## Computer Science 3MI3 – 2020 assignment 3

A representation of Dijkstra's guarded command language

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#### Contents

#### Introduction

This assignment tasks you with representing Dijkstra's "guarded command language" in Ruby and Clojure, and defining various semantics for it.

### Updates and file history

#### December 17th

- An additional problem with the testing was discovered. In the test for part 4 named test\_two\_possible\_assignments\_part2, the test checked if that value 0 could be assigned to variable: y. This should not be; this test and the preceding on should check if 1 and 2 can be assigned to: y.
- A definition for a record type called Config was added to part 3 (the Clojure part.) This is the record used as input and output for the reduce function in the testing (I mistakenly did not add mention of it here earlier.)

#### December 16th

Some corrections have been made to the assignment description, and unfortunately to some of the test cases.

In decreasing order of severity:

- The test cases in the Ruby portions for the "oscillating" statement/program did not correctly add the initial assignment to the variable to the program, and so will fail (the do will never run, because :x is assigned 0 by default which is outside the range for the oscillation, but :x can never become 2 or 8.)
- The Ruby part 4 test which checks the scoping of the program "global; local x in x := x should be well scoped." previously had a typo in the test itself, with the variable on the right of the assignment being a y. This has been corrected.
- Previously, it was stated that the eval method in part 4 was to operate on GCStmt's. However, it should instead operate on GCProgram's, that is, statements with global variable lists.
- Previously, GCAnd and GCOr were incorrectly stated to operate on GCExpr's. They are now correctly stated to operate on GCTest's.
- The broken link to the Ruby testing at the top of that section has been replaced with the links to the two Ruby test files.

#### December 11th

- The testing and Docker setup has been added.
- The method from part 2 has been renamed to stackEval, instead of stack\_eval.
- Mark amounts were added to each part.
- Some minor clarifying statements have been added to parts 2, 3 and 4. They are prepended by "(Added December 11th.)"

#### December 1st

• Initial version posted.

## Boilerplate

#### Documentation

In addition to the code for the assignments, you are required to submit (relatively light) documentation, along the lines of that found in the literate programs from lectures and tutorials.

• Those occasionally include a lot of writing when introducing concepts; you do not have to introduce concepts, so your documentation should be similar to the *end* of those documents, where only the purpose and implementation details of types, functions, etc., are discussed.

This documentation is not assigned its own marks; rather, 20% of the marks of each part of the assignment will be for the documentation.

This documentation **must be** in the literate style, with (nicely typeset) English paragraphs alongside code snippets; comments in your source code do not count. The basic requirement is

- the English paragraphs must use non-fixed width font, whereas
- the code snippets must use fixed width font.
- For example, see these lecture notes on Prolog:
  - https://courses.cs.washington.edu/courses/cse341/98sp/ logic/prolog.html

But you are encouraged to strive for nicer than just "the basic requirement". (the ability to write decent looking documentation is an asset!

You are free to present your documentation in any of these formats:

- an HTML file,
  - (named README.html)
- a PDF (for instance, by writing it in LATEX using the listings or minted package for your code blocks),
  - (named README.pdf), or
- rendering on GitLab (for instance, by writing it in markdown or Org)
  - (named README.md or README.org.)

If you wish to use another format, contact Mark to discuss it.

Not all of your code needs to be shown; only portions which are of interest are needed. Feel free to omit some "repetitive" portions. (For instance, if there are several cases in a definition which look almost identical, only one or two need to be shown.)

#### Submission procedures

The same guidelines as for homework (which can be seen in any of the homework files) apply to assignments, except for the differences below.

#### Assignment naming requirements

Place all files for the assignment inside a folder titled an, where n is the number of the assignment. So, for assignment 1, use the folder a1, for assignment 2 the folder a2, etc. Ensure you do not capitalise the a.

Each part of the assignments will direct you on where to save your code for that part. Follow those instructions!

If the language supports multiple different file extensions, you must still follow the extension conventions noted in the assignment.

Incorrect naming of files may result in up to a 5% deduction in your grade.

This is slightly decreased from the 10% for homeworks.

#### Proper conduct for coursework

Refer to the homework code of conduct available in any of the homework files. The same guidelines apply to assignments.

