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## I Excel



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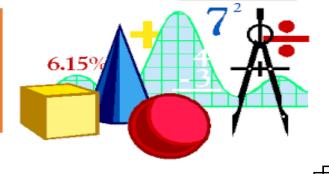
# **Mathematics Geometry**

Name: Class: G8

## Second Term

**Prepared by:** 

**Math Department** 

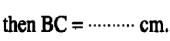


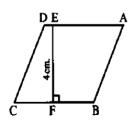
#### Lesson 1

#### The equality of areas of parallelogram

## Complete each of the following:

If the area of  $\triangle 7$  ABCD = 400 cm<sup>2</sup>, ١.



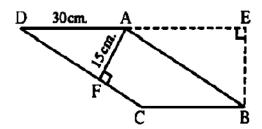


If the area of  $\square$  ABCD = 600 cm<sup>2</sup>.

then 
$$CD = \cdots cm$$
.

$$BE = \cdots cm$$
.

۲.

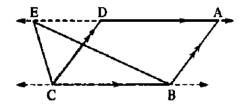


## In the opposite figure:

ABCD is a parallelogram and  $E \in \overrightarrow{AD}$ 

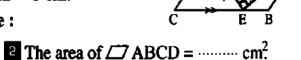
#### ٣. Complete the following:

- 1 The area of  $\triangle$  EBC = ..... the area of  $\square$  ABCD



## In the opposite figure:

- ABCD is a parallelogram, AE = 4 cm., ED = 3 cm.٤.  $_{9}$  m ( $\angle$  AED) = 90° and E  $\in$  BC Complete :
  - 1 The area of  $\triangle$  AED = ...... cm<sup>2</sup>



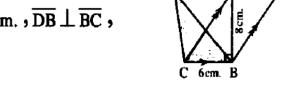
## In the opposite figure:

ABCD is a parallelogram in which, BC = 6 cm.,  $\overline{DB} \perp \overline{BC}$ , such that DB = 8 cm. and  $E \in \overline{AD}$ 

## Complete:

٥.

1 The area of  $\triangle$  ABCD = ....... cm<sup>2</sup> The area of  $\triangle$  EBC = ...... cm<sup>2</sup>.



C	choose the	correct ansv	ver :				
	If the base length of a parallelogram is 7 cm. and the corresponding height is 4 cm., then its area =						
	(a) 11 cm <sup>2</sup> .	(b) 14 cm <sup>2</sup> .	(c) 22 (	cm <sup>2</sup>	(d) 28 cm <sup>2</sup>		
	If the area of a parallelogram is 35 cm <sup>2</sup> and its height is 5 cm., then the length of the corresponding base is						
	(a) 5 cm.	(b) 7 cm.	(c) 9 cm	n.	(d) 30 cm.		
	_	oarallelogram in which		C = 10 cm	. and its smaller		
	(a) 2 cm.	(b) 4 cm.	(c) 8 c	m.	(d) 10 cm.		
	corresponding	m whose area = 50 cm height, then this height	ght =	-			
	(a) 50 cm.	(b) 25 cm.	(c) 10 c	cm.	(d) 5 cm.		
		een the area of the pa n and are included be	_		•		
	(a) 1:2	(b) 1:3	(c) 2:1	(d)	2:3		
		If the area of the triangle is 42 cm <sup>2</sup> and its height = 7 cm. • then the length of the corresponding base =					
	(a) 15 cm.	(b) 12 cm.	(c) 8 cm.	(d) 4	4 cm.		
	The area of a right-angled triangle in which the lengths of the sides of the right angle are 6 cm. and 9 cm. equals						
	(a) 54 cm <sup>2</sup>	(b) $60 \text{ cm}^2$	(c) 27 cm <sup>2</sup> .	(d)	15 cm <sup>2</sup>		
	The area of the rectangle whose dimensions are 6 cm. and 4 cm the area of						
	the triangle wh	ose base length is 12	cm. and the corresp	onding hei	ght is 4 cm.		

## Essay problems:

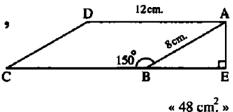
#### In the opposite figure:

ABCD is a parallelogram in which m ( $\angle$  ABC) = 150°,

AD = 12 cm.

