

A Tier-Based Model of Syntactic Agreement

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CLS 60
April 26–28, 2024

1 Introduction

■ Some (paradoxical) properties of agreement ■

Usually. . .	but. . .
Applies over a distance	Subject to blockers
Blockers are predictable	Vary across dependencies/languages
Targets the closest visible DP	Which DPs are visible varies
Probe c-commands goal	Sometimes reversed
One probe ↔ one goal	Sometimes many-to-one

■ Overview ■

Main claim: Agreement patterns are **tier-based strictly local (TSL)**, mirroring findings on movement (Graf 2022b) and case (Hanson 2023b).¹

Why this matters:

- Limits structural configurations
- Defines parameters for variation
- Provides a unified model of locality restrictions
- Shows parallels within/across domains
- Derives typology from issues of efficient computation

■ Roadmap ■

1. What is a TSL pattern?
2. A TSL model of agreement
3. Consequences for locality
4. Typological variation
5. Parallels with phonology
6. Strengths and limitations of the model

¹This is an informal presentation of an analysis done in the framework of MG derivation trees, recast in terms of mainstream Minimalism. See Hanson (2023a) for a more formal presentation (available at <https://www.kennethhanson.net/files/hanson-nyubb2023-agreement-slides.pdf>).

2 TSL patterns

■ What is a TSL pattern? ■

1. Ignore the irrelevant items and treat the rest as if adjacent
2. All constraints must be stated within a fixed-size moving window

Example: Vowel harmony

i/u/o obey front-back harmony, *e* is transparent/neutral, *a* is opaque

All elements: k, b, l, i, e, u, o, a
Tier elements: i, u, o, a
Invisible elements: k, b, l, e
Constraints: *iu, *io, *oi, *ui

Word	Tier	
kubulo	uuo	✓
kibilo	iio	✗
kubelo	uo	✓
kibelo	io	✗
kubalo	uao	✓
kibalo	iao	✓

■ More about TSL ■

- Originally defined to model phonological patterns (Heinz et al. 2011)
- Argued to be relevant in syntax as well (Graf 2022a)
- Inspired by but distinct from autosegmental phonology (Goldsmith 1976)
- Special relational structure (tier successor) with very weak constraint logic (banned substrings) (Lambert et al. 2021)
- By hypothesis, we only need a window of size two (McMullin 2016)



TSL string model with constraint window of size two

See Appendix A.1 for another example and a formal definition.

3 A TSL Model of Agreement

■ Setup ■

Assumptions:

- Bare phrase structure, feature-driven selection, movement, . . .
- Agreement between elements with initially unvalued features (probes) and elements which provide those values (goals)²

Question: What are the possible arrangements of probes and goals for agreement?

Answer: They are TSL constraints on the search path of the probe.

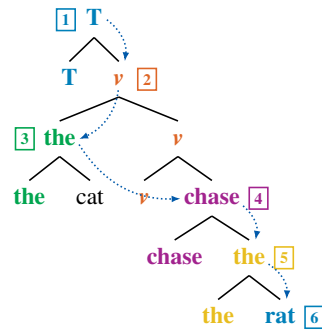
²I use the term **agreement** rather than **Agree** to indicate that we are not presupposing a particular version of the Agree operation, nor dealing with other phenomena that are sometimes subsumed under Agree.

■ The search path ■

The search path follows the **derivational command (d-command)** relation (Graf and Shafiei 2019).

- Head < Spec < Comp
- d-command order \approx height of XP
 \approx order of last merge
 \approx reverse order of selection
- Projections of a head are not distinguished.
- At each branching point, follow the complement spine (Graf and De Santo 2019).

ex. 'The cat chases the rats.'



See Appendix A.2 for how this works using derivation trees.

■ The TSL analysis ■

General principle: a probe must be immediately followed by its goal on a tier projected from the search path (and vice versa).

