

# Simulation Step 8 Statistical Evaluation

July 15, 2024

## 1 Prelude

```
[1]: import matplotlib as mpl
import matplotlib.pyplot as plt
import pulp
import math
import random
import pandas as pd
import numpy as np
import simpy
```

## 2 Utilities

### 2.1 Points and Distances

```
[2]: def dist(p1, p2):
    (x1, y1) = p1
    (x2, y2) = p2
    return int(math.sqrt((x1-x2)**2+(y1-y2)**2))
```

### 2.2 PlotMap

```
[3]: def label(i):
    return (label(i//26-1)+chr(65+i%26)) if i>25 else chr(65+i)
```

```
[4]: def plotMap(G, T=[], P=[], w=None, frame=None,
    style='r-o', lw=1, ms=3,
    styleT='go', msT=3,
    styleP='b-o', lwP=2, msP=3,
    stylePT='go', msPT=7,
    styleW='ro', msW=9,
    text=None, grid=False, labels=False,
    size=4, scale=False):

    def round_down(x, level): return (x//level)*level
    def round_up(x, level): return (x//level+1)*level
```

```

if frame is not None:
    V, E = frame
else:
    V, E = G

xmin = round_down(min([ x for (x, _) in V ]), 100)
xmax = round_up(max([ x for (x, _) in V ]), 100)
ymin = round_down(min([ y for (_, y) in V ]), 100)
ymax = round_up(max([ y for (_, y) in V ]), 100)
dx = xmax-xmin
dy = ymax-ymin
yoffset = (ymax-ymin)//10
xoffset = (xmax-xmin)//20

V, E = G

fig = plt.gcf()
fig.set_size_inches(size, size)
plt.xlim(xmin-xoffset, xmax+xoffset)
plt.ylim(ymin-yoffset, ymax+yoffset)

if not grid:
    plt.axis('off')

if frame is not None:
    for e in frame[1]:
        if e not in E:
            p1, p2 = e
            plt.plot( [ p1[0], p2[0] ], [ p1[1], p2[1] ],
                      'k-', lw=0.5, ms=2)

for e in E:
    p1, p2 = e
    plt.plot( [ p1[0], p2[0] ],
              [ p1[1], p2[1] ],
              style, lw=lw, ms=ms)

if scale:
    # plot 1000m scale
    ybar = ymin-0.9*yoffset
    D = [ (xmin, ybar+50), (xmin, ybar), (xmin+1000, ybar), (xmin+1000,
↪ybar+50) ]
    plt.plot( [ d[0] for d in D ], [ d[1] for d in D ], 'k-', lw=0.5)
    plt.text(xmin+500, ymin-0.7*yoffset, '1000m' ,
↪horizontalalignment='center', size=8)

if labels:

```

```

    for i in range(len(V)):
        x, y = V[i]
        plt.text(x+0.0150*dx, y-0.0350*dy, label(i), size=8)

    for t in T:
        plt.plot( [ t[0] ], [ t[1] ],
                  styleT, ms=msT)

    plt.plot( [ p[0] for p in P ],
              [ p[1] for p in P ],
              styleP, lw=lwP, ms=msP)

    for p in P:
        if p in T:
            plt.plot( [ p[0] ], [ p[1] ],
                      stylePT, ms=msPT)
    if w is not None:
        plt.plot( [ w[0] ], [ w[1] ],
                  styleW, ms=msW)
    if text is not None:
        plt.text(xmax, ymin-0.9*yoffset, text, horizontalalignment='right',
        ↪size=8)
    if grid:
        plt.grid()
    plt.show()

```

## 2.3 Add Targets

```

[5]: def addTarget(M, T):
    V, E = M
    E = E.copy()
    V = V.copy()
    for t in T:
        minD = math.inf
        minE = None
        for e in E:
            P, Q = e
            distT = dist(P, t)+dist(t, Q)-dist(P, Q)
            if distT < minD:
                minD = distT
                minE = e
        P, Q = minE
        E.remove( (P, Q) )
        E.append( (P, t) )
        E.append( (t, Q) )
        V.append(t)
    return V, E

```

## 2.4 Generate Central Warehouse Location

```
[6]: from statistics import median

def generateWarehouseLocation(M):
    V, _ = M
    xc = median([ x for (x, y) in V ])
    yc = median([ y for (x, y) in V ])
    cloc = (xc, yc)
    minloc = V[0]
    mindist = dist(minloc, cloc)
    for i in range(1, len(V)):
        d = dist(V[i], cloc)
        if d < mindist:
            minloc = V[i]
            mindist = dist(V[i], cloc)
    return minloc
```

```
[7]: def generateMultipleWarehouseLocations(M, N=5):
    C = generateWarehouseLocation(M)
    V, _ = M
    distances = [ (i, pathLength(shortestPath(M, V[i], C))) for i in
↪range(len(V)) ]
    faraway = sorted(distances, key=lambda x: x[1], reverse=True)
    index = [ i*(len(faraway)-1)/(N-1) for i in range(N) ]
    locations = [ V[faraway[i][0]] for i in index ]
    return locations
```

## 2.5 Time Handling

**Convention:** In this project we measure simulation time in seconds. The simulation will start at 0:00. Time related methods will be added as they are needed.

timestamp(t) generates a timestamp string in the form [dd] hh:mm:ss.d

```
[8]: def timestamp(t):
    t = round(t, 1)
    day = int(t)/(24*3600)
    t = t - day*24*3600
    hour = int(t)/3600
    t = t - hour*3600
    mins = int(t)/60
    t = t - mins*60
    secs = int(t)
    t = int(round((t-secs)*10,1))
    return f"[{day:2d}] {hour:02d}:{mins:02d}:{secs:02d}.{t:1d}"
```

```
[9]: timestamp(24*3600*3+17*3600+615.1)
```

```
[9]: '[ 3] 17:10:15.1'
```

```
[10]: timestamp(24*3600*12+3*3600+122.1)
```

```
[10]: '[12] 03:02:02.1'
```

```
[11]: def day(now):  
      return int(now//(24*3600))
```

```
[12]: def nextHour(env, hour):  
      beginningOfDay = int(env.now//(24*3600))*24*3600  
      timeOfDay = env.now-beginningOfDay  
      if hour*3600 > timeOfDay:  
          return hour*3600 - timeOfDay  
      else:  
          return hour*3600 + 24*3600 - timeOfDay
```

## 2.6 Plotting Routines

```
[13]: import scipy.stats as stats  
  
def histPlot(data, title="", xlabel="",  
             discrete=False, width=None, height=None):  
  
    minx = min(data)  
    maxx = max(data)  
    = np.mean(data)  
    = np.std(data)  
  
    fig = plt.figure()  
    fig.set_figwidth(width if width is not None else 4)  
    fig.set_figheight(height if height is not None else 2.5)  
    ax = fig.gca()  
  
    if discrete:  
        bins = [ i-0.5 for i in range(maxx+2) ]  
        ax.xaxis.set_major_locator(mpl.ticker.MaxNLocator(integer=True))  
        hist=plt.hist(data, bins=bins, rwidth=0.9, density=True)  
    else:  
        hist=plt.hist(data, density=True)  
    plt.xlabel(xlabel)  
    plt.ylabel('Density')  
    plt.title(title)  
  
    if discrete:  
        poisson=stats.poisson()  
        x = [ i for i in range(maxx+1) ]
```

```

        y = [ poisson.pmf(i) for i in range(maxx+1) ]
        ax.plot(x, y, lw=1, color='red')
    else:
        x = np.linspace(minx, maxx, 100)
        y = [ stats.norm(loc=, scale=).pdf(p) for p in x]
        ax.plot(x, y, lw=1, color='red')

    ax.axvline(x=, color='red')
    maxy = max(max(y), max(hist[0]))
    ax.text(maxx, maxy,
            f'={:2.2f}\n={:2.2f}',
            ha='right', va='top',
            color='red', fontsize=12)

    # ax.grid(True)
    plt.show()

def dailyPlot(data,
               title="", ylabel="",
               width=None, height=None):

    days = len(data)

    fig = plt.figure()
    fig.set_figwidth(width if width is not None else 6)
    fig.set_figheight(height if height is not None else 2)

    ax = fig.gca()
    diff = (max(data)-min(data)+1)*0.1
    ymin = math.floor(min(data))-diff
    ymax = math.ceil(max(data))+diff
    ax.set_xlim(-0.5, days-1+0.5)
    ax.set_ylim(ymin-0.5, ymax+0.5)
    ax.grid(True)

    ms = 2 if len(data)>=100 else 3
    lw = 0.5 if len(data)>=100 else 1

    x = np.arange(0, len(data))
    y = np.array([ y for y in data ])
    b, m = np.polynomial.polynomial.polyfit(x, y, 1)
    ax.xaxis.set_major_locator(mpl.ticker.MaxNLocator(integer=True))
    ax.yaxis.set_major_locator(mpl.ticker.MaxNLocator(integer=True))

    plt.plot(x, y, 'bo-', linewidth=lw, markersize=ms)
    plt.plot(x, m*x+b, 'r-')

```

```

plt.xlabel('Day')
plt.ylabel(ylabel)
plt.title(title)
plt.show()

def countPlot(A, B,
              title="", ylabel="",
              width=None, height=None):

    assert(len(A)==len(B))
    days = len(A)
    xmax = days-1
    ymax = A.max()

    fig = plt.figure()
    fig.set_figwidth(width if width is not None else 6)
    fig.set_figheight(height if height is not None else 4)
    ax = fig.gca()
    ax.set_xlim(-0.5, xmax+0.5)
    ax.set_ylim(0, ymax)

    def double(l, offset=0):
        return [] if l==[] else [l[0]+offset, l[0]+offset]+double(l[1:], offset)

    x = double([i for i in range(days)]+[days])
    xz = double([i+days*0.006 for i in range(days)]+[days])
    y = [0+ymax*0.006] + double(list(A), offset=ymax*0.006)
    z = [0] + double(list(B))

    ax.yaxis.set_major_locator(mpl.ticker.MaxNLocator(integer=True))
    ax.xaxis.set_major_locator(mpl.ticker.MaxNLocator(integer=True))

    for i in range(days):
        ax.fill_between([i, i+1],
                        [z[2*i+1], z[2*i+2]],
                        [y[2*i+1], y[2*i+2]], color='blue', alpha=0.2)

    lw = 1 if days>=50 or ymax>=100 else 2
    ax.plot(x, y, color='blue', lw=lw)
    ax.plot(xz, z, color='red', lw=lw)
    plt.xlabel('Day')
    plt.ylabel(ylabel)
    plt.title(title)
    ax.grid(True)
    plt.show()

```

### 3 Finding Shortest Path (as before)

```
[14]: def pathLength(P):  
    return 0 if len(P)<=1 else \  
        dist(P[0], P[1])+pathLength(P[1:])
```

```
[15]: def shortestPath(M, A, B):  
  
    def h(p):  
        return pathLength(p)+dist(p[-1],B)  
  
    # candidates C are pairs of the path so far and  
    # the heuristic function of that path,  
    # sorted by the heuristic function, as maintained by  
    # insert function  
    def insert(C, p):  
        hp = h(p)  
        c = (p, hp)  
        for i in range(len(C)):  
            if C[i][1]>hp:  
                return C[:i]+[c]+C[i:]  
        return C+[c]  
  
    V, E = M  
    assert(A in V and B in V)  
    C = insert([], [A])  
  
    while len(C)>0:  
        # take the first candidate out of the list of candidates  
        path, _ = C[0]  
        C = C[1:]  
        if path[-1]==B:  
            return path  
        else:  
            for (x, y) in E:  
                if path[-1]==x and y not in path:  
                    C = insert(C, path+[y])  
                elif path[-1]==y and x not in path:  
                    C = insert(C, path+[x])  
  
    return None
```



## 4 Finding Short Delivery Route (as before)

### 4.1 Greedy Algorithm

```
[16]: def FW(M):  
  
    V, E = M  
  
    n = len(V)  
    d = [ [ math.inf for j in range(n) ] for i in range(n) ]  
    p = [ [ None for j in range(n) ] for i in range(n) ]  
  
    for (A, B) in E:  
        a = V.index(A)  
        b = V.index(B)  
        d[a][b] = d[b][a] = dist(A, B)  
        p[a][b] = [A, B]  
        p[b][a] = [B, A]  
  
    for i in range(n):  
        d[i][i] = 0  
        p[i][i] = [V[i]]  
  
    for k in range(n):  
        for i in range(n):  
            for j in range(n):  
                dk = d[i][k] + d[k][j]  
                if d[i][j] > dk:  
                    d[i][j] = dk  
                    p[i][j] = p[i][k][:-1] + p[k][j]  
  
    return d, p
```

```
[17]: def createLoopG(M, T, timing=False):  
  
    def makeLoop(L, V, P):  
        loop = []  
        for i in range(len(L)-1):  
            A = L[i]  
            B = L[i+1]  
            a = V.index(A)  
            b = V.index(B)  
            sub = P[a][b]  
            loop += sub if len(loop)==0 else sub[1:]  
        return loop  
  
    if timing:  
        start_time = time.time()
```

```

last_time = time.time()

V, E = M
D, P = FW(M)    # note these are the distances between all vertices in M
↪(and T)
W = T[0]
customers = T[1:]
if len(T)==1:
    L = T
elif len(T)<=3:
    L = T + [T[0]]
else:
    L = T[:3]+[T[0]]
    T = T[3:]
    while len(T)>0:

        minExt = math.inf
        minInd = None
        selInd = None
        for k in range(len(T)):
            C = T[k]
            c = V.index(C)
            for i in range(0, len(L)-1):
                A = L[i]
                B = L[i+1]
                a = V.index(A)
                b = V.index(B)
                ext = D[a][c] + D[c][b] - D[a][b]
                if ext<minExt:
                    minExt, minInd, selInd = ext, i+1, k
            L = L[:minInd]+[T[selInd]]+L[minInd:]
            T = T[:selInd]+T[selInd+1:]

if timing:
    print(f"createLoopG:    {time.time()-start_time:6.2f}s")

return makeLoop(L, V, P)

```

## 5 Finding Optimal Delivery Route

### 5.1 Iterative Integer Programming

```

[18]: def createTables(M, T):

    def reverse(P):
        return [ P[-i] for i in range(1,len(P)+1) ]

```

```

def index(x, L):
    for i in range(len(L)):
        if x==L[i]:
            return i
    return None

n = len(T)
d = [ [ math.inf for t in T ] for t in T ]
p = [ [ None for t in T ] for t in T ]
for i in range(n):
    d[i][i] = 0
    p[i][i] = [ T[i] ]
for i in range(n):
    for j in range(n):
        if p[i][j] is None:
            s = shortestPath(M, T[i], T[j])
            d[i][j] = d[j][i] = pathLength(s)
            p[i][j] = s
            p[j][i] = reverse(s)
            for m in range(len(s)-1):
                smi = index(s[m], T)
                if smi is None:
                    continue
                for l in range(m+1, len(s)):
                    sli = index(s[l], T)
                    if sli is None:
                        continue
                    sub = s[m:l+1]
                    if p[smi][sli] is None:
                        p[smi][sli] = sub
                        p[sli][smi] = reverse(sub)
                        d[smi][sli] = d[sli][smi] = pathLength(sub)

return d,p

```

```

[19]: def roundtrips(x, n):

    def isElem(x, l):
        for i in range(len(l)):
            if l[i]==x:
                return True
        return False

    def startpoint(trips):
        for i in range(n):
            for t in trips:
                if isElem(i, t):
                    break

```

```

        else:
            return i

def totalLength(trips):
    s=0
    for i in range(0, len(trips)):
        s += len(trips[i])-1
    return s

trips = []
while totalLength(trips)<n:
    start = startpoint(trips)
    trip = [ start ]
    i = start
    while len(trip) < n-totalLength(trips):
        for j in range(0, n):
            if pulp.value(x[i][j])==1:
                trip.append(j)
                i=j
                break
            if pulp.value(x[trip[-1]][start])==1:
                trip.append(start)
                break
        trips.append(trip)
    return sorted(trips, key=lambda t: len(t), reverse=True)

```

```

[20]: import time

def createLoop(M, T, timing=False):

    if timing:
        start_time = last_time = time.time()

    D, P = createTables(M, T)    # These are the distances between customers and
    ↪warehouse only

    if timing:
        print(f"createTables:    {time.time()-start_time:6.2f}s")
        last_time = time.time()

    n = len(T)
    # create variables
    x = pulp.LpVariable.dicts("x", ( range(n), range(n) ),
                               lowBound=0, upBound=1, cat=pulp.LpInteger)

    # create problem
    prob = pulp.LpProblem("Loop",pulp.LpMinimize)
    # add objective function

```

```

prob += pulp.lpSum([ D[i][j]*x[i][j]
                    for i in range(n) for j in range(n) ])

# add constraints
constraints=0
for j in range(n):
    prob += pulp.lpSum([ x[i][j] for i in range(n) if i!=j ]) ==1
constraints += n
for i in range(n):
    prob += pulp.lpSum([ x[i][j] for j in range(n) if i!=j ]) ==1
constraints += n
for i in range(n):
    for j in range(n):
        if i!=j:
            prob += x[i][j]+x[j][i] <= 1
            constraints += 1

def cycles(k, n):
    if k==1:
        return [ [i] for i in range(0,n) ]
    else:
        sc=cycles(k-1, n)
        all=[]
        for c in sc:
            for i in range(0,n):
                if c.count(i)==0:
                    all.append(c+[i])
        return all

for k in range(3, 4):
    cycs=cycles(k,n)
    for c in cycs:
        c.append(c[0])
        prob+=pulp.lpSum([ x[c[i]][c[i+1]] for i in range(0,k)]) <= k-1
        constraints += 1

# initialise solver
solvers = pulp.listSolvers(onlyAvailable=True)
solver = pulp.getSolver(solvers[0], msg=0, timeLimit=2)
res = prob.solve(solver)

if timing:
    print(f"Solver:          {time.time()-last_time:6.2f}s {constraints:6,d}␣
↳Constraints")
    last_time = time.time()

trips = roundtrips(x, n)
while len(trips)>1:

```

```

    longest = max([ len(t) for t in trips ])
    for t in trips:
        if len(t)<longest:
            prob += pulp.lpSum([ x[t[i]][t[i+1]] + x[t[i+1]][t[i]]
                                for i in range(0,len(t)-1) ]) <=
↪len(t)-2
                constraints += 1
        else:
            longest = math.inf

    res = prob.solve(solver)

    if timing:
        print(f"Solver:          {time.time()-last_time:6.2f}s {constraints:
↪6,d} Constraints")
        last_time = time.time()

    trips = roundtrips(x, n)
    trip = trips[0]
    # print(trip)
    loop = []
    for k in range(len(trip)-1):
        sub = P[trip[k]][trip[k+1]]
        loop += sub if len(loop)==0 else sub[1:]

    if timing:
        print(f"createLoop:      {time.time()-start_time:6.2f}s")

    return loop

```

## 6 Static Route Assignment

### 6.1 Chinese Postman Problem

```

[21]: import time

def solveCPP(M, PostOffice, n=1,
            maxLength=None, balance=None,
            timing=False, timeLimit=10):

    start_time = time.time()

    V, E = M

    postoffice = V.index(PostOffice)

    def edge(e): return label(V.index(E[e][0]))+label(V.index(E[e][1]))

```

```

def edges(l): return ",".join([ edge(i) for i in range(len(l)) if l[i]==1 ])
def path(p): return '-'.join([ label(v) for v in p ])

Edges = [ edge(e) for e in range(len(E)) ]

b = pulp.LpVariable.dicts("B", (range(n), range(len(V))), lowBound=0,
↳upBound=1, cat=pulp.LpInteger)

y0 = pulp.LpVariable.dicts("Y0", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)
y1 = pulp.LpVariable.dicts("Y1", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)
yp0 = pulp.LpVariable.dicts("YP0", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)
yp1 = pulp.LpVariable.dicts("YP1", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)
yn0 = pulp.LpVariable.dicts("YN0", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)
yn1 = pulp.LpVariable.dicts("YN1", (range(n), Edges), lowBound=0) # ,↳
↳upBound=len(E), cat=pulp.LpInteger)

e0 = pulp.LpVariable.dicts("E0", (range(n), Edges), lowBound=0, upBound=1,↳
↳cat=pulp.LpInteger)
e1 = pulp.LpVariable.dicts("E1", (range(n), Edges), lowBound=0, upBound=1,↳
↳cat=pulp.LpInteger)
dp0 = pulp.LpVariable.dicts("DP0", (range(n), Edges), lowBound=0,↳
↳upBound=1, cat=pulp.LpInteger)
dn0 = pulp.LpVariable.dicts("DN0", (range(n), Edges), lowBound=0,↳
↳upBound=1, cat=pulp.LpInteger)
dp1 = pulp.LpVariable.dicts("DP1", (range(n), Edges), lowBound=0,↳
↳upBound=1, cat=pulp.LpInteger)
dn1 = pulp.LpVariable.dicts("DN1", (range(n), Edges), lowBound=0,↳
↳upBound=1, cat=pulp.LpInteger)

def vars(l,x): return edges([ int(pulp.value(x[l][e])) for e in Edges ])
def vals(l,x): return [ round(pulp.value(x[l][e]),1) for e in Edges ]

prob = pulp.LpProblem("CPP", pulp.LpMinimize)

def loopLength(l):
    return pulp.lpSum([ dist(v1,v2)*e0[l][e] for e in Edges for v1 in V for↳
↳v2 in V if E[Edges.index(e)]==(v1, v2) ]) + \
        pulp.lpSum([ dist(v1,v2)*e1[l][e] for e in Edges for v1 in V for↳
↳v2 in V if E[Edges.index(e)]==(v1, v2) ])

prob += pulp.lpSum([ loopLength(l) for l in range(n) ])

