

[CSED233-01] Data Structure

List, Stack, and Queue

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POSTECH



Attendance Check

- If you are having trouble with the electronic attendance check
 - Check with TA
 - TA will be at the entrance gate
 - Before ~9:30. No problem
 - 9:30~9:45. Late
 - 9:45~ Absent
 - More than 3 absents without proper reason: F
 - We will not accept the attendance issue after the class finishes.

Academic Dishonesty

- Assignments, exams, ...
- This is just a class. Do not try to risk your entire school life!
- Reported cases will be judged by POSTECH's Committee
- We won't accept any excuse

(Linear) Lists

- List $L = \langle a_1, a_2, \dots, a_n \rangle$
 - a finite, *ordered* collection of elements
 - n : length (size) of the list
 - empty list $\langle \rangle$: $n = 0$ (no elements)

- Position of a_i is i

- head (front) \leftrightarrow tail (rear)

head tail
↓ ↓
 $\langle a_1, a_2, \dots, a_n \rangle$

- "*current*" position

$\langle 20, 23, | 12, 15 \rangle$: separated by *fence*

$\langle 20, 23, | 10 12, 15 \rangle$ after insertion of 10 (at "current" position)

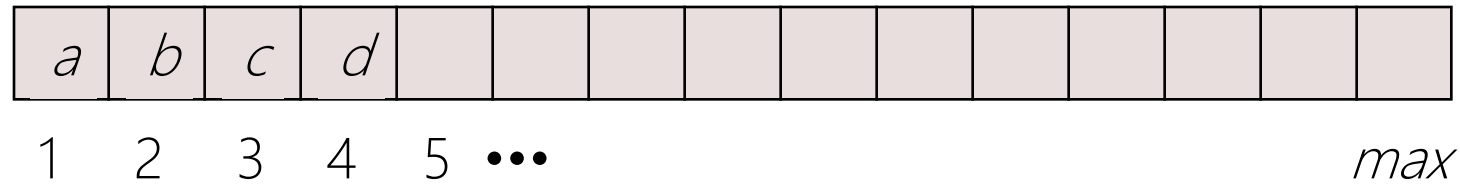
- Sorted list \leftrightarrow Unsorted list
- Don't be confused, ordered and sorted mean different things

List Operations

- $L = \langle a_1, a_2, \dots, a_{p-1}, a_p, a_{p+1}, \dots, a_n \rangle$
 - $Insert(x, p, L)$: insert x at position p in list L
 - $\langle a_1, a_2, \dots, a_{p-1}, x, a_p, \dots, a_n \rangle$
 - $Delete(p, L)$: delete element at position p in L
 - $\langle a_1, a_2, \dots, a_{p-1}, a_{p+1}, \dots, a_n \rangle$
 - $Next(p, L)$: returns the position or pointer immediately following position p
 - $Previous(p, L)$: returns the position or pointer previous to p
 - $Locate(x, L)$: returns the position or pointer of x on L
 - $Retrieve(p, L)$: returns element at position p on L
 - $MakeNull(L)$: causes L to become an empty list and returns position $END(L)$
 - $First(L)$: the first position on L
- This is just one example! There is no rule about the list's function names, arguments, their behavior, and return types.
- Check out STL's vector 😊

Array-Based List Implementation (1)

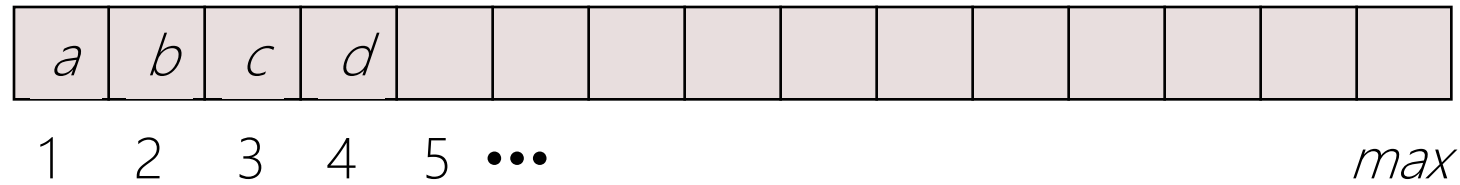
- $L = \langle a, b, c, d \rangle$
 - `char L[max]`



