

Report on Online Learning for Min Sum Set Cover and Pandora's Box

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Abstract

This report presents an analysis and summary of the paper *Online Learning for Min Sum Set Cover and Pandora's Box* which provides a simple but effective skeleton for crafting online learning algorithms for the *Pandora's Box Problem*, the *Min Sum Set Cover Problem (MSSC)*, and other related problems in the field of *Stochastic optimization* [1]. Traditionally, these problems assume prior knowledge of value distributions. However, in this work, we explore an online learning approach where we are presented with information over multiple rounds.

Furthermore, the research, extends this framework to a bandit setting where only the values of the opened boxes are shown to the learner after each round. This extension also encompasses other alternatives of the above-mentioned problems [1].

1 Introduction

The two essential problems in *Stochastic Optimization* are the *Pandora's Box*, and *MSSC* problems. Introduced, by Weitzman [2] the *Pandora's Box* problem offers a general framework for optimizing decisions under uncertainty, with a cost for revealing information. The goal is to minimize the cost of uncovering information. *MSSC*, a variation of *Pandora's box*, deals with scenarios where values are either 0 or ∞ [3].

2 Problem Definitions

Define the MSSC and Pandora's Box problems. Include formal problem statements, such as:

- **Pandora's Box Problem:** Present the goal of minimizing the sum of inspection costs and chosen values.
- **Min Sum Set Cover Problem:** Discuss the special case where values are 0 or ∞ .

3 Methodologies

Summarize the key approaches used in the paper, including:

- Convex relaxations for online learning.
- Online convex optimization frameworks.
- Rounding techniques for fractional to integral solutions.

4 Results

Detail the main results:

- Competitive ratios achieved for Pandora’s Box and MSSC.
- Extensions to bandit settings.
- Performance under matroid constraints.

5 Comparison with Previous Work

Discuss how the paper builds upon or improves results from prior studies. Highlight differences in techniques and results.

6 Applications and Future Work

Explain potential applications of these results in real-world scenarios. Propose future directions for research based on open questions identified in the paper.

7 Conclusion

Provide a concise summary of the main insights gained from the study and their significance in the field of online learning and optimization.

A Appendix

Include any additional proofs, explanations, or extended results here.

References

- [1] Evangelia Gergatsouli and Christos Tzamos. Online learning for min sum set cover and pandora’s box. In *International Conference on Machine Learning*, pages 7382–7403. PMLR, 2022.
- [2] Martin Weitzman. *Optimal search for the best alternative*, volume 78. Department of Energy, 1978.
- [3] Uriel Feige, László Lovász, and Prasad Tetali. Approximating min sum set cover. *Algorithmica*, 40:219–234, 2004.