```

```

# avoid non-trivial loops
# for l in range(n):
#     prob += pulp.lpSum([ b[l][v] for v in range(len(V)) ]) >= 2, f"NT_{l}"

if maxLength is not None:
    for l in range(n):
        prob += loopLength(l) <= maxLength, f"Max_{l}"

if balance is not None:
    d = pulp.LpVariable.dicts("D", range(n), lowBound=0)

    for l in range(n):
        prob += d[l] == loopLength(l), f"D_{l}"

    for l in range(n):
        prob += d[l] <= pulp.lpSum([ d[l] for l in range(n) ])*(1+balance)/
↪n, f"DMAX_{l}"
        prob += d[l] >= pulp.lpSum([ d[l] for l in range(n) ])*(1-balance)/
↪n, f"DMIN_{l}"

# Constraint YE: Y-E Relationship [equivalent to (9)]
BigM = 100*n*len(E)
for e in Edges:
    for l in range(n):
        prob += y0[l][e] <= BigM*e0[l][e], f"YE0_{l}_{e}"
        prob += y1[l][e] <= BigM*e1[l][e], f"YE1_{l}_{e}"

# Constraint C: counting [equivalent (8)]
for v in range(len(V)):
    if v!=postoffice:
        for l in range(n):
            prob += pulp.lpSum([ yp0[l][e]+yp1[l][e] for e in Edges if
↪E[Edges.index(e)][0]==V[v] ]) + \
            pulp.lpSum([ yn0[l][e]+yn1[l][e] for e in Edges if
↪E[Edges.index(e)][1]==V[v] ]) - \
            pulp.lpSum([ yp0[l][e]+yp1[l][e] for e in Edges if
↪E[Edges.index(e)][1]==V[v] ]) - \
            pulp.lpSum([ yn0[l][e]+yn1[l][e] for e in Edges if
↪E[Edges.index(e)][0]==V[v] ]) == -1*b[l][v], \
            f"C_{l}_{v}"+label(v)

# Invariance Constraint F/B: Relation between variables in each loop every
↪edge is passed this way or that way
for e in Edges:
    for l in range(n):

```



```

        prob += dp0[l][e]+dn0[l][e] == e0[l][e], f"EF_{l}_{e}"
        prob += dp1[l][e]+dn1[l][e] == e1[l][e], f"EB_{l}_{e}"
    for e in Edges:
        for l in range(n):
            prob += yp0[l][e]+yn0[l][e] == y0[l][e], f"YF_{l}_{e}"
            prob += yp1[l][e]+yn1[l][e] == y1[l][e], f"YB_{l}_{e}"

    # Constraint E10: The duplicate edge is only used if the primary edge was
    ↪used
    for e in Edges:
        for l in range(n):
            prob += e1[l][e] <= e0[l][e], f"E10_{l}_{e}"

    # Constraint 0: Every edge is passed across all loops at least once
    ↪[equivalent (2)]
    for e in Edges:
        prob += pulp.lpSum( [ e0[l][e]+e1[l][e] for l in range(n) ] ) >= 1, \
            f"0_{e}"

    # Constraint M: In each loop every edge is passed at most twice [equivalent
    ↪(7)]
    for e in Edges:
        for l in range(n):
            prob += e0[l][e]+e1[l][e] <= \
                pulp.lpSum([ 2*b[l][v] for v in range(len(V)) if E[Edges.
    ↪index(e)][0]==V[v] or E[Edges.index(e)][1]==V[v]]), \
                f"M_{l}_{e}"

    # Constraint V: In each loop every vertex is entered as often as it is left
    ↪[equivalent (3)]
    for v in range(len(V)):
        for l in range(n):
            prob += pulp.lpSum([ dp0[l][e]+dp1[l][e]-dn0[l][e]-dn1[l][e] for e
    ↪in Edges if E[Edges.index(e)][0]==V[v] ]) + \
                pulp.lpSum([ dn0[l][e]+dn1[l][e]-dp0[l][e]-dp1[l][e] for e
    ↪in Edges if E[Edges.index(e)][1]==V[v] ]) == 0, \
                f"V_{l}_{v}"

    # print(prob)

    solvers = pulp.listSolvers(onlyAvailable=True)
    solver = pulp.getSolver(solvers[0], msg=False, timeLimit=timeLimit)
    status = prob.solve(solver)

    solverTime = time.time()-start_time

```

```

if timing:
    print(f"Solver time: {solverTime:7.2f}s")

if status!=1:
    print(pulp.LpStatus[status])
    return []

if solverTime >= timeLimit:
    print("Solution possibly not optimal")

print(f"Total Delivery Path Length: {pulp.value(prob.objective)}")

def solutions(l):

    DP0 = [ int(pulp.value(dp0[l][e])) for e in Edges ]
    DP1 = [ int(pulp.value(dp1[l][e])) for e in Edges ]
    DN0 = [ int(pulp.value(dn0[l][e])) for e in Edges ]
    DN1 = [ int(pulp.value(dn1[l][e])) for e in Edges ]

    E0 = [ int(pulp.value(e0[l][e])) for e in Edges ]
    E1 = [ int(pulp.value(e1[l][e])) for e in Edges ]

    # candidates C are the paths so far,
    def insert(C, p): return [p]+C

    def refine(c, v, e0=None, e1=None):
        assert(e0 is not None or e1 is not None)
        if e0 is not None:
            c0 = c[0].copy()
            c0[e0] = 0
            return (c0, c[1], c[2]+[V.index(v)])
        if e1 is not None:
            c1 = c[1].copy()
            c1[e1] = 0
            return (c[0], c1, c[2]+[V.index(v)])

    def isSolution(cand):
        return sum(cand[0])+sum(cand[1])==0

    C = [ (E0, E1, [ V.index(PostOffice) ]) ]
    solutions = []

    while len(C)>0:

        # take the first candidate out of the list of candidates
        cand, C = C[0], C[1:]

```

```

    if isSolution(cand):
        # solutions.append(cand[2])
        return [ cand[2] ]
    else:
        last = cand[2][-1]
        for e in range(len(E)):
            newCand = None
            if V.index(E[e][0]) == last:
                ## print("edge", edge(e), 'forward extends',
↳path(cand[2]))
                # the edge begins in the current position
                if cand[0][e] == 1 and DPO[e] == 1:
                    newCand = refine(cand, E[e][1], e0=e)
                elif cand[1][e] == 1 and DP1[e] == 1:
                    newCand = refine(cand, E[e][1], e1=e)
                elif V.index(E[e][1]) == last: # the edge ends in the
↳current position
                ## print("edge", edge(e), 'backwards extends',
↳path(cand[2]))
                if cand[0][e] == 1 and DNO[e] == 1:
                    newCand = refine(cand, E[e][0], e0=e)
                elif cand[1][e] == 1 and DN1[e] == 1:
                    newCand = refine(cand, E[e][0], e1=e)
            if newCand is not None:
                # if isSolution(newCand): return [ newCand[2] ]
                C = insert(C, newCand)

        return solutions

return [ ( [ path(p) for p in solutions(l) ],
          [ [ V[v] for v in p ] for p in solutions(l) ],
          pulp.value(loopLength(l)) )
        for l in range(n) ]

```

```

[22]: def splitMap(fullMap, L, plot=False):
    Maps, Loops = [], []
    for l in range(len(L)):
        paths, loops, length = L[l]
        loop = loops[0]
        W = loop[0]

        V = []
        E = []
        for i in range(len(loop)-1):
            A, B = loop[i], loop[i+1]
            if A not in V:
                V.append(A)

```

```

        if (A, B) not in E and (B, A) not in E:
            E.append((A, B))
    subMap = V, E
    Maps.append(subMap)
    Loops.append(loop)

    if plot:
        #plotMap(fullMap, P=loop, w=W,
        #        labels=True, scale=True,
        #        text=f"Loop {l}: {int(length):7,d}m")

        plotMap(subMap, w=W, frame=fullMap, scale=True,
                text=f"Map {l}: Full Roundtrip {int(length):,d}m")

    return Maps, Loops

```

shortenLoop(L, T) shortens a complete coverage loop L while adding new targets T

```

[23]: def shortenLoop(L, M, T):
    for t in T:
        minD = math.inf
        minI = None
        for i in range(len(L)-1):
            P, Q = L[i], L[i+1]
            distT = dist(P, t)+dist(t, Q)-dist(P, Q)
            if distT < minD:
                minD = distT
                minI = i
        L = L[:minI+1]+[t]+L[minI+1:]
    success = True
    while success:
        success = False
        for i in range(len(L)-1):
            P = L[i]
            for j in range(i+1, len(L)):
                Q = L[j]

                if Q in T:
                    shortcut = shortestPath(M, P, Q)
                    if pathLength(shortcut)<pathLength(L[i:j+1]):
                        L = L[:i]+shortcut+L[j+1:]
                        success = True
                    break
            if Q==P:
                L = L[:i+1]+L[j+1:]
                success = True
                break

```

```

        if success:
            break
    return L

```

## 6.2 Split Customers into Regions

```

[24]: def pickRegion(C, Maps):
    options = []
    for m in range(len(Maps)):
        V, E = Maps[m]
        for (A, B) in E:
            if dist(A, C)+dist(C, B) - dist(A, B) <= 1:
                options.append(m)
    return random.choice(options)

```

```

[25]: def splitCustomers(C, Maps):
    return [ pickRegion(C[i], Maps) for i in range(len(C)) ]

```

```

[26]: def groupCustomersByRegions(C, Maps):
    regions = splitCustomers(C, Maps)
    n = len(Maps)
    CC = [ [] for i in range(n) ]
    for i in range(n):
        for c in range(len(C)):
            if regions[c]==i:
                CC[i].append(C[c])
    return CC

```

## 6.3 Integrated Planning Using CPP

```

[27]: def planCPP(M, W, C, n=1,
                maxLength=None, balance=None,
                timing=False, timeLimit=10, plot=False):
    L = solveCPP(M, W, n=n,
                maxLength=maxLength, balance=balance,
                timing=timing, timeLimit=timeLimit)
    if len(L)==0: # unfeasible solution
        return None

    MM, LL = splitMap(M, L)
    CC = groupCustomersByRegions(C, MM)

    if plot:
        for i in range(len(MM)):
            plotMap(MM[i], w=W, frame=M, scale=True,
                    text=f"Map {i}: Full Roundtrip {int(L[i][2]):,d}m")
            MMT = addTargets(MM[i], CC[i])

```

```

        path = shortenLoop(LL[i], MMT, [W] + CC[i])
        plotMap(MMT, T=CC[i], P=path, w=W, frame=M, lwP=1, msPT=3,
                text=f"Driver {i:d}: {len(CC[i]):d} Customers, "
                    f"max Roundtrip: {pathLength(path):,d}m")

    return MM, LL, CC

```

```

[28]: def getRegions(CC, C):
        regions = [ None for _ in C ]
        for i in range(len(CC)):
            for c in CC[i]:
                regions[C.index(c)] = i
        return regions

```

## 7 Class Recorder

We will use a class Recorder as a reference point for capturing data during the simulation. There will be only one recorder. It will be created at the beginning of every simulation run. Every entity will carry a reference to the Recorder.

```

[29]: import time

class Recorder:

    def __init__(self, env, M, W, C, D, Plan, days,
                 log=False, plot=False, timing=False):
        self.env = env
        self.M = M
        self.W = W
        self.C = C
        self.D = D
        self.MM, self.LL, self.CC = Plan

        self.parcels = sum([ len(d) for d in D ])
        self.days = days
        self.drivers = len(self.MM)

        self.log = log
        self.plot = plot

        # create a data frame for time records per working day
        self.daily = [ pd.DataFrame() for d in range(self.drivers) ]

        for driver in range(self.drivers):
            self.daily[driver]['begin work at'] = [None]*days
            self.daily[driver]['end work at'] = [None]*days
            self.daily[driver]['tour length'] = [None]*days

```

```

        self.daily[driver]['parcels left over'] = [0]*days
        self.daily[driver]['parcels arrived'] = [0]*days
        self.daily[driver]['parcels out for delivery'] = [0]*days
        self.daily[driver]['parcels returned from delivery'] = [0]*days
        self.daily[driver]['parcels delivered'] = [0]*days

    self.parcel = pd.DataFrame()
    self.parcel['arrived at'] = [None]*self.parcels
    self.parcel['delivered at'] = [None]*self.parcels

    def trace(self, event, driver=None):
        if self.log:
            prefix = "" if driver is None else f"D{driver.id:d}: "
            print(timestamp(self.env.now), prefix+event)

    def recordDriverBeginsWork(self, driver):
        self.trace("arrives for work", driver)
        self.daily[driver.id].at[day(self.env.now), 'begin work at'] = \
↪int(round(self.env.now))

    def recordDriverEndsWork(self, driver):
        self.trace("goes home", driver)
        self.daily[driver.id].at[day(self.env.now), 'end work at'] = \
↪int(round(self.env.now))

    def recordTourLength(self, driver, length):
        self.daily[driver.id].at[day(self.env.now), 'tour length'] = int(length)

    def recordParcelArrived(self, driver, parcel):
        self.trace(str(parcel)+" arr at delivery centre", driver)
        today = day(self.env.now)
        self.daily[driver.id].at[today, 'parcels arrived'] += 1
        self.parcel.at[parcel.i, 'arrived at'] = today

    def recordParcelOutForDelivery(self, driver, parcel):
        self.trace(str(parcel)+" out for delivery", driver)
        self.daily[driver.id].at[day(self.env.now), 'parcels out for delivery'] \
↪+= 1

    def recordParcelReturnedFromDelivery(self, driver, parcel):
        self.trace(str(parcel)+" returned from delivery", driver)
        self.daily[driver.id].at[day(self.env.now), 'parcels returned from \
↪delivery'] += 1

    def recordParcelDelivered(self, driver, parcel):
        self.trace(str(parcel)+" delivered", driver)

```

```

        today = day(self.env.now)
        self.daily[driver.id].at[today, 'parcels delivered'] += 1
        self.parcel.at[parcel.i, 'delivered at'] = today

    def recordParcelsLeftOver(self, driver, n):
        self.trace(f"{n:d} parcels left over for next day", driver)
        self.daily[driver.id].at[day(self.env.now), 'parcels left over'] = n

    def finish(self):
        # simulation is finished for good
        # by removing the simulation environment we can
        # pickle recorder
        self.env = None

        for driver in range(self.drivers):
            self.daily[driver]['working time'] = (self.daily[driver]['end work_
↪at']-self.daily[driver]['begin work at'])//60
            self.daily[driver]['cost'] = self.daily[driver]['working time'].
↪apply(lambda x: max(60, x*30/60))
            self.daily[driver]['cost'] += 0.08/1000*self.daily[driver]['tour_
↪length']
            self.daily[driver]['cost'] = self.daily[driver]['cost'].
↪apply(lambda x: round(x,2))

            self.parcel['delivery delay'] = self.parcel['delivered at']-self.
↪parcel['arrived at']

            self.totalDaily = pd.DataFrame()
            self.totalDaily['cum arrival'] = self.__Data('parcels arrived').cumsum()
            self.totalDaily['cum delivery'] = self.__Data('parcels delivered').
↪cumsum()
            self.totalDaily['cost per parcel'] = self.__Data('cost')/self.
↪__Data('parcels delivered')
            self.totalDaily['cost per parcel'] = self.totalDaily['cost per parcel'].
↪apply(lambda x: round(x,2))

        # the Title() and Data() functions have been introduced
        # solely to maintain the code of the plot/hist methods below
        # as far as possible

    def __Title(self, title, driver):
        return ("Total " if driver is None else "") + \
            title + \
            " (" + f"{self.days:d} days" + \
            (" " if driver is None else f", Driver {driver:d} only") + ")"
```



```

def __Data(self, col, driver=None):
    if driver is None:
        total = pd.DataFrame()
        total['sum'] = [0] * self.days
        for d in range(self.drivers):
            total['sum'] += self.daily[d][col]
        return total['sum']
    else:
        return self.daily[driver][col]

def summary(self):
    df = pd.DataFrame(columns=['col', 'min', '25%', 'mean', '50%', '75%',
↪ 'max'])
    special = 'cost per parcel'
    df.col = list(self.daily[0].columns[2:]) + [special]
    df = df.set_index('col')
    for col in df.index:
        data = self.__Data(col) if col!=special else self.
↪totalDaily[special];
        df.at[col, 'min'] = data.min()
        df.at[col, '25%'] = round(data.quantile(0.25),2)
        df.at[col, 'mean'] = round(data.mean(),2)
        df.at[col, '50%'] = round(data.quantile(0.5),2)
        df.at[col, '75%'] = round(data.quantile(0.75),2)
        df.at[col, 'max'] = data.max()
    return df

def histWorkingTime(self, driver=None):
    histPlot(self.__Data('working time', driver),
              xlabel='Working Time [min]',
              title=self.__Title('Daily Working Time', driver))

def plotWorkingTime(self, driver=None):
    dailyPlot(self.__Data('working time', driver),
              ylabel='Working Time [min]',
              title=self.__Title('Daily Working Time', driver))

def histTourLength(self, driver=None):
    histPlot(self.__Data('tour length', driver),
              xlabel='Tour Length [m]',
              title=self.__Title('Daily Tour Length', driver))

def plotTourLength(self, driver=None):
    dailyPlot(self.__Data('tour length', driver),
              ylabel='Tour Length [m]',
              title=self.__Title('Daily Tour Length', driver))

```

```

def histDailyCost(self, driver=None):
    histPlot(self.__Data('cost', driver),
              xlabel='Cost [€]',
              title=self.__Title('Daily Cost', driver))

def plotDailyCost(self, driver=None):
    dailyPlot(self.__Data('cost', driver),
              ylabel='Cost [€]',
              title=self.__Title('Daily Cost', driver))

def histParcelsArrived(self, driver=None):
    histPlot(self.__Data('parcels arrived', driver),
              discrete=True,
              xlabel='Parcels Arrived',
              title=self.__Title('Daily Parcels Arrived', driver))

def plotParcelsArrived(self, driver=None):
    dailyPlot(self.__Data('parcels arrived', driver),
              ylabel='Parcels',
              title=self.__Title('Parcels Arrived Daily', driver))

def histParcelsOutForDelivery(self, driver=None):
    histPlot(self.__Data('parcels out for delivery', driver),
              discrete=True,
              xlabel='Parcels',
              title=self.__Title('Parcels Daily out for Delivery', driver))

def plotParcelsOutForDelivery(self, driver=None):
    dailyPlot(self.__Data('parcels out for delivery', driver),
              ylabel='Parcels',
              title=self.__Title('Parcels Daily out for Delivery', driver))

def histParcelsReturnedFromDelivery(self, driver=None):
    histPlot(self.__Data('parcels returned from delivery', driver),
              discrete=True,
              xlabel='Parcels',
              title=self.__Title('Parcels Daily Returned From Delivery',
↪driver))

def plotParcelsReturnedFromDelivery(self, driver=None):
    dailyPlot(self.__Data('parcels returned from delivery', driver),
              ylabel='Parcels',
              title=self.__Title('Daily Parcels Returned From Delivery',
↪driver))

def histParcelsDelivered(self, driver=None):
    histPlot(self.__Data('parcels delivered', driver),

```

```

        discrete=True,
        xlabel='Parcels',
        title=self.__Title('Parcels Delivered Daily', driver))

def plotParcelsDelivered(self, driver=None):
    dailyPlot(self.__Data('parcels delivered', driver),
              ylabel='Parcels',
              title=self.__Title('Parcels Delivered Daily', driver))

def histParcelsLeftOver(self, driver=None):
    histPlot(self.__Data('parcels left over', driver),
             discrete=True,
             xlabel='Parcels',
             title=self.__Title('Daily Left-Over Parcels', driver))

def plotParcelsLeftOver(self, driver=None):
    dailyPlot(self.__Data('parcels left over', driver),
              ylabel='Parcels',
              title=self.__Title('Daily Left-Over Parcels', driver))

def countPlot(self):
    countPlot(self.totalDaily['cum arrival'],
              self.totalDaily['cum delivery'],
              ylabel='Parcels',
              title=f'Parcel Arrival/Delivery ({self.parcels:3,d} Parcels,␣
↪{self.days:d} Days)')

def histParcelDeliveryDelay(self):
    histPlot(self.parcel['delivery delay'].dropna(),
             discrete=True,
             xlabel='Days',
             title=f'Parcel Delivery Delay in Days ({self.parcels:3,d}␣
↪Parcels)')

```

## 8 Class Customer

```

[30]: class Customer:

    def __init__(self, rec, id, location):
        self.rec = rec
        self.id = id
        self.location = location
        self.atHome = True
        self.answersDoor = False
        self.parcelsReceived = []
        rec.env.process(self.process())

```

```

def __str__(self):
    return f"Customer {self.id:d} at {str(self.location):s}"

def leaveHouse(self):
    assert(self.atHome and not self.answersDoor)
    # self.rec.trace(str(self)+" leaves house")
    self.atHome = False

def returnHome(self):
    assert(not self.atHome)
    # self.rec.trace(str(self)+" returns home")
    self.atHome = True

def answerDoor(self, driver):
    if self.atHome:
        answerTime = random.expovariate(1/AVG_TIME_ANSWER_DOOR)
        if answerTime < WAIT_TIME_IF_CUSTOMER_DOESNT_ANSWER_DOOR:
            yield self.rec.env.timeout(answerTime)
            self.rec.trace(str(self)+" answers door", driver)
            self.answersDoor = True
        else:
            yield self.rec.env.
↪timeout(WAIT_TIME_IF_CUSTOMER_DOESNT_ANSWER_DOOR)
            self.rec.trace(str(self)+" to slow to answer the door", driver)
            self.answersDoor = False
    else:
        yield self.rec.env.timeout(WAIT_TIME_IF_CUSTOMER_DOESNT_ANSWER_DOOR)
        self.rec.trace(str(self)+" not at home", driver)
        self.answersDoot = False

def acceptParcel(self, driver, parcel):
    assert(self.answersDoor)
    self.parcelsReceived += [parcel]
    self.rec.recordParcelDelivered(driver, parcel)

def signOff(self, driver):
    assert(self.answersDoor)
    self.rec.trace(str(self)+" signs off", driver)
    self.answersDoor = False

def process(self):
    yield self.rec.env.timeout(nextHour(self.rec.env, 8))
    while day(self.rec.env.now)<self.rec.days:
        # in a refinement we may use random times
        self.leaveHouse()
        returnTime = 22 if random.random()<CUSTOMER_NOT_AT_HOME else 18

```

```

yield self.rec.env.timeout(nextHour(self.rec.env, returnTime))
self.returnHome()
yield self.rec.env.timeout(nextHour(self.rec.env, 8))

