The Computational Basis of Locality in Syntactic Agreement

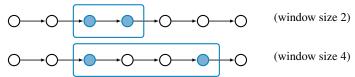
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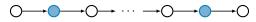
1 Introduction

■ What does it mean to be local? ■

Local → finitely bounded



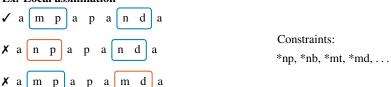
Long-distance (non-local) \rightarrow no finite bound



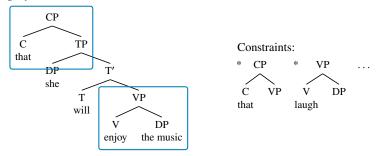
■ Not just local, *strictly local* ■

Strictly local (SL): constraints on substrings (or subtrees) of fixed size (Rogers et al. 2013; Rogers 1997).

Ex. Local assimilation



Ex. Category selection



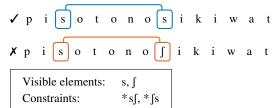
This presentation adapts an MG derivation tree-based analysis to mainstream Minimalism. See Hanson (2023a) for a more formal presentation (https://www.kennethhanson.net/files/hanson-nyubb2023-agreement-slides.pdf).

The full structure is well-formed iff all substructures are well-formed. The contents of different window positions may not be compared.

■ Adding in non-locality ■

Tier-based strictly local (TSL) patterns: like SL, but *irrelevant elements are ignored* (Heinz et al. 2011; Lambert and Rogers 2020).

Ex. Sibilant harmony (Heinz 2018)



Ex. ϕ -agreement (this talk)

✓ There $\mathbf{seem}_{\mathbf{PL}}$ [TP to be some problems_{PL} with this theory].

% There $\mathbf{seems_{sG}}$ [TP to be some problems_{PL} with this theory].

Visible elements: finite T, all D
Constraints: *SG·PL, *PL·SG

(To be revised.)

■ Overview ■

Main claim: Long-distance linguistic dependencies are predominantly TSL with a window size of two – they are **tier-based strictly 2-local (TSL-2)**.

- Phonotactics (McMullin 2016; McMullin and Hansson 2016)
- Morphotactics (Aksënova et al. 2016)
- Movement (Graf 2018; Graf 2022)
- Case assignment (Hanson 2023b)
- Agreement (this work)

Focus for today: TSL-2 provides a unified model of locality based on a moving window of visibility.

- Encompasses relativized minimality (Rizzi 1990; Rizzi 2013), selective opacity (Keine 2019), case discrimination (Bobaliik 2008), and more.
- Derives (one type of) myopia in grammar from computational considerations (Rogers et al. 2013; Lambert et al. 2021).

■ Roadmap ■

- 1. TSL patterns and their properties
- 2. A TSL model of agreement
- 3. Consequences for locality
- 4. Typological variation, parallels across domains
- 5. Strengths and limitations of the model

2 TSL patterns

■ What is a TSL pattern? ■

- 1. Ignore the irrelevant items and treat the rest as if adjacent
- 2. All constraints must be stated within a fixed-size moving window

Example: Vowel harmony

i/u/o obey front-back harmony, e is transparent/neutral, a is opaque

All elements:	k, b, l, i, e , u, o, a
Tier elements:	i, u, o, a
Invisible elements:	k, b, l, e
Window size:	2
Constraints:	*iu, *io, *oi, *ui

Word	Tier	
kubulo	uuo	1
kibilo	iio	Х
kubelo	uo	1
kibelo	io	Х
kubalo	uao	1
k ibalo	iao	1

See Appendix A.1 for another example and a formal definition.

■ More about TSL ■

- Inspired by but distinct from autosegmental phonology (Goldsmith 1976)
- Special relational structure combined with very weak constraint logic (cf. Lambert and Rogers 2020; Lambert et al. 2021; Lambert 2023)
- Related: ITSL and OTSL functions model a wide range of phonological maps (Burness et al. 2021)



Two adjacent elements on a tier

3 A TSL Model of Agreement

■ Setup ■

Assumptions:

- Bare phrase structure, feature-driven selection, movement, some method of case assignment
- Agreement between elements with initially unvalued features (probes) and elements which provide those values (goals)¹

Question: What are the possible arrangements of probes and goals for agreement?