## Part 0 – The guarded command language, GCL

This assignment involves representing a simple kind of *guarded command language*, which we call *GCL*, and a small extension to it which we call *GCLe*, which adds a notion of scope.

#### GCL

The syntax of GCL is given as

```
| 'true' | 'false'
```

That is, the language consists of

- (integer) expressions built from integer constants, variable names, and the binary operations addition, multiplication, subtraction and division.
- (boolean) tests built from equality and inequality checks on expressions, along with and and or.
- statements, which may be
  - skip, the empty statement that does nothing,
  - assignment of an expression to a variable,
  - the composition of two statements,
  - the "choice" construct if applied to a list of guarded commands,
  - the "iteration" construct do applied to a list of guarded commands,
- and guarded command lists, which are a sequence of zero or more guarded commands,
  - where a guarded command consists of a (boolean) test and a statement.

For this language, we use the same notion of (memory) state as in the beginning of the notes on the *WHILE* language: a map or function from variable names to integers. We assume for this language that variables are always initialised to 0.

The semantics of the expressions, tests and the skip, assignment and composition statements are intended to be similar to those of WHILE as described in lecture.

The semantics of the if and do constructs on guarded command lists are as noted in homework 9, which discussed the guarded command. One important note: in both cases, if the guarded command list is empty, the result should be to "do nothing".

#### GCLe

The language GCLe is obtained from GCL by adding these productions to grammer.

```
\langle program \rangle ::= \langle globals \rangle \langle stmt \rangle
\langle globals \rangle ::= 'global' \{ variable \}
\langle stmt \rangle ::= 'local' variable 'in' \langle stmt \rangle
```

The intent is that a *program* now consists of a list of global variables followed by a statement, which we may call the "body" of the program.

Additionally, we add a new kind of statement for declaring local variables.

With these constructs in place, we may now discuss whether a given program is *well-scoped*; that is, if every variable used in the program is either

- a global variable, or
- a local variable declared by some wrapping local statement.

We will assume in the semantics that all programs are well-scoped, and we can make use of a more precise notion of memory state; a memory state is some mapping from *variables which are in scope* to values. Variables which are not in scope are not handled by such a memory state.

## Part 1 – Representations of GCL and a small extension [10 marks]

In Ruby and in Clojure, create a representation of the language GCL described in part 0.

In Ruby, define the types GCExpr, GCTest and GCStmt, with the following subclasses.

#### • GCExpr has subclasses

- GCConst, the constructor of which takes a single integer argument,
- GCVar, the constructor of which takes a symbol for the variable name,
- GCOp, the constructor of which has as its first two arguments are
   GCExpr's and as its third argument a symbol, which is intended to be one of :plus, :times, :minus or :div.

#### • GCTest has subclasses

- GCComp, the constructor of which has as its first two arguments
   GCExpr's and as its third argument a symbol, which is intended to be one of :eq, :less or :greater,
- GCAnd and GCOr, the constructors of which take as arguments two GCExpr's two GCTest's (corrected December 16th.)
- GCTrue and GCFalse, the constructor of which (if it exists) takes no arguments.

#### • GCStmt has subclasses

- GCSkip, the constructor of which (if it exists) takes no arguments.
- GCAssign, the constructor of which takes as arguments a symbol for the variable name and a GCExpr.
- GCCompose, the constructor of which takes two GCStmt's as arguments.
- GCIf and GCDo, the constructors of which take a list of GCTest and GCStmt pairs (pairs being lists of two elements.)

Wrap all of these definitions inside a module named GCL. (This is to avoid name clashes with definitions requested below.)

In Clojure, define *records* (documentation and examples here) for each kind of expression, test and statement (using the same naming as in Ruby.) There is no need to define the GCExpr, GCTest and GCStmt types themselves; only the subtypes as records.

Then, in Ruby, create a separate representation of the language GCLe described in part 0. Create a class GCProgram to represent programs, the

constructor of which takes as its first argument a list of symbols for the global variable names, and as its second argument a GCStmt. Also add an additional subclass to GCStmt, GCLocal, the constructor of which takes as its first argument a symbol for the variable name and as its second argument a GCStmt. Wrap all of these definitions inside a module named GCLe.

### Part 2 – A stack machine for GCL in Ruby [25 marks]

Within the GCL module, define a method stackEval on GCL's, which carries out the evaluation of a GCStmt using a stack machine.