```

## 9 Class Parcel

Parcels follow through a sequence of states: - processing - in transit (from manufacture to distribution centre) - arrived in distribution centre - ready for delivery - out for delivery - customer not present - returned to distribution centre - delivered

```

[31]: class Parcel:

    def __init__(self, rec, i, day, cust):
        self.rec = rec
        self.i = i
        self.arrival = day
        self.cust = cust
        self.status = [ ] # status record and
        self.timing = [ ] # timing

    def __str__(self):
        return f"Parcel {self.i:d} (for cust {self.cust.id:d}"

    def index(self):
        return self.i

    def destination(self):
        return self.cust.location

    def __reg(self, state):
        self.status += [ state ]
        self.timing += [ self.rec.env.now ]

    def arrivedAtDeliveryCentre(self, driver):
        self.__reg('arr at delivery centre')
        self.rec.recordParcelArrived(driver, self)

    def outForDelivery(self, driver):
        self.__reg('out for delivery')
        self.rec.recordParcelOutForDelivery(driver, self)

    def returnFromDelivery(self, driver):
        self.__reg('return from delivery')
        self.rec.recordParcelReturnedFromDelivery(driver, self)

```

## 10 Class Driver

```
[32]: class Driver:

    def __init__(self, rec, id, DC):
        self.rec = rec
        self.id = id
        self.DC = DC
        self.location = None
        self.parcels = None
        self.returns = None
        self.tour = None
        self.rec.env.process(self.process())

    # activity
    def __drive(self, target):
        assert(self.tour[0] == self.location)
        while self.location!=target:
            d = dist(self.location, self.tour[1])
            yield self.rec.env.timeout(d / AVG_SPEED)
            self.location = self.tour[1]
            self.tour = self.tour[1:]
        assert(self.tour[0] == self.location == target)

    def arriveForWork(self):
        self.location = self.DC.W
        self.parcels = []
        self.returns = []
        self.tour = [ self.DC.W ]
        # self.rec.trace("arrives for work", self)
        self.rec.recordDriverBeginsWork(self)

    def goesHome(self):
        self.location = None
        self.parcels = None
        self.returns = None
        self.tour = None
        # self.rec.trace("goes home", self)
        self.rec.recordDriverEndsWork(self)

    def leaveForDelivery(self, tour, parcels, addresses):
        self.tour, self.parcels = tour, parcels
        self.rec.trace(f"leaves for delivery "
                       f"of {len(parcels):d} parcels "
                       f"to {len(addresses):d} customers", self)
        self.rec.trace(f"Length of delivery tour: {pathLength(tour):.d}m", self)
        if self.rec.plot:
```

```

        plotMap(self.rec.Maps[self.id], frame=self.rec.M,
                 T=addresses, P=tour, w=tour[0],
                 text=f"Day {day(self.rec.env.now):d} D{self.id:d}:␣
↪{pathLength(tour):,d}m")

    def process(self):
        yield self.rec.env.timeout(nextHour(self.rec.env, 18))
        while day(self.rec.env.now)<self.rec.days:
            self.arriveForWork()

            ## chnge to deal with time limit
            startTime = self.rec.env.now

            tour, parcels, addresses = self.DC.sendForDelivery(self)
            if len(parcels)==0:
                self.rec.trace("Nothing to do today", self)
                self.rec.recordTourLength(self, 0)
            else:
                yield self.rec.env.timeout(PREP_TIME_PER_PARCEL*len(parcels))
                self.rec.recordTourLength(self, pathLength(tour))
                self.leaveForDelivery(tour, parcels, addresses)
                while len(self.parcels)>0:

                    ## change to deal with time limit
                    currentTime = self.rec.env.now
                    if currentTime-startTime>=self.DC.timeLimit:
                        self.rec.trace("Timelimit reached", self)
                        while len(self.parcels)>0:
                            self.returns += [self.parcels[0]]
                            self.parcels = self.parcels[1:]
                        break

                    # drive to customer
                    custLocation = self.parcels[0].destination()
                    cust = self.parcels[0].cust
                    self.rec.trace("drives to "+str(cust), self)
                    yield from self.__drive(custLocation)
                    self.rec.trace("arrived at "+str(cust), self)
                    # call at customer
                    yield from cust.answerDoor(self)

                    if cust.answersDoor:
                        while len(self.parcels)>0 and \
                            custLocation == self.parcels[0].destination():
                            cust.acceptParcel(self, self.parcels[0])
                            yield self.rec.env.timeout(random.expovariate(1/
↪AVG_TIME_HANOVER))

```

```

        self.parcels = self.parcels[1:]
        cust.signOff(self)
        yield self.rec.env.timeout(random.expovariate(1/
↪AVG_TIME_SIGNOFF))
    else:
        while len(self.parcels)>0 and \
            custLocation == self.parcels[0].destination():
            self.returns += [self.parcels[0]]
            self.parcels = self.parcels[1:]

        # return to delivery centre
        self.rec.trace("returns to delivery centre", self)
        yield from self.__drive(self.DC.W)
        self.rec.trace("arrived at delivery centre", self)

        for parcel in self.returns:
            self.DC.returnFromDelivery(self, parcel)
            yield self.rec.env.timeout(RETURN_TIME_PER_PARCEL)

        self.rec.recordParcelsLeftOver(self,
                                       len(self.returns)+
                                       len(self.DC.leftOver[self.id]))

        yield self.rec.env.timeout(DAY_END_PROCEDURE)

        self.goesHome()

        yield self.rec.env.timeout(nextHour(self.rec.env, 18))

```

## 11 Class Delivery Centre

[33]: `class DeliveryCentre:`

```

    def __init__(self, rec, M, W, C, D, Plan,
                  limit, timeLimit):
        self.rec = rec
        self.M = M
        self.W = W
        self.C = C
        self.D = D
        self.MM, self.LL, self.CC = Plan

        self.limit = limit
        self.timeLimit = timeLimit

        self.overhang = []    # list of parcels to be delivered next day

```



```

# generate and initialise all customers
# allows mapping from custId to Customer object
self.customers = [ Customer(rec, i, C[i]) for i in range(len(C)) ]

# generate and initialise all drivers
self.drivers = [ Driver(rec, i, self) for i in range(len(self.MM)) ]

self.PARCELS = []      # registry of all the parcels processed

rec.env.process(self.process())

def __accept(self, d, parcel):
    custLoc = parcel.destination()

    assert(0<=d<len(self.MM))

    ## chnge to deal with time limit estimate
    timeEstimate = \
        len(self.parcels[d])*(PREP_TIME_PER_PARCEL + AVG_TIME_HANOVER) \
        + len(self.dest[d])*(AVG_TIME_ANSWER_DOOR + AVG_TIME_SIGNOFF)

    if custLoc not in self.dest[d]:

        targets = [self.W] + self.dest[d] + [custLoc]

        if self.rec.plot:
            plotMap(self.MM[d], T=targets, w=self.W, frame=self.M,
                    size=2, text=f"Driver {d:d}: accept Parcel")

        MT = addTarget(self.MM[d], targets)
        SH = createLoopG(MT, targets)

        MT = addTarget(self.MM[i], targets)
        path = shortenLoop(self.LL[i], MT, targets)

        ## chnge to deal with time limit estimate
        if pathLength(SH)<self.limit and \
            timeEstimate + pathLength(SH)/AVG_SPEED + \
            PREP_TIME_PER_PARCEL + AVG_TIME_ANSWER_DOOR + \
            AVG_TIME_HANOVER + AVG_TIME_SIGNOFF <= self.timeLimit:

            self.parcels[d].append(parcel)
            self.dest[d] += [custLoc]
            self.tour[d] = SH
        else:
            self.leftOver[d].append(parcel)

```

```

        ## chnge to deal with time limit estimate
    elif timeEstimate + pathLength(self.tour[d])/AVG_SPEED + \
        PREP_TIME_PER_PARCEL + AVG_TIME_HANOVER <= self.timeLimit:
        self.parcels[d].append(parcel)
    else:
        self.leftOver[d].append(parcel)

def sendForDelivery(self, driver):
    d = driver.id
    parcels = []
    tour = self.tour[d]
    addresses = []

    # pick parcels in sequence to be delivered
    for i in range(1, len(tour)-1):
        dest = tour[i]
        for p in self.parcels[d]:
            if p.destination() == dest and p not in parcels:
                parcels += [p]
                p.outForDelivery(driver)
            if dest not in addresses:
                addresses += [dest]

    # what cant go out goes straight for next day
    for p in self.leftOver[d]:
        self.overhang.append(p)

    return tour, parcels, addresses

def returnFromDelivery(self, driver, parcel):
    parcel.returnFromDelivery(driver)
    self.overhang.append(parcel)

def getInventory(self):
    return len(self.overhang)

def process(self):
    regions = getRegions(self.CC, self.C)
    for day in range(len(self.D)):
        yield self.rec.env.timeout(nextHour(self.rec.env, 17.00))
        # make plan how to split workload for the day

        # initialise the workload for all drivers
        self.leftOver = [ [] for driver in self.drivers ]    # list of
        → parcels that can't go out today

```

```

        self.parcels = [ [] for driver in self.drivers ]      # list of
↳ parcels scheduled for delivery
        self.dest = [ [] for driver in self.drivers ]        # list of
↳ unique customer destinations
        self.tour = [ [self.W] for driver in self.drivers ] # tour planned
↳ for delivery

        # process overhang from previous day (if any)
        for p in self.overhang:
            driverId = regions[p.cust.id]
            self.__accept(driverId, p)
        self.overhang = []

        # generate the parcels newly arriving this day
        for c in self.D[day]:
            parcel = Parcel(self.rec, len(self.PARCELS),
                           day, self.customers[c])
            self.PARCELS.append(parcel)
            driverId = regions[c]
            parcel.arrivedAtDeliveryCentre(self.drivers[driverId])
            self.__accept(driverId, parcel)

```

## 12 Simulation

### 12.1 Parameters from Specification

The hard time limit for the driver. When this time limit is reached on a delivery tour, the driver is supposed to return immediately

[34]: `DELIVERY_TIME_LIMIT = 3*3600 # 3 hours`

The proportion of customers that for whatever are not at home or return home late

[35]: `CUSTOMER_NOT_AT_HOME = 0.1 # 10%`

The maximum bike range. This is passed as parameter to the Delivery Centre and taken into account for the daily tour planning

[36]: `BIKE_RANGE = 40000`

The time required for driving is based on the distance between way points at an average speed of 15km/h.

[37]: `AVG_SPEED = 15/3.6`

The **cumulative preparation time** (route planning and sorting of the parcels in the delivery order and packing the cargo-bike) is assumed to be 50 sec per parcel to be delivered.

[38]: `PREP_TIME_PER_PARCEL = 50`

**Additional assumption:** The time to **process returned parcels** in the delivery centre is 30 sec per parce.

```
[39]: RETURN_TIME_PER_PARCEL = 30
```

The average time to answer the door.

```
[40]: AVG_TIME_ANSWER_DOOR = 40
```

```
[41]: WAIT_TIME_IF_CUSTOMER_DOESNT_ANSWER_DOOR = 60
```

```
[42]: AVG_TIME_HANDOVER = 10
      AVG_TIME_SIGNOFF = 10
```

```
[43]: DAY_END_PROCEDURE = 600
```

## 12.2 Generate Input Data

```
[44]: def generateDeliveries(p, C, days, seed=0):
      ## p is the average number of parcels per day per customer
      ## C is the number of customers to be served
      ## days is the number of days for which data are to be generated.
      random.seed(seed)
      deliveries = [ [ ] for _ in range(days) ]
      for c in range(C):
          arr = 0
          while True:
              arr += random.expovariate(p)
              day = int(arr)
              if day >= days:
                  break
              deliveries[day].append(c)
      return deliveries
```

## 12.3 Simulation Routine

```
[45]: def simulation(M, W, C, Plan, p=0.2, days=10, seed=0,
      log=False, plot=False, timing=False):

      random.seed(seed)
      D = generateDeliveries(p, len(C), days, seed)

      env = simpy.Environment()
      rec = Recorder(env, M, W, C, D, Plan, days,
                     log=log, plot=plot, timing=timing)
```

```

print(f"Simulating delivery of {sum([len(d) for d in D]):d} parcels "
      f"over {len(D):d} days to {len(C):d} customers "
      f"using {rec.drivers:d} drivers")

# initialise all customer processes
# initialises delivery center and creates all parcels
DC = DeliveryCentre(rec, M, W, C, D, Plan,
                   BIKE_RANGE, DELIVERY_TIME_LIMIT)

env.run()
rec.finish()

if DC.getInventory()>0:
    print(f"Delivery Centre Inventory at the end of last day: "
          f"{DC.getInventory():d} parcels")

return rec

```

## 12.4 Testing

### 12.4.1 Simple Test Case

```

[46]: import pickle
      with open('data/simpleData.pickled', 'rb') as f:
          MS, CS = pickle.load(f)

```

```

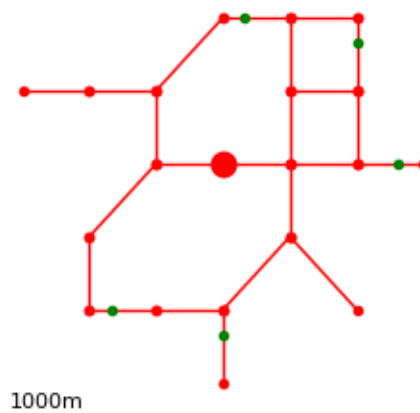
[47]: WS = generateWarehouseLocation(MS)

```

```

[48]: plotMap(MS, T=CS, w=WS, scale=True, size=3)

```

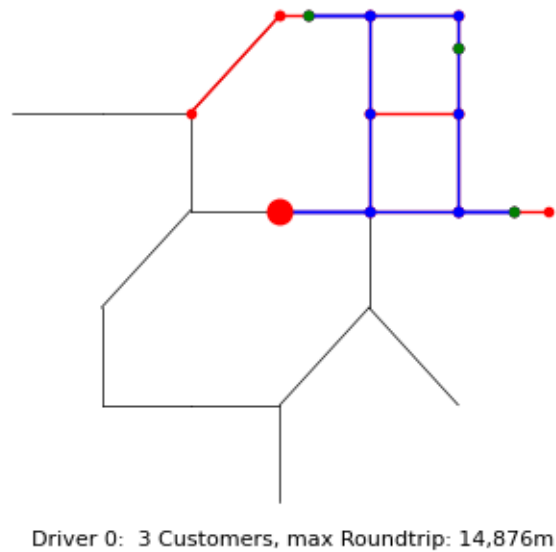
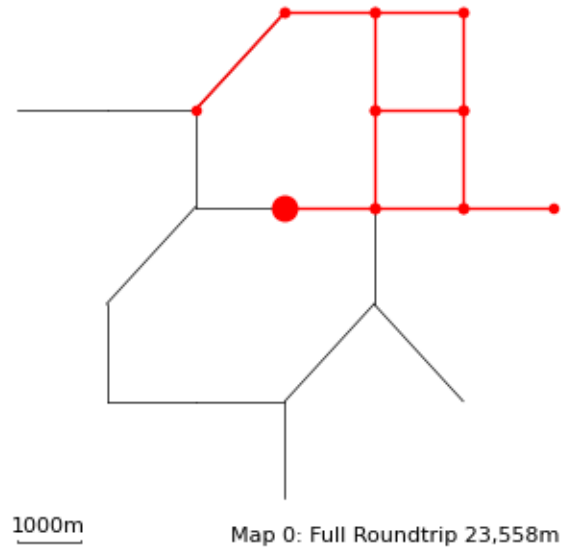


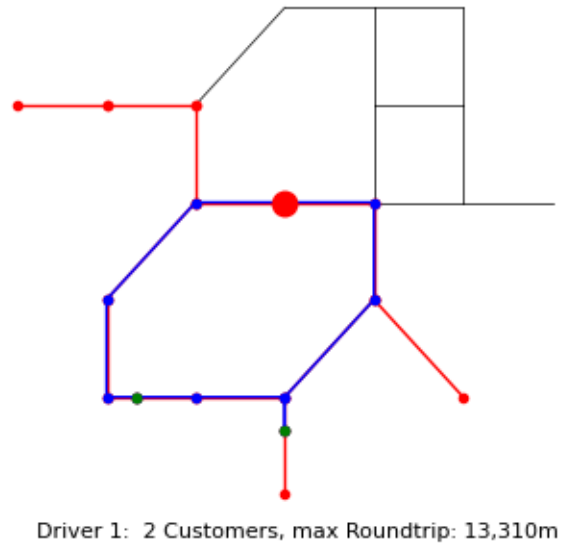
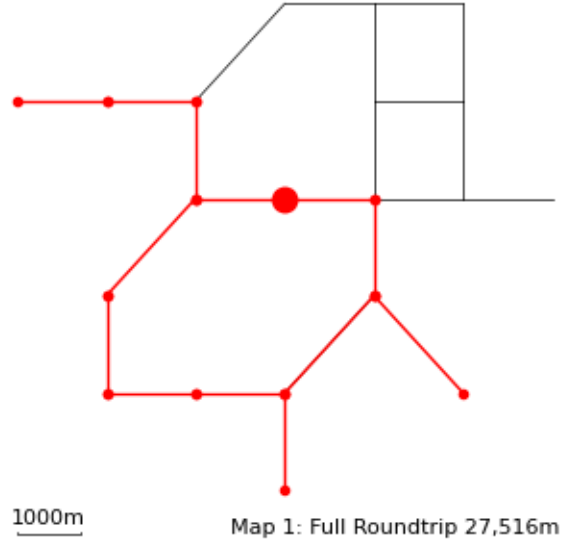
```

[49]: PlanS = planCPP(MS, WS, CS, n=2, balance=0.2, timing=True, plot=True)

```

Solver time: 10.11s  
Solution possibly not optimal  
Total Delivery Path Length: 51074.0





Comparison with Greedy Solution using Static Allocation shows equal performance:

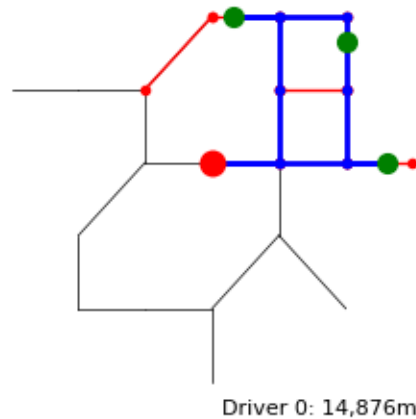
```
[50]: MMS, LLS, CCS = PlanS
      for i in range(len(MMS)):
          print(f"Driver {i:d}")
          MTS = addTargets(MMS[i], CCS[i])
```

```

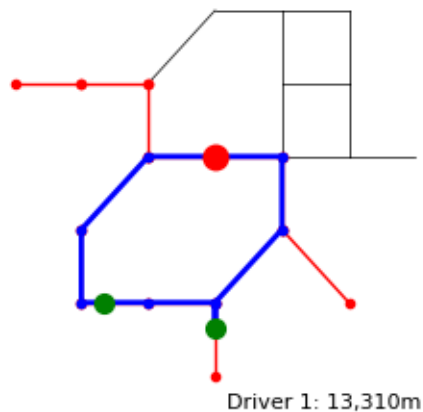
path = createLoopG(MTS, [WS] + CCS[i])
plotMap(MTS, T=CCS[i], P=path, w=WS, frame=MS,
        size=3, text=f"Driver {i:d}: {pathLength(path):,d}m")

```

Driver 0



Driver 1



```

[51]: rec1 = simulation(MS, WS, CS, PlanS, p=0.3, days=7, log=True)

```

Simulating delivery of 12 parcels over 7 days to 5 customers using 2 drivers

```

[ 0] 18:00:00.0 D0: arrives for work
[ 0] 18:00:00.0 D0: Nothing to do today
[ 0] 18:00:00.0 D0: 0 parcels left over for next day
[ 0] 18:00:00.0 D1: arrives for work

```



[ 0] 18:00:00.0 D1: Nothing to do today  
 [ 0] 18:00:00.0 D1: 0 parcels left over for next day  
 [ 0] 18:10:00.0 D0: goes home  
 [ 0] 18:10:00.0 D1: goes home  
 [ 1] 17:00:00.0 D1: Parcel 0 (for cust 1 arr at delivery centre  
 [ 1] 17:00:00.0 D0: Parcel 1 (for cust 2 arr at delivery centre  
 [ 1] 18:00:00.0 D0: arrives for work  
 [ 1] 18:00:00.0 D0: Parcel 1 (for cust 2 out for delivery  
 [ 1] 18:00:00.0 D1: arrives for work  
 [ 1] 18:00:00.0 D1: Parcel 0 (for cust 1 out for delivery  
 [ 1] 18:00:50.0 D0: leaves for delivery of 1 parcels to 1 customers  
 [ 1] 18:00:50.0 D0: Length of delivery tour: 10,342m  
 [ 1] 18:00:50.0 D0: drives to Customer 2 at (4929, 7300)  
 [ 1] 18:00:50.0 D1: leaves for delivery of 1 parcels to 1 customers  
 [ 1] 18:00:50.0 D1: Length of delivery tour: 10,510m  
 [ 1] 18:00:50.0 D1: drives to Customer 1 at (4500, 1224)  
 [ 1] 18:21:31.0 D0: arrived at Customer 2 at (4929, 7300)  
 [ 1] 18:21:51.2 D1: arrived at Customer 1 at (4500, 1224)  
 [ 1] 18:22:08.8 D0: Customer 2 at (4929, 7300) answers door  
 [ 1] 18:22:08.8 D0: Parcel 1 (for cust 2 delivered  
 [ 1] 18:22:42.8 D0: Customer 2 at (4929, 7300) signs off  
 [ 1] 18:22:49.3 D0: returns to delivery centre  
 [ 1] 18:22:51.2 D1: Customer 1 at (4500, 1224) to slow to answer the door  
 [ 1] 18:22:51.2 D1: returns to delivery centre  
 [ 1] 18:43:30.3 D0: arrived at delivery centre  
 [ 1] 18:43:30.3 D0: 0 parcels left over for next day  
 [ 1] 18:43:52.4 D1: arrived at delivery centre  
 [ 1] 18:43:52.4 D1: Parcel 0 (for cust 1 returned from delivery  
 [ 1] 18:44:22.4 D1: 1 parcels left over for next day  
 [ 1] 18:53:30.3 D0: goes home  
 [ 1] 18:54:22.4 D1: goes home  
 [ 2] 17:00:00.0 D1: Parcel 2 (for cust 1 arr at delivery centre  
 [ 2] 17:00:00.0 D0: Parcel 3 (for cust 3 arr at delivery centre  
 [ 2] 18:00:00.0 D0: arrives for work  
 [ 2] 18:00:00.0 D0: Parcel 3 (for cust 3 out for delivery  
 [ 2] 18:00:00.0 D1: arrives for work  
 [ 2] 18:00:00.0 D1: Parcel 0 (for cust 1 out for delivery  
 [ 2] 18:00:00.0 D1: Parcel 2 (for cust 1 out for delivery  
 [ 2] 18:00:50.0 D0: leaves for delivery of 1 parcels to 1 customers  
 [ 2] 18:00:50.0 D0: Length of delivery tour: 10,250m  
 [ 2] 18:00:50.0 D0: drives to Customer 3 at (7300, 6825)  
 [ 2] 18:01:40.0 D1: leaves for delivery of 2 parcels to 1 customers  
 [ 2] 18:01:40.0 D1: Length of delivery tour: 10,510m  
 [ 2] 18:01:40.0 D1: drives to Customer 1 at (4500, 1224)  
 [ 2] 18:21:20.0 D0: arrived at Customer 3 at (7300, 6825)  
 [ 2] 18:22:10.9 D0: Customer 3 at (7300, 6825) answers door  
 [ 2] 18:22:10.9 D0: Parcel 3 (for cust 3 delivered  
 [ 2] 18:22:16.0 D0: Customer 3 at (7300, 6825) signs off