Notation: $p\phi$ = probe $g\phi$ = actual goal ϕ = other potential goal

Example: (canonical) subject-verb agreement

Tier elements: All agreeing elements (T/D) and blockers (C)

Constraints: $*T_{[p\phi]} \cdot D_{[\phi]}$, $*T_{[p\phi]} \cdot C$, $*D \cdot D_{[g\phi]}$, $*D_{[g\phi]} \cdot D_{[g\phi]}$, ...

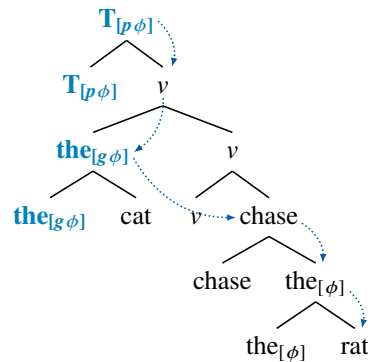
■ The TSL analysis – example ■

ex. The cat **chases** the rats.

Path: $T_{[p\phi]} \cdot v \cdot D_{[g\phi]} \cdot V \cdot D_{[\phi]} \cdot N$

Tier: $T_{[p\phi]} \cdot D_{[g\phi]} \cdot D_{[\phi]}$

Violations: n/a



For simplicity, we substitute most items with their category labels.

4 Consequences for locality

■ Consequences for locality ■

- **Minimality:** if another potential goal intervenes on the tier, agreement is blocked.
- **Invisibility:** if a DP is omitted from the tier, long-distance agreement is possible.
 – e.g. agreement across *there*, case-sensitive agreement
- **Blocking:** if a non-agreeing element intervenes on the tier, agreement is blocked.
 – e.g. probe horizons (Keine 2019), defective intervention

■ Minimality ■

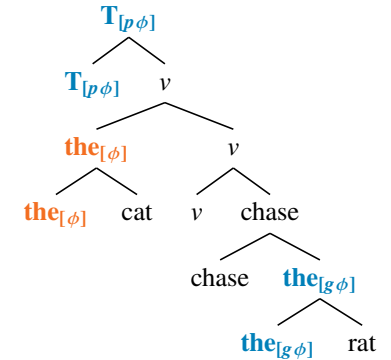
If another potential goal intervenes on the tier, agreement is blocked.

ex. * The cat **chase** the rats.

Path: $T_{[p\phi]} \cdot v \cdot D_{[\phi]} \cdot V \cdot D_{[g\phi]} \cdot N$

Tier: $T_{[p\phi]} \cdot D_{[\phi]} \cdot D_{[g\phi]}$

Violations: $*T_{[p\phi]} \cdot D_{[\phi]}$, $*D_{[\phi]} \cdot D_{[g\phi]}$



■ Invisibility ■

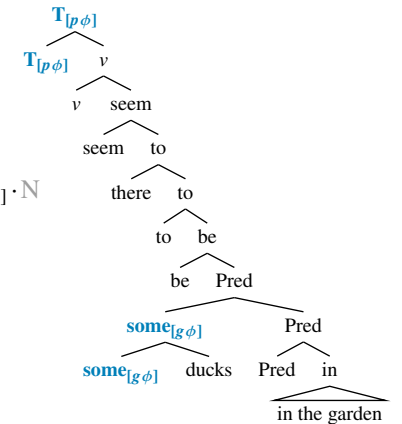
If a DP is omitted from the tier, long-distance agreement is possible.

ex. There **seem** to be some ducks in the garden.

Path: $T_{[p\phi]} \cdot v \cdot V \cdot T \cdot there \cdot v \cdot D_{[g\phi]} \cdot P \cdot D_{[\phi]} \cdot N$

Tier: $T_{[p\phi]} \cdot D_{[g\phi]} \cdot D_{[\phi]}$

Violations: n/a



We can handle optional default agreement in several ways. Ask me if you are interested.

■ Blocking ■

If a non-agreeing element is projected on the tier, agreement is blocked.