, AB = 8 cm.,  $E \in \overrightarrow{CB}$  and  $\overrightarrow{AE} \perp \overrightarrow{CB}$ 

Find: The area of ABCD



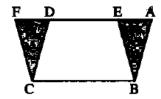
2)

#### In the opposite figure:

ABCD and EBCF are two parallelograms,

 $E \in \overrightarrow{AD}$  and  $F \in \overrightarrow{AD}$ 

**Prove that:** The area of  $\triangle$  ABE = the area of  $\triangle$  DCF



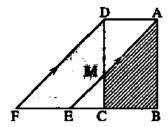
3)

## In the opposite figure:

ABCD is a rectangle  $\sqrt{AE} // \overline{DF}$ 

#### Prove that:

The area of the figure ABCM = the area of the figure DMEF



4)

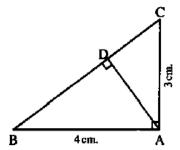
## In the opposite figure:

ABC is a right-angled triangle at A,

 $\overline{AD} \perp \overline{BC}$ , AB = 4 cm. and AC = 3 cm.

Find:  $\blacksquare$  The area of  $\triangle$  ABC

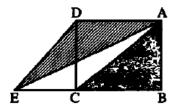
<sup>2</sup> The length of AD



 $\square$  In the opposite figure :

ABCD is a rectangle and  $E \in \overrightarrow{BC}$ 

**Prove that :** The area of  $\triangle$  DAE = the area of  $\triangle$  ABC



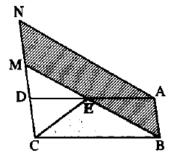
6)

In the opposite figure :

ABCD and ABMN are two parallelograms and  $M \in \overline{CD}$ 

Prove that:

The area of  $\triangle$  EBC =  $\frac{1}{2}$  the area of  $\triangle$ 7 ABMN

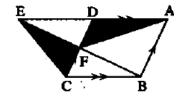


7)

 $\square$  In the opposite figure :

ABCD is a parallelogram  $, E \subseteq \overline{AD}$  and  $\overline{BE} \cap \overline{CD} = \{F\}$ 

**Prove that:** The area of  $\triangle$  AFD = the area of  $\triangle$  EFC

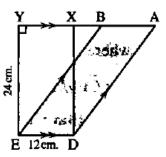


8)

In the opposite figure :

 $\overrightarrow{AB} / \overrightarrow{DE} \cdot X$  and  $Y \in \overrightarrow{AB}$ 

- , XDEY is a rectangle and  $\overline{AD} // \overline{BE}$
- 1 Find the area of the figure ABED
- If: AD = 30 cm., find the length of the perpendicular from B to  $\overline{AD}$



« 288 cm<sup>2</sup> > 9.6 cm. »

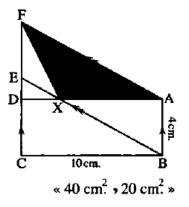
#### In the opposite figure:

ABCD is a rectangle, ABEF is a parallelogram

- $,D \in \overline{CF}, X \in \overline{BE}, E \in \overline{CF}$
- AB = 4 cm. and BC = 10 cm.

Find by proof:

- 1 The area of  $\square$  ABEF
- 2 The area of Δ XAF



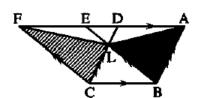
10)

## igspace In the opposite figure :

ABCD and EBCF are two parallelograms ,  $\overline{BE} \cap \overline{CD} = \{L\}$  ,  $D \in \overline{AF}$  and  $E \in \overline{AF}$ 

Prove that:

- 1 The area of  $\triangle$  ABL = the area of  $\triangle$  FCL
- The area of the figure ABCL = the area of the figure FCBL



#### Lesson 2

## The equality of the areas of two triangles

## Complete each of the following:

If ABC is a triangle, D is the midpoint of  $\overline{BC}$ , then:

The area of  $\triangle$  ABD = the area of  $\triangle$  .......

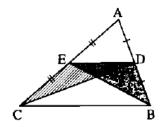
- If  $\overline{XL}$  is a median in  $\Delta XYZ$ , then the area of  $\Delta XYZ = \cdots$  the area of  $\Delta XYL$
- The triangle XYZ in which  $L \subseteq \overline{YZ}$  such that  $YL = \frac{1}{2} LZ$ , then: The area of  $\Delta XYL = \cdots$  the area of  $\Delta XYZ$
- The two triangles drawn on a common base and their vertices located on a straight line parallel to the base are .........
- Triangles with congruent bases and drawn between two parallel lines are .........
- The median in the triangle divides its area into ........