[ 2] 18:22:33.4 D0: returns to delivery centre  
 [ 2] 18:22:41.2 D1: arrived at Customer 1 at (4500, 1224)  
 [ 2] 18:23:25.3 D1: Customer 1 at (4500, 1224) answers door  
 [ 2] 18:23:25.3 D1: Parcel 0 (for cust 1 delivered  
 [ 2] 18:23:25.3 D1: Parcel 2 (for cust 1 delivered  
 [ 2] 18:23:32.1 D1: Customer 1 at (4500, 1224) signs off  
 [ 2] 18:23:52.4 D1: returns to delivery centre  
 [ 2] 18:43:03.4 D0: arrived at delivery centre  
 [ 2] 18:43:03.4 D0: 0 parcels left over for next day  
 [ 2] 18:44:53.6 D1: arrived at delivery centre  
 [ 2] 18:44:53.6 D1: 0 parcels left over for next day  
 [ 2] 18:53:03.4 D0: goes home  
 [ 2] 18:54:53.6 D1: goes home  
 [ 3] 17:00:00.0 D0: Parcel 4 (for cust 2 arr at delivery centre  
 [ 3] 17:00:00.0 D0: Parcel 5 (for cust 3 arr at delivery centre  
 [ 3] 17:00:00.0 D0: Parcel 6 (for cust 4 arr at delivery centre  
 [ 3] 18:00:00.0 D0: arrives for work  
 [ 3] 18:00:00.0 D0: Parcel 4 (for cust 2 out for delivery  
 [ 3] 18:00:00.0 D0: Parcel 5 (for cust 3 out for delivery  
 [ 3] 18:00:00.0 D0: Parcel 6 (for cust 4 out for delivery  
 [ 3] 18:00:00.0 D1: arrives for work  
 [ 3] 18:00:00.0 D1: Nothing to do today  
 [ 3] 18:00:00.0 D1: 0 parcels left over for next day  
 [ 3] 18:02:30.0 D0: leaves for delivery of 3 parcels to 3 customers  
 [ 3] 18:02:30.0 D0: Length of delivery tour: 14,876m  
 [ 3] 18:02:30.0 D0: drives to Customer 2 at (4929, 7300)  
 [ 3] 18:10:00.0 D1: goes home  
 [ 3] 18:23:11.0 D0: arrived at Customer 2 at (4929, 7300)  
 [ 3] 18:23:21.9 D0: Customer 2 at (4929, 7300) answers door  
 [ 3] 18:23:21.9 D0: Parcel 4 (for cust 2 delivered  
 [ 3] 18:23:56.2 D0: Customer 2 at (4929, 7300) signs off  
 [ 3] 18:24:12.5 D0: drives to Customer 3 at (7300, 6825)  
 [ 3] 18:35:35.5 D0: arrived at Customer 3 at (7300, 6825)  
 [ 3] 18:35:59.3 D0: Customer 3 at (7300, 6825) answers door  
 [ 3] 18:35:59.3 D0: Parcel 5 (for cust 3 delivered  
 [ 3] 18:36:00.1 D0: Customer 3 at (7300, 6825) signs off  
 [ 3] 18:36:04.0 D0: drives to Customer 4 at (8167, 4500)  
 [ 3] 18:48:50.1 D0: arrived at Customer 4 at (8167, 4500)  
 [ 3] 18:49:18.4 D0: Customer 4 at (8167, 4500) answers door  
 [ 3] 18:49:18.4 D0: Parcel 6 (for cust 4 delivered  
 [ 3] 18:49:45.4 D0: Customer 4 at (8167, 4500) signs off  
 [ 3] 18:49:46.6 D0: returns to delivery centre  
 [ 3] 19:04:26.7 D0: arrived at delivery centre  
 [ 3] 19:04:26.7 D0: 0 parcels left over for next day  
 [ 3] 19:14:26.7 D0: goes home  
 [ 4] 17:00:00.0 D0: Parcel 7 (for cust 4 arr at delivery centre  
 [ 4] 18:00:00.0 D1: arrives for work  
 [ 4] 18:00:00.0 D1: Nothing to do today

[ 4] 18:00:00.0 D1: 0 parcels left over for next day  
 [ 4] 18:00:00.0 D0: arrives for work  
 [ 4] 18:00:00.0 D0: Parcel 7 (for cust 4 out for delivery  
 [ 4] 18:00:50.0 D0: leaves for delivery of 1 parcels to 1 customers  
 [ 4] 18:00:50.0 D0: Length of delivery tour: 7,334m  
 [ 4] 18:00:50.0 D0: drives to Customer 4 at (8167, 4500)  
 [ 4] 18:10:00.0 D1: goes home  
 [ 4] 18:15:30.1 D0: arrived at Customer 4 at (8167, 4500)  
 [ 4] 18:16:30.1 D0: Customer 4 at (8167, 4500) to slow to answer the door  
 [ 4] 18:16:30.1 D0: returns to delivery centre  
 [ 4] 18:31:10.2 D0: arrived at delivery centre  
 [ 4] 18:31:10.2 D0: Parcel 7 (for cust 4 returned from delivery  
 [ 4] 18:31:40.2 D0: 1 parcels left over for next day  
 [ 4] 18:41:40.2 D0: goes home  
 [ 5] 17:00:00.0 D1: Parcel 8 (for cust 1 arr at delivery centre  
 [ 5] 18:00:00.0 D1: arrives for work  
 [ 5] 18:00:00.0 D1: Parcel 8 (for cust 1 out for delivery  
 [ 5] 18:00:00.0 D0: arrives for work  
 [ 5] 18:00:00.0 D0: Parcel 7 (for cust 4 out for delivery  
 [ 5] 18:00:50.0 D1: leaves for delivery of 1 parcels to 1 customers  
 [ 5] 18:00:50.0 D1: Length of delivery tour: 10,510m  
 [ 5] 18:00:50.0 D1: drives to Customer 1 at (4500, 1224)  
 [ 5] 18:00:50.0 D0: leaves for delivery of 1 parcels to 1 customers  
 [ 5] 18:00:50.0 D0: Length of delivery tour: 7,334m  
 [ 5] 18:00:50.0 D0: drives to Customer 4 at (8167, 4500)  
 [ 5] 18:15:30.1 D0: arrived at Customer 4 at (8167, 4500)  
 [ 5] 18:16:04.4 D0: Customer 4 at (8167, 4500) answers door  
 [ 5] 18:16:04.4 D0: Parcel 7 (for cust 4 delivered  
 [ 5] 18:16:07.8 D0: Customer 4 at (8167, 4500) signs off  
 [ 5] 18:16:09.9 D0: returns to delivery centre  
 [ 5] 18:21:51.2 D1: arrived at Customer 1 at (4500, 1224)  
 [ 5] 18:21:59.5 D1: Customer 1 at (4500, 1224) answers door  
 [ 5] 18:21:59.5 D1: Parcel 8 (for cust 1 delivered  
 [ 5] 18:22:09.0 D1: Customer 1 at (4500, 1224) signs off  
 [ 5] 18:22:19.6 D1: returns to delivery centre  
 [ 5] 18:30:50.0 D0: arrived at delivery centre  
 [ 5] 18:30:50.0 D0: 0 parcels left over for next day  
 [ 5] 18:40:50.0 D0: goes home  
 [ 5] 18:43:20.8 D1: arrived at delivery centre  
 [ 5] 18:43:20.8 D1: 0 parcels left over for next day  
 [ 5] 18:53:20.8 D1: goes home  
 [ 6] 17:00:00.0 D1: Parcel 9 (for cust 0 arr at delivery centre  
 [ 6] 17:00:00.0 D1: Parcel 10 (for cust 1 arr at delivery centre  
 [ 6] 17:00:00.0 D0: Parcel 11 (for cust 2 arr at delivery centre  
 [ 6] 18:00:00.0 D0: arrives for work  
 [ 6] 18:00:00.0 D0: Parcel 11 (for cust 2 out for delivery  
 [ 6] 18:00:00.0 D1: arrives for work  
 [ 6] 18:00:00.0 D1: Parcel 9 (for cust 0 out for delivery

```

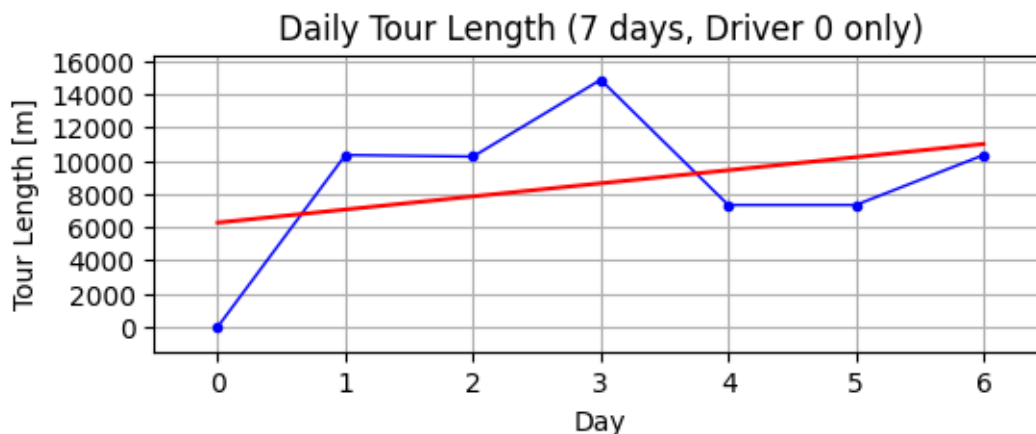
[ 6] 18:00:00.0 D1: Parcel 10 (for cust 1 out for delivery
[ 6] 18:00:50.0 D0: leaves for delivery of 1 parcels to 1 customers
[ 6] 18:00:50.0 D0: Length of delivery tour: 10,342m
[ 6] 18:00:50.0 D0: drives to Customer 2 at (4929, 7300)
[ 6] 18:01:40.0 D1: leaves for delivery of 2 parcels to 2 customers
[ 6] 18:01:40.0 D1: Length of delivery tour: 13,310m
[ 6] 18:01:40.0 D1: drives to Customer 0 at (2176, 1700)
[ 6] 18:21:31.0 D0: arrived at Customer 2 at (4929, 7300)
[ 6] 18:22:31.0 D0: Customer 2 at (4929, 7300) to slow to answer the door
[ 6] 18:22:31.0 D0: returns to delivery centre
[ 6] 18:22:41.2 D1: arrived at Customer 0 at (2176, 1700)
[ 6] 18:23:41.2 D1: Customer 0 at (2176, 1700) to slow to answer the door
[ 6] 18:23:41.2 D1: drives to Customer 1 at (4500, 1224)
[ 6] 18:34:53.2 D1: arrived at Customer 1 at (4500, 1224)
[ 6] 18:35:53.2 D1: Customer 1 at (4500, 1224) not at home
[ 6] 18:35:53.2 D1: returns to delivery centre
[ 6] 18:43:12.1 D0: arrived at delivery centre
[ 6] 18:43:12.1 D0: Parcel 11 (for cust 2 returned from delivery
[ 6] 18:43:42.1 D0: 1 parcels left over for next day
[ 6] 18:53:42.1 D0: goes home
[ 6] 18:56:54.4 D1: arrived at delivery centre
[ 6] 18:56:54.4 D1: Parcel 9 (for cust 0 returned from delivery
[ 6] 18:57:24.4 D1: Parcel 10 (for cust 1 returned from delivery
[ 6] 18:57:54.4 D1: 2 parcels left over for next day
[ 6] 19:07:54.4 D1: goes home
Delivery Centre Inventory at the end of last day: 3 parcels

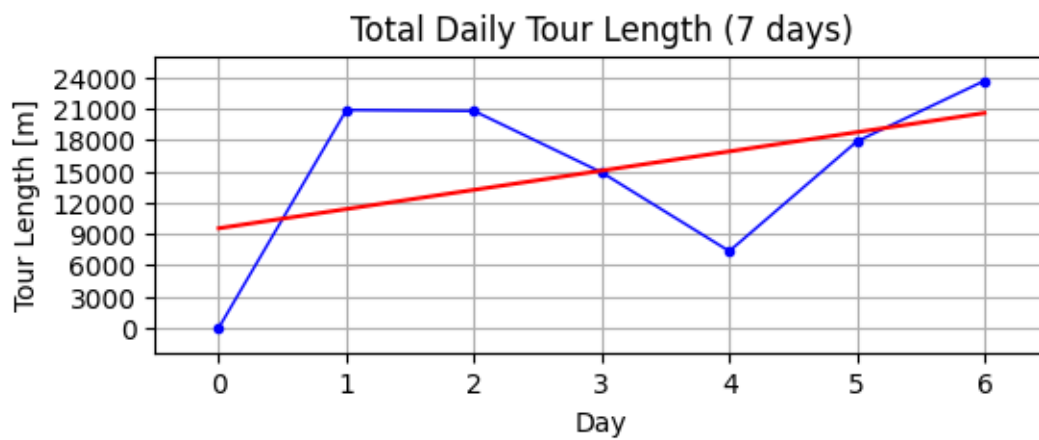
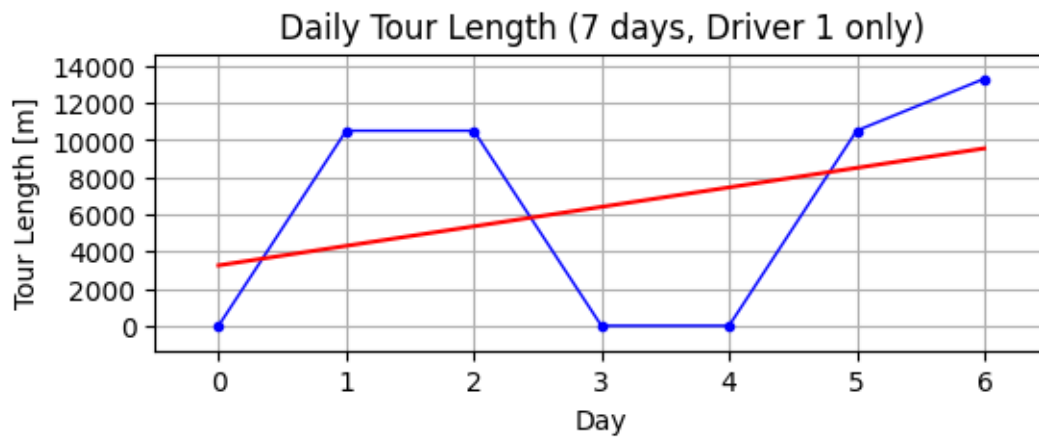
```

```

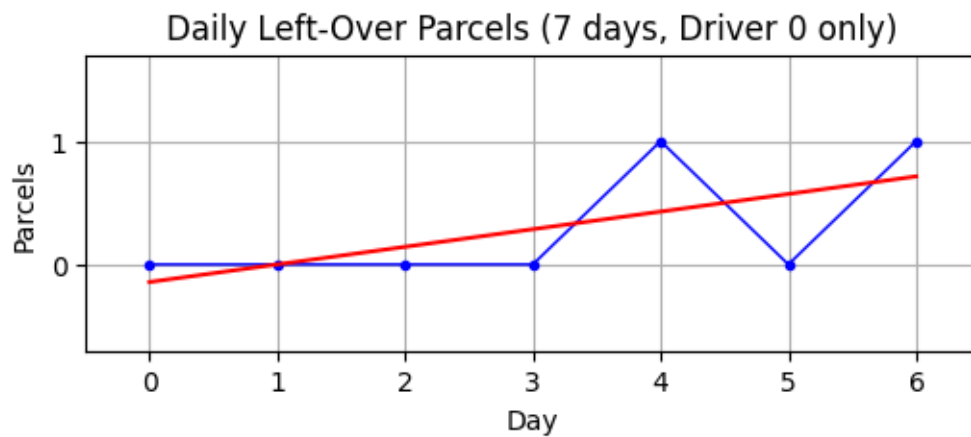
[52]: for i in range(rec1.drivers):
        rec1.plotTourLength(i)
rec1.plotTourLength()

```

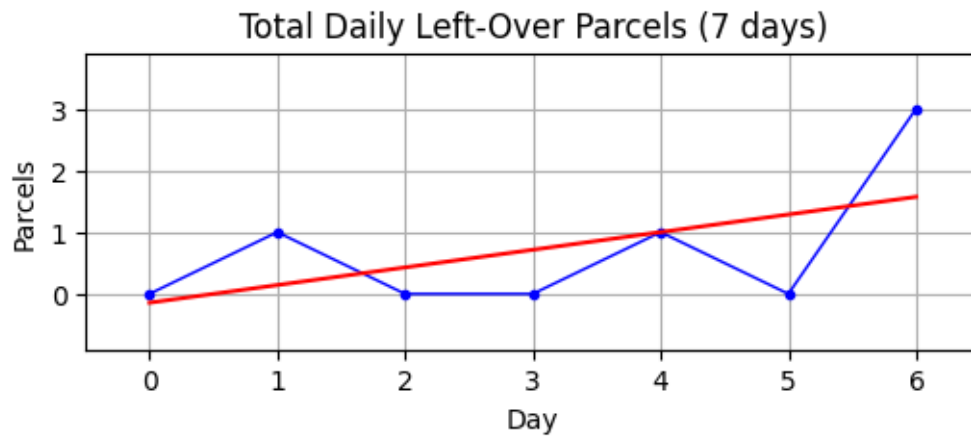




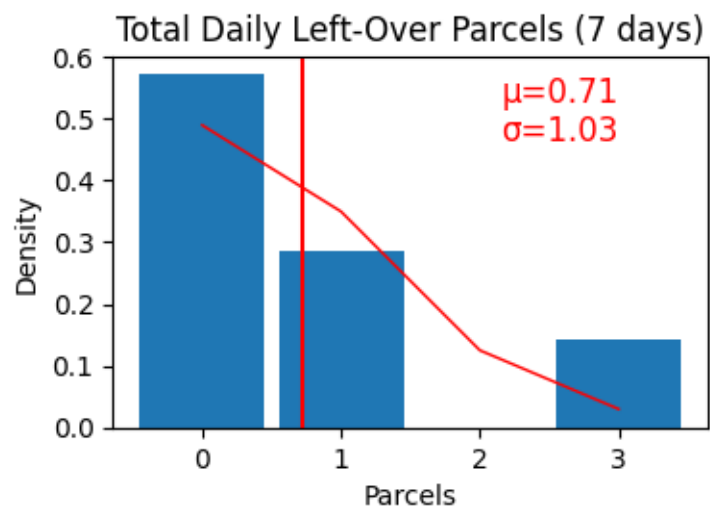
```
[53]: rec1.plotParcelsLeftOver(0)
```



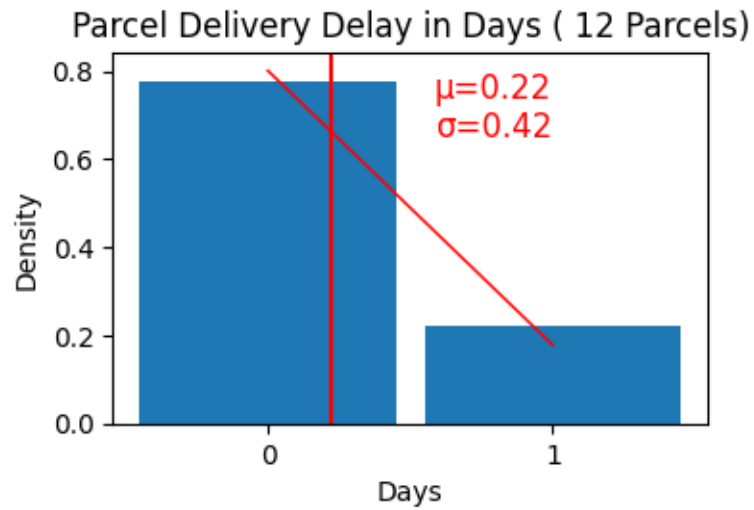
```
[54]: rec1.plotParcelsLeftOver()
```



```
[55]: rec1.histParcelsLeftOver()
```



```
[56]: rec1.histParcelDeliveryDelay()
```

