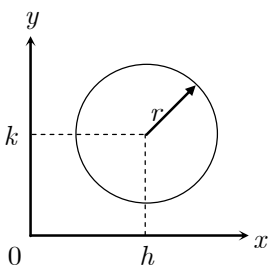
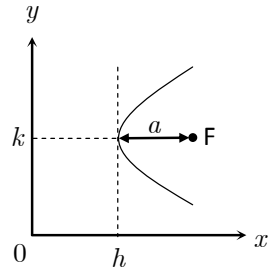
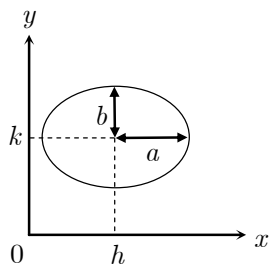
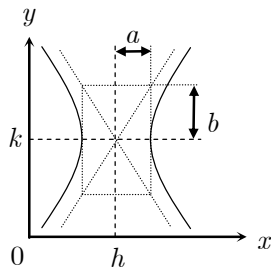


Algebra		
<b>Factoring Formulae</b> $a^2 - b^2 = (a + b)(a - b)$ $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$	<b>Quadratic Formulae</b> If $ax^2 + bx + c = 0$ , where $a, b$ and $c$ are real and $a \neq 0$ , then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	<b>Binomial Theorem</b> If $n$ is a positive integer, then $(a + x)^n = a^n + {}_nC_1a^{n-1}x + {}_nC_2a^{n-2}x^2 + {}_nC_3a^{n-3}x^3 + \dots + x^n$ where ${}_nC_r = \frac{n!}{r!(n-r)!}$

Analytic Geometry & Vectors	
<b>Analytic Geometry</b> Straight line passing through two points $P(x_1, y_1)$ and $Q(x_2, y_2)$ : <ul style="list-style-type: none"> <li>Equation is <math>y = mx + c</math>, where gradient <math>m = \frac{y_2 - y_1}{x_2 - x_1}</math>.</li> <li>Distance from <math>P</math> to <math>Q</math> is: <math>d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}</math></li> <li>Midpoint of <math>PQ</math> is: <math>\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)</math></li> </ul>	<b>Conic Sections</b> Circle: $(x - h)^2 + (y - k)^2 = r^2$  Parabola: $(y - k)^2 = 4a(x - h)$  Ellipse: $\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$  Hyperbola: $\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1$ 
<b>Vectors</b> If the following vectors are defined: $\mathbf{a} = a_1\mathbf{i} + a_2\mathbf{j} + a_3\mathbf{k}$ , $\mathbf{b} = b_1\mathbf{i} + b_2\mathbf{j} + b_3\mathbf{k}$ <ul style="list-style-type: none"> <li>Magnitude of <math>\mathbf{a}</math> is: <math> \mathbf{a}  = \sqrt{a_1^2 + a_2^2 + a_3^2}</math></li> <li>Scalar Product: <math>\mathbf{a} \cdot \mathbf{b} =  \mathbf{a}  \mathbf{b} \cos\theta = a_1b_1 + a_2b_2 + a_3b_3</math></li> <li>Vector Product: <math> \mathbf{a} \times \mathbf{b}  =  \mathbf{a}  \mathbf{b} \sin\theta</math>, <math>\mathbf{a} \times \mathbf{b} = \begin{vmatrix} \mathbf{i} &amp; \mathbf{j} &amp; \mathbf{k} \\ a_1 &amp; a_2 &amp; a_3 \\ b_1 &amp; b_2 &amp; b_3 \end{vmatrix}</math></li> </ul> where $\theta$ is the angle between the two vectors	