## Essay problems:

## In the opposite figure:

D is the midpoint of  $\overline{AB}$  and E is the midpoint of  $\overline{AC}$ 

**Prove that:** The area of  $\triangle$  BDE equals the area of  $\triangle$  CDE



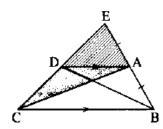
2)

## In the opposite figure:

ABCD is a quadrilateral in which  $\overrightarrow{AD} / / \overrightarrow{BC}$  and  $\overrightarrow{BA} \cap \overrightarrow{CD} = \{E\}$ 

such that BA = AE

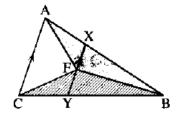
**Prove that :** The area of  $\triangle$  ADC = the area of  $\triangle$  ADE



 $\square$  In the opposite figure :

 $\overline{AC}$  //  $\overline{XY}$  and F is the midpoint of  $\overline{XY}$ 

**Prove that :** The area of  $\triangle$  ABF = the area of  $\triangle$  CBF

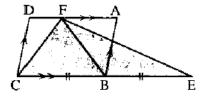


4)

In the opposite figure :

ABCD is a parallelogram.  $E \subset \overrightarrow{CB}$  where BC = BE

**Prove that :** The area of  $\triangle$  FEC = the area of  $\triangle$  ABCD



5)

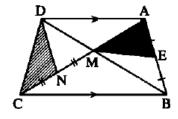
 $\square$  In the opposite figure :

ABCD is a quadrilateral whose diagonals intersect at M,

 $\overline{AD} // \overline{BC}$  and E is the midpoint of  $\overline{AB}$ ,

N is the midpoint of  $\overline{MC}$ 

**Prove that :** The area of  $\triangle$  AEM = the area of  $\triangle$  DNC



6)

In the opposite figure :

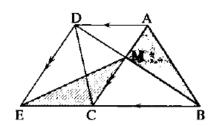
 $\overrightarrow{AD}$  //  $\overrightarrow{BC}$ ,  $\overrightarrow{E} \in \overrightarrow{BC}$  and  $\overrightarrow{AC}$  //  $\overrightarrow{DE}$ ,

 $\overline{AC} \cap \overline{BD} = \{M\}$ 

Prove that:

**1** The area of  $\triangle$  ABM = the area of  $\triangle$  DCM = the area of  $\triangle$  EMC

**2** The area of  $\triangle$  DBC = the area of  $\triangle$  EBM



## Lesson 3

## The area of some geometric figures

## Complete each of the following:

١.	The area of rhombus whose perimeter is 20 cm. and height 4 cm. =
۲.	The length of the diagonal of a square of area 50 cm <sup>2</sup> equals cm.
٣.	The length of side of a square whose area equals the area of a rectangle with dimensions 9 cm., 16 cm. =
٤.	The length of the middle base of a trapezium whose area = 30 cm <sup>2</sup> and height 5 cm. equals
٥.	The area of the rhombus = the side length $\times \cdots = \frac{1}{2}$ of the product of
٦.	The area of the square = the square of the length of $\frac{2}{1}$ $\frac{2}{1}$
٧.	The length of the middle base of the trapezium equals
۸.	The area of the trapezium = half of the sum of lengths of the two parallel bases ×
۹.	The base angles of the isosceles trapezium are
١٠.	The diagonals of an isosceles trapezium are

١.	If the area of a square is 50 cm <sup>2</sup> , then the length of its diagonal =					
	(a) 25 cm.	(b) 5 cm.	(c) 10 cm.	(d) 20 cm.		
۲.	If the perimeter	of a rhombus is 24	cm. and its area = 30 cm	n. <sup>2</sup> then its height =		
٠.	(a) 4 cm.	(b) 5 cm.	(c) 6 cm.	(d) 12 cm.		
	If the product of	If the product of the lengths of the diagonals of a rhombus = 96 cm <sup>2</sup> and its height is				
٠.	6 cm., then its	side length = ······	•	•		
	(a) 12 cm.	(b) 8 cm.	(c) 6 cm.	(d) 4 cm.		
	1	If the area of a trapezium is 32 cm <sup>2</sup> and its height is 4 cm., then the length of its middle base =				
	(a) 4 cm.	(b) 8 cm.	(c) 14 cm.	(d) 16 cm.		
۰.	<b>-</b> .	_	of one of its parallel ba	ses is 15 cm., and its area ther base is		
	(a) 15 cm.	(b) 4 cm.	(c) 12 cm.	(d) 27 cm.		
	The trapezium whose middle base length is $x$ cm. and its height = $\frac{1}{2}$ the length of the middle base, its area = cm <sup>2</sup> .					
				height = $\frac{1}{2}$ the length of		
-				height = $\frac{1}{2}$ the length of  (d) $\frac{x^2}{8}$		
	the middle base  (a) $X^2$	(b) $\frac{x^2}{2}$	cm <sup>2</sup>	(d) $\frac{x^2}{8}$		
	the middle base  (a) $x^2$ ind the ar	(b) $\frac{x^2}{2}$	following fig	(d) $\frac{x^2}{8}$		
<b>F</b>	the middle base  (a) $x^2$ ind the ar  A rhombus of significant in the middle base in the area in the	te, its area =	following fig	(d) $\frac{x^2}{8}$ wres:  « 30 cm <sup>2</sup> »		

A trapezium whose middle base length is 7 cm. and its height = 6 cm.