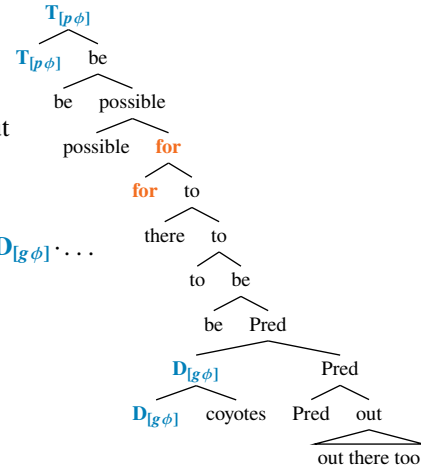
ex. * It **are** possible for there to be coyotes out there too.

cf. It **is** possible. . .

Path: $T_{[p\phi]} \cdot v \cdot V \cdot C \cdot T \cdot there \cdot v \cdot Pred \cdot D_{[g\phi]} \cdot \dots$

Tier: $T_{[p\phi]} \cdot C \cdot D_{[g\phi]}$

Violations: $*T_{[p\phi]} \cdot C, *C \cdot D_{[g\phi]}$



Assume for the sake of demonstration that expletive “it” is inserted late and does not agree.

■ Locality – summary ■

Locality phenomena derive from TSL with a window of size two, a.k.a. **TSL-2**.

- Minimality: closer potential goal intervenes



- Invisibility: hypothetical goal does not appear on tier



- Blocking: some non-agreeing element intervenes on the tier



■ Importance of the finite window ■

- Neither tiers nor the finite window alone are adequate.
 - Tiers allow long-distance dependencies to be treated as if local.
 - The finite constraint window limits the power of the system.
 - Together, they create the right type of relativized locality.

See Appendix A.3 and Appendix A.4 for details.

5 Typological variation

■ Parameters for variation ■

The parameters for TSL-2 (tier elements and constraints) correspond neatly to variation in long-distance dependencies.

- Visibility — which elements are relevant and which are ignored?
 - Case-sensitive agreement (cf. Bobaljik 2008; Preminger 2014)
- Iteration — if you allow AB and BB, then you get ABB, AB BB, etc.
 - Case/gender/number concord
- Directionality — do we ban AB or BA?
 - Upward/downward agreement (cf. Chomsky 2000; Zeijlstra 2012)

■ Case-sensitive agreement ■

In Hindi, the verb agrees with the closest *nominative* argument, which may not be the subject.

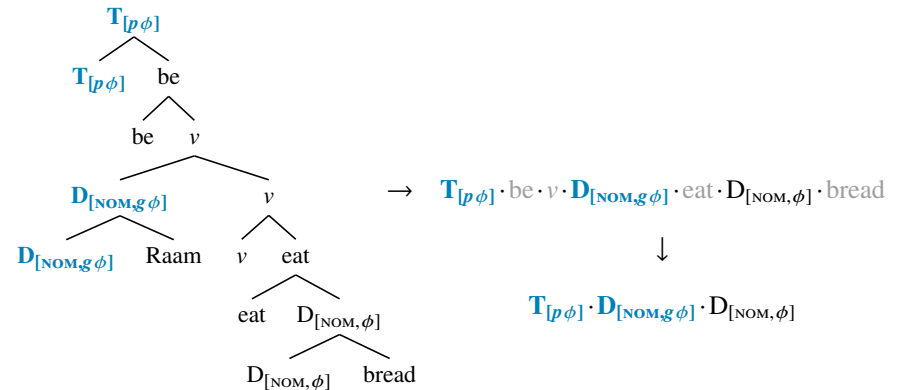
- Hindi verbal agreement ignores ergatives (Mahajan 1990)

- Raam roTii khaataa thaa.
Raam.**M.NOM** bread.**F.NOM** eat.IPFV.**M** be.PST.**M**
'Raam ate bread (habitually).'
- Raam-ne roTii khaayii.
Raam.**M-ERG** bread.**F.NOM** eat.PFV.**F**
'Raam ate bread.'

