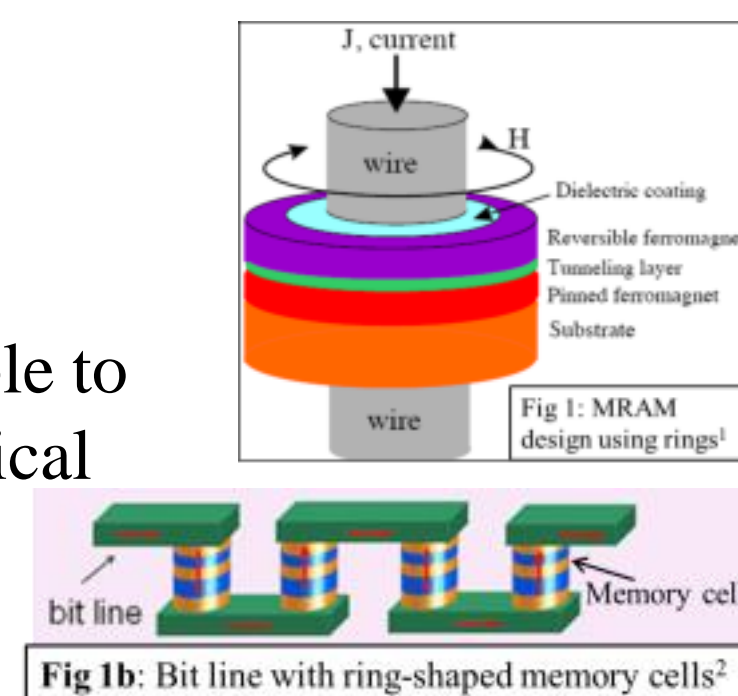


I. MOTIVATION

- Magnetoresistive Random Access Memory (MRAM) allows fast data access and non-volatile data storage needed for a universal computer memory.

- Figure 1(a) shows a schematic of a MRAM proposal using ring-shaped ferromagnetic structures. It is possible to have circular memory cells in a vertical MRAM (Figure 1b).



- Ring-based MRAMs can use magnetoresistive measurements on two lowest energy configurations, i.e. the **clockwise** and **counterclockwise (CW/CCW)** vortex states. Figure 2 shows CW/CCW vortex states in rings.



II. OOMMF SIMULATIONS

- Object Oriented MicroMagnetic Framework (OOMMF) iteratively solves the **Landau-Lifshitz-Gilbert equation**

$$\frac{\partial \vec{M}}{\partial t} = -\frac{\gamma}{1 + \alpha^2} \vec{M} \times \vec{H}_{eff} - \frac{\gamma \alpha}{(1 + \alpha^2) M_s} \vec{M} \times (\vec{M} \times \vec{H}_{eff})$$
 α is a phenomenological damping parameter, γ is the gyromagnetic ratio
- We apply a circular magnetic field as if from an infinite wire passing through the center of ring-based structures.
- Magnetic parameters for permalloy: Saturation of magnetization $M_s = 8.6 \times 10^5$ A/m, Exchange parameter $A = 1.3 \times 10^{-13}$ J/m, Crystalline anisotropy = 0, and $T = 0$ K.

