

Expanding the VOQC Toolkit

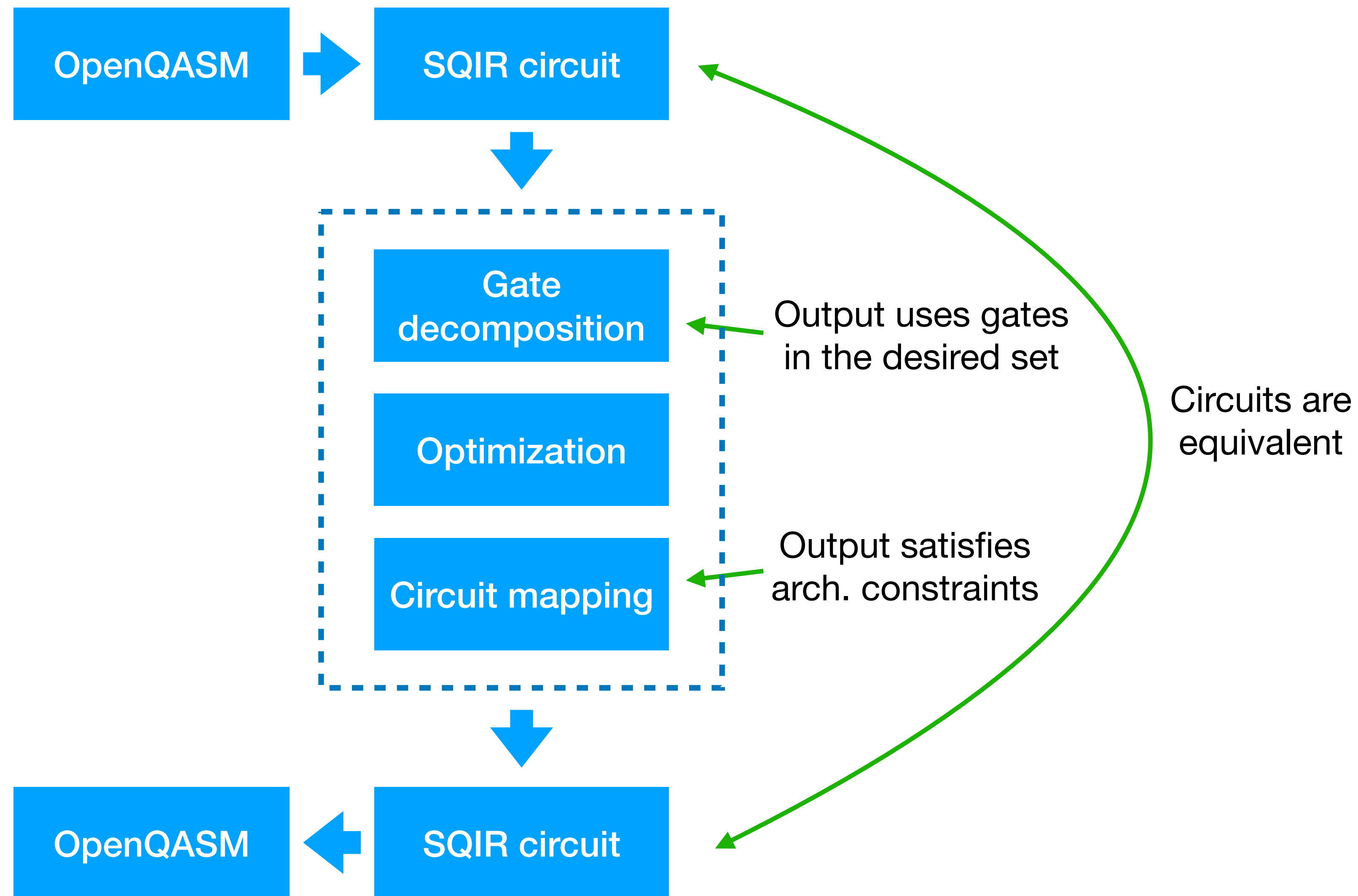
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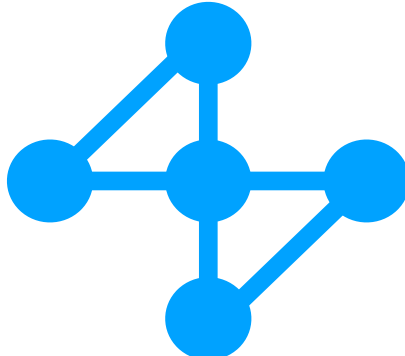