A trapezium whose bases lengths are 8 cm. and 10 cm. and its height = 5 cm. «  $45 \text{ cm}^2$  »

« 42 cm<sup>2</sup> »

A square whose area equals the area of the rectangle whose dimens Find the length of its diagonal.	sions are 2 cm. and 9 cm. « 6 cm. »
Two pieces of land have equal areas, one of them has the si	hape of a rhombus
whose diagonals are 18 m. and 24 m., and the other one has the	e shape of a trapezium
whose height is 12 m. Find the length of its middle base.	« 18 m. »
The area of a trapezium is 180 cm <sup>2</sup> and its height is 12 cm.	Find the lengths of its
parallel bases if the ratio between their lengths is 3:2	« 18 cm. » 12 cm. »
Two land misses are revel in ones, the first is in the shore of a	
Two land pieces are equal in area, the first is in the shape of a in the shape of a rhombus whose diagonals lengths are 8 metres. Find the perimeter of the square-shaped piece.	square and the second is es and 16 metres. « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metres. Find the perimeter of the square-shaped piece.	square and the second is es and 16 metres. « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metres. Find the perimeter of the square-shaped piece.	square and the second is as and 16 metres. « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metres.  Find the perimeter of the square-shaped piece.	square and the second is as and 16 metres. « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metre.  Find the perimeter of the square-shaped piece.  I Find the area of the rhombus whose perimeter is 52 cm. are	square and the second is as and 16 metres.  « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metre.  Find the perimeter of the square-shaped piece.  I Find the area of the rhombus whose perimeter is 52 cm. are	square and the second is as and 16 metres.  « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metre.  Find the perimeter of the square-shaped piece.  I Find the area of the rhombus whose perimeter is 52 cm. are	square and the second is as and 16 metres.  « 32 cm. »
in the shape of a rhombus whose diagonals lengths are 8 metre.  Find the perimeter of the square-shaped piece.  I Find the area of the rhombus whose perimeter is 52 cm. are	square and the second is as and 16 metres.  « 32 cm. »

## Lesson 4 (Similarity)

## Complete each of the following:

- If the measures of the corresponding angles in the two triangles are equal, then the two triangles are ........
- If the ratio between the lengths of two corresponding sides in two similar triangles is equal to 1, then the two triangles are .........
- If two polygons are similar and the ratio between the lengths of two corresponding sides is 3:4, then the ratio between their perimeters is .........
- o. If two polygons are similar, then the corresponding ...... are equal in measure.
- If two polygons are similar, then the corresponding ...... are proportional.
- V. If each of two polygons is similar to a third, then they are .........
- A. The two triangles are similar if the corresponding ...... are proportional.

## Choose the correct answer:

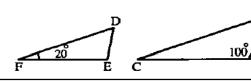
- If the ratio between the lengths of two corresponding sides of two squares is 1 and the perimeter of one of them is 20 cm., then the area of the other square = .........
  - (a)  $20 \text{ cm}^2$
- (b) 25 cm<sup>2</sup>.
- (c)  $16 \text{ cm}^2$
- (d) 25 cm.

## In the opposite figure:

- If  $\triangle$  ABC  $\sim$   $\triangle$  DEF, then m ( $\angle$  A) = ......
- (a) 20°

۲.

- (b) 60°
- (c) 80°
- (d) 100°

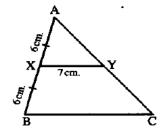


## In the opposite figure:

If 
$$\triangle$$
 ABC  $\sim$   $\triangle$  AXY,

$$AX = XB = 6 \text{ cm}.$$

- XY = 7 cm., then  $BC = \cdots$
- (a) 6 cm.
- (b) 7 cm.
- (c) 12 cm.
- (d) 14 cm.



If  $\triangle$  ABC  $\sim$   $\triangle$  DEF and AB =  $\frac{1}{5}$  DE, then perimeter of  $\triangle$  ABC = ..... perimeter of  $\Delta$  DEF

(a) 5

(a) 1, 2

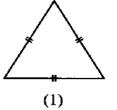
٤.

