

# Report on Online Learning for Min Sum Set Cover and Pandora's Box

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## Abstract

This report presents an analysis and summary of the paper *Online Learning for Min Sum Set Cover and Pandora's Box* [1]. The focus is on understanding the problems studied, the methodologies applied, and the key results, including their implications and potential applications.

## 1 Introduction

Provide an overview of the problems of Min Sum Set Cover (MSSC) and Pandora's Box as introduced in the source paper. Discuss the motivation and background for studying these problems in stochastic and online optimization settings [2].

## 2 Problem Definitions

Define the MSSC and Pandora's Box problems. Include formal problem statements, such as:

- **Pandora's Box Problem:** Present the goal of minimizing the sum of inspection costs and chosen values.
- **Min Sum Set Cover Problem:** Discuss the special case where values are 0 or  $\infty$ .

## 3 Methodologies

Summarize the key approaches used in the paper, including:

- Convex relaxations for online learning.
- Online convex optimization frameworks.
- Rounding techniques for fractional to integral solutions.

## 4 Results

Detail the main results:

- Competitive ratios achieved for Pandora's Box and MSSC.
- Extensions to bandit settings.
- Performance under matroid constraints.

## 5 Comparison with Previous Work

Discuss how the paper builds upon or improves results from prior studies. Highlight differences in techniques and results.

## 6 Applications and Future Work

Explain potential applications of these results in real-world scenarios. Propose future directions for research based on open questions identified in the paper.

## 7 Conclusion

Provide a concise summary of the main insights gained from the study and their significance in the field of online learning and optimization.

## A Appendix

Include any additional proofs, explanations, or extended results here.

## References

- [1] Uriel Feige, László Lovász, and Prasad Tetali. Approximating min sum set cover. *Algorithmica*, 40:219–234, 2004.
- [2] Evangelia Gergatsouli and Christos Tzamos. Online learning for min sum set cover and pandora’s box. In *International Conference on Machine Learning*, pages 7382–7403. PMLR, 2022.