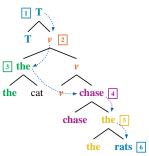
Answer: They are TSL-2 constraints on the "search path" of the probe.

■ The search path ■

I assume that the search path follows the **derivational command (d-command)** relation (Graf and Shafiei 2019).

- Head < Spec < Comp
- d-command order \approx height of XP
 - ≈ order of last merge
 - \approx reverse order of selection
- Projections of a head are not distinguished.
- At each branching point, follow the complement spine (Graf and De Santo 2019).

ex. 'The cat chases the rats.'



See Appendix A.3 for how this works using derivation trees.

■ The TSL analysis ■

General principle: a probe must be immediately followed by its goal on a tier projected from the search path (and vice versa).

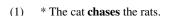
Notation: $p\phi$ = probe $g\phi$ = actual goal ϕ = other potential goal

Example: (canonical) subject-verb agreement

Tier elements: All agreeing elements (T/D) and blockers (C)

Constraints: ${}^*T_{[p\phi]} \cdot D_{[\phi]}, {}^*T_{[p\phi]} \cdot C, {}^*D \cdot D_{[g\phi]}, {}^*D_{[g\phi]} \cdot D_{[g\phi]}, \dots$

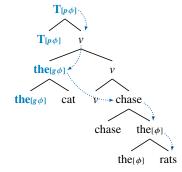
■ The TSL analysis – example ■



Path: $\mathbf{T}_{[p\phi]} \cdot v \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{V} \cdot \mathbf{D}_{[\phi]} \cdot \mathbf{N}$

Tier: $\mathbf{T}_{[p\phi]} \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{D}_{[\phi]}$

Violations: n/a



For simplicity, we substitute most items with their category labels in the path and tier projection.

4 Consequences for locality

■ Consequences for locality **■**

- **Blocking:** if another element intervenes on the tier, agreement is blocked, regardless of whether the blocker itself can agree.
 - relativized minimality (Rizzi 1990; Rizzi 2013)

¹I use the term **agreement** rather than **Agree** to indicate that we are not dealing with other phenomena that are sometimes subsumed under Agree. I retain the terms probe and goal for convenience.

- domain-based blocking
- Invisibility: if a DP is omitted from the tier, strict minimality may be violated.
 - agreement across there
 - case-sensitive agreement (Bobaljik 2008; Preminger 2014)

■ Minimality ■

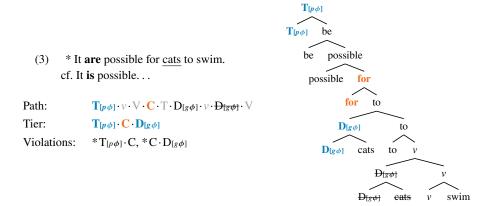
If another potential goal intervenes on the tier, agreement is blocked.

(2) * The cat **chase** the rats.

Path: $\mathbf{T}_{[p\phi]} \cdot \mathbf{V} \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{V} \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{N}$ Tier: $\mathbf{T}_{[p\phi]} \cdot \mathbf{D}_{[\phi]} \cdot \mathbf{D}_{[g\phi]}$ Violations: * $\mathbf{T}_{[p\phi]} \cdot \mathbf{D}_{[\phi]} \cdot \mathbf{D}_{[g\phi]}$ the $[\phi]$ cat v chase the $[g\phi]$ rat

■ Domain-based blocking **■**

If a non-agreeing element is projected on the tier, agreement is likewise blocked.



Assume for the sake of demonstration that expletive "it" is inserted late and does not agree.

■ Invisibility ■

If a DP is omitted from the tier, strict minimality may be violated.

seem (4) There **seem** to be some ducks in the garden. seem to there Path: $\mathbf{T}_{[p\phi]} \cdot v \cdot \mathbf{V} \cdot \mathbf{T} \cdot \text{there} \cdot v \cdot \text{Pred} \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{P} \cdot \mathbf{D}_{[\phi]} \cdot \mathbf{N}$ Tier: $\mathbf{T}_{[p\phi]} \cdot \mathbf{D}_{[g\phi]} \cdot \mathbf{D}_{[\phi]}$ to be Violations: n/a Pred be Pred $some[g\phi]$ $some[g\phi]$ ducks Pred in the garden

We can handle optional default agreement in several ways. Ask me if you are interested.