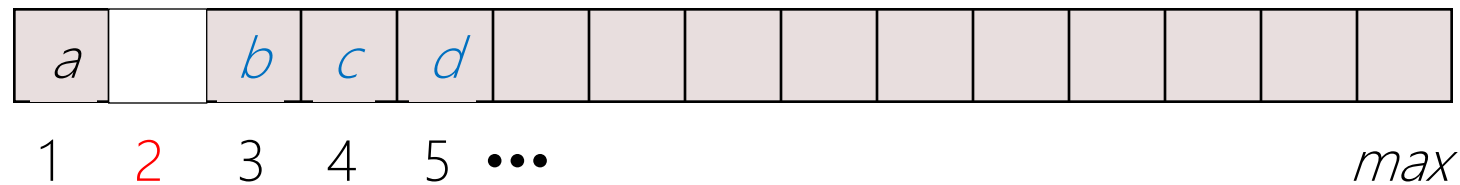
- Integer *size* = 4 or
 - Integer *last* = the position of the last element
- *Insert* ($x, 2, L$) ?

Array-Based List Implementation (2)

- $L = \langle a, b, c, d \rangle$
 - `char L[max]`

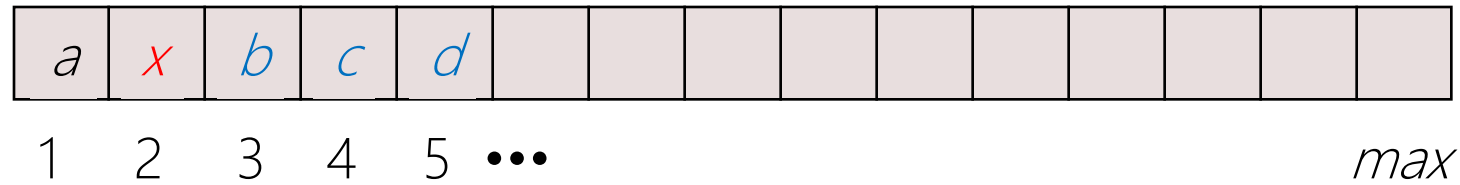


- Integer *size* = 4 or
 - Integer *last* = the position of the last element
- *Insert* (*x*, 2, *L*) ?



Array-Based List Implementation (3)

- *Insert* ($x, 2, L$)
 - *void insert(char x, int i, char* L)*



- Before insertion, we need to *shift right* all following elements by one position
 - *size* = 5
 - Running time? $O(n)$ – Linear time
-
- *Delete*(p, L), *Locate*(x, L)
 - Running time? $O(n)$ – Linear time
 - What does this mean?

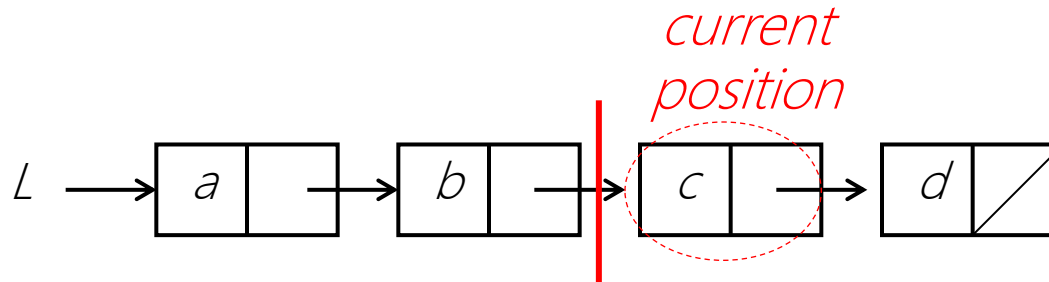
Pointer-Based List Implementation (1)

- **Singly-linked** list (**One-way** list)

Of course, we also have doubly-linked list ☺

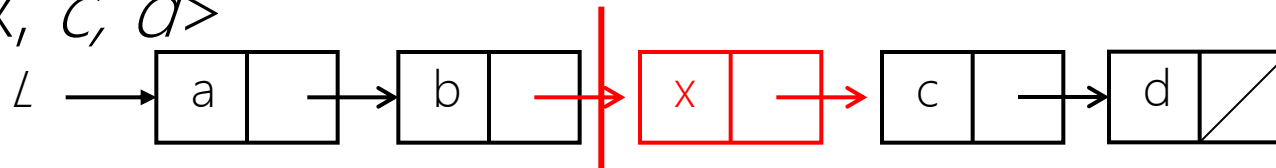
$$L = \langle a, b, \mid c, d \rangle$$

```
Struct item{  
  char info;  
  item* link;  
};
```