Analysis: Project D only if nominative. Tier constraints are unchanged.

■ Case-sensitive agreement (2) ■

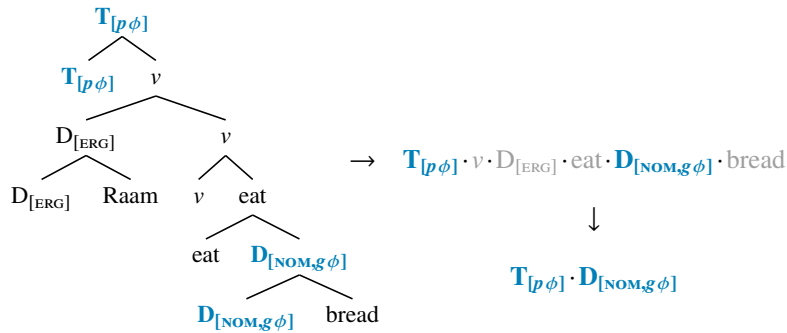
'Raam ate bread (habitually).' (Nominative subject, subject agrees)



We ignore agreement on the non-finite verb for simplicity. Concord will be discussed later.

■ Case-sensitive agreement (3) ■

‘Raam ate bread.’ (Ergative subject, object agrees)



■ Ergative ≠ Invisible ■

Ergatives are not invisible in Nepali (though datives are).

(2) Agreement with ergative in Nepali (Coon and Parker 2019)

- a. Maile yas pasal-mā patrikaā kin-ē.
1SG.ERG DEM store-LOC newspaper.ABS buy-**1SG**
 ‘I bought the newspaper in this store.’
- b. Ma thag-i-ē.
1SG.ABS cheat-PASS-**1SG**
 ‘I was cheated.’

No problem! We project $D_{[NOM]}$ and $D_{[ERG]}$ but not $D_{[DAT]}$.

■ Formal vs substantive constraints ■

- Bobaljik’s (2008) case visibility hierarchy: Nom > Acc/Erg > Obliques
- We can encode the attested patterns in a TSL-2 grammar, but the implicational hierarchy itself requires a separate explanation.

■ Concord in the DP ■

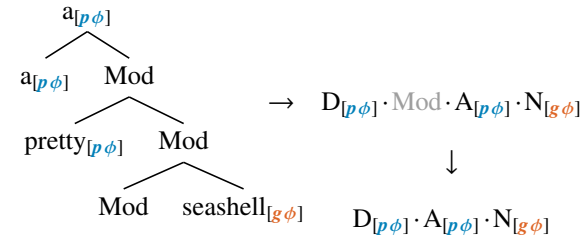
To allow for iterated agreement, just permit $p\phi \cdot p\phi$.

- (3) Gender concord in German
 Ich habe [eine hübsche Muschel] gefunden.
 I have [a.**F** pretty.**F** seashell.**F**] found
 ‘I found a pretty seashell.’

Analysis: Ignore Mod on the tier, permit $D_{[p\phi]} \cdot A_{[p\phi]}$ and $A_{[p\phi]} \cdot A_{[p\phi]}$.

■ Concord in the DP (2) ■

Analysis: Ignore Mod on the tier, permit $D_{[p\phi]} \cdot A_{[p\phi]}$ and $A_{[p\phi]} \cdot A_{[p\phi]}$.



The Mod head is not crucial. If direct adjunction is used, then the pattern is local: the tier contains everything.

■ Upward agreement ■

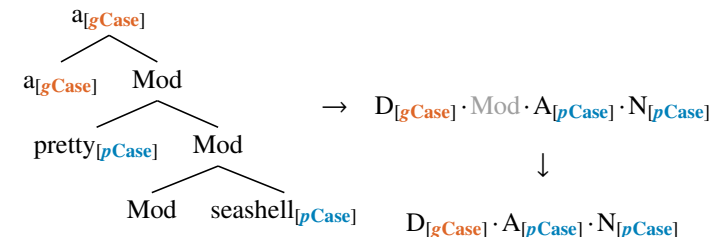
If the constraints are mirrored, then the direction of agreement is reversed.