■ Case-sensitive agreement **■**

In Hindi, the verb agrees with the closest nominative argument, which may not be the subject.

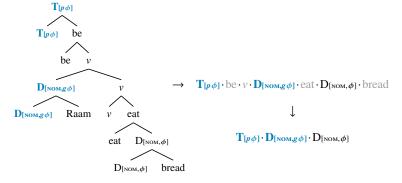
- (5) Hindi verbal agreement ignores ergatives (Mahajan 1990)
 - a. Raam roTii khaataa thaa. Raam.m.nom bread.F.nom eat.ipfv.m be.pst.m
 - 'Raam ate bread (habitually).'
 - b. Raam-ne roTii khaayii. Raam.**M-ERG** bread.**F**.NOM eat.PFV.**F**

'Raam ate bread.'

Analysis: Project D only if nominative. Tier constraints are unchanged.

■ Case-sensitive agreement (2) ■

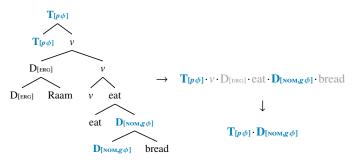
'Raam ate bread (habitually).' (Nominative subject, subject agrees)



We ignore agreement on the non-finite verb for simplicity.

■ Case-sensitive agreement (3) ■

'Raam ate bread.' (Ergative subject, object agrees)



■ Locality – interim summary ■

Locality phenomena derive from TSL with a window of size two, a.k.a. **TSL-2**.

• Blocking: some (non-)agreeing element intervenes on the tier

$$T_{[p\phi]}\dots C\dots D_{[g\phi]}$$
 $T_{[p\phi]}\dots D_{[\phi]}\dots D_{[g\phi]}$

• Invisibility: hypothetical goal does not appear on tier

$$T_{[p\phi]}\dots$$
 there. . . $D_{[g\phi]}$ $T_{[p\phi]}\dots D_{[\text{erg},\phi]}\dots D_{[\text{nom},g\phi]}$

■ The importance of the finite window **■**

- Neither tiers nor the finite window alone are adequate.
 - Tiers provide relativized locality.
 - Keeping all constraints within the moving window limits the power of the system.
- Other combinations of locality profile and constraint logic are either too powerful, too weak, or both.

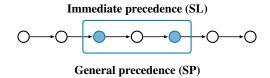
See Appendix A.4 for details.

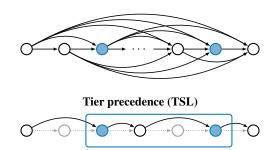
■ Limits on structural configurations **■**

TSL computations can relate elements at a distance, but are otherwise severely restricted in what they can do.

- No arbitrary logic "a DP can A-move out of a finite CP, but only if there is A'-movement within some (other) CP in the sentence"
- No counting "up to three reflexive pronouns may occur in a sentence if each obeys the Binding Theory"

■ Three models of locality **■**





Name of formal class combining locality model with logic of banned substructures in parentheses. SP stands for strictly piecewise.

■ Three models of locality (2) ■

- SL (immediate precedence) can handle local spreading.
- SP (general precedence) can handle unbounded processes, but can't handle blockers.
- Only TSL (tier precedence) can handle unbounded processes with blocking.

Typological variation

■ Variation in visibility ■

- Not all of invisibility and blocking can be analyzed purely in terms of relativized minimality
- Sometimes, even items which almost certainly possess the relevant features are invisible nonetheless
- Conversely, irrelevant items may block agreement
- Both types of exception are subject to variation across languages and dependencies

■ Case discrimination, revisited ■

Ergatives are not invisible in Nepali (though datives are).

- (6) Agreement with ergative in Nepali (Coon and Parker 2019)
 - a. Maile yas pasal-mā patrikaā kin-ē. 1sg.erg dem store-loc newspaper.abs buy-1sg 'I bought the newspaper in this store.'
 - thag-ī-ē. b. Ma 1sg.abs cheat-pass-1sg 'I was cheated.'

No problem! We project $D_{[NOM]}$ and $D_{[ERG]}$ but not $D_{[DAT]}$.