Trigonometry				
<b>Definitions</b> $\sec x = \frac{1}{\cos x}$ $\csc x = \frac{1}{\sin x}$ $\tan x = \frac{\sin x}{\cos x}$ $\cot x = \frac{\cos x}{\sin x}$	<b>Basic Identities</b> $\sin(-x) = -\sin x$ $\cos(-x) = \cos x$ $\tan(-x) = -\tan x$ $\sin^2 x + \cos^2 x = 1$ $1 + \tan^2 x = \sec^2 x$ $1 + \cot^2 x = \csc^2 x$	<b>Compound Angle Formulae</b> $\sin(x + y) = \sin x \cos y + \cos x \sin y$ $\sin(x - y) = \sin x \cos y - \cos x \sin y$ $\cos(x + y) = \cos x \cos y - \sin x \sin y$ $\cos(x - y) = \cos x \cos y + \sin x \sin y$ $\tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$ $\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$	<b>Double Angle Formulae</b> $\sin 2x = 2 \sin x \cos x$ $\cos 2x = \cos^2 x - \sin^2 x$ $\phantom{\cos 2x} = 2 \cos^2 x - 1$ $\phantom{\cos 2x} = 1 - 2 \sin^2 x$ $\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$	<b>Formulae for Reducing Power</b> $\sin^2 x = \frac{1 - \cos 2x}{2}$ $\cos^2 x = \frac{1 + \cos 2x}{2}$
<b>Amplitude &amp; Phase-Angle Formulae</b> If $a$ and $b$ are positive constants, $a \sin \theta + b \cos \theta = R \sin(\theta + \alpha)$ $a \sin \theta - b \cos \theta = R \sin(\theta - \alpha)$ $a \cos \theta + b \sin \theta = R \cos(\theta - \alpha)$ $a \cos \theta - b \sin \theta = R \cos(\theta + \alpha)$ where $R = \sqrt{a^2 + b^2}$ and $\alpha = \tan^{-1}\left(\frac{b}{a}\right)$	<b>Sum to Product Identities</b> $\sin x + \sin y = 2 \sin \frac{x + y}{2} \cos \frac{x - y}{2}$ $\sin x - \sin y = 2 \cos \frac{x + y}{2} \sin \frac{x - y}{2}$ $\cos x + \cos y = 2 \cos \frac{x + y}{2} \cos \frac{x - y}{2}$ $\cos x - \cos y = -2 \sin \frac{x + y}{2} \sin \frac{x - y}{2}$	<b>Product to Sum Identities</b> $\sin x \cos y = \frac{1}{2} [\sin(x + y) + \sin(x - y)]$ $\cos x \sin y = \frac{1}{2} [\sin(x + y) - \sin(x - y)]$ $\cos x \cos y = \frac{1}{2} [\cos(x + y) + \cos(x - y)]$ $\sin x \sin y = \frac{1}{2} [\cos(x - y) - \cos(x + y)]$		

Complex Numbers		
A complex number $z$ can be expressed in one of the following forms: <ul style="list-style-type: none"> <li>Rectangular/Cartesian form <math>z = a + jb</math></li> <li>Trigonometric form <math>z = r(\cos \theta + j \sin \theta)</math></li> <li>Polar form <math>z = r \angle \theta</math></li> <li>Exponential form <math>z = re^{j\theta}</math> (<math>\theta</math> in radians)</li> </ul> where $a$ and $b$ are real numbers, $j = \sqrt{-1}$ and $j^2 = -1$ , $r =  z  = \sqrt{a^2 + b^2}$ , and $\theta = \arg(z)$ such that $\tan \theta = \frac{b}{a}$ , $-\pi < \theta \leq \pi$	<b>Complex Conjugates</b> If $z = a + jb$ , then $\bar{z} = a - jb$ , such that $z\bar{z} = a^2 + b^2$ .	<b>Multiplication &amp; Division</b> $z_1 z_2 = (r_1 \angle \theta_1)(r_2 \angle \theta_2) = r_1 r_2 \angle (\theta_1 + \theta_2)$ $\frac{z_1}{z_2} = \frac{(r_1 \angle \theta_1)}{(r_2 \angle \theta_2)} = \frac{r_1}{r_2} \angle (\theta_1 - \theta_2)$
	<b>De Moivre's Theorem</b> $(r \angle \theta)^n = r^n \angle n\theta = r^n (\cos n\theta + j \sin n\theta)$	<b>Euler's Formula</b> $e^{j\theta} = \cos \theta + j \sin \theta$