- (4) Case concord in German
 Ich habe [eine hübsche Muschel] gefunden.
 I have [a.**ACC** pretty.**ACC** seashell.**ACC**] found

Analysis: allow $D_{[gCase]} \cdot A_{[pCase]}$ instead of $D_{[pCase]} \cdot A_{[gCase]}$, etc.

■ Upward agreement (2) ■

Analysis: allow $D_{[gCase]} \cdot A_{[pCase]}$ instead of $D_{[pCase]} \cdot A_{[gCase]}$, etc.



We can handle definiteness agreement on the adjective (ignored here) in the same way.

■ What does it mean to probe upward? ■

- In the MG derivation tree formalism (Graf and Shafiei 2019), we have a static representation of the entire derivation, so there is no problem.
- In a bottom-up Minimalist derivation, it is not obvious what it means for a probe to search upward. Some possibilities:
 - Let valued features search downward for unvalued features (Adger 2003)
 - Replace the search metaphor with the sliding window metaphor

■ Typological variation – summary ■

Example	Tier Elements	Tier Constraints
(Canonical) subject-verb agreement	All T/D/C	Strict pairing of $p\phi$ and $g\phi$
Case-sensitive agreement	All T/C D only if right case	(as above)
Concord within DP	All D/Adj/N	Allow sequential $p\phi$
Upward agreement	(as above)	Swap order of $p\phi/g\phi$

■ Parallels with phonology ■

Parameter	ϕ -agreement	Vowel harmony
Participants	Probe and most DPs	Most vowels
Invisible	Non-DPs, some DPs	Consonants, some vowels
Blockers	Finite C, some DPs	Some vowels
Directionality	Downward/upward	Progressive/regressive
Chaining	Concord/no concord	Spreading/“icy targets”

See McMullin (2016) and McMullin and Hansson (2016) regarding long-distance harmony.

■ What else is TSL? ■

Phenomenon	One line summary
Defective intervention*	Some DPs project even if they are never $g\phi$
Probe horizons (Keine 2019)	V/v/T/C project even if they are never $p\phi$
A'-agreement (Van Urk 2015)*	Only project DPs with a certain A' feature
Omnivorous number	Only project DPs with [PL], not [SG]
Upward C agr. (Diercks 2013)*	C probes up, only project DPs that EPP-move
Default agreement*	Allow lone $p\phi$ under limited circumstances
Interaction/Satisfaction (Deal 2015)*	Allow multiple $g\phi$ under limited circumstances
Independent subfeatures of ϕ	Each probe gets its own tier/constraints

Also: many movement (Graf 2022b) and case patterns (Vu et al. 2019; Hanson 2023b), though these analyses use a different tier-based model.

*See Hanson (2023a) and Hanson (2024a) for details.

■ What *isn't* TSL? ■

Not all linguistic patterns are TSL. Of those that are not, most appear to be SS-TSL (structure-sensitive TSL). These include:

- Some long-distance harmony (De Santo and Graf 2019; Graf and Mayer 2018)

- Some tone patterns (e.g. unbounded tone plateauing)
- Some binding rules (Graf and Shafiei 2019)

6 Strengths and limitations of the model

■ Advantages of the model ■

- Clear separation of concerns:
 - Structural representation
 - Computations over said structure
 - Substance of elements of structure
- Insights:
 - Agreement is especially similar to harmony as both involve feature matching; the same seems to be true of movement
 - If case is different, this is plausibly because it involves different kinds of constraints (e.g. dependent case)

■ Limitations of the model ■

Puzzles for the path-based approach:

- What to do about violations of c-command (e.g. sub-command)?
- How to handle exceptions to the complement spine generalization?