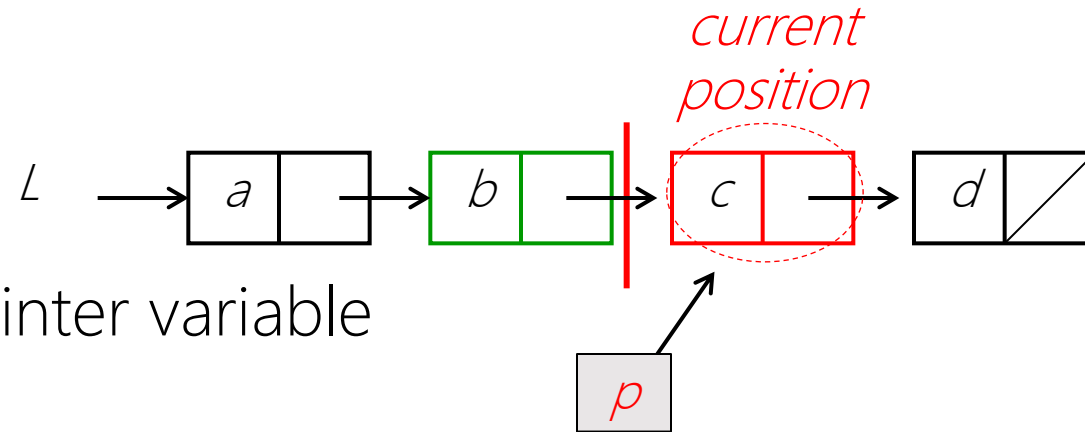
- Node (or cell) = info + link
- *Insert* (x, p, L) when $p = \text{current}$

$$L = \langle a, b, \mid x, c, d \rangle$$



Pointer-Based List Implementation (2)

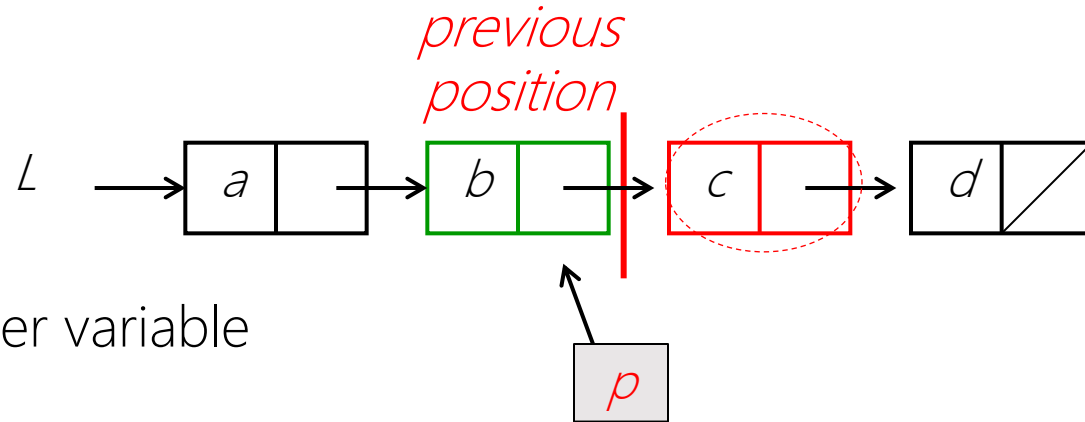
- How to represent the logical fence?



- We need a pointer variable
- Option-1:
 - P directly points to the **current** element
 - What difficulty for $Insert(x, p, L)$?
 - Inconvenient access to the **preceding** node of the current one
 - We have to change the link of the preceding node

Pointer-Based List Implementation (3)

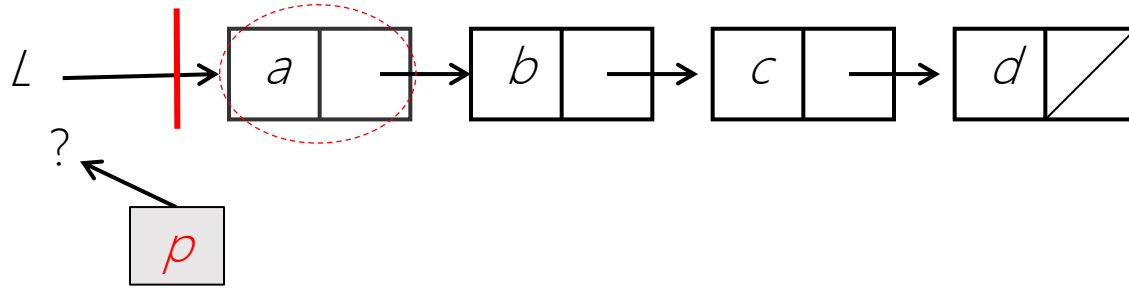
- How to represent the logical fence?