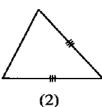
(b) 1

(c)  $\frac{1}{5}$ 

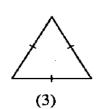
(d)  $\frac{2}{5}$ 

In the following figures, there are two similar triangles, they are ......

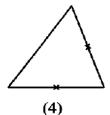




(b) 1,3

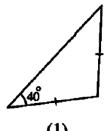


(c) 1,4

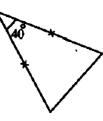


(d) 2, 4

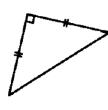
In the following figures, there are two similar triangles, they are .........



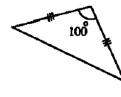
(1)



(2)



(3)



**(4)** 

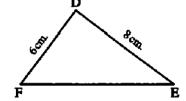
- (a) 1, 2
- (b) 1,3

- (c) 2,4
- (d) 1,4

In the opposite figure:

If  $\triangle$  ABC  $\sim$   $\triangle$  DEF, then EF = ........

- (a) 5 cm.
- (b) 6 cm.
- (c) 8 cm.
- (d) 10 cm.



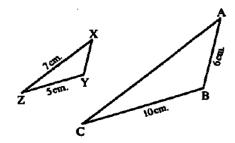
## Essay problems:

In the opposite figure:

 $\triangle$  ABC  $\sim$   $\triangle$  XYZ

Find: AC and XY

« 14 cm. • 3 cm. »



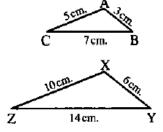
## In the opposite figure:

**1 Prove that :**  $\triangle$  ABC and  $\triangle$  XYZ are similar.

2 If:  $m (\angle B) + m (\angle C) = 60^{\circ}$ ,

find:  $m (\angle X)$ 

« 120°»



3)

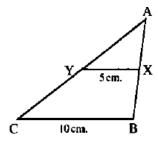
## In the opposite figure:

If  $\triangle AXY \sim \triangle ABC$ 

XY = 5 cm. and BC = 10 cm.,

Prove that :  $1 \overline{XY} / \overline{BC}$ 

 $\mathbf{Z}$  Y is the midpoint of  $\overline{\mathbf{AC}}$ 



4)

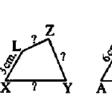
## In the opposite figure:

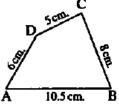
The polygon ABCD ~ the polygon XYZL

If AB = 10.5 cm., BC = 8 cm., CD = 5 cm.

DA = 6 cm. and LX = 3 cm.

Find the length of each of :  $\overline{XY}$ ,  $\overline{YZ}$  and  $\overline{ZL}$ 





« 5.25 cm. • 4 cm. • 2.5 cm. »

5)

## In the opposite figure:

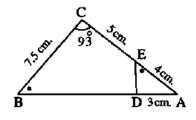
 $\triangle ABC, D \in \overline{AB}, E \in \overline{AC}$ 

AE = 4 cm. EC = 5 cm. BC = 7.5 cm.

, AD = 3 cm., m ( $\angle$  AED) = m ( $\angle$  B) and m ( $\angle$  C) = 93°

**1** Prove that :  $\triangle$  AED  $\sim$   $\triangle$  ABC

**2** Find the length of each of :  $\overline{BD}$  and m ( $\angle ADE$ )



« 9 cm. • 93° »

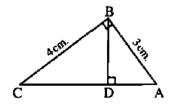
## In the opposite figure :

ABC is a right-angled triangle at B in which:

AB = 3 cm., BC = 4 cm. and  $\overline{BD} \perp \overline{AC}$ 

**1** Prove that :  $\triangle$  BAC  $\sim$   $\triangle$  DAB

**2** Find the length of each of :  $\overline{AD}$  and  $\overline{DC}$ 



« 1.8 cm. • 3.2 cm. »

7)

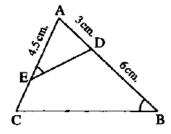
## In the opposite figure :

 $m (\angle AED) = m (\angle B)$ , AD = 3 cm.

AE = 4.5 cm. and BD = 6 cm.

1 Prove that :  $\triangle$  ADE  $\sim$   $\triangle$  ACB

**2** Find the length of :  $\overline{EC}$ 



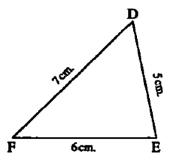
« 1.5 cm. »

## **Lesson 5** (the converse of Pythagorean theorem)

## Complete each of the following:

Complete and show which of the following triangles is a right-angled triangle:

1

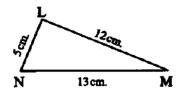


$$(DF)^2 = \cdots$$

$$(DE)^2 + (EF)^2 = \cdots$$

... The triangle is ........