■ Selective opacity ■

"A particular structure may allow one movement [or agreement] type to proceed out of it but at the same time block other types of extraction [agreement]." – Keine (2019)

			Size of clause	
	Probe location	CP (finite)	TP (nonfinite)	vP (nonfinite)
ϕ -agreement	T	*	*	/
A-movement	T	*	*	✓
Wh-licensing	C	*	✓	✓
A'-movement	C	✓	✓	✓

Selective opacity in Hindi (adapted from Keine 2019)

■ Formal vs substantive constraints **■**

- Case visibility hierarchy (Bobaljik 2008):
 Nom > Acc/Erg > Obliques
- Height-locality connection (Keine 2019): The possible horizons for a (nonvacuous) probe on a head X which is a projection of Y exclude all extended projections of Y below X e.g. T cannot be a horizon for a probe on C
- We can encode the attested patterns in a TSL-2 grammar, but the implicational hierarchy itself requires a separate explanation.

■ Parameters for variation ■

The parameters for TSL-2 (tier elements and constraints) correspond neatly to variation in long-distance dependencies.

- 1. Visibility which elements are relevant and which are ignored?
 - Case-sensitive agreement (cf. Bobaljik 2008; Preminger 2014)
 - Probe horizons (Keine 2019)
- 2. Iteration if you allow AB and BB, then you get ABB, ABBB, etc.
 - · Case/gender/number concord
- 3. Directionality do we ban AB or BA?
 - Upward/downward agreement (cf. Chomsky 2000; Zeijlstra 2012; Carstens 2016)

For #2 & #3, see Appendix A.2

■ What else is TSL-2? ■

Phenomenon	One line summary
Defective intervention*	Some DPs project even if they are never $g\phi$
A'-agreement (Van Urk 2015)*	Only project DPs with a certain A' feature
Omnivorous number	Only project DPs with [PL], not [SG]
Upward C agr. (Diercks 2013)*	C probes up, only project DPs that EPP-move
Default agreement*	Allow lone $p\phi$ under limited circumstances
Interaction/Satisfaction (Deal 2015)*	Allow multiple $g\phi$ under limited circumstances
Parasitic agreement (Bhatt 2005)	Allow parasitic elements btw. $p\phi$ and $g\phi$
Independent subfeatures of ϕ	Each probe gets its own tier/constraints

Also: many movement (Graf 2022) and case patterns (Vu et al. 2019; Hanson 2023b), though these analyses use a different tier-based model.

■ What isn't TSL? ■

Not all linguistic patterns are TSL. Of those that are not, most appear to be SS-TSL (structure-sensitive TSL). These include:

- Some long-distance harmony (De Santo and Graf 2019; Graf and Mayer 2018)
- Some tone patterns (e.g. unbounded tone plateauing)
- Some binding rules (Graf and Shafiei 2019)

6 Parallels across domains

■ Parallels across domains ■

Parameter	ϕ -agreement	Wh-movement	Vowel harmony
Participants	Probe and most DPs	Probe and Wh-DPs	Most vowels
Invisible	Non-DPs, some DPs	Non-Wh elements	Consonants, some vowels
Blockers	Finite C, some DPs	Certain islands	Some vowels
Directionality	Downward/upward	???	Progressive/regressive
Chaining	Concord/no concord	Wh-agreement ²	Spreading/"icy targets"

■ Locality and typology ■

Type	Class	Example	Visible Cs
Unbounded	TSL-2	Aari	Only sibilants
LD w/ blocking	TSL-2	Slovenian	All coronals
Transvocalic	TSL-2	Koyra	All consonants
At most 1 C intervenes	TSL-3	Unattested	
Exactly 1 C intervenes	TSL-3	Unattested	
At least 1 C intervenes	TLT^3	Unattested	_

Typology of consonant (dis)-harmony (adapted from McMullin and Hansson 2016)

■ Locality and typology (2) ■

Non-TSL-2 and unattested island types (Graf 2022):

- Gang-up islands: A mover can escape n islands, but not n + 1.
- Configurational islands: XP is an island iff it is inside an embedded clause.
- Cowardly islands: XP is an island iff there are at least n XPs in the same clause.
- Narcissist islands: XP is an island iff there are no other XPs in the same clause.
- Rationed island effects: At most *n* phrases per clause can be an island.
- Discerning islands: XP is an island only for movers that contain a PP.