What the TSL model (alone) does not tell us:

- Why does case matter for ϕ -agreement? Why should nominatives always be visible, ergatives sometimes visible, and datives usually invisible?
- Why do probes seem to look downward more often than upward?
- How do children identify the visible elements and constraints for each dependency? (see Hanson 2024b; Belth 2023)

7 Conclusion

■ Summary ■

- Agreement patterns in syntax are largely TSL with a window size of 2.
- If we vary the tier projection and constraints slightly, we can account for a wide range of variation across languages and constructions.
- This variation is similar to other linguistic phenomena, especially phonological harmony.
- Most of the logical possibilities of the model are realized within a single phenomenon — this is not necessarily expected!

■ Some open questions ■

- Do we ever need a window size larger than 2?

- Are there patterns that are not TSL under any reasonable analysis?
- How far can we take the parallel with harmony in phonology?

■ Takeaways ■

- Computational approaches to linguistic analysis reveal insights that might otherwise not be obvious.
- In other cases, they provide independent support to conclusions reached in other ways (e.g. visibility is parameterized).
- A clear understanding of the formal patterns can help us understand other aspects of linguistic structure.

■ Acknowledgments ■

This work was partly supported by NSF Grant BCS-1845344 and by the Institute for Advanced Computational Science at Stony Brook University.

Thanks to Thomas Graf, Sandhya Sundaresan, Tom McFadden, and John Bailyn for comments and feedback throughout the project.

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A Extras

A.1 Even more on TSL

■ Extra example: Sibilant harmony ■

Sibilants match in anteriority, *t* blocks harmony, other *C*’s transparent
(based on Slovenian)

All elements:	{s, ʃ, t, k, a}
Tier elements:	{s, ʃ, t}
Constraints:	{*sʃ, *ʃs}

Word	Tier	
s a s a s a	s s s	✓
s a s a ʃ a	s s ʃ	✗
s a k a s a	s s	✓
s a k a ʃ a	s ʃ	✗
s a t a s a	s t s	✓
s a t a ʃ a	s t ʃ	✓

■ TSL string languages – formal definition ■

In a **tier-based strictly *k*-local (TSL-*k*)** language, a string is well-formed iff its **tier projection** does not contain any forbidden substrings of some length *k*.

- Σ = “alphabet” = set of all symbols
- T = “tier alphabet” = set of visible symbols
- G = “grammar” = forbidden substrings
- The tier projection is obtained by deleting all non-tier elements and concatenating the remaining elements.

Example: vowel harmony (redux)

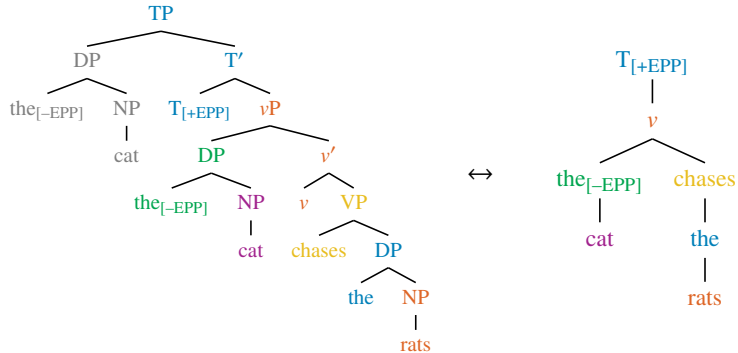
$\Sigma = \{k, b, l, i, e, u, o, a\}$
 $T = \{i, u, o, a\}$
 $k = 2$
 $G = \{iu, *ui, *io, *oi\}$

String	Tier projection	Substrings	
kubulo	uuo	$\{uu, uo\}$	✓
kibilo	iio	$\{ii, io\}$	✗
kubelo	uo	$\{uo\}$	✓
kibelo	io	$\{io\}$	✗
kubalo	uao	$\{ua, ao\}$	✓
kibalo	iao	$\{ia, ao\}$	✓

A.2 Some formal details

MG derivation trees

- All nodes appear in base position.
- The rightmost child of a node is its complement; others are specifiers.
- Movement is indicated using feature diacritics.