VOQC: Verified Optimizer for Quantum Circuits

- An optimizer for quantum circuits *formally verified* in the Coq proof assistant
 - Optimizations are proved to be *semantics preserving*, i.e., they do not change the “meaning” of the input circuit
- Circuits expressed in SQIR, a Simple Quantum Intermediate Representation
- VOQC and SQIR were presented in a distinguished paper at [POPL 2021](#)
- Followup paper to appear at [ITP 2021](#) shows how to use SQIR as a source language for verifying quantum algorithms (e.g. Grover’s, QPE)

VOQC: **V**erified **O**ptimizer for **Q**uantum **C**ircuits



In This Talk

- New gate sets and optimizations 
- Better support for circuit mapping 
- Interoperability (via Python) 

“IBM” Gate Set

- Consists of the gates {U1, U2, U3, CX}
- U1, U2, U3 are parameterized by real rotation angles

$$U_1(\lambda) = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\lambda} \end{pmatrix}, \quad U_2(\phi, \lambda) = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & -e^{i\lambda} \\ e^{i\phi} & e^{i(\phi+\lambda)} \end{pmatrix}, \quad U_3(\theta, \phi, \lambda) = \begin{pmatrix} \cos(\theta/2) & -e^{i\lambda} \sin(\theta/2) \\ e^{i\phi} \sin(\theta/2) & e^{i(\phi+\lambda)} \cos(\theta/2) \end{pmatrix}$$

Qiskit's Optimize1qGates

- Finds adjacent single-qubit gates (U1, U2, U3) and combines them

- E.g. merging U1, U2

$$U_1(\lambda_1); U_1(\lambda_2) \rightarrow U_1(\lambda_1 + \lambda_2)$$

$$U_1(\lambda_1); U_2(\phi, \lambda_2) \rightarrow U_2(\lambda_2, \lambda_1 + \phi)$$

- More complicated: merging U3

$$\begin{aligned}
 U_3(\theta_1, \phi_1, \lambda_1); U_3(\theta_2, \phi_2, \lambda_2) &= R_z(\phi_2) \cdot R_y(\theta_2) \cdot R_z(\lambda_2) \cdot R_z(\phi_1) \cdot R_y(\theta_1) \cdot R_z(\lambda_1) \\
 &= R_z(\phi_2) \cdot [R_y(\theta_2) \cdot R_z(\lambda_2 + \phi_1) \cdot R_y(\theta_1)] \cdot R_z(\lambda_1) \\
 &= R_z(\phi_2) \cdot \underline{[R_z(\gamma) \cdot R_y(\beta) \cdot R_z(\alpha)]} \cdot R_z(\lambda_1) \\
 &= R_z(\phi_2 + \gamma) \cdot R_y(\beta) \cdot R_z(\alpha + \lambda_1) \\
 &= U_3(\beta, \phi_2 + \gamma, \alpha + \lambda_1)
 \end{aligned}$$

Note:

