Quiz 1 Solution: CS CS4640

1. Given a transform matrix, T, whose form is:

$$T = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & a \\ \sin(\theta) & \cos(\theta) & b \\ 0 & 0 & 1 \end{bmatrix}$$

Give the Matlab statements to robustly extract the parameters a, b and θ from T; e.g., $a = \ldots$, etc. Note that an instance of T is a 3×3 matrix with fixed values.

```
a = T(1,3);
b = T(2,3);
theta = atan2(T(2,1),T(1,1));
```

2. Suppose scaling is allowed and the transform matrix, T, has the form:

$$T = \begin{bmatrix} s \times \cos(\theta) & -\sin(\theta) & a \\ \sin(\theta) & s \times \cos(\theta) & b \\ 0 & 0 & 1 \end{bmatrix}$$

Give the Matlab statements to robustly extract the parameters a, b, s and θ from T; e.g., $a = \ldots$, etc.

```
a = T(1,3);
b = T(2,3);
theta = asin(T(2,1));
cos_theta = cos(theta);
if abs(cos_theta)>0
    s = T(1,1)/cos_theta;
end
```

3. Suppose an image, im, is to be created from a 2-D function, f(x, y), that has min value -1 and max value 7. For each Q and set of f values below, give the corresponding image values generated by CS4640_create_im. Note that there image values will be in the range [0,1,...,Q-1].

a.
$$Q=8$$

 $f(x,y)=-0.5$
 $f(x,y)=3.2$
 $f(x,y)=5.9$
im $(x,y)=0$
im $(x,y)=6$
b. $Q=3$
 $f(x,y)=0$
 $f(x,y)=2$
im $(x,y)=0$
im $(x,y)=0$
im $(x,y)=0$

4. Suppose we have the following Matlab statement:

im(x,y) = 1

$$samps = rand(10000,1);$$

f(x,y) = 4

Draw the figure resulting from calling *hist(samps)*. Flat line above x-axis.

5. Suppose we have the following Matlb statement:

samps =
$$randn(10000,1);$$

Draw the figure resulting from calling hist(samps). Bell curve above x-axis