2

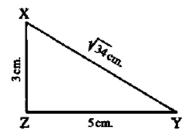


$$(MN)^2 = \cdots$$

$$(ML)^2 + (NL)^2 = \cdots$$

.. The triangle is .....

3

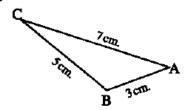


$$(XY)^2 = (\sqrt{34})^2 = \cdots$$

$$(\mathbf{YZ})^2 + (\mathbf{ZX})^2 = \cdots$$

:. The triangle is .....

4



$$(AC)^2 = \cdots$$

$$(AB)^2 + (BC)^2 = \cdots$$

.. The triangle is ......

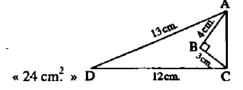
## Essay problems:

## In the opposite figure:

 $m (\angle B) = 90^{\circ}, AB = 4 \text{ cm.}, BC = 3 \text{ cm.}$ 

AD = 13 cm. and DC = 12 cm.

Find: The area of the figure ABCD



## <u>2)</u>

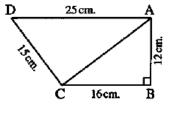
#### In the opposite figure:

ABCD is a quadrilateral in which:  $m (\angle B) = 90^{\circ}$ ,

AB = 12 cm., BC = 16 cm., CD = 15 cm. and DA = 25 cm.

**1** Find: The length of  $\overline{AC}$ 

Prove that:  $m (\angle ACD) = 90^{\circ}$ 



« 20 cm. »

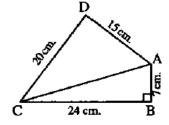
## <u>3)</u>

## In the opposite figure:

ABCD is a quadrilateral in which:  $m (\angle ABC) = 90^{\circ}$ ,

AB = 7 cm., BC = 24 cm., CD = 20 cm. and DA = 15 cm.

**Prove that :**  $m (\angle ADC) = 90^{\circ}$ 



#### 4)

## In the opposite figure :

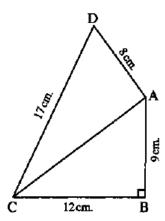
ABCD is a quadrilateral in which:  $m (\angle B) = 90^{\circ}$ ,

AB = 9 cm., BC = 12 cm.,

CD = 17 cm. and DA = 8 cm.

Prove that:  $m (\angle DAC) = 90^{\circ}$ ,

then find: The area of the figure ABCD «114 cm<sup>2</sup>.»



## Lesson 6 (Projection)

## Complete each of the following:

	Example 1			A		
١.	In the opposite	figure :				
	$\triangle$ ABC is right-angled at A and $\overline{AD} \perp \overline{BC}$					
	Complete the following:					
	===	ction of AB on BC is		tion of AC on BC is		
		ction of BC on AC is		tion of BC on AB is		
		ction of $\overline{AC}$ on $\overline{AD}$ is		tion of $\overrightarrow{AD}$ on $\overrightarrow{BC}$ is		
	7 The proje	ction of AB on AD is	•••			
۲.	If X ∈ $\overrightarrow{AB}$ , th	en the projection of X or	AB is			
٣.	If $\overline{AB} \perp \overline{BC}$ ,	then the projection of $\overline{\mathbf{A}}$	on BC is			
٤.	In A ABC, if r	$n(\angle B) = 90^{\circ}$ , then the	projection of C or	1 AB is		
٥.	ABC is a right-angled triangle at A, then the projection of BA on AC is					
$\boldsymbol{C}$	Choose the correct answer:					
C	noose me	correct answer	•			
	T	of a ray on a straight lin		lar to it is ·······		
١.	T			lar to it is (d) a straight line.		
	The projection  (a) a point.  The length of	of a ray on a straight lir	e not perpendicu (c) a ray.	(d) a straight line.		
١.	The projection  (a) a point.  The length of	of a ray on a straight ling (b) a line segment.  the projection of a line segment are segment.	e not perpendicu (c) a ray.	(d) a straight line.		
۲.	The projection (a) a point.  The length of the li (a) ≤  The length of the li	to of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >  the projection of a line segment itself.	(c) ≥	(d) a straight line.		
١.	The projection (a) a point.  The length of the li (a) ≤  The length of the li	of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >	(c) ≥	(d) a straight line.  straight line the  (d) =		
۲.	The projection (a) a point.  The length of the li (a) ≤  The length of	to of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >  the projection of a line segment line segment.  (b) >	c) a ray.  gment on a given  (c) ≥  gment on a straig  (c) =	(d) a straight line.  straight line ······ the  (d) =  ght line parallel to it ······  (d) ≠		
۲.	The projection  (a) a point.  The length of the lingth of the length of	to of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >  the projection of a line segment line segment.  (b) >	(c) ≥  gment on a given  (c) ≥  gment on a straig  (c) =	(d) a straight line.  straight line the  (d) =		
۲.	The projection  (a) a point.  The length of the lingth of the length of	to of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >  the projection of a line segment line segment.  (b) >	c) a ray.  gment on a given  (c) ≥  gment on a straig  (c) =  tent on a straight line segment.	(d) a straight line.  straight line ······ the  (d) =  ght line parallel to it ······  (d) ≠		
۲.	The projection  (a) a point.  The length of the lingth of the length of	to of a ray on a straight line (b) a line segment.  the projection of a line segment itself.  (b) >  the projection of a line segment line segment.  (b) >  the projection of a line segment.  (b) >	c) a ray.  gment on a given  (c) ≥  gment on a straig  (c) =  ent on a straight line segment.  segment.	(d) a straight line.  I straight line the  (d) =  ght line parallel to it  (d) ≠  ine perpendicular to it is		