The stack machine in question should really be a method taking three arguments:

- 1. the command stack (implemented using a list),
- 2. the results stack (implemented a list), and
- 3. the memory state (implemented using a lambda; that is, a block.)

The method should return an updated state (that is, another lambda/block.) (Added December 11th.) As part of the GCL module, also define a method emptyState which takes no arguments and

- which returns a lambda for the empty memory state function
  - (that is, a lambda that maps all arguments to 0),

and a method updateState which takes 3 arguments;

- a lambda (for the previous memory state),
- a variable name (i.e., a symbol), and
- an integer.

Then updateState(sigma,x,n) returns a lambda which maps x to n, and any other variable to the same value as the lambda sigma. (Technically, only the emptyState method is required to be as described for the testing. But a method similar to updateState will be necessary in your stackEval method.)

# Part 3 – The small-step semantics of GCL in Clojure [25 marks]

Define in Clojure a function reduce which takes a *GCL* statement and a memory state (a function mapping symbols, representing the variable names, to integers) and performs *one step* of the computation, returning the remaining code to be run and the updated memory state.

(Added December 11th.) Also define functions emptyState and updateState for use with your reduce function. These should behave equivalently to the methods of the same name described in part 2 (returning anonymous functions.) (Once again, only the emptyState method is needed during testing.)

(Added December 17th.) The testing code makes use of a record called Config for the argument (and return type) of the reduce function. This record type was mistakenly not shared with you previously. Here is a definition for it.

#### (defrecord Config [stmt sig])

For your code to be compatible with the tests, you should use this record type as both the input and output for reduce.

Note that the reduce function was always stated to return both the remaining code to be run and the updated memory state. Bundling these two return values is the purpose of this record, and since it exists, it may as well be used as the argument type as well.

# Part 4 – The big-step semantics of GCLe in Ruby [40 marks]

This portion of the assignment should be done in the GCLe module created in part 1.

Begin by defining a method wellScoped [20 marks] which checks that all variables appearing within the body of a GCProgram (either in an expression or on the left side of an assignment) are within scope at the point of their use; that is, either the variable is one declared to be global, or there is a local statement for that variable wrapping the use.

• This method should take a GCStmt as its only argument should take a GCProgram as its only argument, and return a boolean (Corrected December 16th.)

- Hint: This operation is similar to typechecking. Use your experience working with typeOf as a starting point.
  - Helper methods are always permitted.

Then define the semantics of the language, this time defining a method eval [20 marks] directly (without making use of a stack machine.) That is, define the *big-step* semantics of the language (remember that big-step semantics are called evaluation semantics.)

• This method also should take a GCStmt as its only argument. It should return a Hash mapping the global variable names to integers.

You may decide what the behaviour is for programs which do not initialise variables before their first use.

- Your choice may be judged in the marking.
  - It is suggested that such programs "fail gracefully", reporting an error that a variable was used before initialisation.
  - Otherwise, it's suggested that they behave as predictably as possible.

(Added December 11th.) Because the eval method does not require a "state" argument, in this part the tests do not rely upon the emptyState method (or the updateState method.) But you will still need to define similar methods.

## Part 5 – GCLe in Clojure

As a bonus, repeat part 4 in Clojure.

Place the code for this portion in a file a3b.clj.

This time, you may choose the underlying approach to the operational semantics (you do not have to use big-step semantics.)

Document this portion especially well, and include your own tests in a file a3bt.clj. This file should output the results of the tests when executed using cat a3bt.clj | lein from the command line.

#### Submission checklist

For your convenience, this checklist is provided to track the files you need to submit. Use it if you wish.

```
- [ ] Documentation; one of
  - [ ] README.html
 - [ ] README.pdf
 - [ ] README.md
  - [ ] README.org
- [ ] Code files
  - [] a3.rb
  - [] a3.clj
- [] Part 2 tests
  - [ ] a3p2_test.rb tests have passed! (No submission
  → needed.)
- [] Part 3 tests
  - [ ] a3_test.clj tests have passed! (No submission needed.)
- [] Part 4 tests
  - [ ] a3p4_test.rb tests have passed! (No submission
  → needed.)
- [ ] Part 5 (Bonus)
  - [ ] a3b.clj
 - [ ] a3bt.clj
```

### Testing

Unit tests for the requested types, methods and predicates are available here.

```
• a3p2_test.rb
```

- a3p4\_test.rb
- a3\_test.clj

The contents of the unit test files are also repeated below.