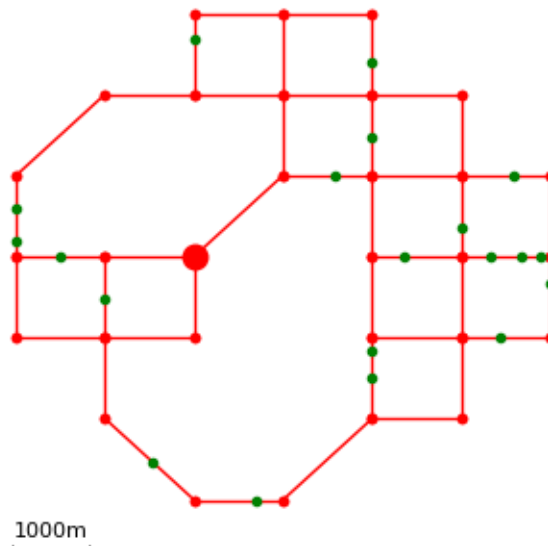


#### 12.4.2 Stable Base Case

```
[57]: import pickle
      with open('data/testData.pickled', 'rb') as f:
          MT, CT = pickle.load(f)
```

```
[58]: WT = generateWarehouseLocation(MT)
```

```
[59]: plotMap(MT, T=CT, w=WT, scale=True)
```

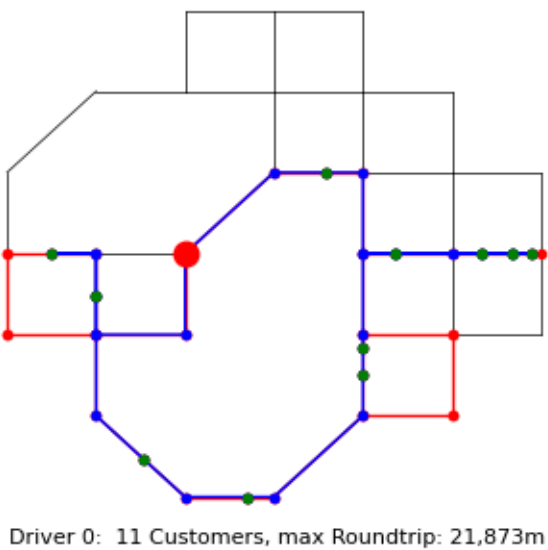
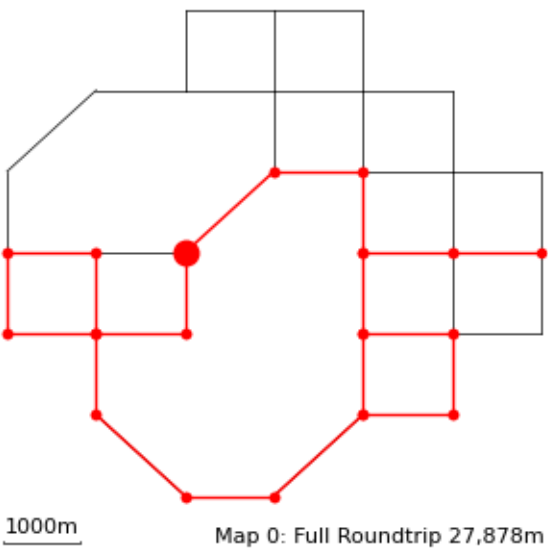


```
PlanT = planCPP(MT, WT, CT, n=2, balance=0.2, timing=True, plot=True)
```

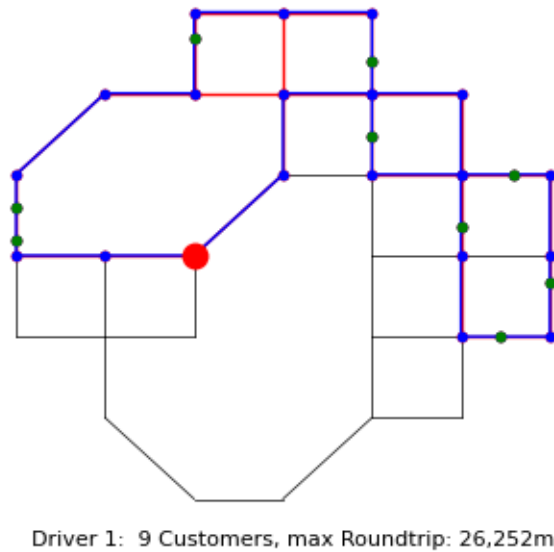
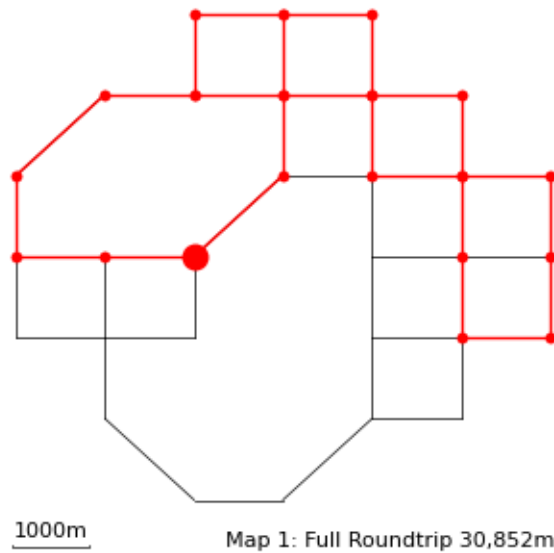
Solver time: 10.16s

Solution possibly not optimal

Total Delivery Path Length: 58730.0







Comparison with Greedy Solution using Static Allocation

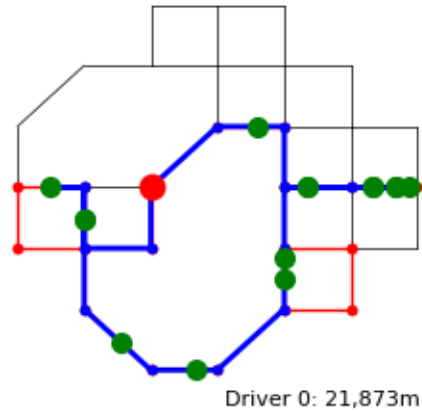
```
[61]: MMT, LLT, CCT = PlanT
      for i in range(len(MMT)):
          print(f"Driver {i:d}")
          MMTT = addTargets(MMT[i], CCT[i])
```

```

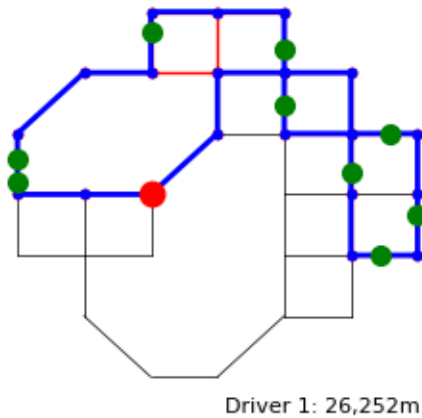
path = createLoopG(MMTT, [WT] + CCT[i])
plotMap(MMTT, T=CCT[i], P=path, w=WT, frame=MT,
        size=3, text=f"Driver {i:d}: {pathLength(path):,d}m")

```

Driver 0



Driver 1

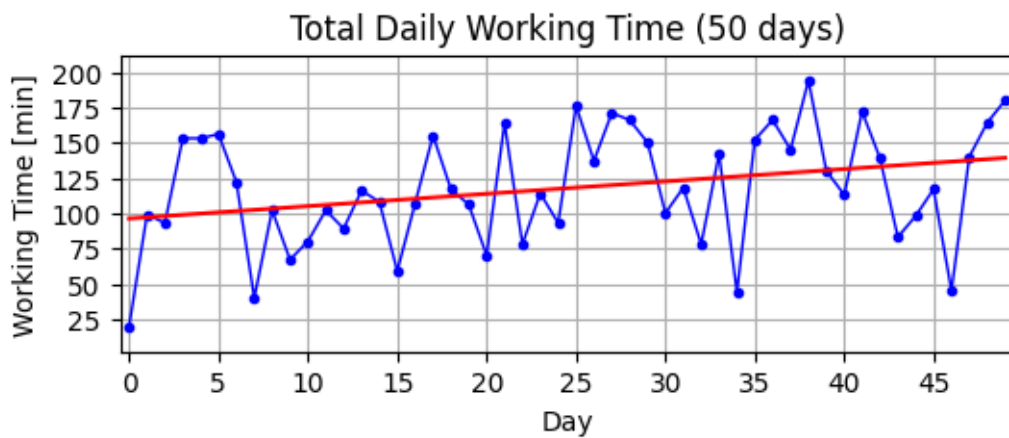
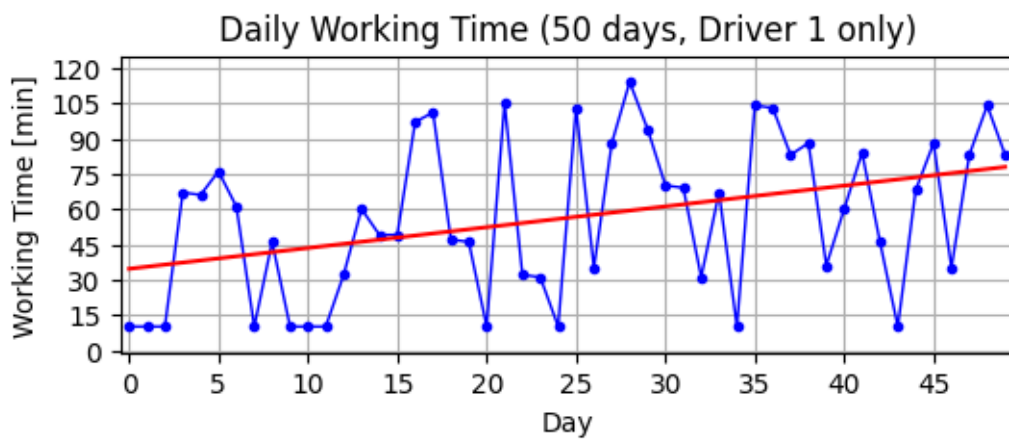
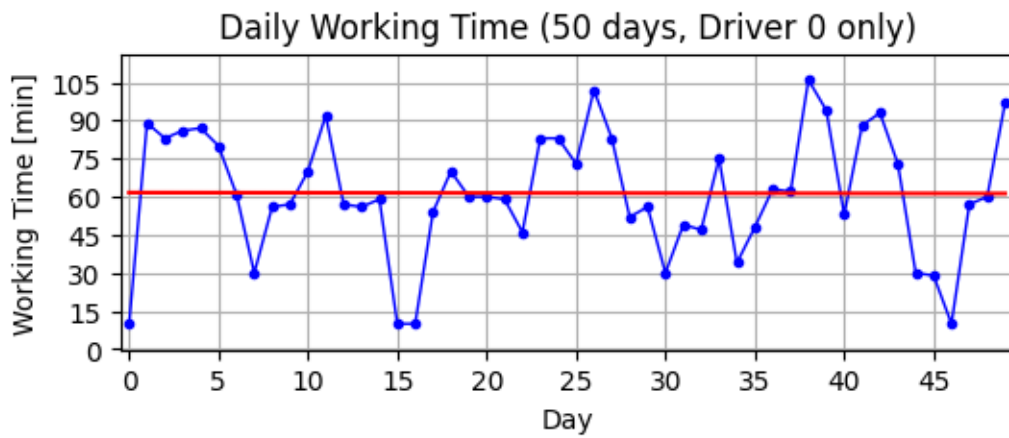


```
[62]: rec2 = simulation(MT, WT, CT, PlanT, p=0.15, days=50)
```

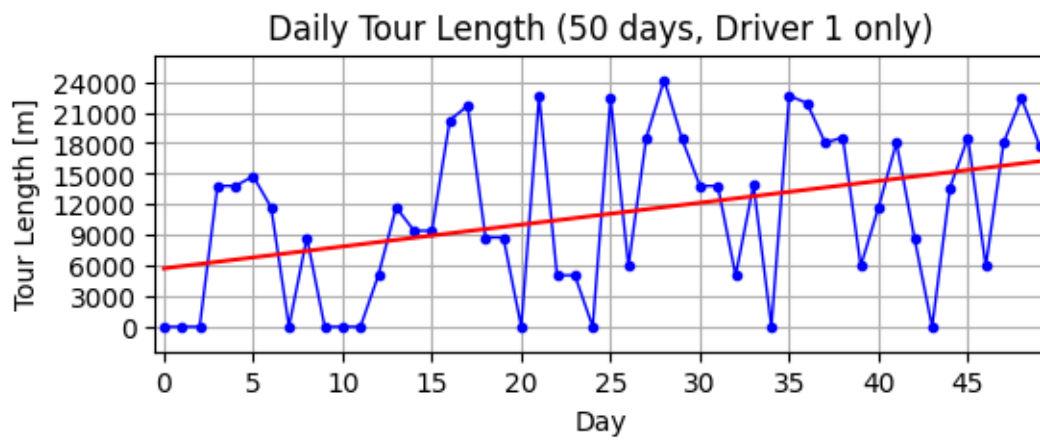
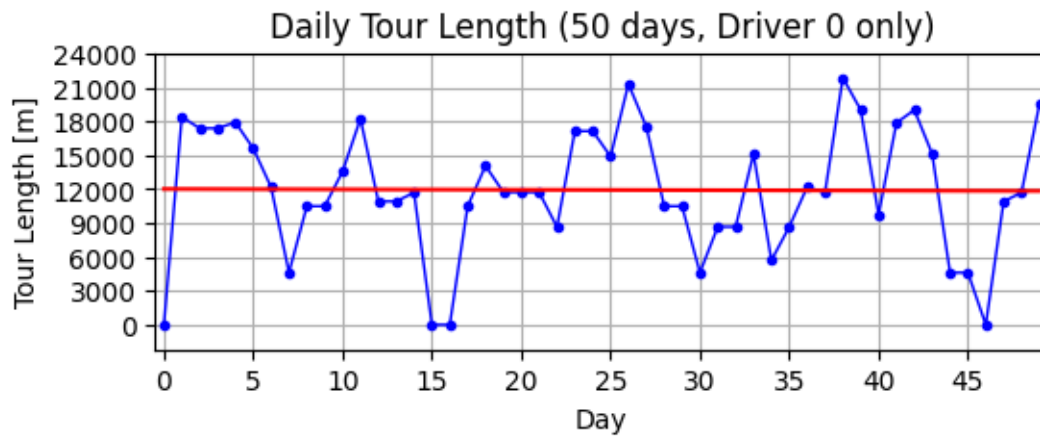
Simulating delivery of 134 parcels over 50 days to 20 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 3 parcels

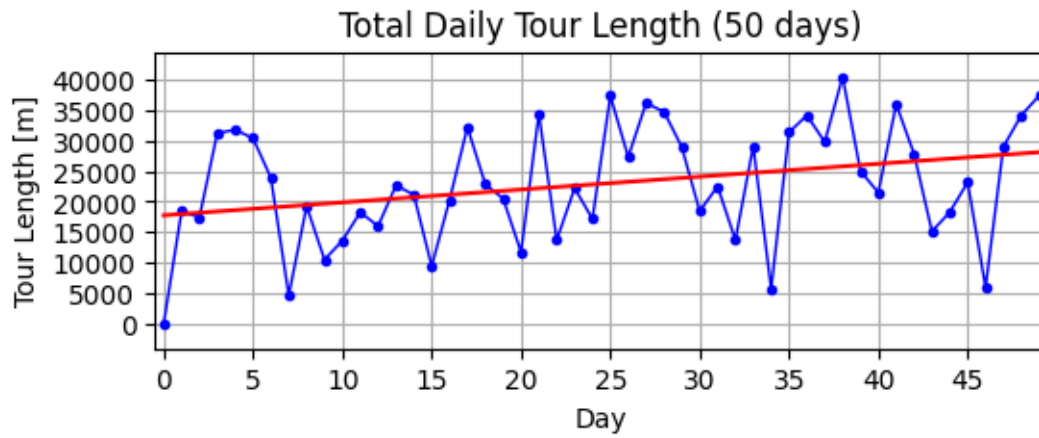
```
[63]: for i in range(rec1.drivers):
        rec2.plotWorkingTime(i)
```

```
rec2.plotWorkingTime()
```

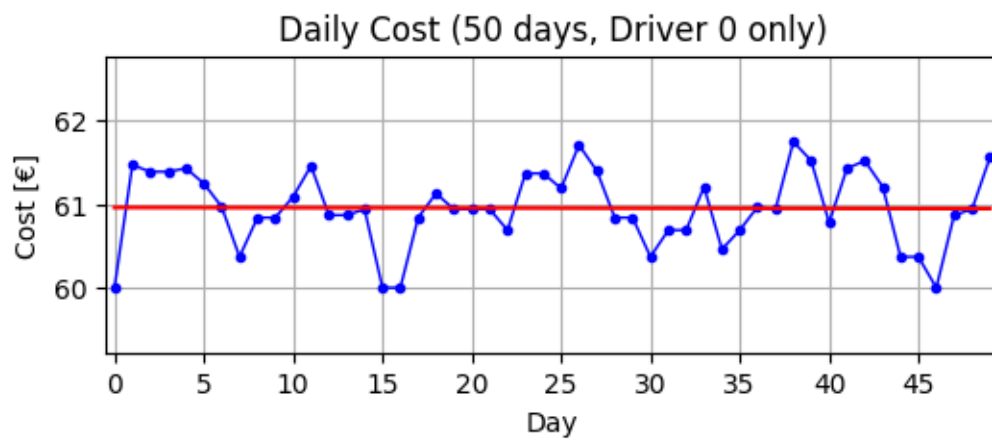


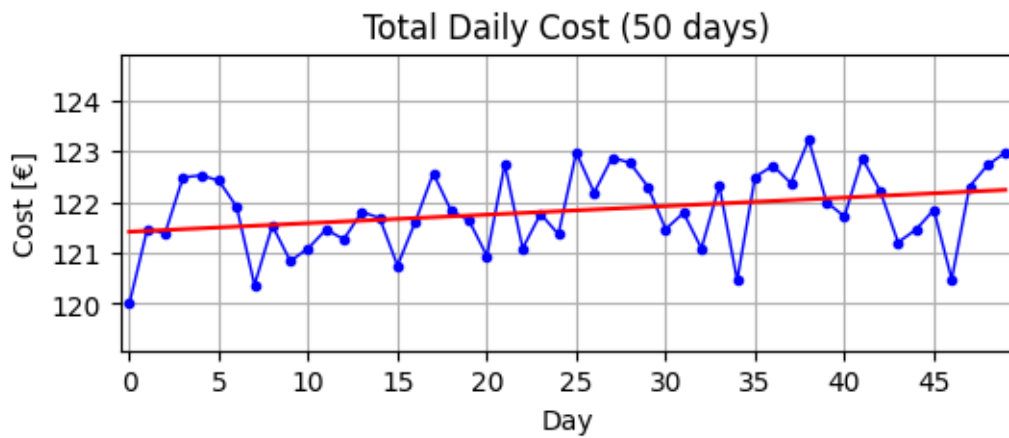
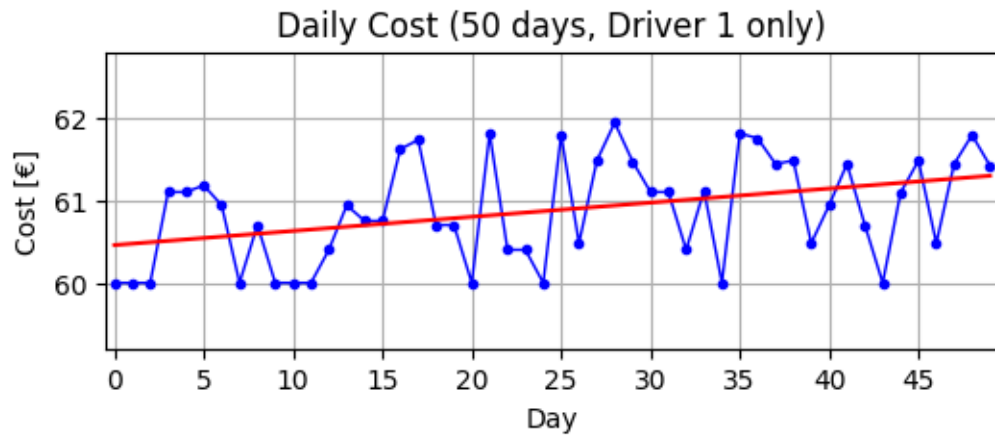
```
[64]: for i in range(rec1.drivers):
        rec2.plotTourLength(i)
rec2.plotTourLength()
```



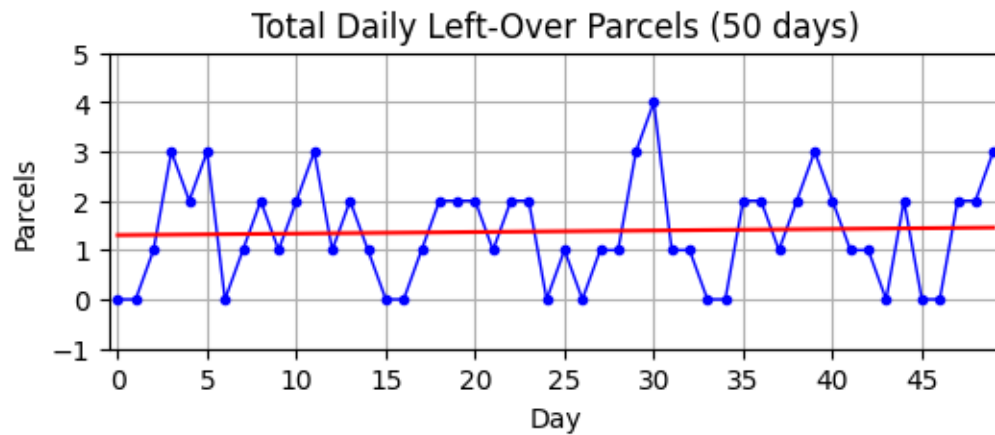


```
[65]: for i in range(rec1.drivers):
        rec2.plotDailyCost(i)
rec2.plotDailyCost()
```