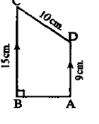
## Essay problems:

## In the opposite figure :

ABCD is a trapezium in which  $\overline{AD}$  //  $\overline{BC}$  and m ( $\angle$  ABC) = 90° If AD = 9 cm., DC = 10 cm. and CB = 15 cm.

#### Find:

- 1 The length of the projection of  $\overline{DC}$  on  $\overline{BC}$
- The length of the projection of  $\overline{DC}$  on  $\overrightarrow{AB}$



«6 cm., 8 cm.»

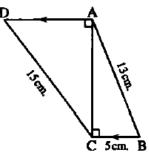
2)

## In the opposite figure :

 $\overrightarrow{AD}$  //  $\overrightarrow{BC}$ ,  $\overrightarrow{AB} = 13$  cm.,  $\overrightarrow{BC} = 5$  cm.,  $\overrightarrow{CD} = 15$  cm. and m ( $\angle ACB$ ) = m ( $\angle DAC$ ) = 90°

#### Find:

- 1 The length of the projection of  $\overline{AB}$  on  $\overline{AC}$
- The length of the projection of  $\overline{CD}$  on  $\overline{AD}$



« 12 cm., 9 cm. »

## **Lesson 7** (Eucledian theorem )

## Complete each of the following:

#### In the opposite figure:

 $\triangle$  ABC is right-angled at A,  $\overline{AD} \perp \overline{BC}$ 

#### Complete each of the following:

$$(AC)^2 = \cdots + \cdots$$

$$(AC)^2 = \cdots \times \cdots$$



4 
$$(AD)^2 = \cdots \times \cdots$$

 $2 \text{ AD} = \cdots \text{ cm}$ .

2)

#### In the opposite figure :

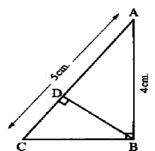
ABC is a triangle in which m ( $\angle$  ABC) = 90°, AB = 4 cm.,

 $AC = 5 \text{ cm. and } \overline{BD} \perp \overline{AC}$ 

#### Complete:

$$\mathbf{BC} = \cdots \cdots \mathbf{cm}$$
.

The area of 
$$\triangle$$
 DBC = ...... cm<sup>2</sup>.



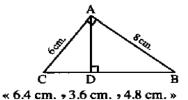
## Essay problems:

#### $\square$ In the opposite figure :

ABC is a triangle in which m ( $\angle$  BAC) = 90°,  $\overline{AD} \perp \overline{BC}$ 

AB = 8 cm. and AC = 6 cm.

Find: BD, CD and AD



4)

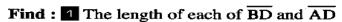
## In the opposite figure :

ABCD is a quadrilateral where

$$m (\angle BCD) = m (\angle BAD) = 90^{\circ}$$
,

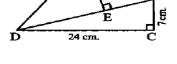
$$\overline{AE} \perp \overline{BD}$$
, BC = 7 cm., CD = 24 cm.

and AB = 15 cm.



The length of the projection of 
$$\overrightarrow{AB}$$
 on  $\overrightarrow{BD}$ 

The length of the projection of 
$$\overrightarrow{AD}$$
 on  $\overrightarrow{AE}$ 



« 25 cm. , 20 cm. , 9 cm. , 12 cm. »

## In the opposite figure:

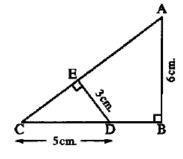
 $\Delta$  ABC is right-angled at B

 $,\overline{DE} \perp \overline{AC}, AB = 6 \text{ cm}.$ 

, ED = 3 cm. and CD = 5 cm.