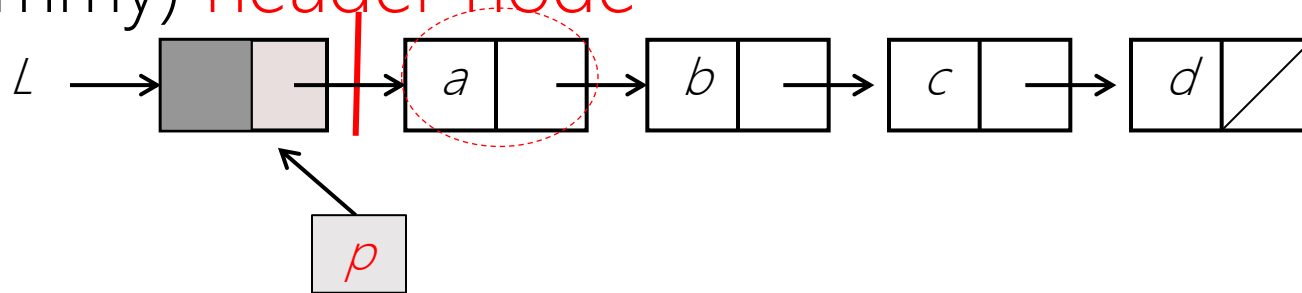
- We need a pointer variable
- Option-2 (*One-step ahead* convention):
 - P points to the *previous* element of the current position
 - Different definition of position
 - P is the position of the element "b" (not "c")

Pointer-Based List Implementation (4)

- *Insert* (x, p, L)
 - When the list is empty or the left partition is empty, What difficulty ?

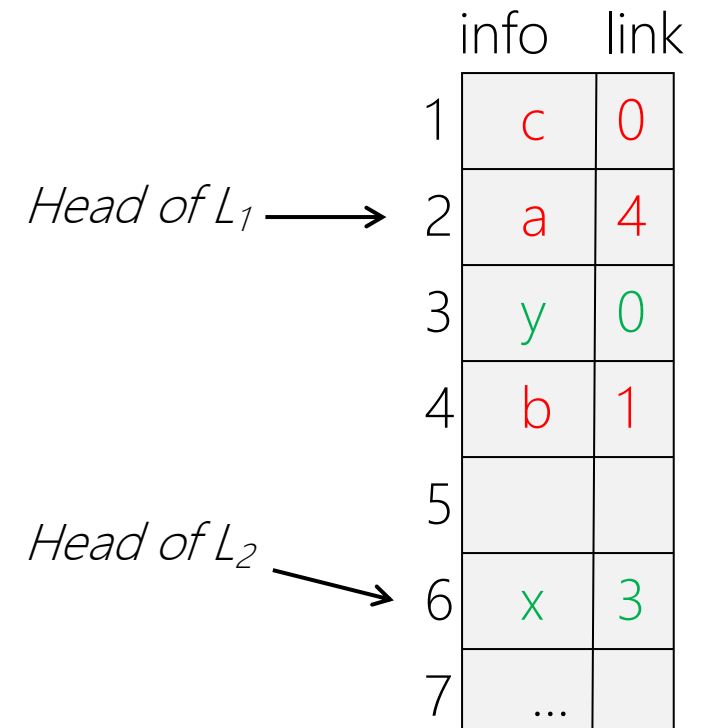


- Need to implement a number of special cases
- Solution: (dummy) header node



Cursor-Based List Implementation

- Cursor (Simulated Pointer)
 - Integer index indicating positions in array to simulate pointers
 - We maintain the heads of the lists
 - Zero value of the link means the tail of the list
- *Example*
 - $L_1 = \langle a, b, c \rangle$ $L_2 = \langle x, y \rangle$
- Time complexity of insert and delete
 - $O(1)$
- Time complexity of retrieve
 - $O(n)$



Stacks

- All insertions & deletions take place at one end (called *Top*)
- Special type of list
 - LIFO (Last-In, First-Out)
 - Pushdown list
- You can implement stacks using any type of list implementation (pointer, array, cursor, ...)