The tests can be run by placing the test files in the same directory as your code files.

To run the tests for the Ruby portions, us the commands

```
ruby a3_test.rb
```

To run the tests for the Clojure portions, us the commands

```
cat a3_test.clj | lein repl
```

## You are strongly encouraged to add your own additional test cases to those provided for you.

The provided test cases check a very minimal amount!

#### Automated testing via Docker

The Docker setup and usage scripts are available at the following links. Their contents are also repeated below.

- Dockerfile
- docker-compose.yml
- setup.sh
- run.sh

Place them into your a3 directory where your code files and the test files (linked to above) exist, then run setup.sh and run.sh.

Note that the use of the setup.sh and run.sh scripts assumes that you are in a bash like shell; if you are on Windows, and not using WSL or WSL2, you may have to run the commands contained in those scripts manually.

#### The tests

#### Ruby

```
def test_two_possible_assignments_part1
  constant_one = GCConst.new(1)
  constant two = GCConst.new(2)
  assign_constant_one = GCAssign.new(:y, constant_one)
  assign constant two = GCAssign.new(:y, constant two)
  branch = GCIf.new([[GCTrue.new, assign_constant_one],
                      [GCTrue.new, assign constant two]])
  # Run the program 50 times, to make relatively sure
  # both possible results (y = 1 \text{ and } y = 2) are seen.
  results = []
  50.times do results.push(GCL::stackEval([branch], [],

→ emptyState).call(:y)) end

  assert_equal(true,results.include?(1), "An if statement

→ which randomly assigns 1 or 2 never assigned 1.")
end
def test_two_possible_assignments_part2
  constant one = GCConst.new(1)
  constant_two = GCConst.new(2)
  assign constant one = GCAssign.new(:y, constant one)
  assign_constant_two = GCAssign.new(:y, constant_two)
  branch = GCIf.new([[GCTrue.new, assign_constant_one],
                      [GCTrue.new, assign_constant_two]])
  # Run the program 50 times, to make relatively sure
  # both possible results (y = 1 \text{ and } y = 2) are seen.
  results = []
  50.times do results.push(GCL::stackEval([branch], [],

→ emptyState).call(:y)) end

  assert_equal(true,results.include?(2), "An if statement

→ which randomly assigns 1 or 2 never assigned 2.")
end
def test_oscillating
 x_var = GCVar.new(:x)
  assign_x_5 = GCAssign.new(:x,GCConst.new(5))
```

```
inc_x_1 =
     GCAssign.new(:x,GCOp.new(x_var,GCConst.new(1),:plus))
     GCAssign.new(:x,GCOp.new(x_var,GCConst.new(1),:minus))
    check_x_less_8
                      = GCComp.new(x_var,GCConst.new(8),:less)
    check_x_greater_2 =
     GCComp.new(x_var,GCConst.new(2),:greater)
    check x within 37 =
     GCAnd.new(check_x_greater_2,check_x_less_8)
    # A program to increment or decrement the value of
     \hookrightarrow variable x
    # randomly until it is less than 3 or greater than 7,
    oscillate_x = GCDo.new([[check_x_within_3_7, dec_x_1],
                             [check_x_within_3_7, inc_x_1]])
    assign_then_oscillate = GCCompose.new(assign_x_5,

    oscillate_x)

    # Run the program 50 times, to make relatively sure
    # both possible results (x = 2 \text{ and } x = 8) are seen.
    results = []
    50.times do

¬ results.push(GCL::stackEval([assign_then_oscillate],
     assert_equal(true,results.include?(2), "A do statement
     \hookrightarrow which oscillates the value of x between 2 and 8 never
     \hookrightarrow got to 2.")
    assert_equal(true,results.include?(8), "A do statement
     \hookrightarrow which oscillates the value of x between 2 and 8 never

→ got to 8.")

  end
   a3p4_test.rb
require "test/unit"
require_relative "a3"
include GCLe
```