III. PREVIOUS EXPERIMENTS

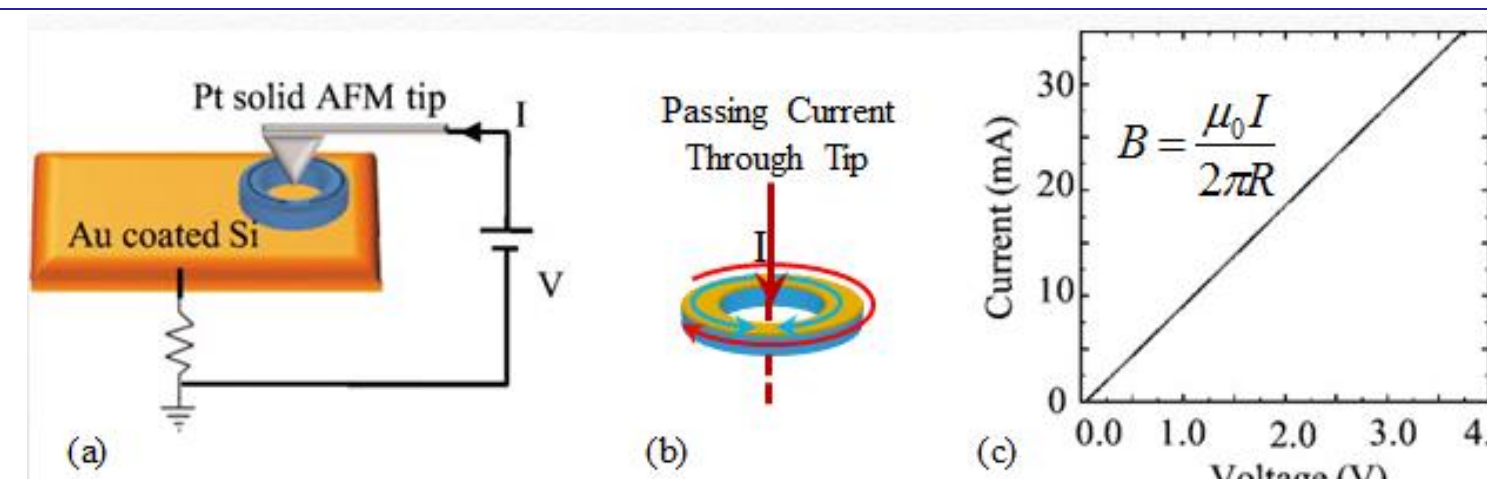
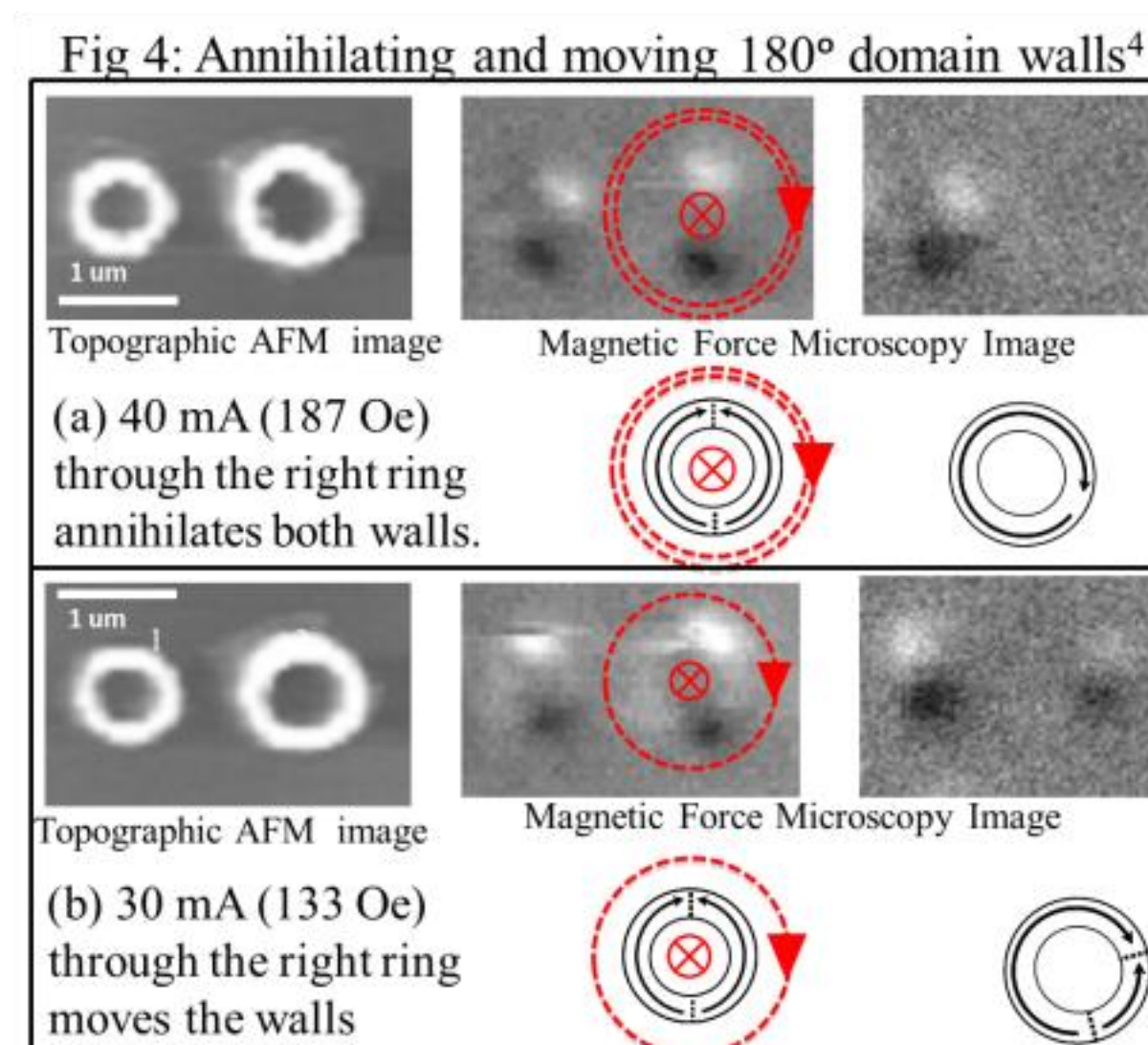


Fig 3 (a) Schematic of the experimental setup. (c) A current-voltage plot generated directly from the experimental setup in (a).³



We have passed current through thin rings using the setup shown in Figure 3. We have annihilated and moved domain walls as shown in Figure 4.