Differentiation

<b><u>Standard Derivatives</u></b> $\frac{d}{dx}(x^n) = nx^{n-1}$ $\frac{d}{dx}(\ln x) = \frac{1}{x}$ $\frac{d}{dx}(a^x) = a^x \ln a$ $\frac{d}{dx}(e^x) = e^x$ $\frac{d}{dx}(\sin x) = \cos x$ $\frac{d}{dx}(\cos x) = -\sin x$ $\frac{d}{dx}(\tan x) = \sec^2 x$ $\frac{d}{dx}(\cot x) = -\csc^2 x$ $\frac{d}{dx}(\sec x) = \sec x \tan x$ $\frac{d}{dx}(\csc x) = -\csc x \cot x$ $\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$ $\frac{d}{dx}(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}}$ $\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$	<b><u>Rules of Differentiation</u></b> Let $u \equiv u(x)$ , $v \equiv v(x)$ and $y \equiv y(u)$ <ul style="list-style-type: none"><li>Constant Multiple Rule <math>\frac{d}{dx}(ku) = k \frac{du}{dx}</math></li><li>Sum Rule <math>\frac{d}{dx}(u+v) = \frac{du}{dx} + \frac{dv}{dx}</math></li><li>Product Rule <math>\frac{d}{dx}(u \cdot v) = u \frac{dv}{dx} + v \frac{du}{dx}</math></li><li>Quotient Rule <math>\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}</math></li><li>Chain Rule <math>\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}</math></li></ul>	<b><u>Approximation Formula</u></b> If $y = f(x)$ , then $\Delta y \approx \frac{dy}{dx} \Delta x$  If $u = f(x_1, x_2, \dots, x_n)$ , then $\Delta u \approx \frac{\partial u}{\partial x_1} \Delta x_1 + \frac{\partial u}{\partial x_2} \Delta x_2 + \dots + \frac{\partial u}{\partial x_n} \Delta x_n$
		<b><u>Newton's Method</u></b> Newton's method of Approximation to a root of the equation $f(x) = 0$ is $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$ where $f'(x_n) = \left. \frac{df}{dx} \right _{x=x_n}$

Integration

<b><u>Standard Integrals</u></b>		
$\int x^n dx = \frac{x^{n+1}}{n+1} + C$ $\int \frac{1}{x} dx = \ln x  + C$ $\int a^x dx = \frac{a^x}{\ln a} + C$ $\int e^x dx = e^x + C$ $\int \sin x dx = -\cos x + C$ $\int \cos x dx = \sin x + C$ $\int \tan x dx = -\ln \cos x  + C$ $\int \cot x dx = \ln \sin x  + C$ $\int \sec x dx = \ln \sec x + \tan x  + C$ $\int \csc x dx = -\ln \csc x + \cot x  + C$	$\int \sec^2 x dx = \tan x + C$ $\int \csc^2 x dx = -\cot x + C$ $\int \sec x \tan x dx = \sec x + C$ $\int \csc x \cot x dx = -\csc x + C$ $\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$ $\int \frac{1}{x^2 - a^2} dx = \frac{1}{2a} \ln \left  \frac{x-a}{x+a} \right  + C$ $\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} + C$ $\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left  x + \sqrt{x^2 + a^2} \right  + C$ $\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln \left  x + \sqrt{x^2 - a^2} \right  + C$	
<b><u>Integration by Parts</u></b> $\int u dv = uv - \int v du$	<b><u>Mean Value</u></b> $\bar{y} = \frac{1}{b-a} \int_a^b y dx$	<b><u>Root Mean Square Value</u></b> $y_{rms} = \sqrt{\frac{1}{b-a} \int_a^b y^2 dx}$

<b><u>Area &amp; Volume Formula</u></b>	
<ul style="list-style-type: none"><li>Area enclosed by the curve <math>y = f(x)</math>, the <math>x</math>-axis, and the lines <math>x = a</math> and <math>x = b</math>, where <math>f(x) &gt; 0</math> for <math>a \leq x \leq b</math>, is <math>A = \int_a^b y dx</math>.</li><li>Volume of solid of revolution of <math>y = f(x)</math> about the <math>x</math>-axis between <math>x = a</math> and <math>x = b</math> is <math>V = \pi \int_a^b y^2 dx</math>.</li></ul>	
<b><u>Arc Length</u></b> $S = \int_a^b \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx$	<b><u>Centroid of Area</u></b> $\bar{x} = \frac{\int_a^b xy dx}{\int_a^b y dx}, \quad \bar{y} = \frac{\frac{1}{2} \int_a^b y^2 dx}{\int_a^b y dx}$
<b><u>Numerical Integration</u></b>	
Let $y = f(x)$ and $y_0, y_1, \dots, y_{n-1}, y_n$ be the values of $f(x)$ at $x_0 = a$ , $x_1 = a + h$ , $\dots$ , $x_{n-1} = a + (n-1)h$ , $x_n = a + nh = b$ where $h = \frac{b-a}{n}$ .	
<ul style="list-style-type: none"><li>Trapezoidal Rule:<math display="block">\int_a^b f(x) dx \approx \frac{1}{2} h [y_0 + y_n + 2(y_1 + y_2 + \dots + y_{n-1})]</math></li><li>Simpson's Rule:<math display="block">\int_a^b f(x) dx \approx \frac{1}{3} h [y_0 + y_n + 4(y_1 + y_3 + \dots + y_{n-1}) + 2(y_2 + y_4 + \dots + y_{n-2})]</math>where <math>n</math> is an even positive integer.</li></ul>	

