

Bubble Sort

Bubble Sort is a simple algorithm which is used to sort a given set of n elements provided in form of an array with n number of elements. Bubble Sort compares all the element one by one and sort them based on their values.

Implementation

```
#include<stdio.h>

int n;
void Sort(int ara[])
{
    for(int i=0; i<n; i++)
        for(int j=0; j<(n-i-1); j++)
        {
            if(ara[j]>ara[j+1])
            {
                int p=ara[j];
                ara[j]=ara[j+1];
                ara[j+1]=p;
            }
        }
}

int main()
{
    int ara[]={5,1,4,2,8};
    n=6;
    printf("Array before swap: ");
    for(int i=0; i<n; i++)
        printf("%d ",ara[i]);
    printf("\n");
    Sort(ara);
    printf("Array after swap: ");
    for(int i=0; i<n; i++)
        printf("%d ",ara[i]);
    printf("\n");
}
```

Analysis:

Let's consider an array: (5, 1, 4, 2, 8)

We want to sort it in ascending order:

So,

1st Iteration:

(**5** 1 4 2 8) → (**1** 5 4 2 8), Here, algorithm compares the first two elements, and swaps since $5 > 1$.

(**1** **5** 4 2 8) → (**1** **4** 5 2 8), Swap since $5 > 4$

(**1** 4 **5** 2 8) → (**1** 4 **2** 5 8), Swap since $5 > 2$

(**1** 4 2 **5** 8) → (**1** 4 2 **5** 8), Now, since these elements are already in order ($8 > 5$), algorithm does not swap them.

2nd Iteration:

(**1** **4** 2 5 8) → (**1** **4** 2 5 8)

(**1** **4** **2** 5 8) → (**1** **2** 4 5 8), Swap since $4 > 2$

(**1** 2 **4** **5** 8) → (**1** 2 **4** **5** 8)

(**1** 2 4 **5** 8) → (**1** 2 4 **5** 8)

Now, the array is already sorted, but our algorithm does not know if it is completed. The algorithm needs one **whole** pass without **any** swap to know it is sorted.

3rd Iteration:

(**1** **2** 4 5 8) → (**1** **2** 4 5 8)

(**1** **2** **4** 5 8) → (**1** **2** **4** 5 8)

(**1** 2 **4** **5** 8) → (**1** 2 **4** **5** 8)

(**1** 2 4 **5** 8) → (**1** 2 4 **5** 8)

Time Complexity

In Bubble Sort, (n-1) comparisons will be done in the 1st pass, (n-2) in 2nd pass, (n-3) in 3rd pass and so on. So the total number of comparisons will be,

$$(n-1) + (n-2) + (n-3) + (n-4) + \dots + 3 + 2 + 1$$

$$= (n-1)*n/2$$

Ignoring the constant co-efficient, we can say that the complexity is: $O(n^2)$

By using the following process we have to do same number operation for best case, worst case and average case.

So complexity is: $O(n^2)$

Optimized Bubble sort

Sample :

```
void bubbleOpt(int ara[])
{
    bool flg;
    for(int i=0; i<n; i++)
    {
        flg=true;
        for(int j=0; j<(n-i-1); j++)
            if(ara[j]>ara[j+1])
                swap(ara[j],ara[j+1]),flg=false;

        if(!flg)
            break;
    }
}
```

It can be optimized by stopping the algorithm if inner loop didn't cause any swap.

Worst and Average Case: $O(n*n)$. Worst case occurs when array is reverse sorted.

Best Case: $O(n)$. Best case occurs when array is already sorted.