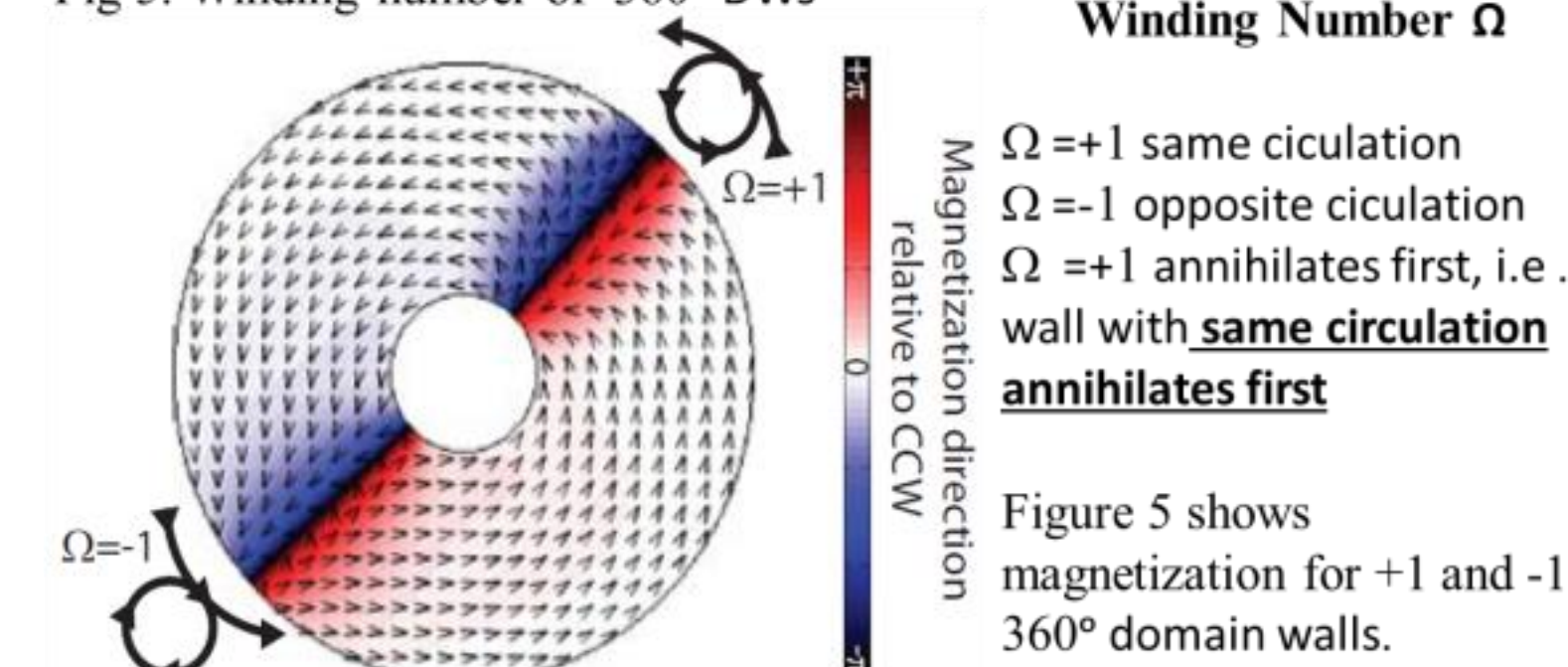
IV. VORTEX SWITCHING AND 360° DOMAIN WALLS (DWs)

TOPOLOGICAL WINDING NUMBER

Equation for DW exchange energy and winding number (Ω)⁴:

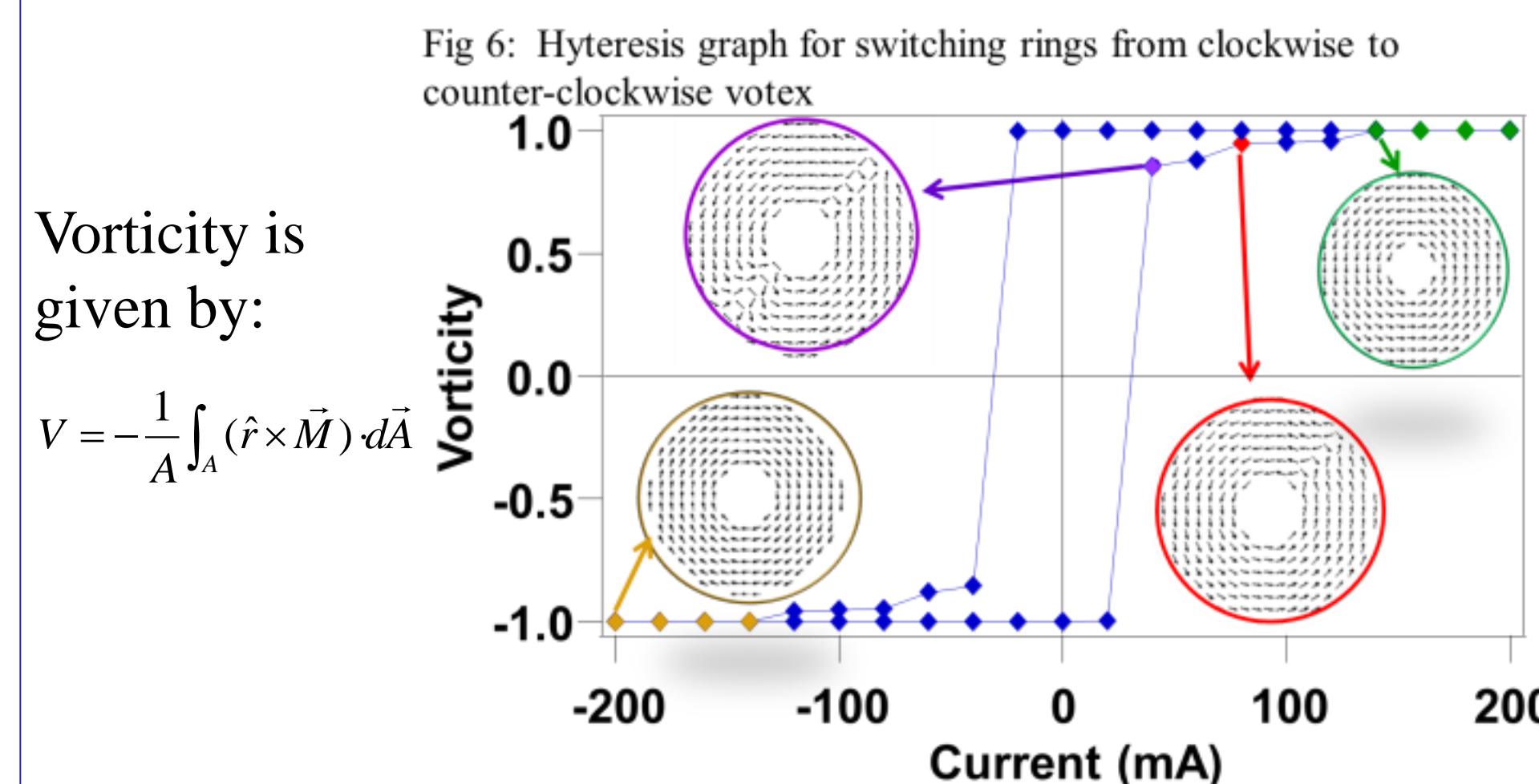
$$E_{ex} = \frac{\mu_0 M_s^2 t^2}{2} \ln\left(\frac{R_2}{R_1}\right) [2\pi(1 + 2\Omega) + \int_0^{2\pi} \left(\frac{\partial \phi}{\partial \theta}\right)^2 d\theta]$$