■ Locality and typology (3) ■

Non-TSL-2 and unattested subject-verb agreement types:

• Matrix T agrees with the embedded subject, and embedded T with the matrix subject.

^{*}See Hanson (2023a) and Hanson (2024a) for details.

²See Graf (2022).

³Maybe also SS-TSL, specifically OTSL [K.H.].

- T agrees with the subject only in a ditransitive clause, otherwise default agreement is required.
- T agrees with the subject unless there is a temporal adjunct, in which case it agrees with the
 object.
- When finite clauses are coordinated, agreement occurs in exactly one of them.
- Only DPs which contain a relative clause which contains two PPs can agree.

7 Strengths and limitations of the model

■ Advantages of the model ■

- Clear separation of concerns:
 - Structural representation
 - Computations over said structure
 - Substance of elements of structure
- Restrictive, independently rooted in well-understood mathematics
 - Subregular language hierarchy, relativized adjacency, etc.
- Agnostic to many analytical choices
 - e.g. Basic functional hierarchy vs cartographic hierarchy

■ Limitations of the model **■**

Puzzles for the path-based approach:

- What to do about violations of c-command (e.g. sub-command)?
- How to handle exceptions to the complement spine generalization?

What the formal model does not tell us:

- Why does case matter for φ-agreement? Why should nominatives always be visible, ergatives sometimes visible, and datives usually invisible?
- Why do probes seem to look downward more often than upward?
- How do children identify the visible elements and constraints for each dependency? (see Hanson 2024b; Belth 2023)

8 Conclusion

■ Summary ■

- A wide range of facts about the locality profiles of linguistic dependencies are explained if they are TSL with a window size of 2.
- From this perspective, agreement turns out to be especially similar to phonological harmony
 perhaps because both are feature-matching phenomena.
- Most of the logical possibilities of the model are realized within a single phenomenon this is not necessarily expected!

■ Some open questions ■

- Do we ever need a window size larger than 2?
- Are there agreement patterns that are not TSL under any reasonable analysis?
- How far can we take the parallel with harmony in phonology?

■ Takeaways ■

- Computational approaches to linguistic analysis reveal insights that might otherwise not be
 obvious.
- In other cases, they provide independent support to conclusions reached in other ways (e.g. visibility is parameterized).
- A clear understanding of the formal patterns can help us understand other aspects of linguistic structure.

■ Acknowledgments ■

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Extras

A.1 Even more on TSL

■ Extra example: Sibilant harmony ■

Sibilants match in anteriority, t blocks harmony, other C's transparent (based on Slovenian)

All elements:	$\{s, \int, t, k, a\}$
Tier elements:	$\{s, \int, t\}$
Constraints:	{*s∫, *∫s}

Word	Tier	
sasasa	SSS	1
s a s a ∫ a	s s ∫	X
sakasa	SS	✓
s a k a∫a	$s \int$	X
satasa	s t s	✓
sata∫a	s t∫	✓

■ TSL string languages – formal definition ■

In a tier-based strictly k-local (TSL-k) language, a string is well-formed iff its tier projection does not contain any forbidden substrings of some length k.

- Σ = "alphabet" = set of all symbols
- T = "tier alphabet" = set of visible symbols
- G = "grammar" = forbidden substrings
- The tier projection is obtained by deleting all non-tier elements and concatenating the remaining elements.

Example: vowel harmony (redux)

$\Sigma = \{k, b, l, i, e, u, o, a\}$
$T = \{i, u, o, a\}$
k = 2
$G = \{iu, *ui, *io, *oi\}$

String	Tier projection	Substrings	
kubulo	uuo	{uu,uo}	/
kibilo	iio	{ii,io}	X
kubelo	uo	{uo}	1
kibelo	io	{ io }	X
kubalo	uao	{ua,ao}	1
kibalo	iao	{ia,ao}	1

A.2 More agreement patterns

■ Concord in the DP ■

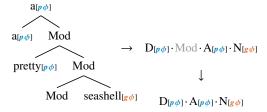
To allow for iterated agreement, just permit $p\phi \cdot p\phi$.

(7) Gender concord in German Ich habe [eine hübsche Muschel] gefunden. I have [a.F pretty.F seashell.F] found 'I found a pretty seashell.'