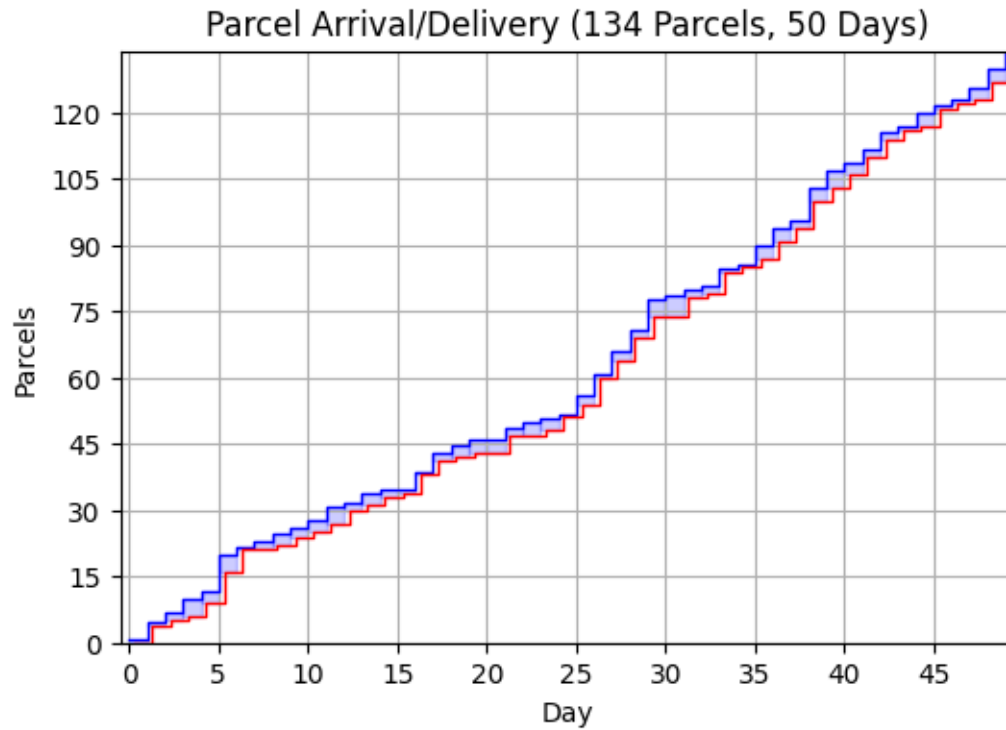




```
[66]: rec2.plotParcelsLeftOver()
```



```
[67]: rec2.countPlot()
```

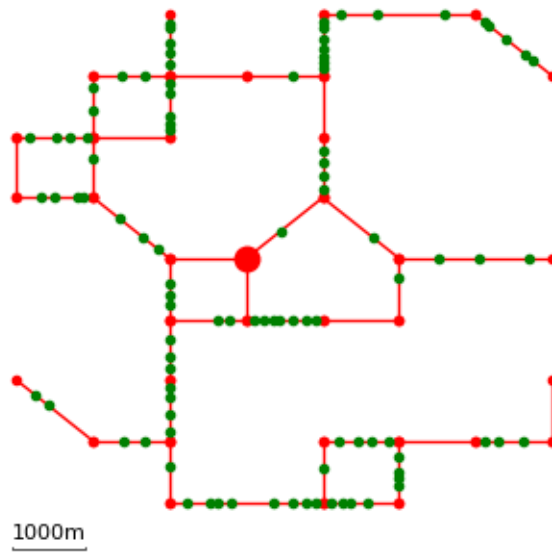


### 12.4.3 High Demand System

```
[68]: import pickle
with open('data/data.pickled', 'rb') as f:
    M, C = pickle.load(f)
```

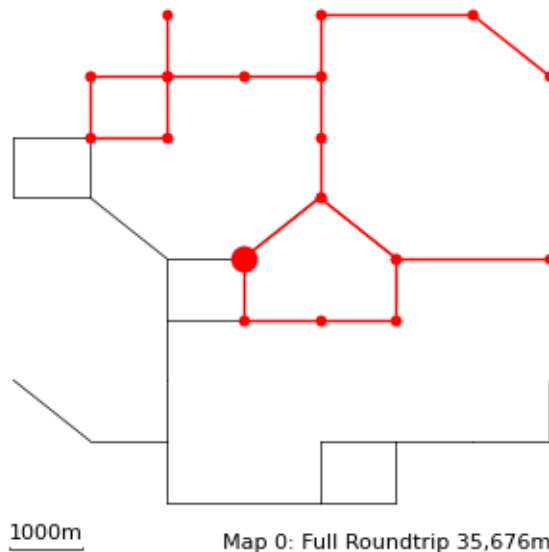
```
[69]: W = generateWarehouseLocation(M)
```

```
[70]: plotMap(M, T=C, w=W, scale=True)
```

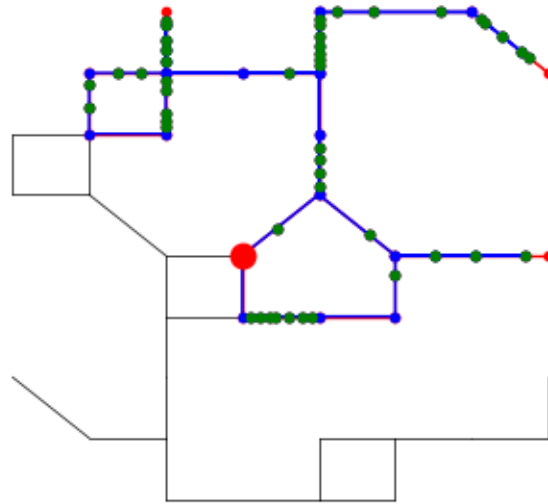


```
[71]: Plan = planCPP(M, W, C, n=2,
                    maxLength=40000, balance=0.1, timeLimit=10,
                    timing=True, plot=True)
```

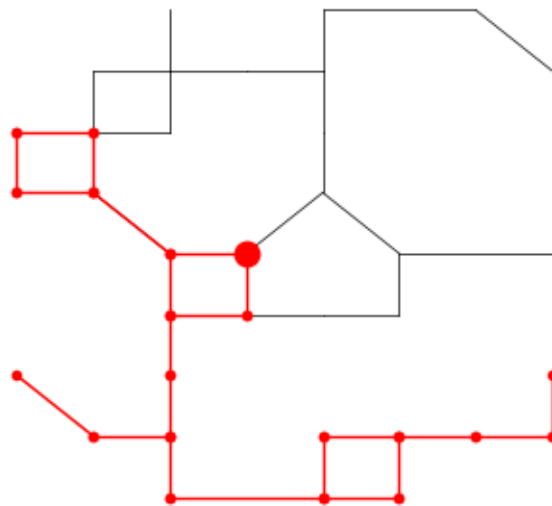
Solver time: 10.19s  
 Solution possibly not optimal  
 Total Delivery Path Length: 73472.0





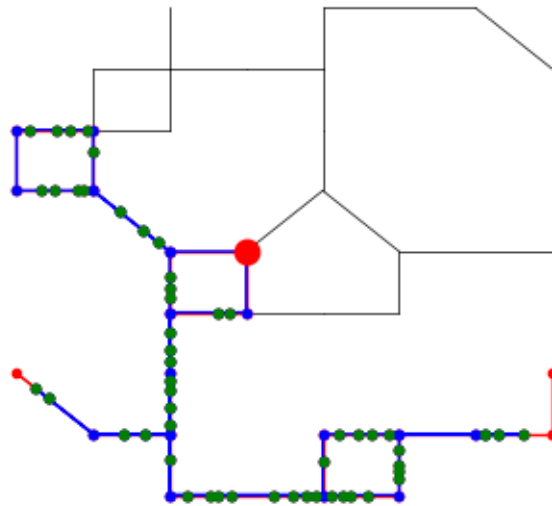


Driver 0: 47 Customers, max Roundtrip: 33,976m



1000m

Map 1: Full Roundtrip 37,796m



Driver 1: 53 Customers, max Roundtrip: 34,096m

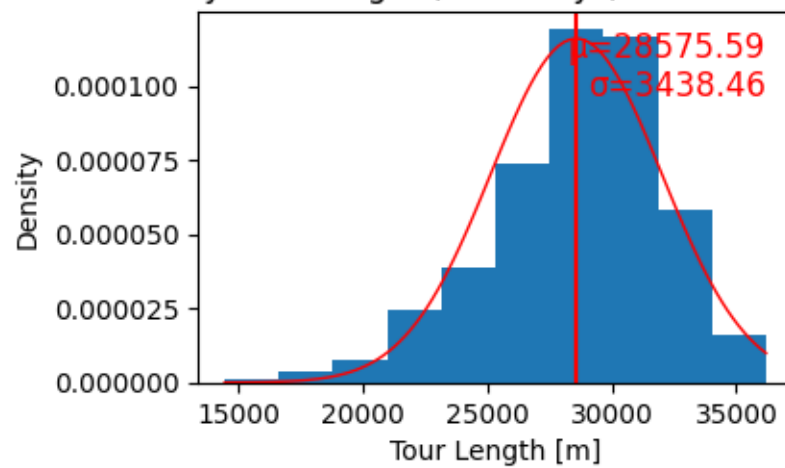
```
[72]: rec5 = simulation(M, W, C, Plan, p=0.25, days=1000)
```

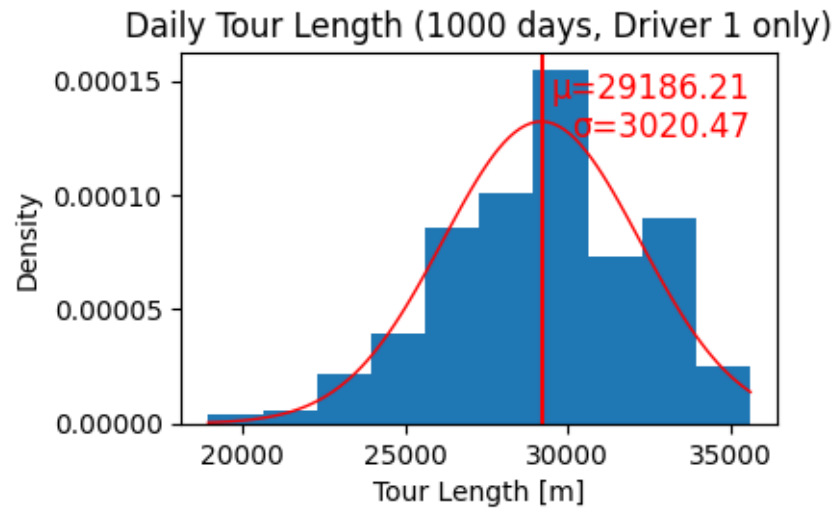
Simulating delivery of 25058 parcels over 1000 days to 100 customers using 2 drivers

Delivery Centre Inventory at the end of last day: 13 parcels

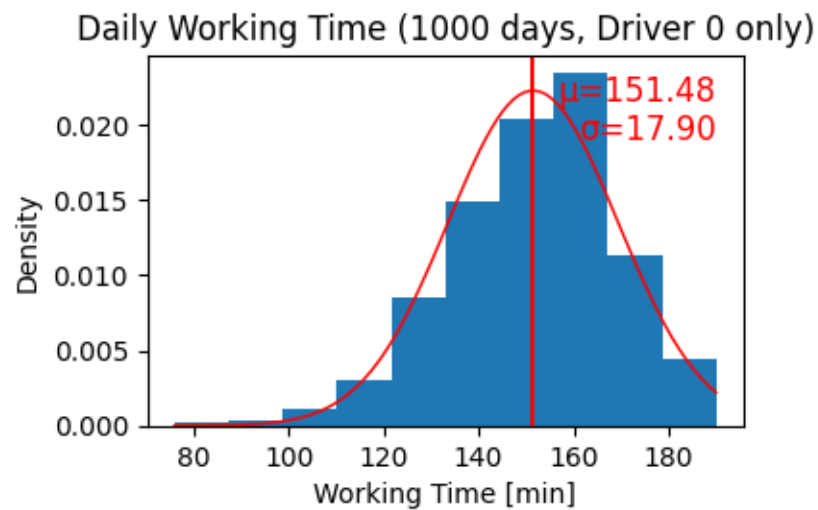
```
[73]: for i in range(rec5.drivers):
      rec5.histTourLength(i)
```

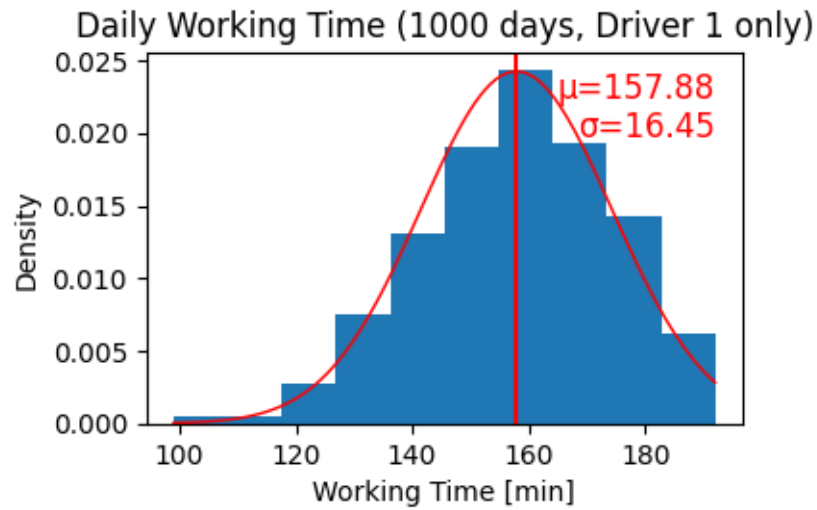
Daily Tour Length (1000 days, Driver 0 only)



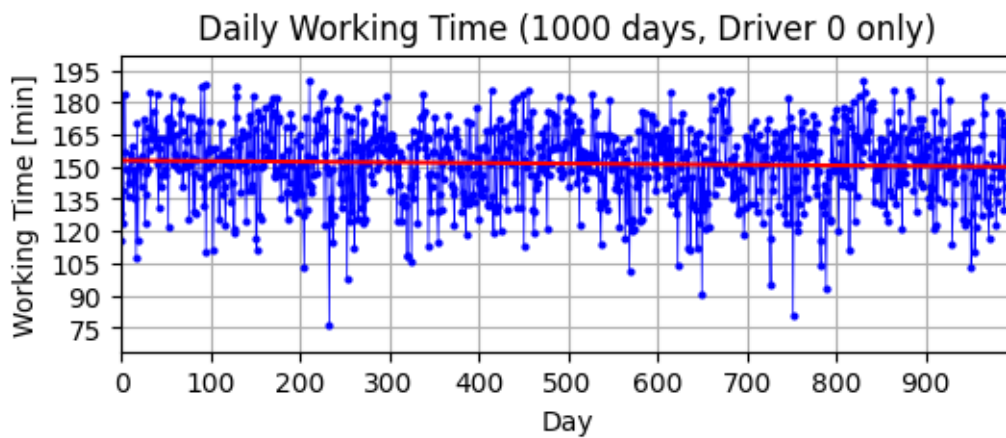


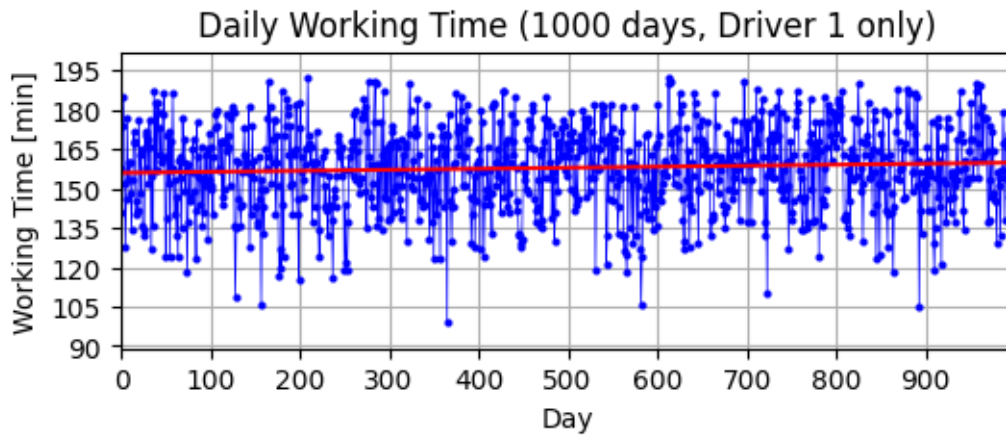
```
[74]: for i in range(rec5.drivers):  
      rec5.histWorkingTime(i)
```



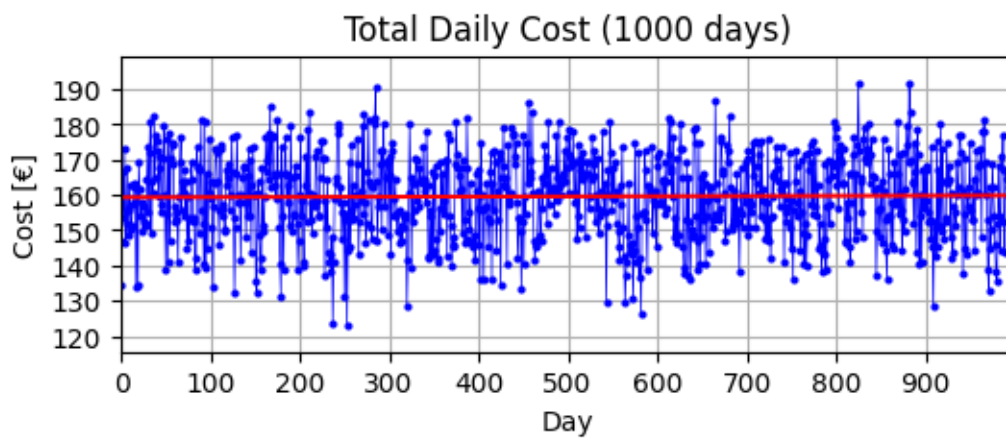


```
[75]: for i in range(rec5.drivers):
      rec5.plotWorkingTime(i)
```

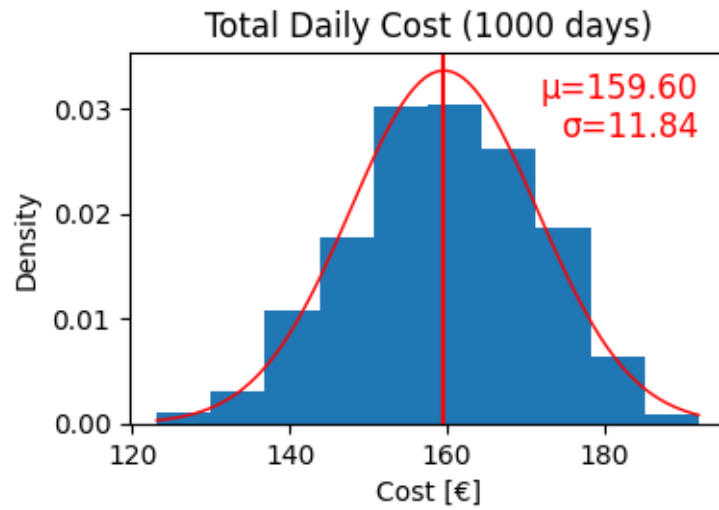




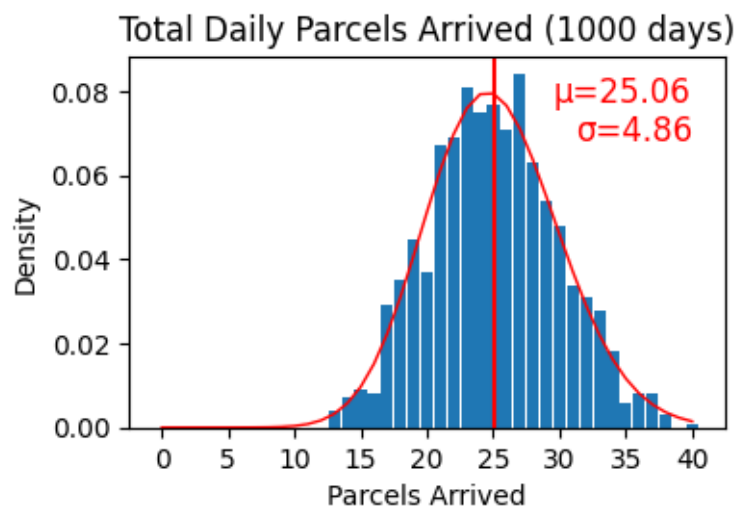
```
[76]: rec5.plotDailyCost()
```



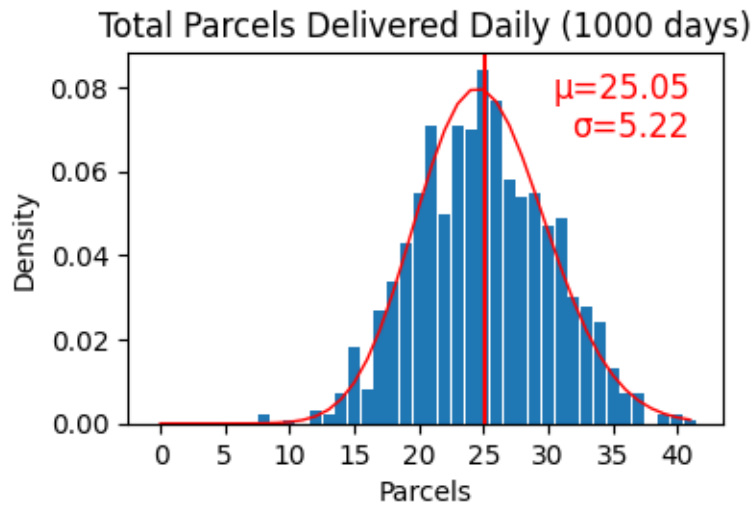
```
[77]: rec5.histDailyCost()
```



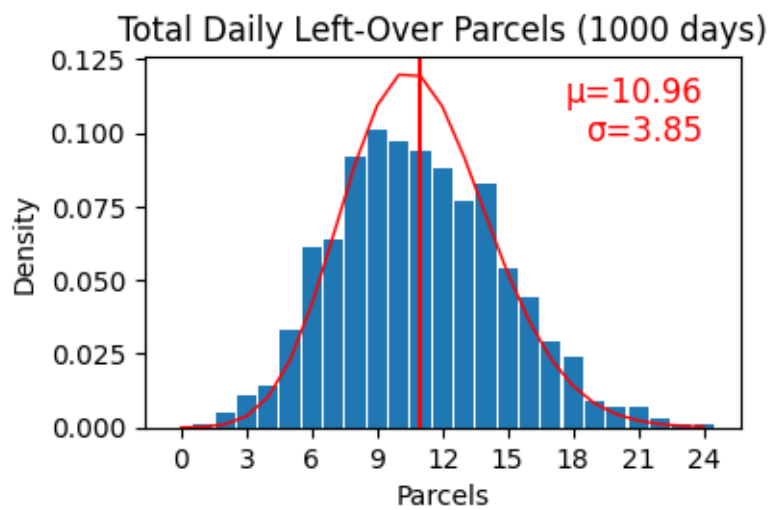
```
[78]: rec5.histParcelsArrived()
```



```
[79]: rec5.histParcelsDelivered()
```