$$S = \langle a_1, a_2, \dots, a_n \rangle$$

↑
Top

- $Push(x, S)$
- $Pop(S)$
- $Top(S)$
- $MakeNull(S)$
- $IsEmpty(S)$

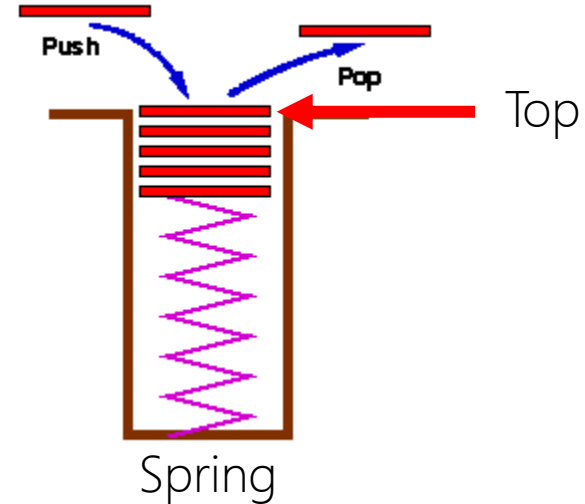
$$S = \langle x, a_1, a_2, \dots, a_n \rangle$$

$$S = \langle a_2, \dots, a_n \rangle$$

$$a_1$$

$$S = \langle \rangle$$

$$\text{true if } S = \langle \rangle$$

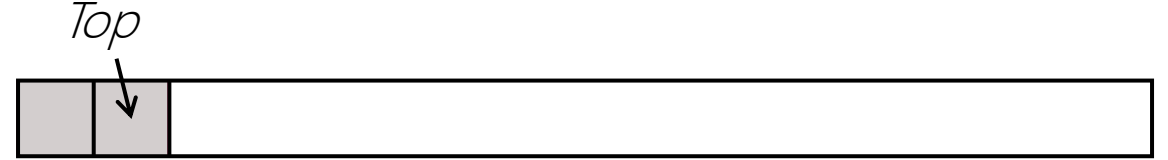


Stack Implementations

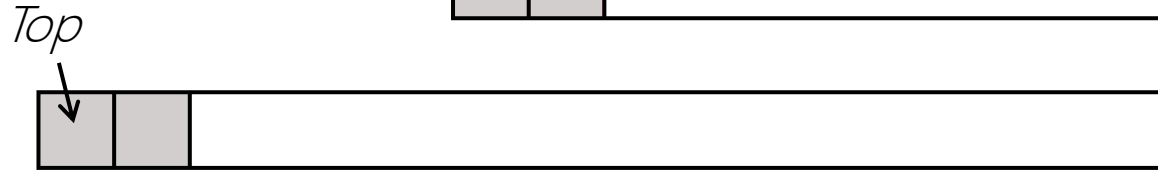
- **Array-based** stacks

- *How to implement TOP?* (in terms of cost of *pop/push*)