Series

<b><u>Arithmetic Series</u></b> $a + (a+d) + (a+2d) + (a+3d) + \dots$ The $n^{\text{th}}$ term is: $u_n = a + (n-1)d$ The sum of the first $n$ terms is: $S_n = \frac{n}{2} [2a + (n-1)d]$	<b><u>Fourier Series</u></b> If $f(t)$ is a periodic function of period $T$ , then its trigonometric Fourier series is given by: $f(t) = a_0 + \sum_{n=1}^{\infty} (a_n \cos n\omega t + b_n \sin n\omega t)$ where $\omega = \frac{2\pi}{T}$ , $a_0 = \frac{1}{T} \int_k^{k+T} f(t) dt$ , $a_n = \frac{2}{T} \int_k^{k+T} f(t) \cos n\omega t dt$ , $b_n = \frac{2}{T} \int_k^{k+T} f(t) \sin n\omega t dt$
<b><u>Geometric Series</u></b> $a + ar + ar^2 + ar^3 + \dots$ The $n^{\text{th}}$ term is: $u_n = ar^{n-1}$ The sum of the first $n$ terms is: $S_n = \frac{a(1-r^n)}{1-r}$ If $-1 < r < 1$ , then the sum to infinity is: $S_{\infty} = \frac{a}{1-r}$	<b><u>Fourier Transform</u></b> The Fourier transform $F(\omega)$ of $f(t)$ is: $F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt$
<b><u>Taylor's Series about <math>x = a</math></u></b> $f(x) = f(a) + f'(a)(x-a) + \frac{f''(a)}{2!}(x-a)^2 + \frac{f'''(a)}{3!}(x-a)^3 + \dots$	<b><u>Standard Power Series</u></b> <ul style="list-style-type: none"><li>Binomial Series: <math>(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots</math> where <math>-1 &lt; x &lt; 1</math> and <math>n</math> is not a positive integer</li><li>Logarithm Series: <math>\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots</math>, <math>-1 &lt; x \leq 1</math></li><li>Exponential Series: <math>e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots</math></li><li>Sine &amp; Cosine Series: <math>\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots</math>, <math>\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots</math></li></ul>
<b><u>Maclaurin's Series</u></b> $f(x) = f(0) + f'(0)x + \frac{f''(0)}{2!}x^2 + \frac{f'''(0)}{3!}x^3 + \dots$	

Differential Equations

First Order Linear ODE

$$\frac{dy}{dx} + P(x)y = Q(x)$$

Integrating factor:

$$\mu(x) = e^{\int P(x) dx}$$

General solution:

$$y \cdot \mu(x) = \int \mu(x)Q(x) dx$$

Second Order Homogeneous ODE with Constant Coefficients

$$a \frac{d^2 y}{dx^2} + b \frac{dy}{dx} + cy = 0$$

Auxiliary equation:  $a\lambda^2 + b\lambda + c = 0$  , where  $\lambda_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

General solution:

Case 1: $b^2 - 4ac > 0$	Case 2: $b^2 - 4ac = 0$	Case 3: $b^2 - 4ac < 0$
2 real roots: $\lambda_1$ and $\lambda_2$	2 equal roots: $\lambda_1 = \lambda_2 = \lambda$	2 complex roots: $\lambda = \alpha \pm j\beta$
$y = Ae^{\lambda_1 x} + Be^{\lambda_2 x}$	$y = e^{\lambda x} (Ax + B)$	$y = e^{\alpha x} (A \cos \beta x + B \sin \beta x)$

where  $A$  and  $B$  are arbitrary constants.