Prove that :  $\triangle$  CED  $\sim$   $\triangle$  CBA and find : The length of  $\overline{AC}$ 

and the length of the projection of  $\overline{AB}$  on  $\overline{AC}$ 



« 10 cm. • 3.6 cm. »

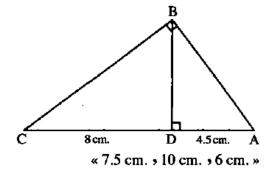
6)

## In the opposite figure:

 $\Delta$  ABC is right-angled at B and  $\overline{BD} \perp \overline{AC}$ 

If AD = 4.5 cm. and DC = 8 cm.,

find: The length of each of  $\overline{AB}$ ,  $\overline{BC}$  and  $\overline{BD}$ 



## Lesson 8 (classifying triangles according to angles)

## Complete each of the following:

١.	In $\triangle$ ABC, if $(AB)^2 = (AC)^2 - (BC)^2$ , then $\angle$ C is
----	--

In 
$$\triangle$$
 ABC, if  $(AC)^2 - (AB)^2 = (BC)^2 - 3$ , then  $\triangle$  B is ......

In 
$$\triangle$$
 ABC, if  $(AB)^2 + (BC)^2 = 48$  cm<sup>2</sup>, AC = 7 cm., then  $\angle$  B is ......

i. In 
$$\triangle XYZ$$
, if  $90^{\circ} < m (\angle Y) < 180^{\circ}$ , then  $(XZ)^2 \cdots (XY)^2 + (YZ)^2$ 

•. If 
$$\angle$$
 A complements  $\angle$  B in  $\triangle$  ABC, then  $(AB)^2 \cdots (AC)^2 + (BC)^2$ 

- If the two lengths of two sides in a triangle are 3 cm. and 5 cm, then the length of the third side is between ........
- ABC is a triangle whose sides lengths are 6 cm., 8 cm. and 11 cm.

  Δ ABC is similar to the triangle XYZ, then Δ XYZ is ..... according to its angles.

## Choose the correct answer:

`	Atriangle whose side lengths are: 5 cm, 12 cm and 13 cm. its area = cm?					
١.	(a) 30	(b) 32.5	(c) 78	(d) 60		
ABC is an obtuse-angled triangle at A, if AB = 4 cm., BC = 7 cm., then A be equals cm.						
	(a) 5	(b) 6	(c) 7	(d) 8		

- ABC is a triangle in which:  $(BC)^2 = (AB)^2 + (AC)^2$ ,  $m (\angle B) = 40^\circ$ , then  $m (\angle C) = \cdots$ 
  - (a) 40° (b) 50°
- (c) 90°
- (d) 140°

ABC is an obtuse-angled triangle at B if AB = 5 cm., BC = 3 cm., then AC can be equals ......... cm.

- (a) 4
- (b) 5

- (c) 7
- (d) 8

ABC is an acute-angled triangle in which AB = 6 cm. , BC = 8 cm. , then the length of  $\overline{AC}$  can be equals ...... cm.

- (a) 2
- (b) 6

- (c) 10
- (d) 14

## Essay problems:

Identify the type of  $\angle$  A in  $\triangle$  ABC if AB = 6 cm., BC = 10 cm. and AC = 8 cm.

7)

Identify the type of  $\angle$  B in  $\triangle$  ABC if AB = 10 cm.  $\Rightarrow$  BC = 12 cm. and AC = 15 cm.

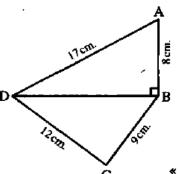
8)

## In the opposite figure:

ABCD is a quadrilateral in which AB = 8 cm., BC = 9 cm., CD = 12 cm., AD = 17 cm.

and  $\overline{DB} \perp \overline{AB}$ 

- 1 Find the length of the projection of  $\overline{AD}$  on  $\overline{BD}$
- 2 Determine the type of  $\triangle$  BCD according to its angles.



« 15 cm. »

9)

Identify the type of  $\angle Y$  in  $\triangle XYZ$  if XY = 4 cm.  $\Rightarrow YZ = 5$  cm. and XZ = 7 cm.

10)

## 

ABCD is a parallelogram in which

BC = 15 cm., CD = 8 cm. and AC = 19 cm.

**Prove that**:  $\angle$  ABC is an obtuse angle.