$$U_3(\theta, \phi, \lambda) = R_z(\phi) \cdot R_y(\theta) \cdot R_z(\lambda)$$

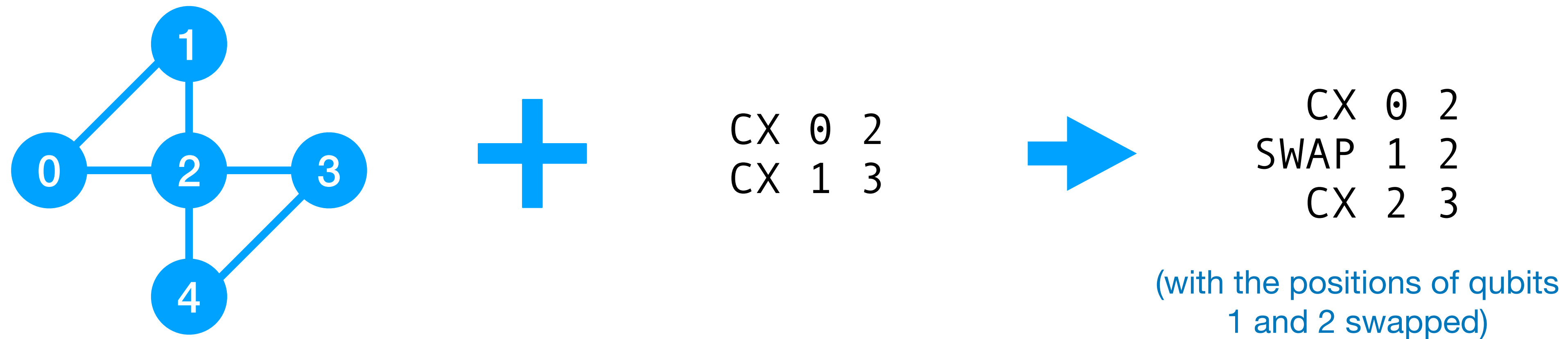
for rotations R_y, R_z

The hard part is $zyz \rightarrow yzy$ conversion

Summary of Features

- Gate sets
 - “RzQ” {X, H, Rz, CX}
 - “IBM” {U1, U2, U3, CX}
 - “Full” {I, X, Y, Z, ..., CX, CZ, SWAP, CCX, CCZ}
- Optimizations
 - Five passes from [Nam et al. \[2018\]](#) (evaluated in our POPL paper)
 - [Optimize1qGates](#) and [CXCancellation](#) from Qiskit
- Simple circuit mapping

Circuit Mapping



- We want this transformation to...
 - Be *semantics-preserving* (the two programs should be denoted by the same matrix, up to a permutation of qubits)
 - Produce an output that satisfies the architecture's constraints

Composing VOQC Transformations

- Coq program to optimize a circuit and then map it to a 10-qubit LNN architecture (OCaml syntax is similar)

```
Definition optimize_then_map c :=  
  let gr := make_lnn 10 in      (* 10-qubit LNN architecture *)  
  let la := trivial_layout 10 in (* trivial layout on 10 qubits *)  
  if check_well_typed c 10      (* check that c is well-typed & uses ≤10 qubits *)  
  then  
    let c' := optimize_nam c in  (* optimization #1 *)  
    let c'' := optimize_ibm c' in (* optimization #2 *)  
    Some (simple_map c'' la gr)   (* map *)  
  else None.
```

Composing VOQC Transformations

- Coq program to map a circuit to a 10-qubit LNN architecture and then perform optimization (OCaml syntax is similar)

```
Definition map_then_optimize c :=  
  let gr := make_lnn 10 in          (* 10-qubit LNN architecture *)  
  let la := trivial_layout 10 in    (* trivial layout on 10 qubits *)  
  if check_well_typed c 10          (* check that c is well-typed & uses ≤10 qubits *)  
  then  
    let (c', la') := simple_map c la gr in (* map *)  
    let c'' := optimize_nam c' in          (* optimization #1 *)  
    Some (optimize_ibm c'', la')          (* optimization #2 *)  
  else None.
```

- To support optimization after mapping, we prove that all optimizations are *mapping preserving*

(Light) Evaluation

- Is it better to optimize or map first?
- We mapped 26 arithmetic circuits to a 6x6 2D grid architecture (= 36 qubits) and compared the gate count reduction due to optimizing before vs. after

Optimize -> Map	Map -> Optimize	Optimize -> Map -> Optimize
10.4%	8.6%	10.9%

- A verified optimizer allows us to combine different transformations without worrying about correctness
- *In our POPL paper*: evaluation on a larger set of benchmarks; comparison with PyZX, Qiskit, and tket

pyvoqc

- We want to make VOQC a drop-in replacement for circuit optimizers used in frameworks like Qiskit, pytket, pyQuil, Cirq (all written in [Python](#))
- So we added Python bindings for VOQC optimizations