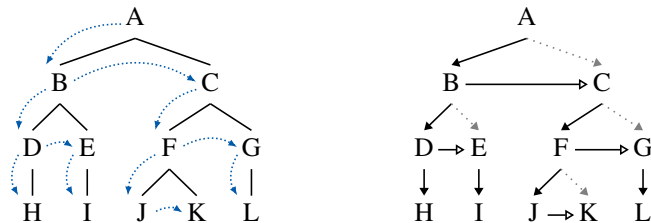


See Graf and Kostyszyn (2021) for a formal definition. Related: Brody (2000).

Command strings

A **command string** (c-string) is a derivational ordering of nodes.

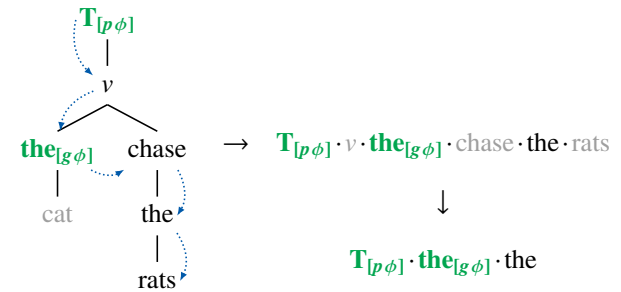
- There is a c-string from the root to each node.
- Among each head and its arguments: Head < Specifier < Complement.



See Graf and Shafiei (2019) for details.

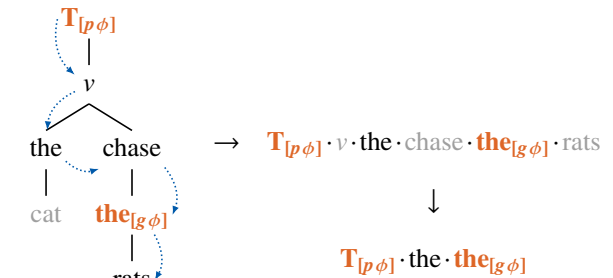
Tiers over command strings

✓ The cat **chases** the rats. (subject agreement)



Tiers over command strings (2)

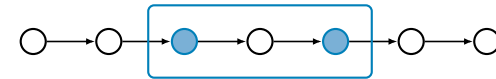
✗ The cat **chase** the rats. (object agreement)



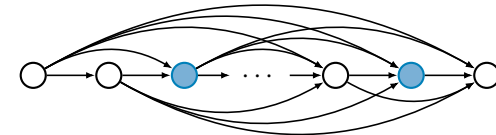
A.3 More on locality

Three models of locality

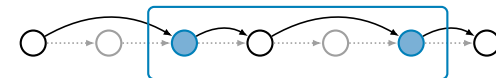
Immediate precedence (SL)



General precedence (SP)



Tier precedence (TSL)



■ Three models of locality (2) ■

- The immediate precedence (SL) model can handle local spreading.
- The general precedence (SP) model can handle unbounded processes, but can't handle blockers.
- Only the tier precedence (TSL) model can handle unbounded processes with blocking.

A.4 Computational considerations

■ Limits on structural configurations ■

TSL computations can relate elements at a distance, but are otherwise severely restricted in what they can do.

- No arbitrary logic — “a DP can A-move out of a finite CP, but only if there is A'-movement within some (other) CP in the sentence”
- No counting — “up to three reflexive pronouns may occur in a sentence if each obeys the Binding Theory”

These characteristics derive from the restriction that all constraints must be stated within the moving window.

■ Conditions for efficient learning ■

- The restrictions on TSL patterns help to make them efficiently learnable by limiting the amount of memory needed (Lambert et al. 2021).
- But there are too many possible tiers to test them all individually.
- We also need to consider other aspects of language acquisition such as the Tolerance Principle (see eg. Belth 2023; Hanson 2024b).