Analysis: Ignore Mod on the tier, permit $D[p\phi] \cdot A[p\phi]$ and $A[p\phi] \cdot A[p\phi]$.

■ Concord in the DP (2) ■

Analysis: Ignore Mod on the tier, permit $D[p\phi] \cdot A[p\phi]$ and $A[p\phi] \cdot A[p\phi]$.



The Mod head is not crucial. If direct adjunction is used, then the pattern is local: the tier contains everything

■ Upward agreement ■

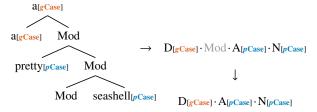
If the constraints are mirrored, then the direction of agreement is reversed.

(8) Case concord in German Ich habe [eine hübsche Muschel] gefunden. I have [a.acc pretty.acc seashell.acc] found

Analysis: allow $D[gCase] \cdot A[pCase]$ instead of $D[pCase] \cdot A[gCase]$, etc.

■ Upward agreement (2) ■

Analysis: allow $D[gCase] \cdot A[pCase]$ instead of $D[pCase] \cdot A[gCase]$, etc.



We can handle definiteness agreement on the adjective (ignored here) in the same way.

■ What does it mean to probe upward? ■

- In the MG derivation tree formalism (Graf and Shafiei 2019), we have a static representation of the entire derivation, so there is no problem.
- In a bottom-up Minimalist derivation, it is not obvious what it means for a probe to search upward. Some possibilities:
 - Let valued features search downward for unvalued features (Adger 2003)
 - Let Agree be upward, triggered once the relevant items are merged (Zeijlstra 2012)
 - Replace the search metaphor with the sliding window metaphor (my suggestion)

■ Interaction and satisfaction (Deal 2015) ■

Basic idea: Every probe has features that it interacts with (interaction set) and features that cause probing to stop (satisfaction set).

TSL analysis: Probe may be followed by zero or more interacting heads, followed by one that satisfies it.

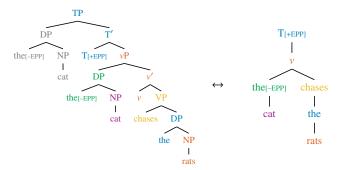
Formally:

- Let $p\phi$ denote the probe.
- Let $i\phi$ denote a feature in the interaction set but not the satisfaction set.
- Let $s\phi$ denote a feature in the satisfaction set.
- Let X stand for a head of any category.
- Allowed pairs: $X_{[p\phi]} \cdot X_{[s\phi]}, X_{[p\phi]} \cdot X_{[i\phi]}, X_{[i\phi]} \cdot X_{[s\phi]}$
- Banned pairs: everything else

A.3 A more formal syntactic model

■ MG derivation trees ■

- All nodes appear in base position.
- The rightmost child of a node is its complement; others are specifiers.
- Movement is indicated using feature diacritics.

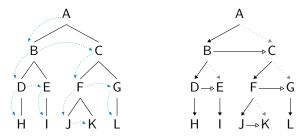


See Graf and Kostyszyn (2021) for a formal definition. Related: Brody (2000).

■ Command strings **■**

A **command string** (c-string) is a derivational ordering of nodes.

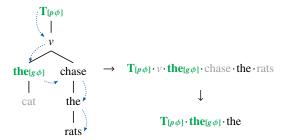
- There is a c-string from the root to each node.
- Among each head and its arguments: Head < Specifier < Complement.



See Graf and Shafiei (2019) for details.

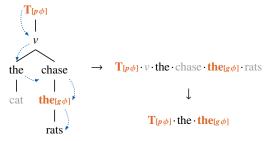
■ Tiers over command strings **■**

✓ The cat **chases** the rats. (subject agreement)



■ Tiers over command strings (2) ■

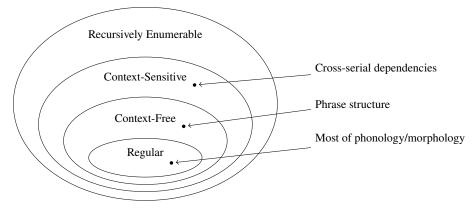
X The cat chase the rats. (object agreement)



A.4 Computational background

■ The Chomsky Hierarchy ■

Syntax is "mildly context sensitive" when analyzed over surface strings. It becomes subregular when analyzed over derivation trees.



■ The Subregular Hierarchy ■