Fig 5: Winding number of 360° DWs



HYSTERESIS CURVE FOR RINGS

Figure 6 shows a hysteresis curve for a 5 nm thick ring. The outer diameter is 800nm and inner diameter is 200nm.



Vorticity is given by:

$$V = -\frac{1}{A} \int_A (\hat{r} \times \vec{M}) \cdot d\vec{A}$$

The **clockwise (CW)** vortex has a vorticity of -1. As we apply a counter-clockwise (CCW) field, we get **two 360° domain walls**. Stronger CCW field **annihilates the $\Omega = +1$ wall first** and then the **$\Omega = -1$ wall is annihilated**. Finally, we have a counter-clockwise vortex with vorticity +1.

ENERGY GRAPHS $\Omega=+1$ and $\Omega=-1$

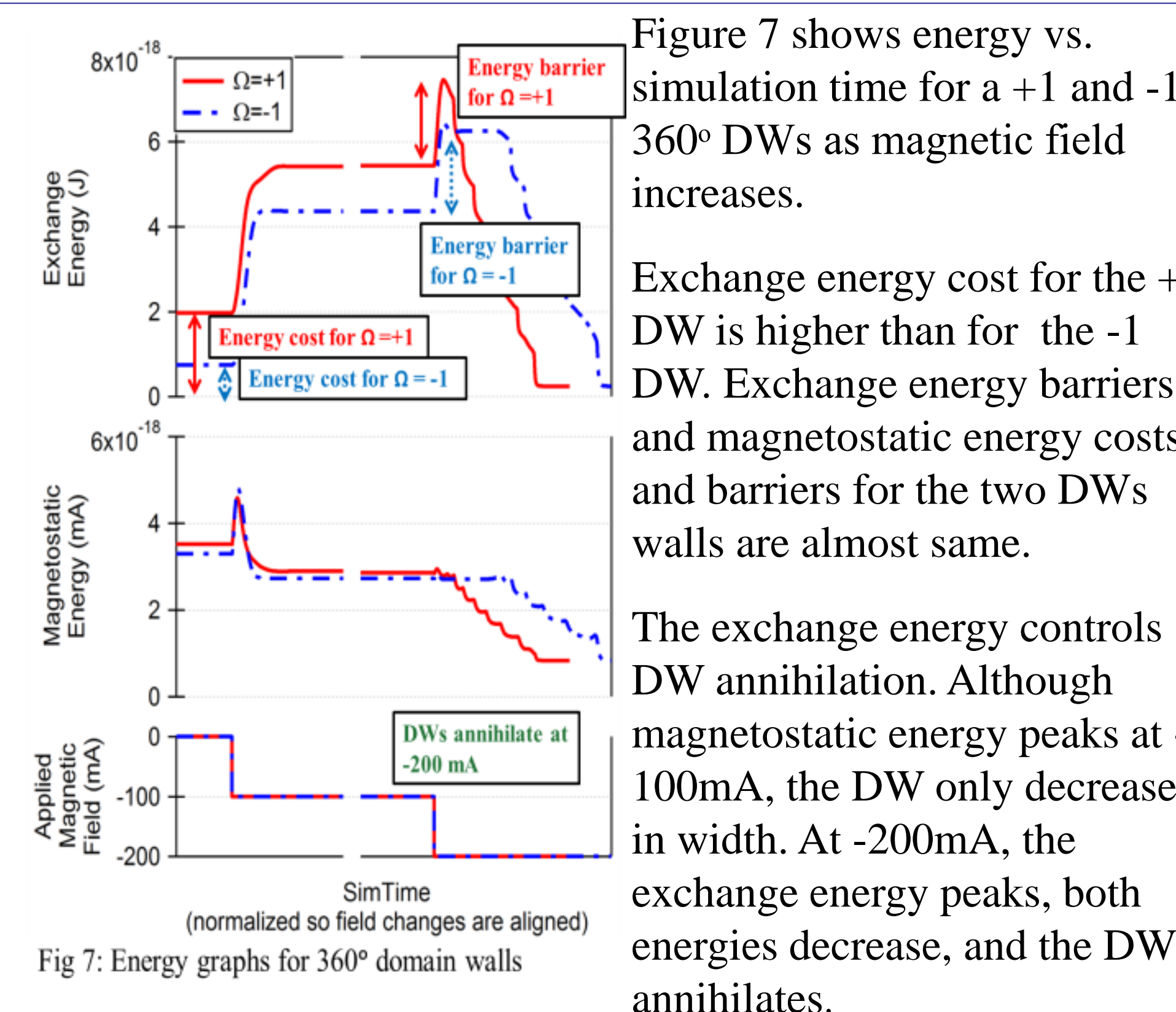


Figure 7 shows energy vs. simulation time for a +1 and -1 360° DWs as magnetic field increases.

Exchange energy cost for the +1 DW is higher than for the -1 DW. Exchange energy barriers and magnetostatic energy costs and barriers for the two DWs walls are almost same.

The exchange energy controls DW annihilation. Although magnetostatic energy peaks at -100mA, the DW only decreases in width. At -200mA, the exchange energy peaks, both energies decrease, and the DW annihilates.