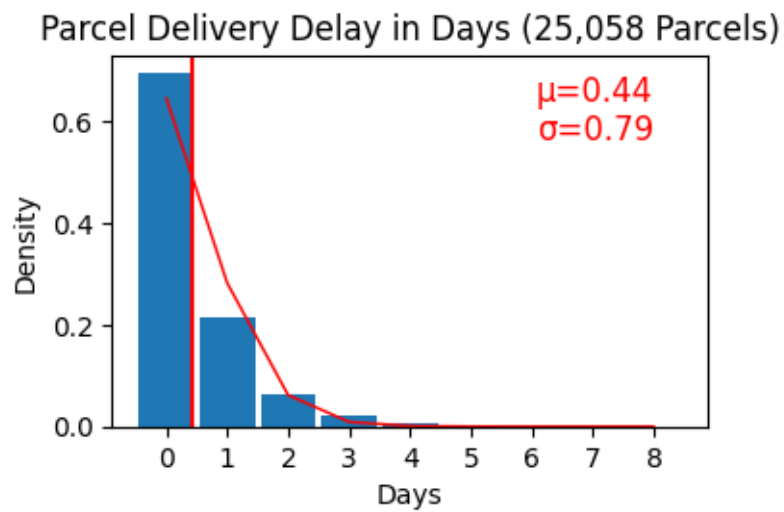
```
[80]: rec5.histParcelsLeftOver()
```



```
[81]: rec5.countPlot()
```



```
[82]: rec5.histParcelDeliveryDelay()
```





## 13 Preparing Statistics

### 13.1 Accessing Statistics

The class Recorder has been extended by a method `summary()` that returns a dataframe providing the usual 6-number descriptive statistic for the data available in the Recorder. From the summary data frame we can extract individual data.

```
[83]: summary = rec5.summary()
      summary
```

```
[83]:
```

	min	25%	mean	50%	75%	\
col						
tour length	39391	55010.25	57761.81	57978.5	60984.25	
parcels left over	1	8.0	10.96	11.0	14.0	
parcels arrived	13	22.0	25.06	25.0	28.0	
parcels out for delivery	19	32.0	35.95	36.0	40.0	
parcels returned from delivery	1	8.0	10.91	11.0	14.0	
parcels delivered	8	21.0	25.04	25.0	29.0	
working time	217	294.0	309.36	311.0	327.0	
cost	123.15	151.76	159.6	160.09	168.49	
cost per parcel	4.26	5.65	6.63	6.39	7.34	

	max
col	
tour length	68141
parcels left over	24
parcels arrived	40
parcels out for delivery	55
parcels returned from delivery	23
parcels delivered	41
working time	373
cost	191.95
cost per parcel	18.86

```
[84]: summary.at['cost per parcel', 'mean']
```

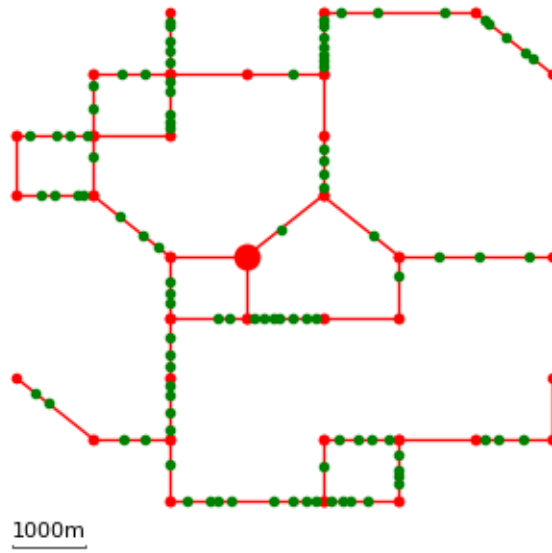
```
[84]: 6.63
```

### 13.2 Running Multiple Simulations per Warehouse Location

```
[85]: import pickle
      with open('data/data.pickled', 'rb') as f:
          M, C = pickle.load(f)
```

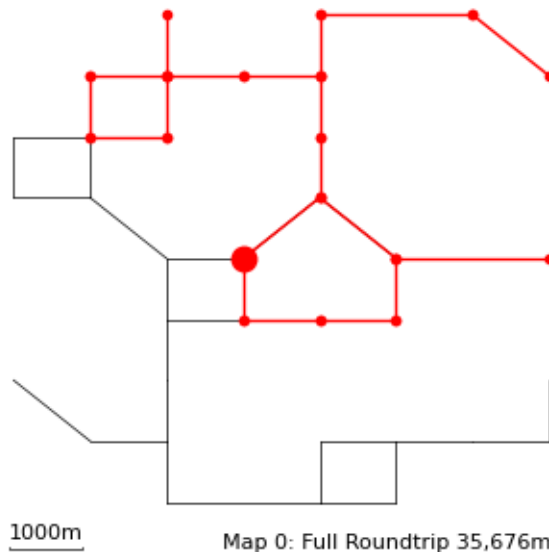
```
[86]: W = generateWarehouseLocation(M)
```

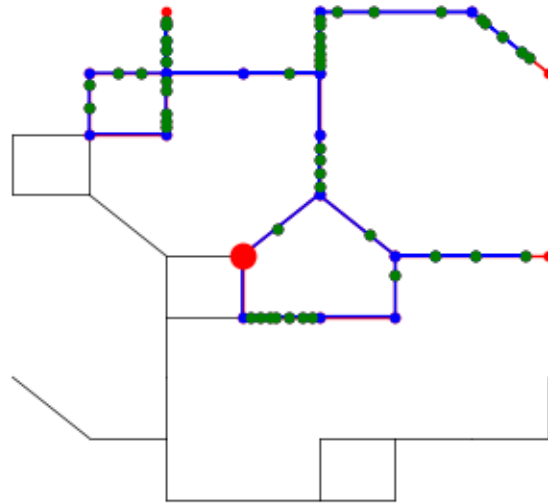
```
[87]: plotMap(M, T=C, w=W, scale=True)
```



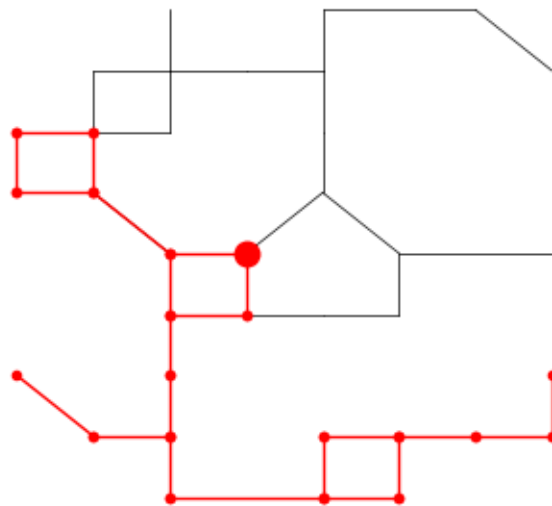
```
[88]: Plan = planCPP(M, W, C, n=2,
                    maxLength=40000, balance=0.1, timeLimit=10,
                    timing=True, plot=True)
```

Solver time: 10.19s  
 Solution possibly not optimal  
 Total Delivery Path Length: 73472.0



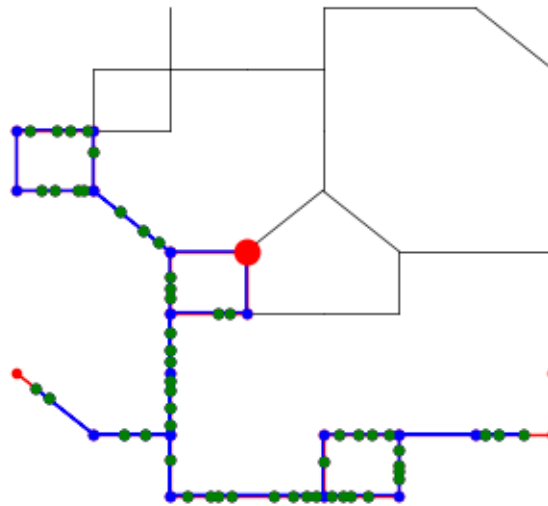


Driver 0: 47 Customers, max Roundtrip: 33,976m



1000m

Map 1: Full Roundtrip 37,796m



Driver 1: 53 Customers, max Roundtrip: 34,096m

```
[89]: res = []
for seed in range(10):
    rec = simulation(M, W, C, Plan, p=0.25, days=30, seed=seed)
    summary = rec.summary()
    costPP = summary.at['cost per parcel', 'mean']
    res.append(costPP)
    print(f"mean cost/parcel {costPP:7.2f}€")
    print()
print(res)
```

Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 11 parcels  
 mean cost/parcel 6.69€

Simulating delivery of 748 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 7 parcels  
 mean cost/parcel 6.66€

Simulating delivery of 732 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 8 parcels  
 mean cost/parcel 6.65€

Simulating delivery of 770 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 16 parcels  
 mean cost/parcel 6.92€

Simulating delivery of 689 parcels over 30 days to 100 customers using 2 drivers

Delivery Centre Inventory at the end of last day: 5 parcels  
mean cost/parcel 6.98€

Simulating delivery of 763 parcels over 30 days to 100 customers using 2 drivers  
Delivery Centre Inventory at the end of last day: 18 parcels  
mean cost/parcel 6.67€

Simulating delivery of 783 parcels over 30 days to 100 customers using 2 drivers  
Delivery Centre Inventory at the end of last day: 5 parcels  
mean cost/parcel 6.63€

Simulating delivery of 754 parcels over 30 days to 100 customers using 2 drivers  
Delivery Centre Inventory at the end of last day: 8 parcels  
mean cost/parcel 6.79€

Simulating delivery of 704 parcels over 30 days to 100 customers using 2 drivers  
Delivery Centre Inventory at the end of last day: 7 parcels  
mean cost/parcel 7.31€

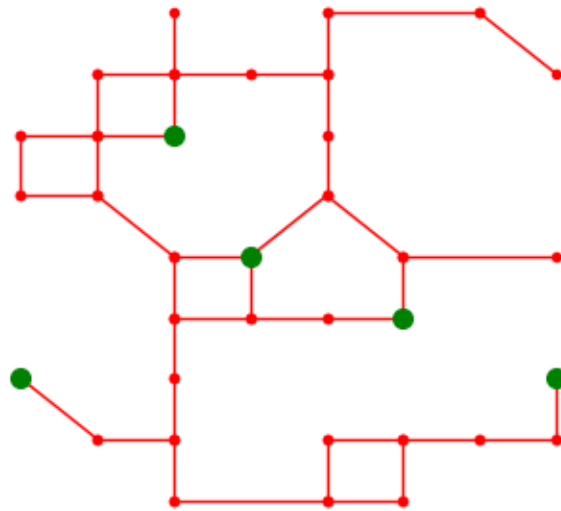
Simulating delivery of 785 parcels over 30 days to 100 customers using 2 drivers  
Delivery Centre Inventory at the end of last day: 11 parcels  
mean cost/parcel 6.48€

[6.69, 6.66, 6.65, 6.92, 6.98, 6.67, 6.63, 6.79, 7.31, 6.48]

### 13.3 Generating Warehouse Locations

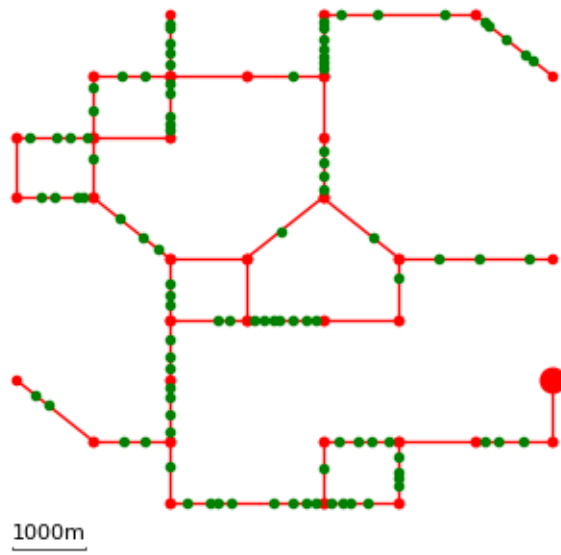
```
[90]: import pickle
      with open('data/data.pickled', 'rb') as f:
          M, C = pickle.load(f)
```

```
[92]: Warehouses = generateMultipleWarehouseLocations(M)
      plotMap(M, T=Warehouses, msT=7)
```

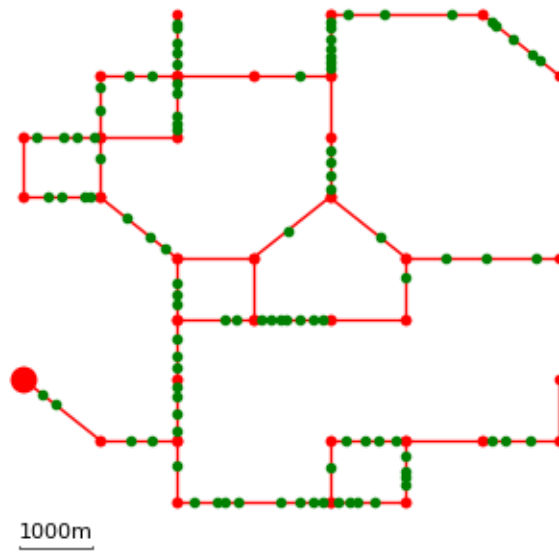


#### 13.4 Test Run maxLength=40,000 timeLimit=10

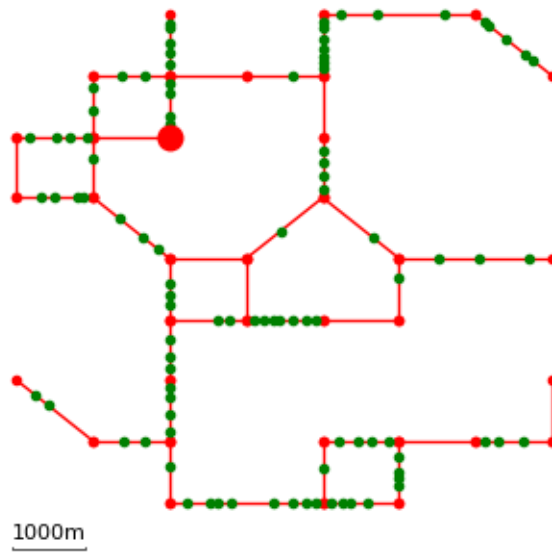
```
[93]: for W in Warehouses:
    plotMap(M, T=C, w=W, scale=True)
    Plan = planCPP(M, W, C, n=2,
                  maxLength=40000, timeLimit=10,
                  timing=True)
    if Plan is None:
        print("Simulation not possible")
    else:
        rec = simulation(M, W, C, Plan, p=0.25, days=30)
        summary = rec.summary()
        print(f"mean cost/day      {summary.at['cost', 'mean']:7.2f}€")
        print(f"mean cost/parcel {summary.at['cost per parcel', 'mean']:7.2f}€")
```



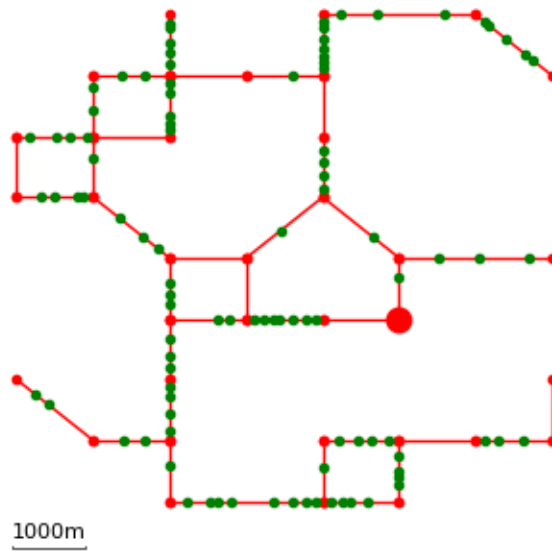
Solver time: 10.19s  
 Not Solved  
 Simulation not possible



Solver time: 10.24s  
 Not Solved  
 Simulation not possible

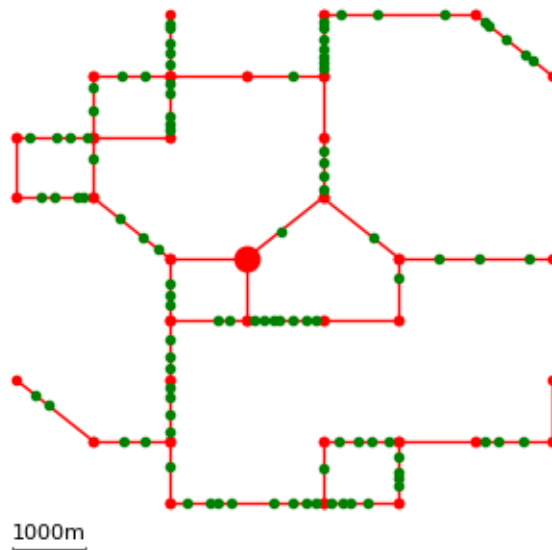


Solver time: 10.21s  
 Not Solved  
 Simulation not possible



Solver time: 10.25s  
 Not Solved  
 Simulation not possible



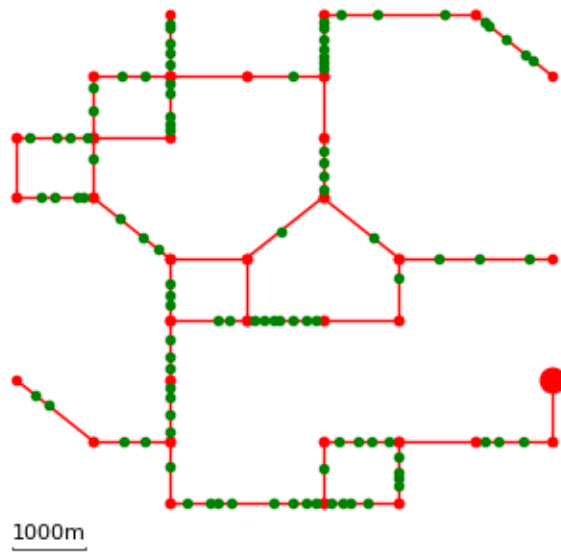


Solver time: 10.27s  
 Solution possibly not optimal  
 Total Delivery Path Length: 73472.0  
 Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 11 parcels  
 mean cost/day 155.86€  
 mean cost/parcel 6.44€

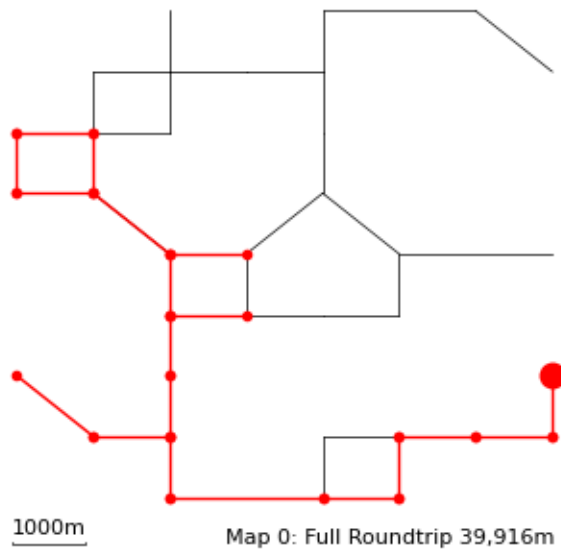
### 13.5 Test Run balance=0.2 timeLimit=20

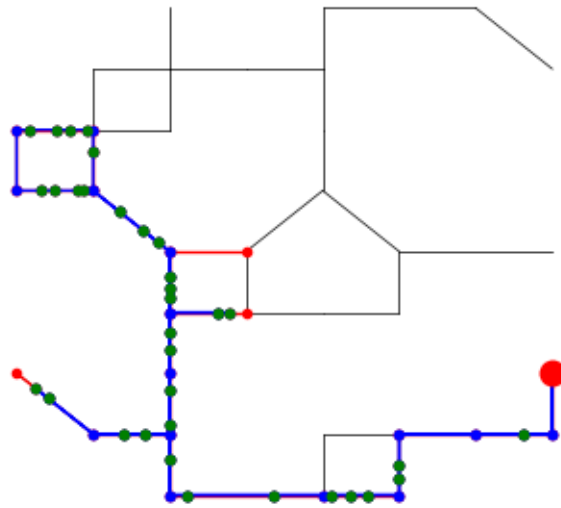
```

[94]: for W in Warehouses:
    plotMap(M, T=C, w=W, scale=True)
    Plan = planCPP(M, W, C, n=2,
                  balance=0.2, timeLimit=20,
                  timing=True, plot=True)
    if Plan is None:
        print("Simulation not possible")
    else:
        rec = simulation(M, W, C, Plan, p=0.25, days=30)
        summary = rec.summary()
        print(f"mean cost/day {summary.at['cost', 'mean']:7.2f}€")
        print(f"mean cost/parcel {summary.at['cost per parcel', 'mean']:7.2f}€")
  
```

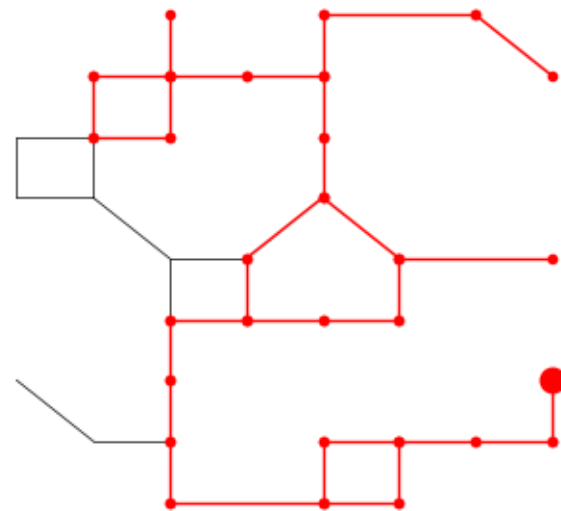


Solver time: 20.22s  
 Solution possibly not optimal  
 Total Delivery Path Length: 98912.0