Determinants & Matrices

Determinants

Order 2:  $\begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{vmatrix} = a_{11}a_{22} - a_{12}a_{21}$

Order 3:  $\begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11}A_{11} + a_{12}A_{12} + a_{13}A_{13}$

where  $A_{11}, A_{12}$  and  $A_{13}$  are cofactors of elements  $a_{11}, a_{12}$  and  $a_{13}$  respectively, and given by

$$A_{11} = + \begin{vmatrix} a_{22} & a_{23} \\ a_{32} & a_{33} \end{vmatrix} = + (a_{22}a_{33} - a_{23}a_{32}) ,$$
$$A_{12} = - \begin{vmatrix} a_{21} & a_{23} \\ a_{31} & a_{33} \end{vmatrix} = - (a_{21}a_{33} - a_{23}a_{31}) ,$$
$$A_{13} = + \begin{vmatrix} a_{21} & a_{22} \\ a_{31} & a_{32} \end{vmatrix} = + (a_{21}a_{32} - a_{22}a_{31})$$

Inverse Matrix

If  $|A| \neq 0$ , then inverse of  $3 \times 3$  matrix  $A$  is:  $A^{-1} = \frac{1}{|A|} \text{adj } A$

where  $\text{adj } A = \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix}^T$  and  $A_{ij}$  are cofactors of elements  $a_{ij}$ .

Cramer's Rule

For a system of 3 linear equations:

$$\begin{aligned} a_{11}x_1 + a_{12}x_2 + a_{13}x_3 &= k_1 \\ a_{21}x_1 + a_{22}x_2 + a_{23}x_3 &= k_2 \\ a_{31}x_1 + a_{32}x_2 + a_{33}x_3 &= k_3 \end{aligned}$$

The solutions are:

$$x_1 = \frac{1}{|A|} \begin{vmatrix} k_1 & a_{12} & a_{13} \\ k_2 & a_{22} & a_{23} \\ k_3 & a_{32} & a_{33} \end{vmatrix}, \quad x_2 = \frac{1}{|A|} \begin{vmatrix} a_{11} & k_1 & a_{13} \\ a_{21} & k_2 & a_{23} \\ a_{31} & k_3 & a_{33} \end{vmatrix}, \quad x_3 = \frac{1}{|A|} \begin{vmatrix} a_{11} & a_{12} & k_1 \\ a_{21} & a_{22} & k_2 \\ a_{31} & a_{32} & k_3 \end{vmatrix}, \text{ where } |A| = \begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix}$$

Probability & Statistics

Statistical Measure for Population

Mean:  $\mu = \frac{\sum f_i x_i}{N}$

Standard deviation:  $\sigma = \sqrt{\frac{\sum f_i (x_i - \mu)^2}{N}}$

Median:  $\tilde{x} = L_m + \frac{\frac{N}{2} - F_c}{f_m} C$

where  $x_i$  = class mark of the  $i^{\text{th}}$  class,  
 $f_i$  = frequency of the  $i^{\text{th}}$  class,  
 $L_m$  = lower class boundary of the median class,  
 $N = \sum f_i$  = total frequency,  
 $F_c$  = sum of frequencies of all classes below the median class,  
 $f_m$  = frequency of the median class,  
 $C$  = class width.

Probability Rules

Addition Rule:  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

Subtraction Rule:  $P(A) = 1 - P(\bar{A})$

Multiplication Rule:  $P(A \cap B) = P(A)P(B)$  if  $A$  and  $B$  are independent events.

Conditional Probability:  $P(A|B) = \frac{P(A \cap B)}{P(B)}$

Bayes' Theorem:

$$P(A) = P(A|B_1)P(B_1) + P(A|B_2)P(B_2)$$
$$P(B_1|A) = \frac{P(A|B_1)P(B_1)}{P(A|B_1)P(B_1) + P(A|B_2)P(B_2)}$$

where  $B_1 \cap B_2 = \emptyset$  and  $B_1 \cup B_2 = S$  the sample space.

Sample Statistics

Mean:  $\bar{x} = \frac{\sum f_i x_i}{n}$

Standard deviation:  $s = \sqrt{\frac{\sum f_i (x_i - \bar{x})^2}{n - 1}}$

where  $x_i$  = class mark of the  $i^{\text{th}}$  class,  
 $f_i$  = frequency of the  $i^{\text{th}}$  class,  
 $n$  = sample size.

Test Statistics

Test for Population Mean	Test for Difference of Means	Test for Proportions
$z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$	$z = \frac{(\bar{x} - \bar{y}) - (\mu_x - \mu_y)}{\sqrt{\frac{\sigma_x^2}{n_x} + \frac{\sigma_y^2}{n_y}}}$	$z = \frac{\hat{p} - p_0}{\sqrt{p_0(1 - p_0)/n}}$

Discrete Probability Distributions

Mean:  $\mu = E(X) = \sum_{\text{all } x} xP(X = x)$

Variance:  $\sigma^2 = \text{Var}(X) = E(X^2) - \mu^2$   
where  $E(X^2) = \sum_{\text{all } x} x^2 P(X = x)$