V. MULTI-LEVEL BIT: CREATING 4 NON-DEGENERATE STABLE DWs

CENTERED ELLIPSE CREATES 2 PAIRS OF DEGENERATE DWs

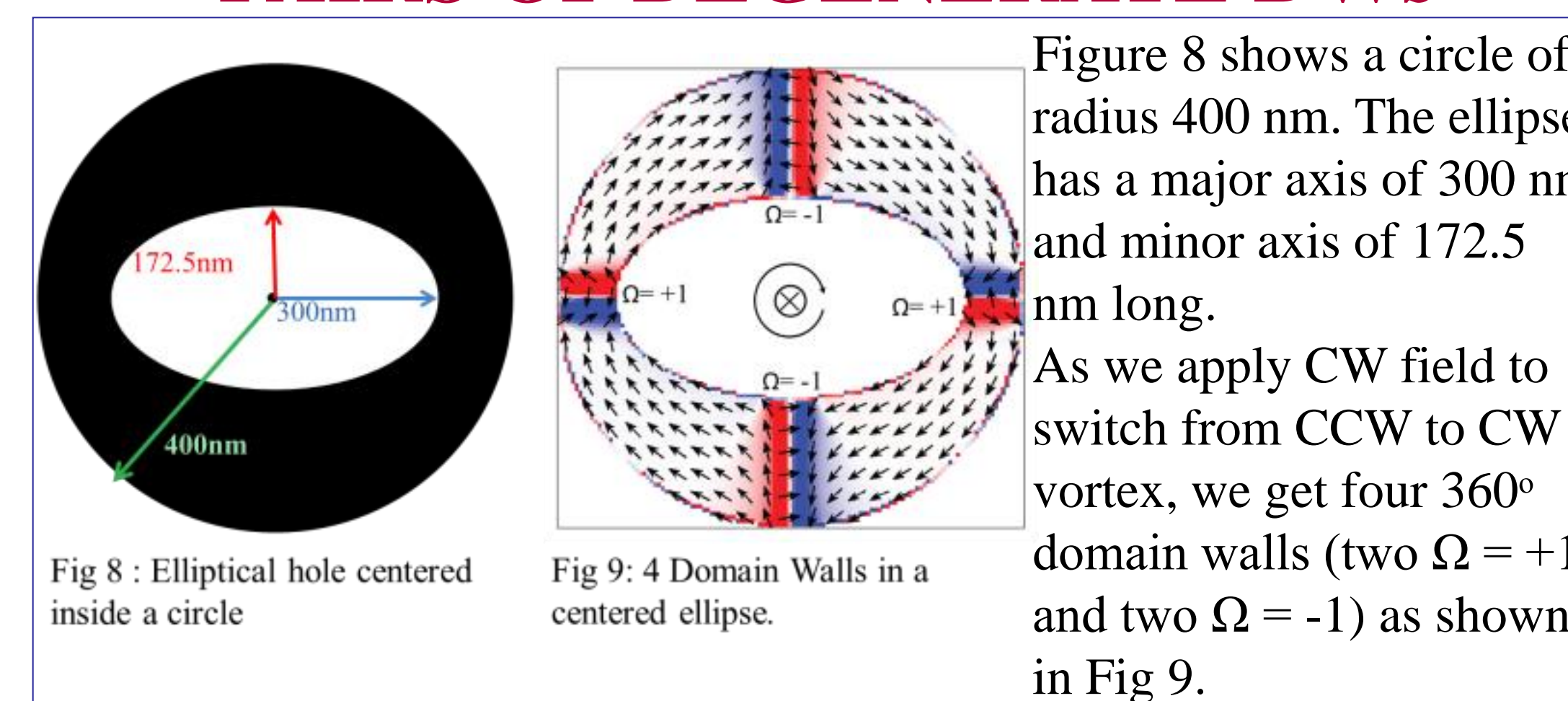
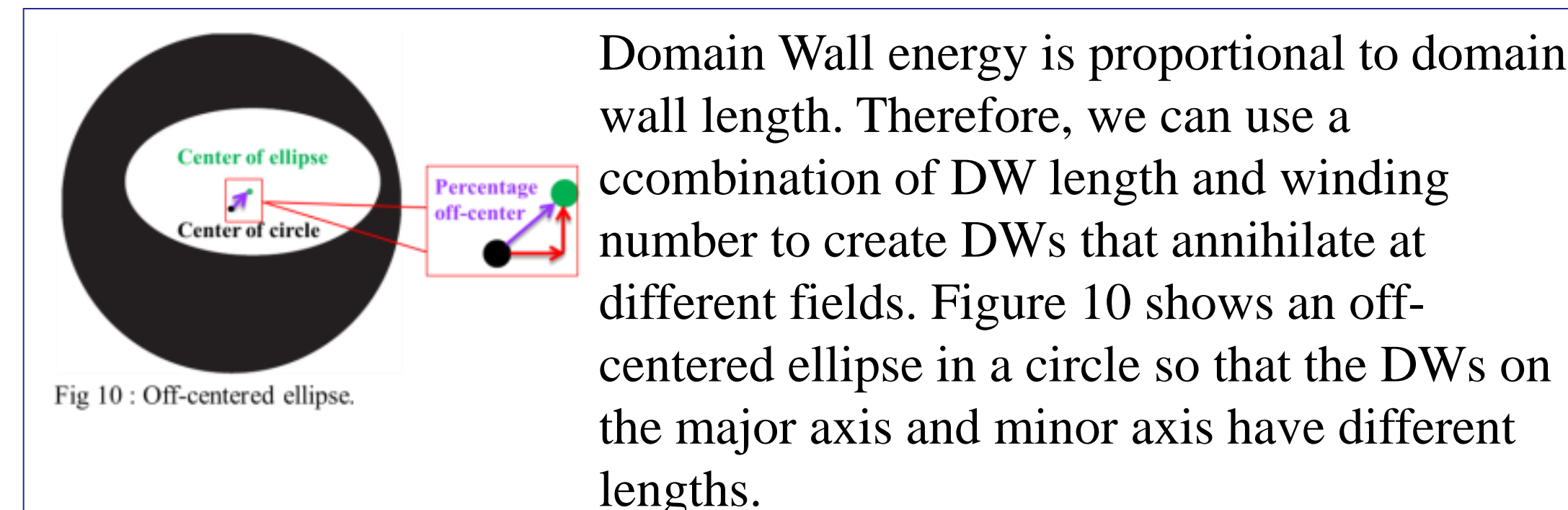
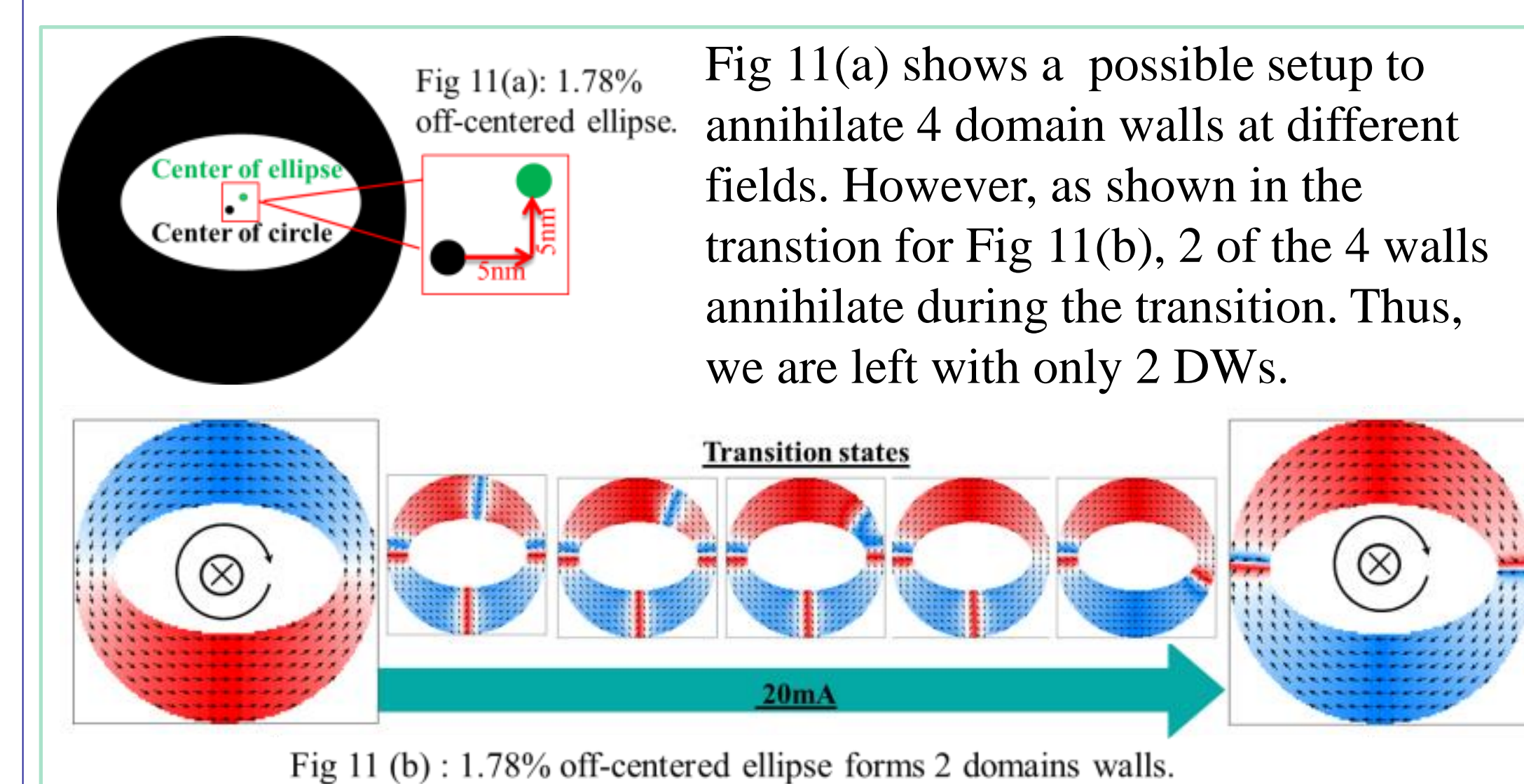


