{4}{\mu \pi \sigma_2}\right) \left(d_4 - d_2 + \frac{3}{1000}\right)^2}{\mu_0 \pi \sigma_2 \sigma_1^3}$$

$$\sigma_{1} = \frac{\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} + \frac{3}{500}}{\mu \left(\frac{d_{1}^{2}}{4} - \frac{d_{2}^{2}}{4}\right)} + \frac{2}{l_{1} \mu \pi} + \frac{2}{l_{3} \mu \pi} + \frac{4 \left(\frac{l_{1}}{2} + \frac{l_{3}}{2} + l_{4} - lc + \frac{3}{500}\right)}{\mu \pi \sigma_{2}} + \frac{4 lc}{\mu_{0} \pi \sigma_{2}}$$

$$\sigma_2 = d_4^2 - d_5^2$$

dCC

dFmag_dCC =

$$\frac{\text{CC PR}^2 l_4^2 \left(d_4 - d_2 + \frac{3}{1000}\right)^2}{\mu_0 \pi \sigma_1 \left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 + \frac{3}{500}\right) + \frac{2}{l_1 \mu \pi} + \frac{2}{l_3 \mu \pi} + \frac{4\left(\frac{l_1}{2} + \frac{l_3}{2} + l_4 - \text{lc} + \frac{3}{500}\right)}{\mu \pi \sigma_1} + \frac{4 \text{lc}}{\mu_0 \pi \sigma_1}\right)^2}$$

where

$$\sigma_1 = d_4{}^2 - d_5{}^2$$

dPR

 $dFmag_dPR =$

$$\frac{\text{CC}^{2} \text{PR } l_{4}^{2} \left(d_{4}-d_{2}+\frac{3}{1000}\right)^{2}}{\mu_{0} \pi \sigma_{1} \left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}+\frac{3}{500}}{\mu\left(\frac{d_{1}^{2}}{4}-\frac{d_{2}^{2}}{4}\right)}+\frac{2}{l_{1} \mu \pi}+\frac{2}{l_{3} \mu \pi}+\frac{4 \left(\frac{l_{1}}{2}+\frac{l_{3}}{2}+l_{4}-\text{lc}+\frac{3}{500}\right)}{\mu \pi \sigma_{1}}+\frac{4 \text{lc}}{\mu_{0} \pi \sigma_{1}}\right)}$$

$$\sigma_1 = d_4^2 - d_5^2$$

```
density6061 = 2700;
density430F = 7800;
densityCopper = 8960;
W_copper = PR * 0.25 * 14 * (d2^2 - d3^2) * densityCopper
```

W_copper =

$$-2240 \,\mathrm{PR} \,l_4 \,\left(\left(d_4 + \frac{3}{1000}\right)^2 - d_2^2\right)$$

double(subs(W_copper,[PR,d2,d4,14],[0.7,27E-3,8E-3,25E-3]))

ans = 0.0238

$$W_{coilformer} = 0.25 * (d2^2 * (12 - 14) + d3^2 * 14 - d4^2 * 12) * density6061$$

W coilformer =

$$\frac{81 d_2^2}{20} - 675 d_4^2 \left(l_4 + \frac{3}{500} \right) + 675 l_4 \left(d_4 + \frac{3}{1000} \right)^2$$

$$W_shell = 0.25 * (d1^2 - d2^2) * 12 * density430F$$

 $W_shell =$

$$7800 \left(\frac{{d_1}^2}{4} - \frac{{d_2}^2}{4} \right) \left(l_4 + \frac{3}{500} \right)$$

$$W_{magtop} = 0.25 * ((d1^2 - d5^2) * 11 + (d4^2 - d5^2) * 12 * 0.5) * density430F$$

W_magtop =

1950
$$l_1 \left(d_1^2 - d_5^2 \right) + 975 \left(d_4^2 - d_5^2 \right) \left(l_4 + \frac{3}{500} \right)$$

$$W_magbot = 0.25 * (d1^2 - d5^2) * 13 * density430F$$

W_magbot =

$$7800 l_3 \left(\frac{{d_1}^2}{4} - \frac{{d_5}^2}{4} \right)$$

 $W_magpintle = 0.25 * (d4^2 - d5^2) * 12 * 0.5 * density430F$

W_magpintle =

$$3900 \left(\frac{d_4^2}{4} - \frac{d_5^2}{4} \right) \left(l_4 + \frac{3}{500} \right)$$

Weight = W_copper + W_coilformer + W_shell + W_magtop + W_magbot + W_magpintle

Weight =

$$1950 l_1 \left(d_1^2 - d_5^2\right) + 7800 l_3 \left(\frac{{d_1}^2}{4} - \frac{{d_5}^2}{4}\right) + 975 \left({d_4}^2 - {d_5}^2\right) \left(l_4 + \frac{3}{500}\right) + \frac{81 d_2^2}{20} + 7800 \left(\frac{{d_1}^2}{4} - \frac{{d_2}^2}{4}\right) \left(l_4 + \frac{3}{500}\right) + \frac{1}{20} \left(l_4 + \frac{3}{20}\right) \left(l_4 + \frac{3}{20}\right) \left(l_4 + \frac{3}{20}\right) + \frac{1}{20} \left(l_4 + \frac{3}{20}\right) \left(l_4 + \frac{3}{20}\right)$$

where

$$\sigma_1 = \left(d_4 + \frac{3}{1000}\right)^2$$

double(subs(Weight,[PR,d1,d2,d4,d5,l1,l3,l4],[0.8,30E-3,27E-3,8E-3,0E-3,3E-3,3E-3,25E-3]))

ans = 0.0556

dPR

dWeight_dcop = diff(Weight,PR)

dWeight_dcop =

$$-2240 l_4 \left(\left(d_4 + \frac{3}{1000} \right)^2 - d_2^2 \right)$$

dd1

dWeight_dd1 = diff(Weight,d1)

dWeight_dd1 =

$$3900 d_1 l_1 + 3900 d_1 l_3 + 3900 d_1 \left(l_4 + \frac{3}{500} \right)$$

dd2

dWeight_dd2 = diff(Weight,d2)

dWeight_dd2 =

$$\frac{81 d_2}{10} - 3900 d_2 \left(l_4 + \frac{3}{500} \right) + 4480 \,\mathrm{PR} \,d_2 \,l_4$$

dd4

dWeight_dd4 = diff(Weight,d4)

dWeight_dd4 =

$$2550 d_4 \left(l_4 + \frac{3}{500}\right) + 675 l_4 \left(2 d_4 + \frac{3}{500}\right) - 2240 \,\mathrm{PR} \,l_4 \left(2 d_4 + \frac{3}{500}\right)$$

dd5

dWeight_dd1 =

$$-3900 d_5 l_1 - 3900 d_5 l_3 - 3900 d_5 \left(l_4 + \frac{3}{500}\right)$$

dl1

dWeight_dl1 =
$$1950 d_1^2 - 1950 d_5^2$$

dl3

dWeight_dl3 =
$$1950 d_1^2 - 1950 d_5^2$$

dl4

dWeight dl4 =

$$675 \left(d_4 + \frac{3}{1000}\right)^2 - 2240 \,\mathrm{PR} \,\left(\left(d_4 + \frac{3}{1000}\right)^2 - d_2^2\right) + 1950 \,d_1^2 - 1950 \,d_2^2 + 1275 \,d_4^2 - 1950 \,d_5^2$$