end

```
class SimpleTests < Test::Unit::TestCase</pre>
 def test_wellscoped1
   assert_equal(true, GCLe::wellScoped(GCProgram.new([:x,:y],
    GCAssign.new(:x, GCVar.new(:x)))),
                 "global x y; x := x should be well scoped.")
 end
 def test_wellscoped2
   assert_equal(true, GCLe::wellScoped(GCProgram.new([:x,:y],
    GCAssign.new(:x, GCVar.new(:y)))),
                 "global x y; x := y should be well scoped.")
 end
 def test_wellscoped3
   assert_equal(true, GCLe::wellScoped(GCProgram.new([],

GCLocal.new(:x, GCAssign.new(:x, GCVar.new(:x))))),
                 "global; local x in x := x should be well

→ scoped. TEST UPDATED DEC16.")

 end
 def test_not_wellscoped1
   assert_equal(false, GCLe::wellScoped(GCProgram.new([:y],
    GCAssign.new(:x, GCVar.new(:x)))),
                 "global y; x := x should NOT be well

    scoped.")

 end
 def test_not_wellscoped2
   assert_equal(false, GCLe::wellScoped(GCProgram.new([:x],
    GCAssign.new(:x, GCVar.new(:y)))),
                 "global x; x := y should NOT be well
                 ⇔ scoped.")
 end
 def test_not_wellscoped3
   assert_equal(false, GCLe::wellScoped(GCProgram.new([],
    GCLocal.new(:y, GCAssign.new(:x, GCVar.new(:y))))),
```

```
"global; local y in x := y should NOT be well

→ scoped. DESCRIPTION UPDATED DEC16.")

end
def test_assign_zero
  constant one = GCConst.new(1)
  assign_constant_one = GCAssign.new(:z, constant_one)
  updated state =
  GCLe::eval(GCProgram.new([:z],assign_constant_one))
  assert_equal(1, updated_state[:z], "Assigning 1 to z did
  → not work.")
end
def test_two_possible_assignments_part1
  constant_one = GCConst.new(1)
  constant_two = GCConst.new(2)
  assign_constant_one = GCAssign.new(:t, constant_one)
  assign_constant_two = GCAssign.new(:t, constant_two)
 branch = GCIf.new([[GCTrue.new, assign_constant_one],
                     [GCTrue.new, assign constant two]])
  assign_t_to_y = GCAssign.new(:y, GCVar.new(:t))
  the program =
  GCProgram.new([:y],GCLocal.new(:t,GCCompose.new(branch,

¬ assign_t_to_y)))
  # Run the program 50 times, to make relatively sure
  # both possible results (y = 1 \text{ and } y = 2) are seen.
  results = []
  50.times do results.push(GCLe::eval(the_program)[:y]) end
  assert_equal(true,results.include?(1), "An if statement

→ which randomly assigns 1 or 2 never assigned 1.")
end
def test two possible assignments part2
  constant one = GCConst.new(1)
  constant_two = GCConst.new(2)
  assign_constant_one = GCAssign.new(:t, constant_one)
  assign_constant_two = GCAssign.new(:t, constant_two)
```

```
branch = GCIf.new([[GCTrue.new, assign_constant_one],
                     [GCTrue.new, assign_constant_two]])
  assign_t_to_y = GCAssign.new(:y, GCVar.new(:t))
  the_program =
  GCProgram.new([:y],GCLocal.new(:t,GCCompose.new(branch,

¬ assign_t_to_y)))
  # Run the program 50 times, to make relatively sure
  # both possible results (y = 1 \text{ and } y = 2) are seen.
  results = []
  50.times do results.push(GCLe::eval(the_program)[:y]) end
  assert_equal(true,results.include?(2), "An if statement

→ which randomly assigns 1 or 2 never assigned 2.")

end
def test_oscillating
 x_var = GCVar.new(:x)
  assign_x_5 = GCAssign.new(:x,GCConst.new(5))
  inc_x_1 =
  GCAssign.new(:x,GCOp.new(x_var,GCConst.new(1),:plus))
  dec x 1 =
  GCAssign.new(:x,GCOp.new(x var,GCConst.new(1),:minus))
  check_x_less_8
                    = GCComp.new(x_var,GCConst.new(8),:less)
  check_x_greater_2 =
  GCComp.new(x_var,GCConst.new(2),:greater)
  check_x_within_3_7 =
  GCAnd.new(check_x_greater_2,check_x_less_8)