- Position k (when k elements in stack): $O(1)$



- (Fixed) Position 1: $O(n)$

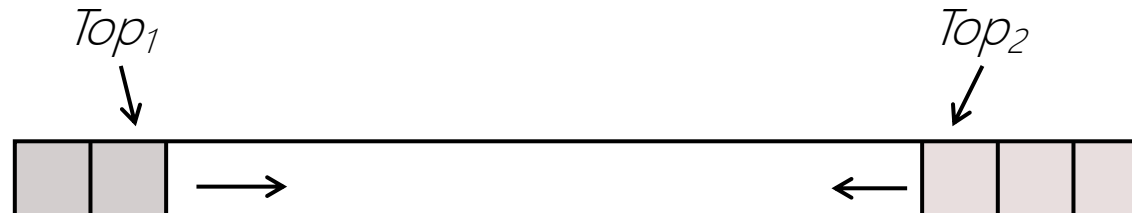


- We can even store multiple stacks in a single array

- **Linked** stacks

- Very much similar to the pointer-based list implementation

- Example: call stack



Queues

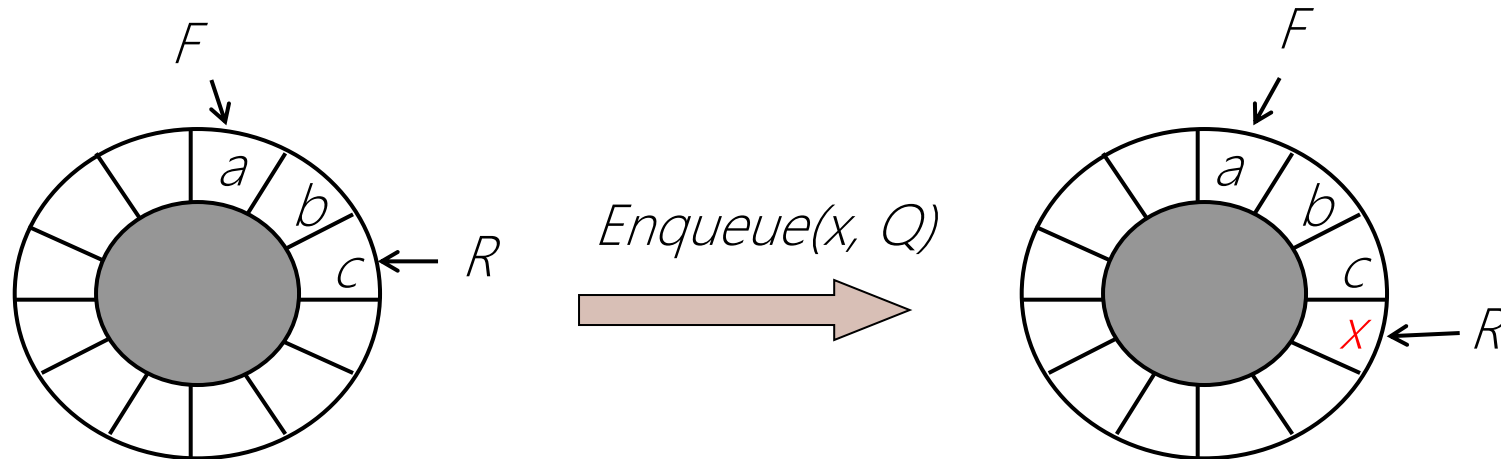
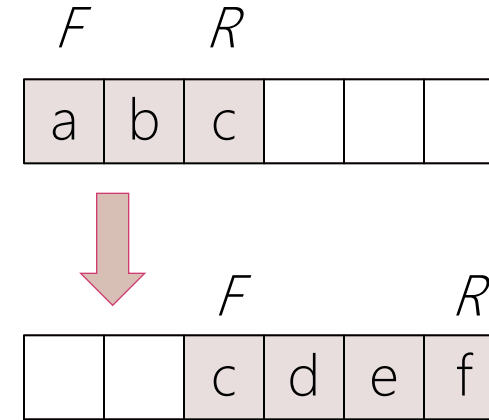
- **FIFO** (First-In First-Out) list
- Similar to top in the stack, here we have front and rear
- $Q = \langle a_1, a_2, \dots, a_n \rangle$
 \uparrow \uparrow
 Front Rear

- | | |
|-------------------|---|
| • $Enqueue(x, Q)$ | $Q = \langle a_1, a_2, \dots, a_n, x \rangle$ |
| • $Dequeue(Q)$ | $Q = \langle a_2, a_3, \dots, a_n \rangle$ |
| • $Front(Q)$ | a_1 |
| • $MakeNull(Q)$ | $Q = \langle \rangle$ |
| • $IsEmpty(Q)$ | true if $Q = \langle \rangle$ |