Figure 8 shows a circle of radius 400 nm. The ellipse has a major axis of 300 nm and minor axis of 172.5 nm long. As we apply CW field to switch from CCW to CW vortex, we get four 360° domain walls (two $\Omega = +1$ and two $\Omega = -1$) as shown in Fig 9.

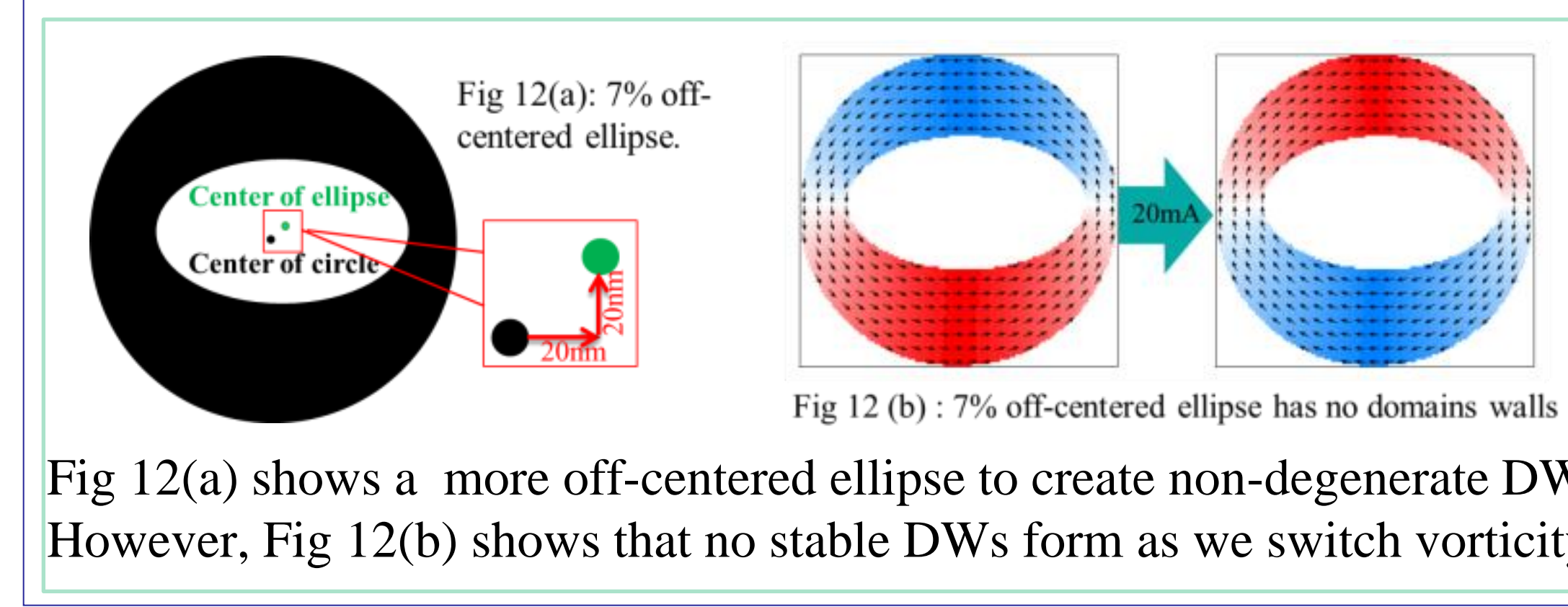
OFF-CENTERED ELLIPSE TO BREAK LENGTH DEGENERACY: 0 to 2 DWs