pyvoqc

```
from qiskit import QuantumCircuit
from pyvoqc.qiskit.voqc_pass import QiskitVOQC
from qiskit.transpiler import PassManager

# create a circuit using Qiskit's interface
circ = QuantumCircuit(2)
circ.x(0)
circ.t(0)
circ.t(1)
circ.cz(0, 1)
circ.t(0)
circ.tdg(1)
print("Before Optimization:")
print(circ)

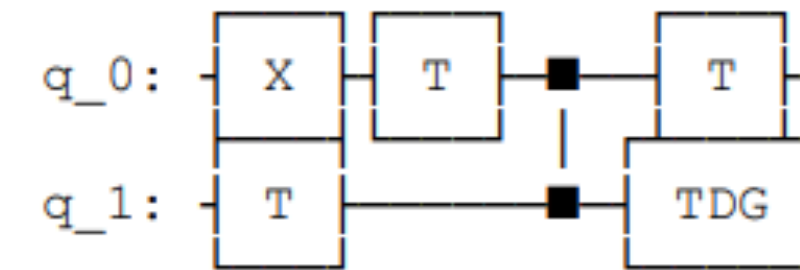
# create a Qiskit PassManager
pm = PassManager()

# decompose CZ gate
pm.append(QiskitVOQC(["decompose_to_cnot"]))
new_circ = pm.run(circ)
print("\n\nAfter 'decompose_to_cnot':")
print(new_circ)

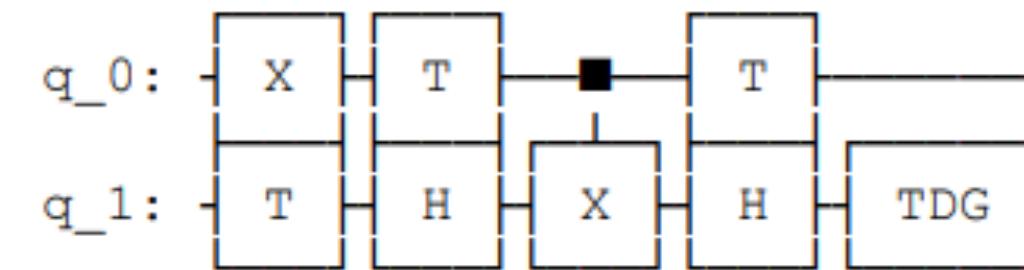
# run optimizations from Nam et al.
pm.append(QiskitVOQC(["optimize_nam", "replace_rzq"]))
new_circ = pm.run(circ)
print("\n\nAfter 'optimize_nam':")
print(new_circ)

# run IBM gate merging
pm.append(QiskitVOQC(["optimize_ibm"]))
new_circ = pm.run(circ)
print("\n\nAfter 'optimize_ibm':")
print(new_circ)
```

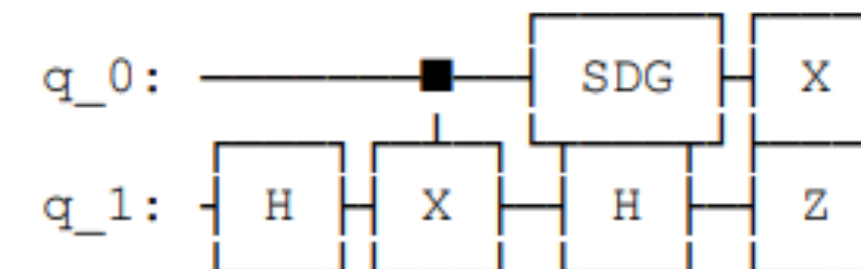
Before Optimization:



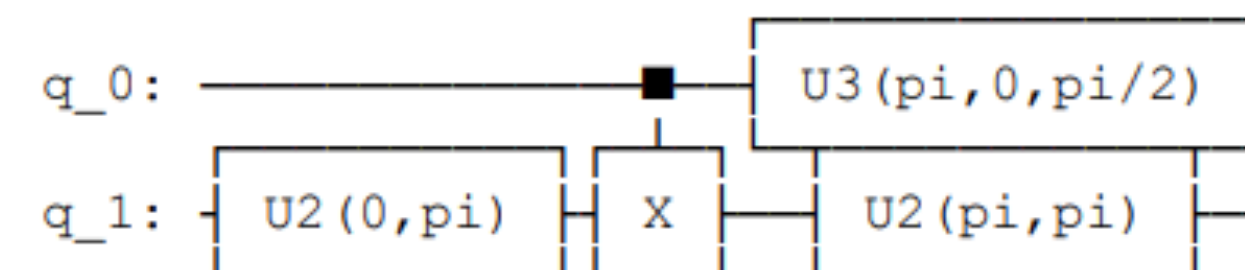
After 'decompose_to_cnot':



After 'optimize_nam':



After 'optimize_ibm':



Ongoing Work

- More thorough evaluation of VOQC (e.g. using [Arline's benchmarks](#))
- New optimizations, especially approximate
- More sophisticated mapping & mapping-aware optimizations
- *In progress*: Compilation from classical (reversible) programs to SQIR circuits

Resources

- Our Coq definitions and proofs are available at github.com/inQWIRE/SQIR.
- Our OCaml library is available at github.com/inQWIRE/mlvoqc and can be installed with “opam install voqc”.
 - Documentation on the OCaml library interface is available at <https://inqwire.github.io/mlvoqc/voqc/Voqc/index.html>.
- Our Python bindings and a tutorial are available at github.com/inQWIRE/pyvoqc.
- ***We welcome contributions!*** Feel free to file issues or pull requests.