  # A program to increment or decrement the value of
  \rightarrow variable x
  # randomly until it is less than 3 or greater than 7,
  oscillate_x = GCDo.new([[check_x_within_3_7, dec_x_1],
                          [check_x_within_3_7, inc_x_1]])
  assign_then_oscillate = GCCompose.new(assign_x_5,

→ oscillate_x)
  the_program = GCProgram.new([:x],assign_then_oscillate)
```

```
# Run the program 50 times, to make relatively sure
    # both possible results (x = 2 \text{ and } x = 8) are seen.
    results = []
    50.times do results.push(GCLe::eval(the_program)[:x]) end
    assert_equal(true,results.include?(2), "A do statement
     \hookrightarrow which oscillates the value of x between 2 and 8 never
     \hookrightarrow got to 2.")
    assert_equal(true,results.include?(8), "A do statement
     \hookrightarrow which oscillates the value of x between 2 and 8 never
     \hookrightarrow got to 8.")
  end
end
Clojure
a3_test.clj
(ns testing)
(use 'clojure.test)
(load-file "a3.clj")
;; A function to compute a given expression a number of times,
;; creating a list of the results.
;; Used to test the non-determinacy of GC programs involvings
\rightarrow ifs and dos.
(defn times [n f]
  "Repeatedly evaluate `f` `n` times and concatenate together

    → the results."

  (concat
   (repeatedly n #(eval f))))
(deftest test-state-assign-constant-one
                   ((.sig (reduce (Config. (GCAssign. :x
  (is (= 1
   GCConst. 1)) emptyState))) :x))))
(deftest test-stmt-assign-constant-one
```

```
(is (= (GCSkip.) (.stmt (reduce (Config. (GCAssign. :x
  (deftest test-two-possible-branches-first
  (let [branch (GCIf. [[(GCTrue.) (GCAssign. :x (GCConst. 0))]
  → [(GCTrue.) (GCAssign. :x (GCConst. 1))]])]
    (is (some #(= (GCAssign. :x (GCConst. 0)) %) (times 50
    → `(.stmt (reduce (Config. ~branch emptyState))))))))
(deftest test-two-possible-branches-second
  (let [branch (GCIf. [[(GCTrue.) (GCAssign. :x (GCConst. 0))]
  → [(GCTrue.) (GCAssign. :x (GCConst. 1))]])]
    (is (some #(= (GCAssign. :x (GCConst. 1)) %) (times 50
    → `(.stmt (reduce (Config. ~branch emptyState))))))))
;; If we define `test-ns-hook`, it is called when running
   `run-tests`,
;; instead of just calling all tests in the namespace.
;; This lets us control the order of the tests.
(deftest test-ns-hook
  (test-state-assign-constant-one)
  (test-stmt-assign-constant-one)
  (test-two-possible-branches-first))
(run-tests 'testing)
The Docker setup
Dockerfile
# Define the argument for openjdk version
ARG OPENJDK_TAG=8u232
FROM clojure:openjdk-8
# Install Ruby
RUN apt-get update && apt-get install -y
→ --no-install-recommends --no-install-suggests curl bzip2
→ build-essential libssl-dev libreadline-dev zlib1g-dev && \
   rm -rf /var/lib/apt/lists/* && \
```

```
curl -L https://github.com/rbenv/ruby-
   → build/archive/v20201118.tar.gz | tar -zxvf - -C /tmp/
   cd /tmp/ruby-build-* && ./install.sh && cd / && \
   ruby-build -v 2.7.2 /usr/local && rm -rfv
   → /tmp/ruby-build-*
# Set the name of the maintainers
MAINTAINER Habib Ghaffari Hadigheh, Mark Armstrong

→ <ghaffh1@mcmaster.ca, armstmp@mcmaster.ca>
# Set the working directory
WORKDIR /opt/a3
  docker-compose.yml
version: '2'
services:
 service:
   build: .
   image: 3mi3_a3_docker_image
   volumes:
    - .:/opt/a3
   container_name: 3mi3_a3_container
   command: bash -c
    "echo 'Ruby part 2 testing';
      ٠ ------
     timeout 2m ruby a3p2_test.rb ;
      printf '\\n\\n\ ;
     echo 'Ruby part 4 testing';
     echo
      ر ا ------
     timeout 2m ruby a3p4_test.rb ;
```