1.78% OFF-CENTERED ELLIPSE: 2 NON-DEGENERATE STABLE DWs



7% OFF-CENTERED ELLIPSE: 0 DOMAIN WALLS



ADDING NOTCHES TO GET 4 NON-DEGENERATE STABLE DWs

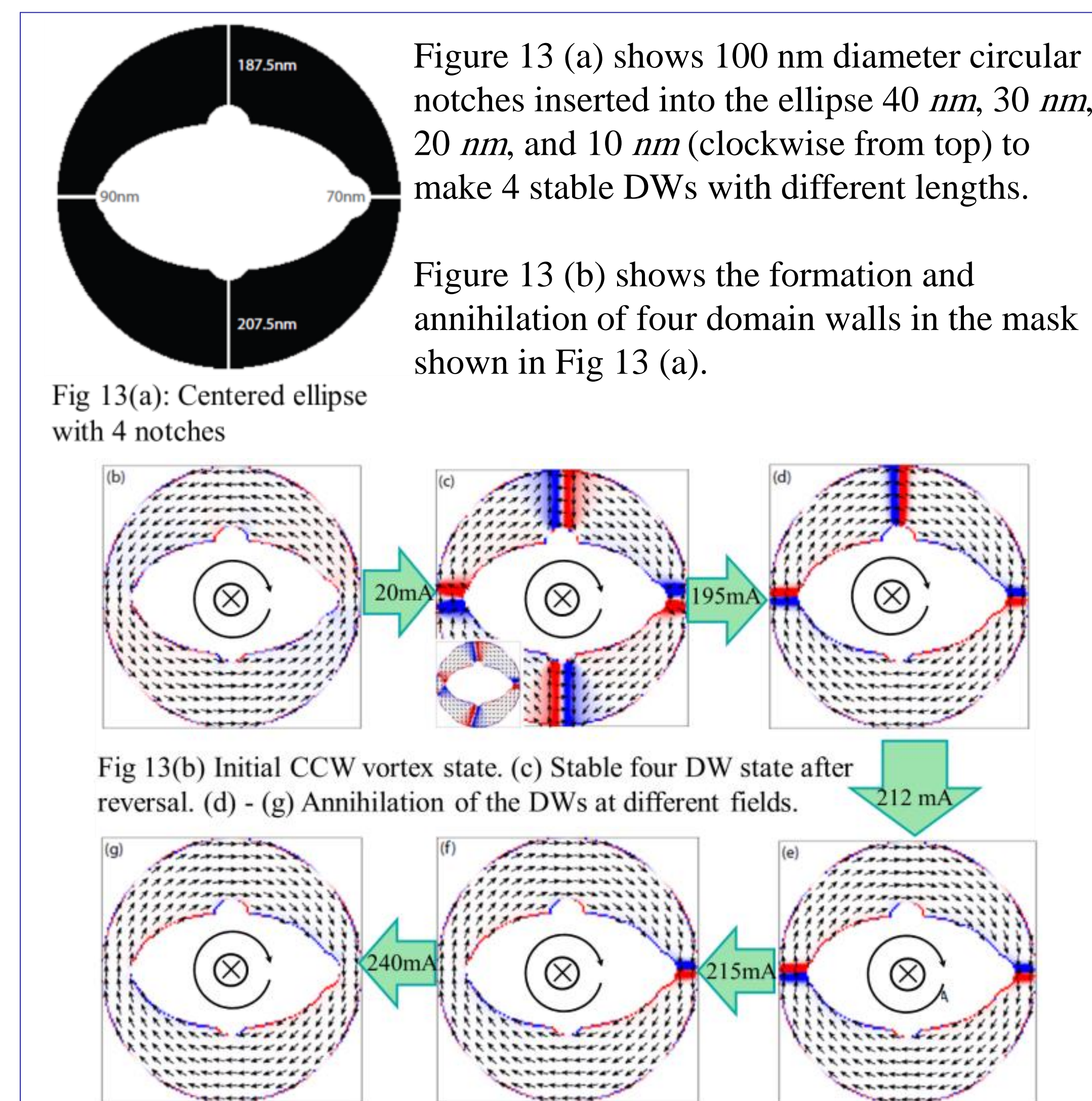


Figure 13 (a) shows 100 nm diameter circular notches inserted into the ellipse 40 nm, 30 nm, 20 nm, and 10 nm (clockwise from top) to make 4 stable DWs with different lengths. Figure 13 (b) shows the formation and annihilation of four domain walls in the mask shown in Fig 13 (a).

VI. CONCLUSIONS

- The switching process between vortex states in thin rings occurs through pairs of DWs with opposite winding number. The DW energy depends on both DW winding number and DW length.
- We can use a careful combination of variation in DW winding number and DW length to get 4 non-degenerate DW. We have used a circular ring with an elliptical center and 4 notches to get 4 non-degenerate stable DWs.
- Our simulations demonstrate a proof of concept for multi-level bit storage device. However, fabricating nanorings with precise geometries and notches is experimentally challenging.

VII. ACKNOWLEDGEMENTS

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VIII. REFERENCES

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- [2] J.-G. Zhu, Y. Zheng, and G. A. Prinz, *J. Appl. Phys.* 87, 6668 (2000).
- [3] T. Yang, KEA, *APL*, 98, 242505 (2011).
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