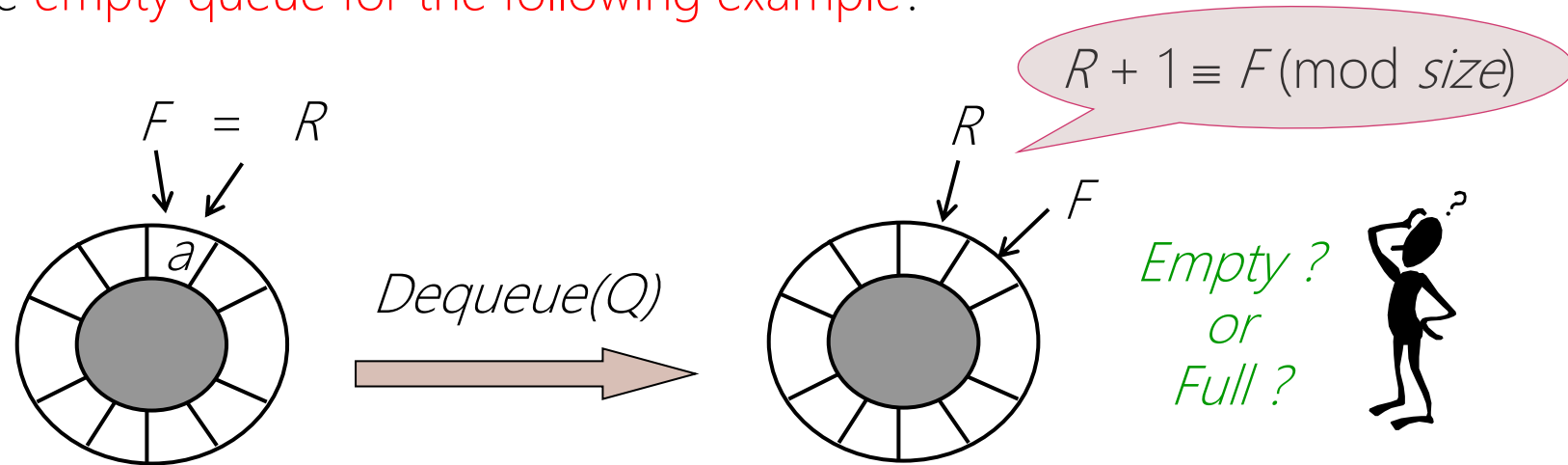
Array-Based Queues (1)

- Simple array implementation
 - "drifting queue" problem
 - We can solve this in an Inefficient way...
 - *Enqueue & Dequeue*: $O(1)$ & $O(n)$ or vice versa
- Circular array
 - Modulus/modulo operator: $n + 1 \equiv 1 \pmod{n}$
 - Mathematically connect the last element to the first element via modulo operator



Array-Based Queues (2)

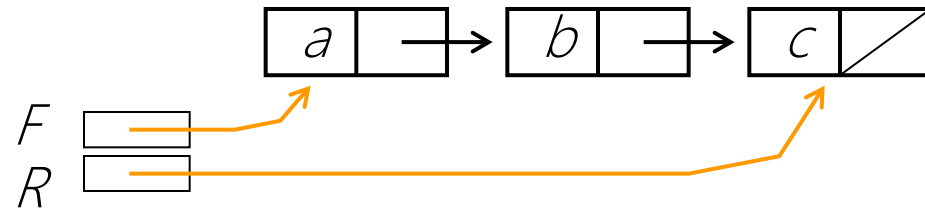
- For the circular array, we have a problem...
 - How to recognize **empty queue** for the following example?



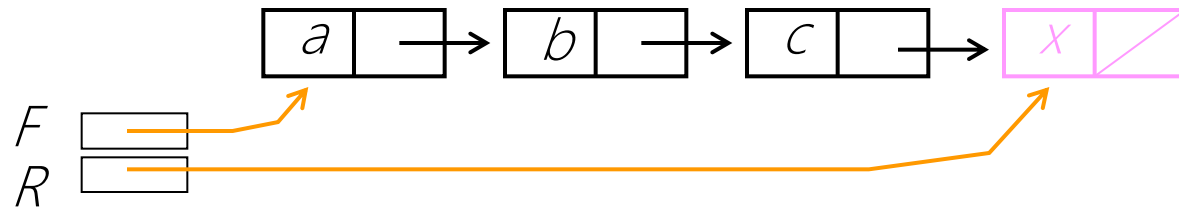
- Problem** - indistinguishable from **full queue**
- Several solutions
 - Explicit count variable (# of elements in queue)
 - For the enqueue: `cnt ++;`
 - For the dequeue: `cnt --;`
 - Boolean variable (to indicating empty queue)
 - `bool isempty;`

Linked Queues (1)

- Two pointers (F , R) (without a **dummy header**)



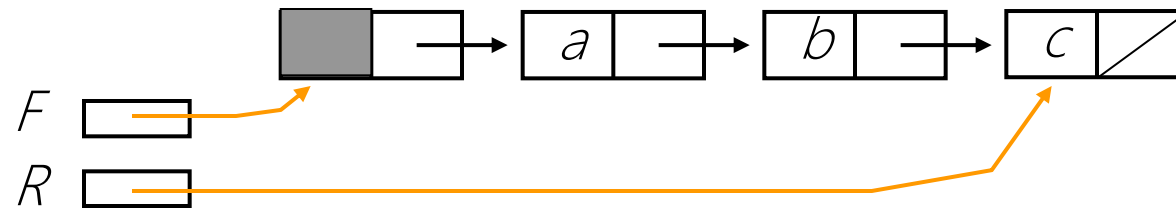
- $Empty(Q)$
 - true if ($F = R \rightarrow \text{null}$)
- $Enqueue(x, Q)$



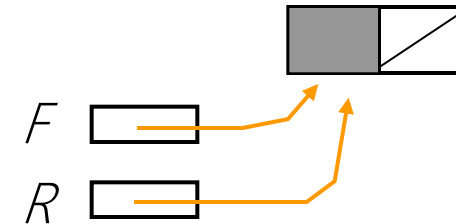
- Problem:** Can we use the same code when inserting into an empty queue?