Standard deviation:  $\sigma = \sqrt{\text{Var}(X)}$

- Binomial Distribution:  $X \sim B(n, p)$   
 $P(X = x) = {}_n C_x p^x q^{n-x}$   
Mean:  $\mu = np$  , standard deviation:  $\sigma = \sqrt{npq}$
- Poisson Distribution:  $X \sim P(\lambda)$   
 $P(X = x) = \frac{\lambda^x}{x!} e^{-\lambda}$   
Mean:  $\mu = \lambda$  , standard deviation:  $\sigma = \sqrt{\lambda}$

Sampling Distribution

Mean:  $\mu_{\bar{x}} = \mu$

Standard error:

- for finite population:  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \sqrt{\frac{N-n}{N-1}}$
- for infinite population:  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$

Continuous Probability Distributions

$P(a < X < b) = \int_a^b f(x) dx$

Mean:  $\mu = E(X) = \int_{-\infty}^{\infty} x f(x) dx$

Variance:  $\sigma^2 = \text{Var}(X) = E(X^2) - \mu^2$   
where  $E(X^2) = \int_{-\infty}^{\infty} x^2 f(x) dx$

Standard deviation:  $\sigma = \sqrt{\text{Var}(X)}$

- Normal Distribution:  $X \sim N(\mu, \sigma^2)$   
$$f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left( \frac{x - \mu}{\sigma} \right)^2}$$
  
Mean =  $\mu$  , standard deviation =  $\sigma$

Simple Linear Regression

Least Squares Line (y = mx + c)

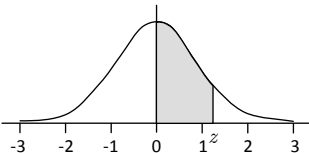
m = (n Σ xy - (Σ x)(Σ y)) / (n Σ x^2 - (Σ x)^2), c = (Σ y - m Σ x) / n

Correlation coefficient: r = (Σ (x - x̄)(y - ȳ)) / (√(Σ (x - x̄)^2 · Σ (y - ȳ)^2))

Standard Normal Table

Area under the Standard Normal Curve from 0 to z

z = (x - μ) / σ



z	0	1	2	3	4	5	6	7	8	9
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0754
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2996	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000

Hyperbolic Functions

Definitions

sinh x = (e^x - e^-x) / 2, cosh x = (e^x + e^-x) / 2, tanh x = sinh x / cosh x

Basic Identities

cosh^2 x - sinh^2 x = 1, 1 - tanh^2 x = sech^2 x, coth^2 x - 1 = csch^2 x

Laplace Transforms

Definition

L{f(t)} = ∫\_0^∞ e^-st f(t) dt = F(s)

Table of Laplace Transforms

Function f(t)	Laplace Transform F(s)
1	1/s
t^n n is a positive integer	n! / s^(n+1)
e^at	1 / (s - a)
sin at	a / (s^2 + a^2)
cos at	s / (s^2 + a^2)
t sin at	2as / (s^2 + a^2)^2
t cos at	(s^2 - a^2) / (s^2 + a^2)^2
First Shift Theorem e^at f(t)	F(s - a)
dy/dt	sL{y} - y(0)
d^2y/dt^2	s^2L{y} - sy(0) - y'(0)
∫_0^t f(t) dt	(1/s)L{f(t)}
Unit Step Function u(t - c)	e^-cs / s
Second Shift Theorem f(t - c)u(t - c)	e^-cs L{f(t)}
f(t)u(t - c)	e^-cs L{f(t + c)}
Unit Impulse Function δ(t - c)	e^-cs
f(t)δ(t - c)	f(c)e^-cs

Boolean Algebra

Commutative Laws	x · y = y · x x + y = y + x
Associative Laws	x · (y · z) = (x · y) · z = x · y · z x + (y + z) = (x + y) + z = x + y + z
Distributive Laws	x + (y · z) = (x + y) · (x + z) x · (y + z) = (x · y) + (x · z)
Identity Laws	x · 1 = x x + 0 = x
Complement Laws	x · x̄ = 0 x + x̄ = 1
Involution Law	̄̄x = x
Idempotent Laws	x · x = x x + x = x
Bound Laws	x · 0 = 0 x + 1 = 1
De Morgan's Theorem	̄(x · y) = x̄ + ȳ ̄(x + y) = x̄ · ȳ
Absorption Laws	x · (x + y) = x x · (x̄ + y) = x̄ · y x + (x · y) = x x + (x̄ · y) = x̄ + y