

Tutorial 5

Three-Phase Circuits: Balanced Star Connected Load

1. A three-phase, four-wire, 208 V system serves a balanced star-connected load with impedances of $20\angle-30^\circ \Omega$ each. Find the line currents and draw the phasor diagram, taking $V_{AN} = 120.09 \angle -90^\circ \text{ V}$.
Ans: $I_A = 6\angle 300^\circ \text{ A}$ or $6\angle -60^\circ \text{ A}$, $I_B = 6\angle 180^\circ \text{ A}$ or $6\angle -180^\circ \text{ A}$, $I_C = 6\angle 60^\circ \text{ A}$ or $6\angle -300^\circ \text{ A}$
2. An ABC three-phase, 4-wire system serves a star-connected load with impedances of $10\angle 30^\circ \Omega$ each. The line current I_A drawn is found to be $12\angle -30^\circ \text{ A}$. Find all the line voltages, the phase voltages and the remaining line currents.
**Ans: $V_{AN} = 120\angle 0^\circ \text{ V}$, $V_{BN} = 120\angle -120^\circ \text{ V}$, $V_{CN} = 120\angle -240^\circ \text{ V}$,
 $V_{AB} = 208\angle 30^\circ \text{ V}$, $V_{BC} = 208\angle -90^\circ \text{ V}$, $V_{CA} = 208\angle -210^\circ \text{ V}$,
 $I_A = 12\angle -30^\circ \text{ A}$, $I_B = 12\angle -150^\circ \text{ A}$, $I_C = 12\angle -270^\circ \text{ A}$**
3. A three-phase, four wire, 208 V system serves a balance star-connected load drawing a line current $I_A = 10\angle 145^\circ \text{ A}$. Find the line current I_C and the load impedance in each phase, taking V_{BC} as reference.
Ans: $I_C = 10 \angle -95^\circ \text{ A}$, $Z = 12.01 \angle -55^\circ \Omega$
4. Given a balanced three-phase, three-wire system with a Y-connected load for which the line voltage is 230 V and the impedance of each phase is $(6 + j 8) \Omega$. Taking V_{AB} as reference, find the line current I_A and power absorbed by each phase.
Ans: $I_A = 13.28 \angle -83.13^\circ \text{ A}$, $P_{PH} = 1058 \text{ W}$
5. A balanced star load, having a power factor of 0.8 lagging, is connected to a 400 V, 3-phase, 3-wire balanced star supply. The total power consumption of the load is 3 kW. Find the impedances of the load in polar form.
Ans: $Z = 42.67 \angle 36.87^\circ \Omega$
6. A small plant requires the installation of a new three-phase device. The device is to be connected using a 4-wire system with a line voltage of 208 V. Each of the 3-phases has impedance of $10\angle 60^\circ \Omega$. Calculate the line currents for each phase and the overall power dissipated if the impedances are connected in star. Take V_{AN} as the reference voltage and phase sequence as ACB (negative sequence).
Ans: $I_A = 12\angle -60^\circ \text{ A}$, $I_B = 12\angle -300^\circ \text{ A}$, $I_C = 12\angle -180^\circ \text{ A}$, $P = 2161.59 \text{ W}$



Quiz – 3 questions
(Three Phase Supply &
Generation)
– 3 questions
(Balanced Star Load)