Linked Queues (2)

- With a **dummy header**



- $Empty(Q)$
 - true if ($F = R \rightarrow$ **header**)
- $Enqueue(x, Q)$

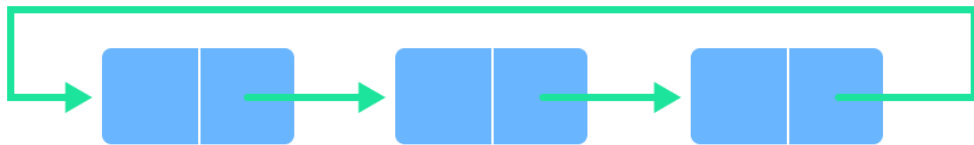
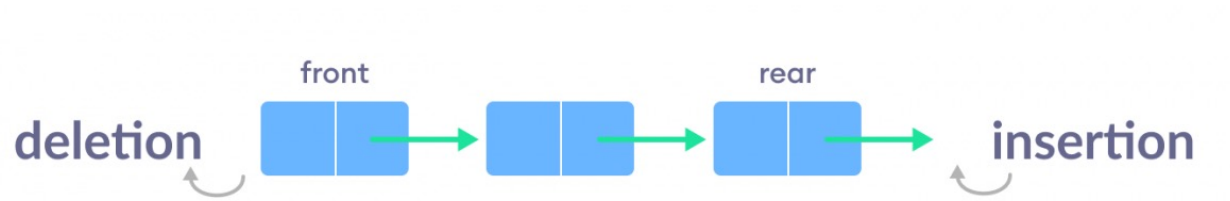


Linked Queues (3)

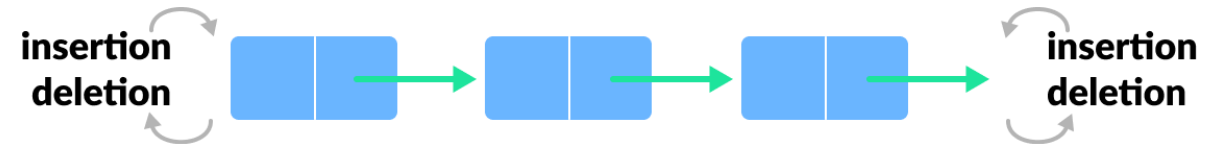
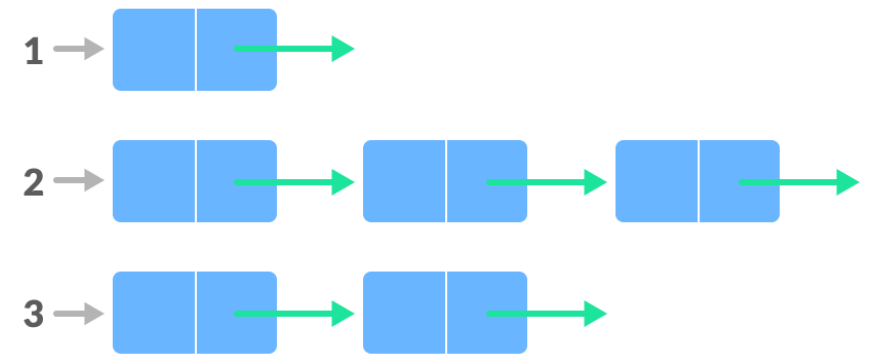
- Comparison (with & without header)
 - Speed
 - Space utilization
 - Code conciseness - the same codes for
 - Insertion into an empty queue
 - Deletion when queue has only one element

Type of Queues

- Queue, circular queue, priority queue, double-ended queue



Priority



References

- Further reading list and references
 - <https://www.geeksforgeeks.org/binary-tree-data-structure/?ref=shm>
- Slide credit
 - Jaesik Park
 - Seung-Hwan Baek
 - Jong-Hyeok Lee