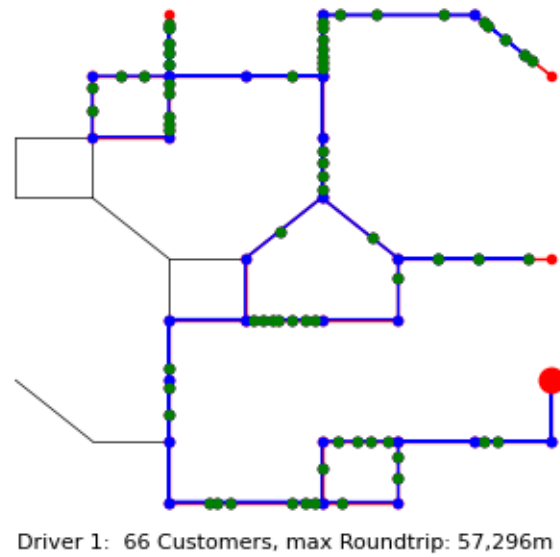


Driver 0: 34 Customers, max Roundtrip: 36,588m

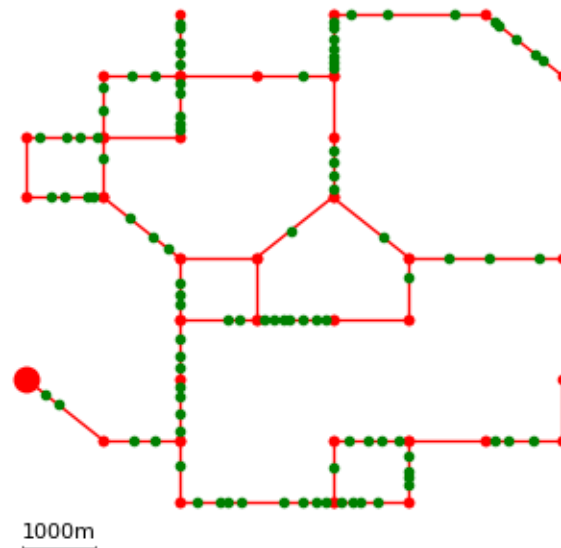


1000m

Map 1: Full Roundtrip 58,996m

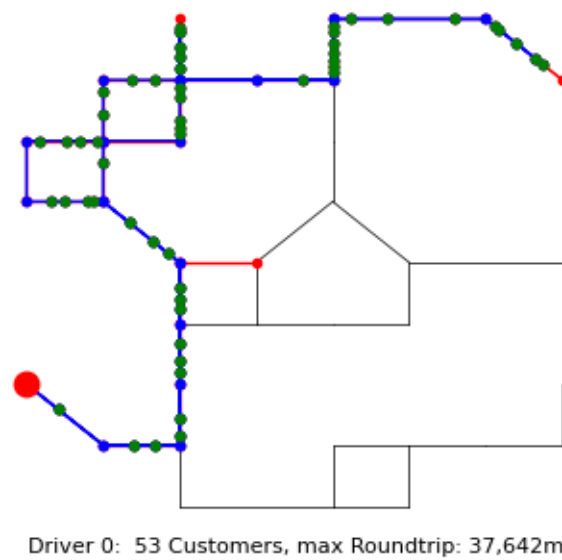
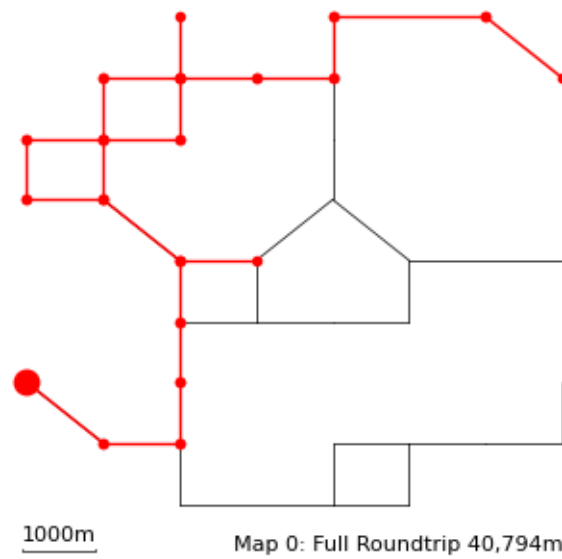


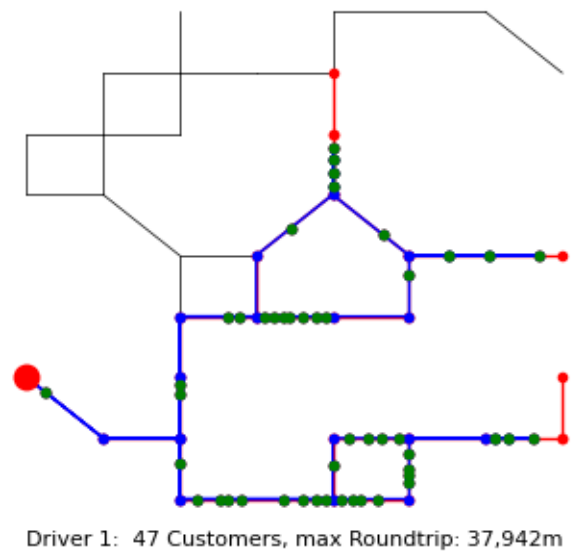
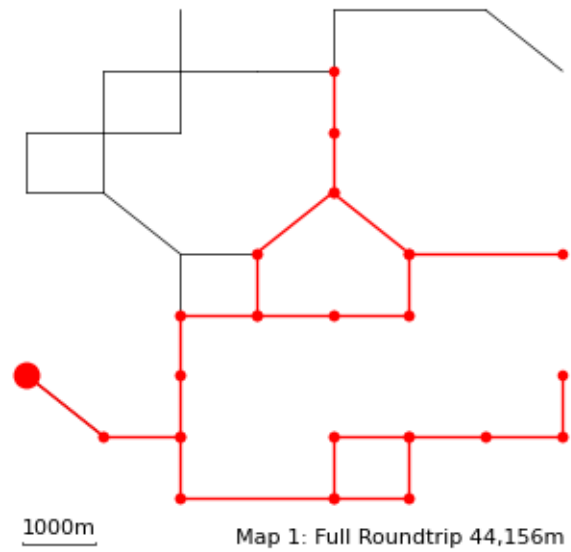
Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 227 parcels  
 mean cost/day 180.73€  
 mean cost/parcel 10.49€



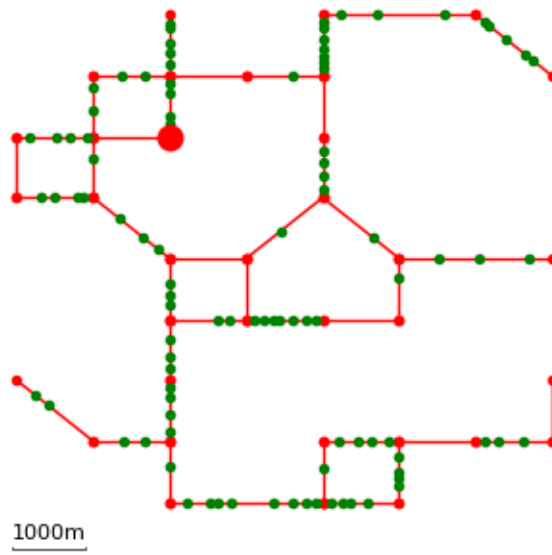
Solver time: 20.17s  
 Solution possibly not optimal

Total Delivery Path Length: 84950.0

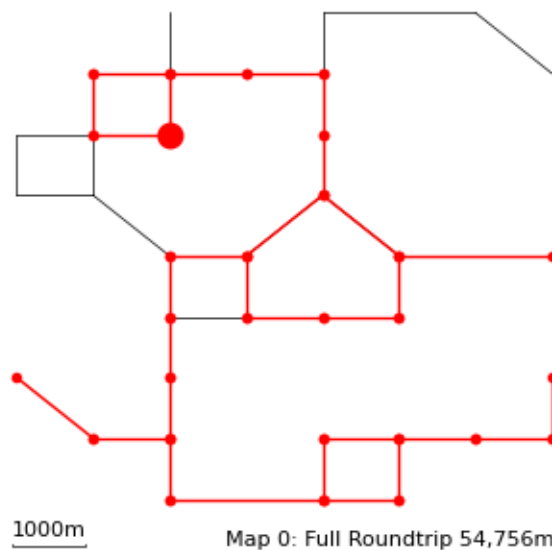


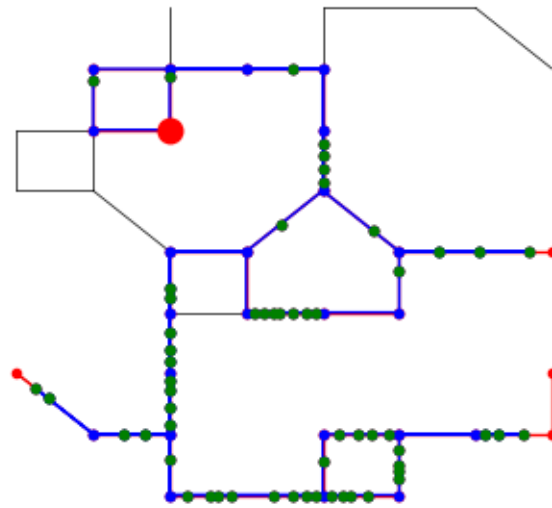


Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 12 parcels  
 mean cost/day 180.89€  
 mean cost/parcel 7.57€

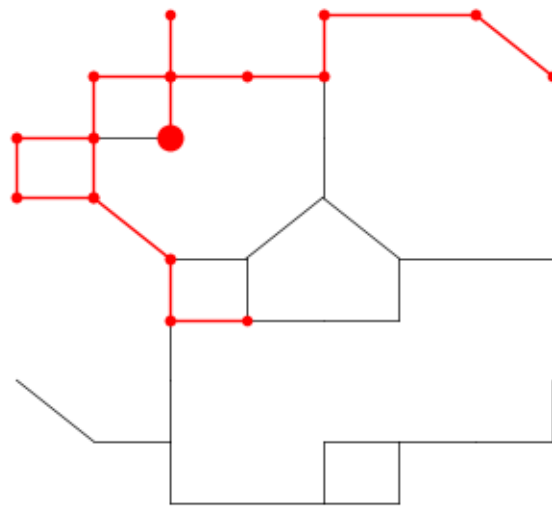


Solver time: 20.16s  
 Solution possibly not optimal  
 Total Delivery Path Length: 92552.0





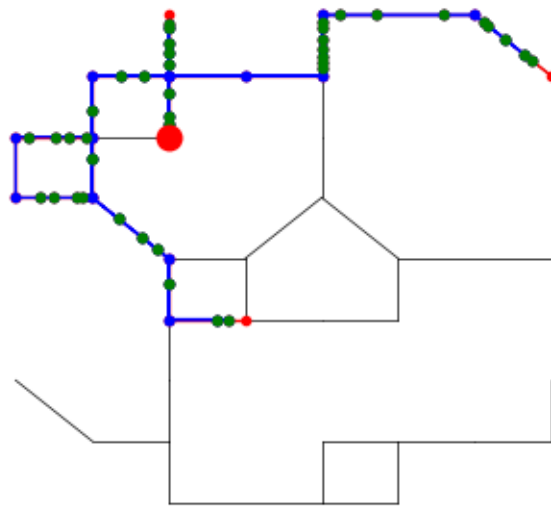
Driver 0: 58 Customers, max Roundtrip: 50,386m



1000m

Map 1: Full Roundtrip 37,796m





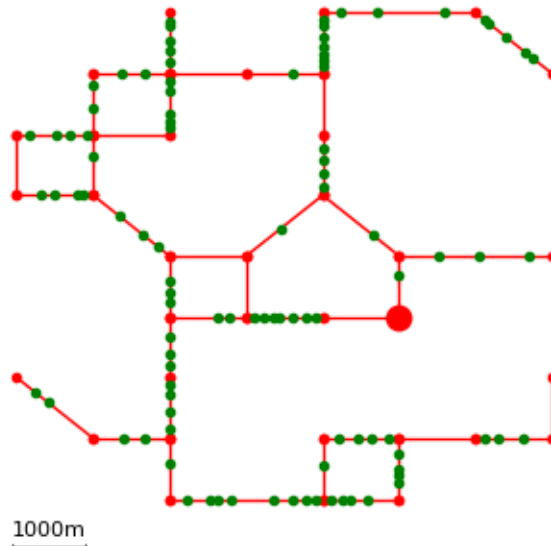
Driver 1: 42 Customers, max Roundtrip: 34,202m

Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers

Delivery Centre Inventory at the end of last day: 126 parcels

mean cost/day 168.77€

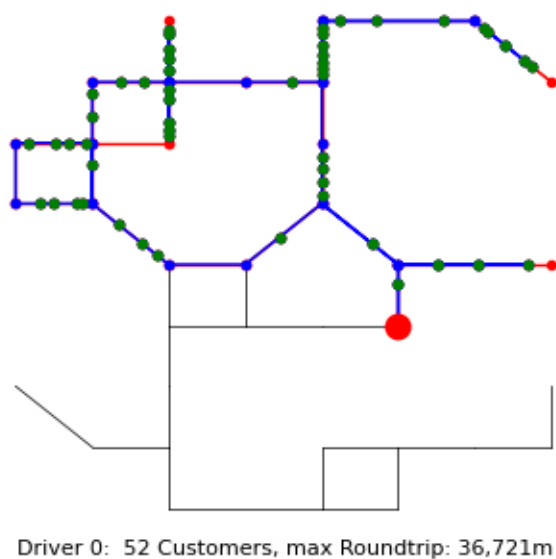
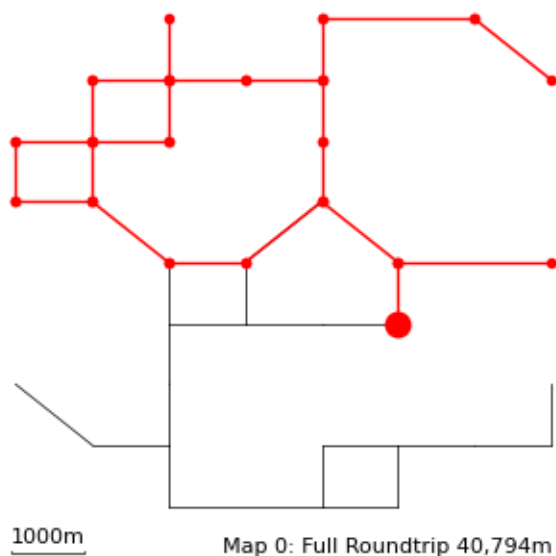
mean cost/parcel 8.42€

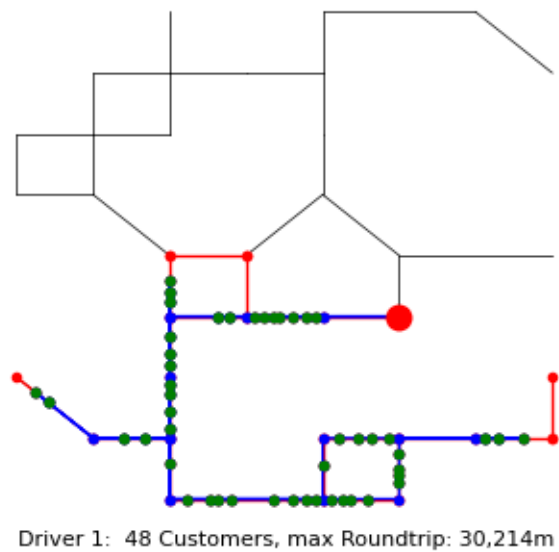
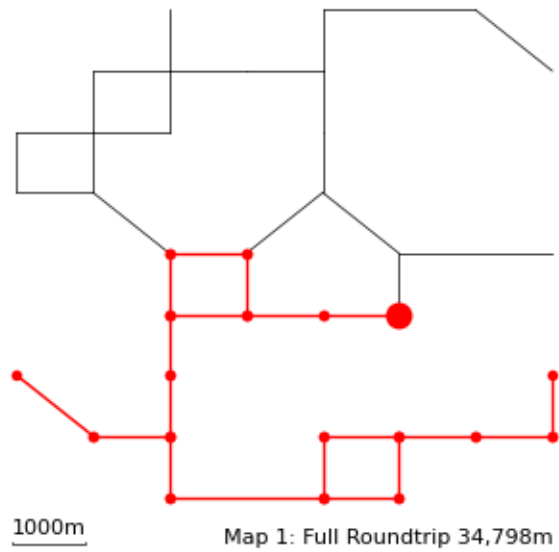


Solver time: 20.16s

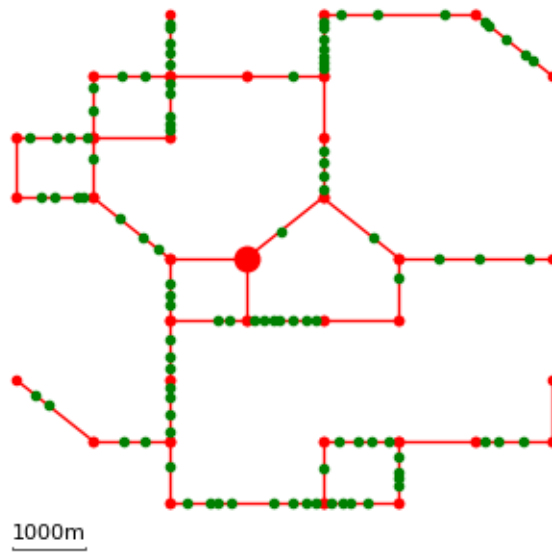
Solution possibly not optimal

Total Delivery Path Length: 75592.0

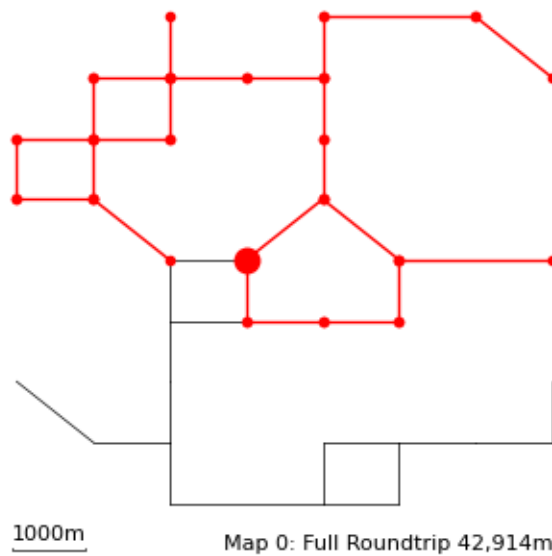


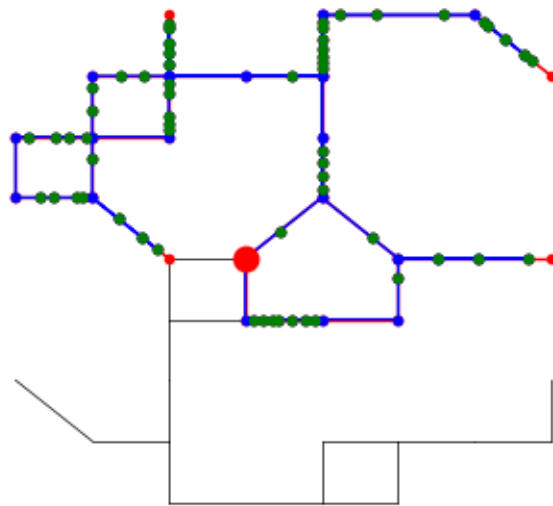


Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 12 parcels  
 mean cost/day      156.78€  
 mean cost/parcel    6.73€

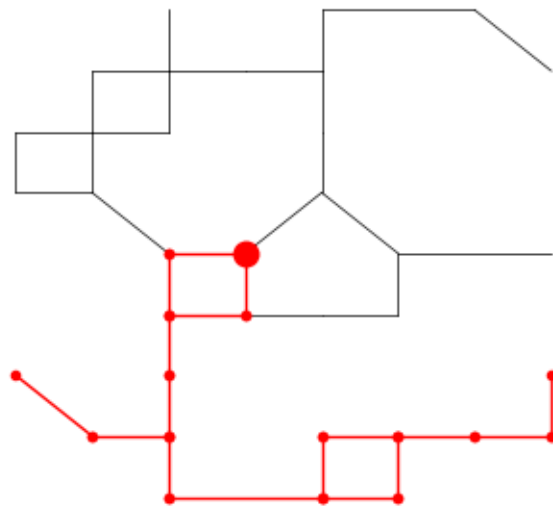


Solver time: 20.16s  
 Solution possibly not optimal  
 Total Delivery Path Length: 73472.0



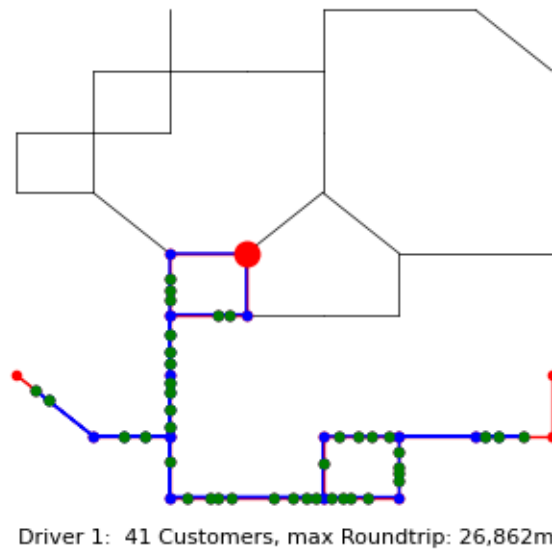


Driver 0: 59 Customers, max Roundtrip: 40,782m



1000m

Map 1: Full Roundtrip 30,558m



Simulating delivery of 761 parcels over 30 days to 100 customers using 2 drivers  
 Delivery Centre Inventory at the end of last day: 6 parcels  
 mean cost/day      159.85€  
 mean cost/parcel    6.68€

[ ]: